

## INTRO TO COURSE ([slides](#))

what is computer science?

- systematic study of computer systems, algorithms, data, and applications/impacts
- interdisciplinary → math, engineering, empirical science, art, social science

what are algorithms?

- precise sequence of unambiguous steps that effectively compute an output given an input
- intuitive English → precise English → pseudocode → software
  - algorithm design: mathematical, logic of program, problem solving, language independent
  - implementation: semantics and syntax, language dependent, programming on a real machine

theory

- design an algorithm, analyze performance, data structure tradeoffs

practice

- write a Java program, debug/test, measure performance

data structures

- store different kinds of informatists are on in different ways, with algorithmic tradeoffs
- relates to efficiency of accessing or transforming data during operation of a program
- efficiency matters at higher scales (affects program speed)

## INTRO TO JAVA ([slides](#))

Java is a compiled language

- compiled
  - studies it all at once
  - **compiler**: program that translates source code into machine code
  - run the executable, the output of the compiler
- interpreted
  - line at a time
  - **interpreter**: program that translates and runs a program line by line
  - Python is an interpreted language
- Java Virtual Machine: write and compile once, run on multiple devices

command line

Command	Meaning	Details
<code>pwd</code>	Print Working Directory	Shows the full file path to the directory you are currently in
<code>ls</code>	List Files	Shows all files and directories contained in the current directory
<code>cd</code>	Change Directory	<ul style="list-style-type: none"><li>• <code>cd</code> by itself goes to your home directory</li><li>• <code>cd directory</code> goes to the specified directory</li><li>• <code>cd ..</code> goes to the enclosing directory</li></ul>
<code>mkdir</code>	Make Directory	<ul style="list-style-type: none"><li>• <code>mkdir directory</code> creates a directory</li></ul>
<code>cp</code>	Copy	<code>cp source target</code> Copies the source file and names the result target.
<code>rm</code>	Remove	<code>rm file</code> deletes the specified file. No backups!!!

compile and run Java

Command	Meaning	Details
<code>javac</code>	Compile .java files to .class files	<ul style="list-style-type: none"> <li><code>javac file.java</code> compiles and creates <code>file.class</code></li> <li><code>javac *.java</code> compiles <b>all</b> .java files in current directory to .class files.</li> </ul>
<code>java</code>	Run java class files	<code>java file</code> executes the main method of <code>file.class</code> . Must have already been compiled from <code>file.java</code> .

## Java basics

- each Java program file contains a single class → <className>.java
- run with public static void main (PSVM) method
  - **public**: can call outside of class
  - **static**: belongs to class, not an object
  - **void**: no return
  - **main**: starting point for a program to run
  - **args**: allows for command-line arguments
- strongly typed

## primitive types

- byte, short, int, long, float, double, boolean, char
- String objects are not primitive but you can create them without “new”

## basic operators

- + - \* / % < <= > >= == ! && ||

## reference types

- <object type> <name> = new <constructor>();
- **Constructor**: method that initializes objects
- variable stores a reference to an object (place in memory)
- access instance variables and method calls with “.”

## Arrays

- store fixed number of entries of a single type
- `Type[] name = new Type[length]`

## Strings

- hold an Array of characters → can use `toCharArray()` to `char[]`
  - characters are ordered, comparable, and correspond to integer values

## Loops

- `for (int i = 0; i < num; i++) {}`
- `for (Object object : objects) {}`
- `while (boolean) {}`

## Methods

- function defined in a class
- `<Object/void> methodName(<parameters>) { }`
- **dynamic methods:** called on a created object, has access to object data and arguments
  - `s.equals()`
- **static methods:** called on the class, only has access to arguments
  - `Math.sqrt()`

## Java API data structures

- only store reference types (no primitives, int vs Integer)
- brief examples
  - **ArrayList:** list of values of the same type, can grow dynamically
  - **HashSet:** unordered collection, does not store duplicates

## style

- comments // one line or /\* \*/ multiple lines
- informative lowerCamelCase variable and method names

- informative CapitalizedCamelCase class names

- javadoc:

```
/**  
 * descriptor  
 * @param/return/throws  
 */
```

## OBJECT-ORIENTED PROGRAMMING ([slides](#))

**object-oriented**: programs in that language are organized by the specification and use of objects

**object**: has some internal data items plus operations that can be performed on that data

**class**: blueprint for objects; specifies data and operations for a type of object

- objects are an instance of a class
- instance variables
- constructor: specifies how to create a new object
- . operator accesses instance variable or method of this object (on what it's called)

reasons to call a method

- side effect → what it did to an object
- return value

equals() (not == like for primitives) → @Override in Jdoc

- == → checks if these two are the same object in memory
- equals() without implementation → default Object checks if these two are the same object in memory

Object: default class from which all objects inherit

- you must always allocate memory and create each object

privacy

- public: can be accessed by code outside of class
- private: can only be accessed by code inside of class
- protected: can be access by code inside the package

immutability

- cannot change after creation (vs mutable), Strings are immutable

static

- belong to the class (method → called on a class, usually functional)

## INTERFACES & IMPLEMENTATIONS ([slides](#))

**ADT (Abstract data type):** specifies what a data structure does (functionality) but not how it does it (implementation)

**API (Application program interface) perspective:** what methods can I call on these objects, what inputs do they take, what outputs do they return?

