

INTRO TO COURSE ([slides](#))

what is computer science?

- systematic study of computer systems, algorithms, data, and applications/impacts
- interdisciplinary → math, engineering, empirical science, art, social science

what are algorithms?

- precise sequence of unambiguous steps that effectively compute an output given an input
- intuitive English → precise English → pseudocode → software
 - algorithm design: mathematical, logic of program, problem solving, language independent
 - implementation: semantics and syntax, language dependent, programming on a real machine

theory

- design an algorithm, analyze performance, data structure tradeoffs

practice

- write a Java program, debug/test, measure performance

data structures

- store different kinds of information in different ways, with algorithmic tradeoffs
- relates to efficiency of accessing or transforming data during operation of a program
- efficiency matters at higher scales (affects program speed)

INTRO TO JAVA ([slides](#))

Java is a compiled language

- compiled
 - studies it all at once
 - **compiler**: program that translates source code into machine code
 - run the executable, the output of the compiler
- interpreted
 - line at a time
 - **interpreter**: program that translates and runs a program line by line
 - Python is an interpreted language
- Java Virtual Machine: write and compile once, run on multiple devices

command line

Command	Meaning	Details
<code>pwd</code>	Print Working Directory	Shows the full file path to the directory you are currently in
<code>ls</code>	List Files	Shows all files and directories contained in the current directory
<code>cd</code>	Change Directory	<ul style="list-style-type: none">• <code>cd</code> by itself goes to your home directory• <code>cd directory</code> goes to the specified directory• <code>cd ..</code> goes to the enclosing directory
<code>mkdir</code>	Make Directory	<ul style="list-style-type: none">• <code>mkdir directory</code> creates a directory
<code>cp</code>	Copy	<code>cp source target</code> Copies the source file and names the result target .
<code>rm</code>	Remove	<code>rm file</code> deletes the specified file. No backups!!!

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compile and run Java

Command	Meaning	Details
javac	Compile .java files to .class files	<ul style="list-style-type: none"> • javac file.java compiles and creates file.class • javac *.java compiles all .java files in current directory to .class files.
java	Run java class files	java file executes the main method of file.class. Must have already been compiled from file.java.

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Java basics

- each Java program file contains a single class → <className>.java
- run with public static void main (PSVM) method
 - public: can call outside of class
 - static: belongs to class, not an object
 - void: no return
 - main: starting point for a program to run
 - args: allows for command- line arguments
- strongly typed

primitive types

- byte, short, int, long, float, double, boolean, char
- String objects are not primitive but you can create them without “new”

basic operators

- + - * / % < <= > >= == ! && ||

reference types

- <object type> <name> = new <constructor>();
 - **Constructor:** method that initializes objects
- variable stores a reference to an object (place in memory)
- access instance variables and method calls with “.”

Arrays

- store fixed number of entries of a single type
- `Type[] name = new Type[length]`

Strings

- hold an Array of characters → can use `toCharArray()` to `char[]`
 - characters are ordered, comparable, and correspond to integer values

Loops

- `for (int i = 0; i < num; i++) { }`
- `for (Object object : objects) { }`
- `while (boolean) { }`

Methods

- function defined in a class
- `<Object/void> methodName(<parameters>) { }`
- **dynamic methods**: called on a created object, has access to object data and arguments
 - `s.equals()`
- **static methods**: called on the class, only has access to arguments
 - `Math.sqrt()`

Java API data structures

- only store reference types (no primitives, `int` vs `Integer`)
- brief examples
 - **ArrayList**: list of values of the same type, can grow dynamically
 - **HashSet**: unordered collection, does not store duplicates

style

- comments `//` one line or `/* */` multiple lines
- informative lowerCamelCase variable and method names

- informative CapitalizedCamelCase class names
- javadoc:

```
/**
```

```
 * descriptor
```

```
 * @param/return/throws
```

```
 */
```

OBJECT-ORIENTED PROGRAMMING ([slides](#))

object-oriented: programs in that language are organized by the specification and use of objects

object: has some internal data items plus operations that can be performed on that data

class: blueprint for objects; specifies data and operations for a type of object

- objects are an instance of a class
- instance variables
- constructor: specifies how to create a new object
- . operator accesses instance variable or method of this object (on what it's called)

reasons to call a method

- side effect → what it did to an object
- return value

`equals()` (not `==` like for primitives) → `@Override` in Jdoc

- `==` → checks if these two are the same object in memory
- `equals()` without implementation → default `Object` checks if these two are the same object in memory