**interface:** specify a set of abstract methods that an implementing class must override and define (ADT)

- **collection:** a group of objects
  - **List:** ordered sequence of values → **ArrayList, LinkedList**
  - **Set:** unordered collection of unique values → **HashSet, TreeSet**
  - **Map:** collection that associates keys and values → **HashMap, TreeMap**
- need an implementing class at creation (`List<String> l = new ArrayList<>()`)
- implement list → public class NewList implements List
  - Must have at least all the same methods as the interface
  - As a parameter, you can just have `List<Object>` since any implementing class can use the same methods
- vs superclass → you get the implementation but not for interfaces

algorithmic tradeoffs

- efficiency of operations on data structures depends on scale

ex: `ArrayList`

- `get()` → direct lookup, constant (advantage)
- `contains()` → loops through Array calling `equals()`, takes longer with more size
- `size()` → returns an instance variable tracking size, constant
- `add()` → depends
  - keeps an Array with space at the end → add to open position or create new copied Array
  - space left → constant time, one Array value assignment
  - no space left → takes N array assignments, copy entire list

- how many times you have to copy an ArrayList:

**Geometric growth**

$$1 + 2 + 4 + \dots + N$$

$$= \sum_{i=0}^{\approx \log_2 N} 2^i$$

$$\approx 2N$$

Geometric series formula:

$$\sum_{i=0}^n ar^i = a\left(\frac{1 - r^{n+1}}{1 - r}\right)$$

**Arithmetic growth**

$$1 + 101 + 201 + \dots + N$$

$$= \sum_{i=0}^{\approx N/100} 1 + 100i$$

$$\approx \frac{N^2}{200}$$

Arithmetic series formula:

$$\sum_{i=1}^n a_i = \left(\frac{n}{2}\right)(a_1 + a_n)$$

- geometric is better for larger size, arithmetic is better for smaller size
- Java API uses geometric growth
- adding to the front of an ArrayList is NOT efficient
  - have to shift everything over
  - worst case: Array is full and must allocate space
- can use Arrays.asList and toArray to convert between List and Array

## SETS & MAPS ([slides](#))

### Sets

- stores unique elements, not necessarily stored in order
- usage
  - contains() → constant time efficiency
  - add() → constant time efficiency
  - remove()
  - loop with enhanced for ( : )
  - addAll() to convert to and from List
- **HashSet**
  - constant time: does not depend on the number of values stored in the Set
  - very efficient add, contains
  - ex: countUniqueWords
    - HashSet → constant time operation, linear complexity
    - ArrayList → must check all the words so far for each word, quadratic complexity
  - HashSet and HashMap implemented with hash table data structure
- **TreeSet**
  - nearly as efficient as HashSet, keeps values sorted
  - TreeSet and TreeMap implemented with binary tree data structure

### Maps

- interface that pairs keys with values → lookup the value with the key
- usage
  - put(k, v) → associate value v with key k, constant time efficiency
  - get(k) → gets the value with key k, constant time efficiency
  - containsKey(k) → returns if key k is in the Map, constant time efficiency

- `putIfAbsent(k, v)`
- check `containsKey` first because calling `get` on a key not in the Map crashes the program
- updating Maps
  - single values
    - `get()` returns a copy of the value
    - must use `put()` to update → no `+=` directly
  - collection values
    - `get()` returns reference to collection
    - updates the collection directly
- **HashMap**
  - very efficient put, get, `containsKey`
- **TreeMap**
  - nearly as efficient as HashMap, keeps keys sorted

## HASHING - HASHMAP & HASHSET ([slides](#))

hash table concept

- implement HashMap with ArrayList
- calculate hash (int) of key to determine where to store and lookup
- have the same hash for put and get that tells you where to look in the table instead of looping
  - $\text{hash} = \text{Math.abs(key.hashCode()) \% list.size()}$  → gets the hash code and mods from size

HashSet methods in detail

- add() → look up bucket corresponding to hashCode(), check if it's equal to anything in bucket

HashMap methods in detail

- put(k, v) → adds (<k, v>) to list at index hash, if key already there, update value
- get(k) → return value paired with key at index hash position of list
- containsKey(k) → check if key exists at index hash position of list

collisions

- when two different keys hash to the same position in the table
- hash table is an ArrayList of “buckets” (lists) that store multiple <k, v> pairs → chaining
- put(k, v) → add to hash index bucket, update value if key is already in bucket
- get(k) → loop over keys in hash index bucket and return the one that is equal
- ^ amortized constant time to account for rehashing and searching through the ArrayList

correct storage

- need to override equals() for the key type → otherwise cannot detect duplicates
- need hashCode() to work correctly for the key type → equals() have the same hashCode()

hashing efficiency

- runtime of get(), put(), containsKey() → time to get hash, time to search over the hash index bucket (calling equals() on everything inside)
- HashMaps are faster with more buckets bu that takes more memory
- correctness requirement: any equal() keys have the same hashCode() → not efficient

## SUHA (simple uniform hashing assumption)

- suppose we hash  $N$  pairs to  $M$  buckets
- SUHA: any given key  $k \in K$  is equally likely to be hashed to one of the  $M$  possible values, independently of what values other keys might hash to
- assuming uniform hashing, probability two random keys hash to same bucket is  $1/M$
- expected number of pairs per bucket is  $N/M$  (very likely true)
- time to get the hash is constant, but time to search over hash index “bucket” by calling `.equals()` on everything will take  $N/M$  runtime
- we face memory/runtime tradeoff with  $N$  pairs and  $M$  buckets, where...
  - if  $N \gg M$  – too many pairs in too few buckets, runtime  $N/M$  is NOT constant
  - if  $M \gg N$  – too many buckets, constant runtime but NOT memory efficient
  - usually “load factor”, or maximum  $N/M$  ratio allowed in Java is 0.75, where  $M$  is slightly bigger than  $N$ , overall constant runtime but reasonable memory usage
  - HashMap/Set resizes if load factor is exceeded

## RUNTIME EFFICIENCY ([slides](#))

ex: two methods for repeated concatenation

- using String object and + operator
  - quadratic complexity, asymptotic  $\rightarrow O(N^2)$
  - all the characters in original and concatenated section are copied over
  - grows arithmetically  $\rightarrow$  ex: input size  $2N = \text{runtime } 2t$
- vs using stringBuilder object and append()
  - linear amortized complexity
  - like an ArrayList for characters  $\rightarrow$  oversized Array that copies over when full
  - tradeoff for memory
  - grows geometrically (like ArrayList and HashMap)  $\rightarrow$  ex: input size  $2N = \text{runtime } 2t$
- Strings are an **immutable** (value cannot be changed after creation) Array of characters
- String **buffers** support mutable strings

ex: HashMaps  $\rightarrow$  designing more efficient algorithms

- NM (original) vs N+M (HashMap, only go through once) efficiency

## ASYMPTOTIC (BIG-O) ANALYSIS ([slides](#))

runtime and memory

- 2 fundamental resources
  - processor cycles: number of operations per second machine can perform
  - memory: space for storing variables, data, etc

constant time

- runtime does not depend on size of input
- ex:
  - index into an array (ar[1])
  - arithmetic, comparison
  - accessing object attribute (length)
  - ArrayList get, size, add (to end, amortized)
  - HashMap/Set get, put (amortized)
- non constant time usually includes a loop or method call

Big-O notation

- let N be the size of input
- $T(N) \rightarrow$  number of constant time operations in the code as function of N

**Definition (big O notation).**  $T(N)$  is  $O(g(N))$  if

$\lim_{N \rightarrow \infty} \frac{T(N)}{g(N)} \leq c$  for some constant  $c$  that does not depend on  $N$ .

- $T(N)$  is  $O(g(N))$  if it is at most a constant factor times slower than  $g(N)$  for large input N
- general rules

- 1. Can drop constants
  - $2N+3 \rightarrow O(N)$
  - $0.001N + 1,000,000 \rightarrow O(N)$
- 2. Can drop lower order terms
  - $2N^2+3N \rightarrow O(N^2)$
  - $N+\log(N) \rightarrow O(N)$
  - $2^N + N^2 \rightarrow O(2^N)$

- hierarchy of complexity class

Big O	Name	Example
$O(2^N)$	Exponential	Calculate all subsets of a set
$O(N^3)$	Cubic	Multiply NxN matrices
$O(N^2)$	Quadratic	Loop over all <i>pairs</i> from N things
$O(N \log(N))$	Nearly-linear	Sorting algorithms
$O(N)$	Linear	Loop over N things
$O(\log(N))$	Logarithmic	Binary search a sorted list
$O(1)$	Constant	Addition, array access, etc.

- log: cutting in size (division)
- nested loops = multiplication
- side note: consecutive nums until x sum =  $(x)(x+1)/2$
- $\text{outer}(\text{inner}(n)) \rightarrow$  big o inner(n) + big o of outer() called on return value of inner(n)