`Object`: default class from which all objects inherit

- you must always allocate memory and create each object

privacy

- `public`: can be accessed by code outside of class
- `private`: can only be accessed by code inside of class
- `protected`: can be access by code inside the package

immutability

- cannot change after creation (vs mutable), `Strings` are immutable

static

- belong to the class (method → called on a class, usually functional)

INTERFACES & IMPLEMENTATIONS ([slides](#))

ADT (Abstract data type): specifies what a data structure does (functionality) but not how it does it (implementation)

API (Application program interface) perspective: what methods can I call on these objects, what inputs do they take, what outputs do they return?

interface: specify a set of abstract methods that an implementing class must override and define (ADT)

- **collection:** a group of objects
 - **List:** ordered sequence of values → **ArrayList, LinkedList**
 - **Set:** unordered collection of unique values → **HashSet, TreeSet**
 - **Map:** collection that associates keys and values → **HashMap, TreeMap**
- need an implementing class at creation (`List<String> l = new ArrayList<>()`)
- implement list → public class NewList implements List
 - Must have at least all the same methods as the interface
 - As a parameter, you can just have `List<Object>` since any implementing class can use the same methods
- vs superclass → you get the implementation but not for interfaces

algorithmic tradeoffs

- efficiency of operations on data structures depends on scale

ex: ArrayList

- `get()` → direct lookup, constant (advantage)
- `contains()` → loops through Array calling `equals()`, takes longer with more size
- `size()` → returns an instance variable tracking size, constant
- `add()` → depends
 - keeps an Array with space at the end → add to open position or create new copied Array
 - space left → constant time, one Array value assignment
 - no space left → takes N array assignments, copy entire list

- how many times you have to copy an ArrayList:

Geometric growth

$$1 + 2 + 4 + \dots + N$$

$$= \sum_{i=0}^{\approx \log_2 N} 2^i$$

$$\approx 2N$$

Geometric series formula:

$$\sum_{i=0}^n ar^i = a \left(\frac{1-r^{n+1}}{1-r} \right)$$

Arithmetic growth

$$1 + 101 + 201 + \dots + N$$

$$= \sum_{i=0}^{\approx N/100} 1 + 100i$$

$$\approx \frac{N^2}{200}$$

Arithmetic series formula:

$$\sum_{i=1}^n a_i = \left(\frac{n}{2} \right) (a_1 + a_n)$$

- geometric is better for larger size, arithmetic is better for smaller size
- Java API uses geometric growth
- adding to the front of an ArrayList is NOT efficient
 - have to shift everything over
 - worst case: Array is full and must allocate space
- can use Arrays.asList and toArray to convert between List and Array

SETS & MAPS ([slides](#))

Sets

- stores unique elements, not necessarily stored in order
- usage
 - contains() → constant time efficiency
 - add() → constant time efficiency
 - remove()
 - loop with enhanced for (:)
 - addAll() to convert to and from List
- **HashSet**
 - constant time: does not depend on the number of values stored in the Set
 - very efficient add, contains
 - ex: countUniqueWords
 - HashSet → constant time operation, linear complexity
 - ArrayList → must check all the words so far for each word, quadratic complexity
 - HashSet and HashMap implemented with hash table data structure
- **TreeSet**
 - nearly as efficient as HashSet, keeps values sorted
 - TreeSet and TreeMap implemented with binary tree data structure

Maps

- interface that pairs keys with values → lookup the value with the key
- usage
 - put(k, v) → associate value v with key k, constant time efficiency
 - get(k) → gets the value with key k, constant time efficiency
 - containsKey(k) → returns if key k is in the Map, constant time efficiency

- putIfAbsent(k, v)
- check containsKey first because calling get on a key not in the Map crashes the program
- updating Maps
 - single values
 - get() returns a copy of the value
 - must use put() to update → no += directly
 - collection values
 - get() returns reference to collection
 - updates the collection directly
- **HashMap**
 - very efficient put, get, containsKey
- **TreeMap**
 - nearly as efficient as HashMap, keeps keys sorted

HASHING - HASHMAP & HASHSET ([slides](#))

hash table concept

- implement HashMap with ArrayList
- calculate hash (int) of key to determine where to store and lookup
- have the same hash for put and get that tells you where to look in the table instead of looping
 - $\text{hash} = \text{Math.abs}(\text{key.hashCode()}) \% \text{list.size()}$ → gets the hash code and mods from size

HashSet methods in detail

- add() → look up bucket corresponding to hashCode(), check if it's equal to anything in bucket

HashMap methods in detail

- put(k, v) → adds (<k, v>) to list at index hash, if key already there, update value
- get(k) → return value paired with key at index hash position of list
- containsKey(k) → check if key exists at index hash position of list

collisions

- when two different keys hash to the same position in the table
- hash table is an ArrayList of "buckets" (lists) that store multiple <k, v> pairs → chaining
- put(k, v) → add to hash index bucket, update value if key is already in bucket
- get(k) → loop over keys in hash index bucket and return the one that is equal
- ^ amortized constant time to account for rehashing and searching through the ArrayList

correct storage

- need to override equals() for the key type → otherwise cannot detect duplicates
- need hashCode() to work correctly for the key type → equals() have the same hashCode()

hashing efficiency

- runtime of get(), put(), containsKey() → time to get hash, time to search over the hash index bucket (calling equals() on everything inside)
- HashMaps are faster with more buckets but that takes more memory
- correctness requirement: any equal() keys have the same hashCode() → not efficient

SUHA (simple uniform hashing assumption)

- suppose we hash N pairs to M buckets
- SUHA: any given key $k \in K$ is equally likely to be hashed to one of the M possible values, independently of what values other keys might hash to
- assuming uniform hashing, probability two random keys hash to same bucket is $1/M$
- expected number of pairs per bucket is N/M (very likely true)
- time to get the hash is constant, but time to search over hash index “bucket” by calling `.equals()` on everything will take N/M runtime
- we face memory/runtime tradeoff with N pairs and M buckets, where...
 - if $N \gg M$ – too many pairs in too few buckets, runtime N/M is NOT constant
 - if $M \gg N$ – too many buckets, constant runtime but NOT memory efficient
 - usually “load factor”, or maximum N/M ratio allowed in Java is 0.75, where M is slightly bigger than N , overall constant runtime but reasonable memory usage
 - HashMap/Set resizes if load factor is exceeded

RUNTIME EFFICIENCY ([slides](#))

ex: two methods for repeated concatenation

- using String object and + operator
 - quadratic complexity, asymptotic $\rightarrow O(N^2)$
 - all the characters in original and concatenated section are copied over
 - grows arithmetically \rightarrow ex: input size $2N$ = runtime $2t$
- vs using stringBuilder object and append()
 - linear amortized complexity
 - like an ArrayList for characters \rightarrow oversized Array that copies over when full
 - tradeoff for memory
 - grows geometrically (like ArrayList and HashMap) \rightarrow ex: input size $2N$ = runtime $2t$
- Strings are an **immutable** (value cannot be changed after creation) Array of characters
- String **buffers** support mutable strings

ex: HashMaps \rightarrow designing more efficient algorithms

- NM (original) vs $N+M$ (HashMap, only go through once) efficiency

ASYMPTOTIC (BIG-O) ANALYSIS ([slides](#))

runtime and memory

- 2 fundamental resources
 - processor cycles: number of operations per second machine can perform
 - memory: space for storing variables, data, etc

constant time

- runtime does not depend on size of input
- ex:
 - index into an array (ar[1])
 - arithmetic, comparison
 - accessing object attribute (length)
 - ArrayList get, size, add (to end, amortized)
 - HashMap/Set get, put (amortized)
- non constant time usually includes a loop or method call

Big-O notation

- let N be the size of input
- $T(N) \rightarrow$ number of constant time operations in the code as function of N

Definition (big O notation). $T(N)$ is $O(g(N))$ if

$\lim_{N \rightarrow \infty} \frac{T(N)}{g(N)} \leq c$ for some constant c that does not depend on N .

- $T(N)$ is $O(g(N))$ if it is at most a constant factor times slower than $g(N)$ for large input N
- general rules

1. Can drop constants

- $2N+3 \rightarrow O(N)$
- $0.001N + 1,000,000 \rightarrow O(N)$

2. Can drop lower order terms

- $2N^2+3N \rightarrow O(N^2)$
- $N+\log(N) \rightarrow O(N)$
- $2^N + N^2 \rightarrow O(2^N)$

- hierarchy of complexity class

Big O	Name	Example
$O(2^N)$	Exponential	Calculate all subsets of a set
$O(N^3)$	Cubic	Multiply NxN matrices
$O(N^2)$	Quadratic	Loop over all <i>pairs</i> from N things
$O(N \log(N))$	Nearly-linear	Sorting algorithms
$O(N)$	Linear	Loop over N things
$O(\log(N))$	Logarithmic	Binary search a sorted list
$O(1)$	Constant	Addition, array access, etc.

- log: cutting in size (division)
- nested loops = multiplication
- side note: consecutive nums until x sum = $(x)(x+1)/2$
- $\text{outer}(\text{inner}(n)) \rightarrow \text{big o inner}(n) + \text{big o of outer}()$ called on return value of inner(n)