Lighting Cheatsheet

1 Definitions

incident light: light hitting surface of object

directional light: light with a uniform direction and intensity

point light: light with a location, direction and intensity depend on relative location and distance

2 Light Sources

 l_s : intensity (RGB) of specular component of light from light source l l_d : intensity (RGB) of diffuse component of light from light source l l_a : intensity (RGB) of ambient component of light from light source l a: intensity (RGB) of ambient light

- uniform for entire scene
- base ambient light for scene plus sum of all l_a from individual light sources

 r_l : "radius"; distance from light source l to fragment, only applicable to point point lights

3 Materials

 $\boldsymbol{m_s}$: specular reflection constant of material \boldsymbol{m}

- ratio of incident light reflected specularly
- may be a single constant, or a (red, greenblue) triple

 m_d : diffuse reflection constant of material m

- ratio of incident light reflected diffusely
- may be a single constant, or a (red, greenblue) triple

 m_a : ambient reflection constant of material m

- ratio of ambient light reflected
- may be a single constant, or a (red, greenblue) triple

 α : shininess constant

- higher for smoother, more mirror-like surfaces
- lower for rougher, duller surfaces
- high α means small, bright specular reflection
- \bullet low α means large dim specular reflection

C: color (RGB) of surface

- if m_s , m_d and m_a are (RGB) triples, this is redundant and is not used
- for textured models, often m_s , m_d and m_a are single constants, and C is sampled from a texture and used with illumination (defined below) to determine displayed fragment color

4 Spacial Factors

 S_l : normalized vector pointing toward light source l from surface

- if l is a directional light, S_l is just the negation of l's light direction
- if l is a point light, S_l is the unit vector from the surface toward the light source (i.e. lightPosition fragPosition, normalized)

N : surface normal

 R_l : direction of light from S_l , perfectly reflected off of surface:

$$2(S_l \cdot N)N - S_l$$

 $oldsymbol{V}$: normalized direction from surface to viewer / camera

5 Putting it all together

D: set of all directional light sources

P: set of all point light sources

I: illumination (RGB) on surface:

$$I = m_a a + \sum_{l \in D} \left(m_d (S_l \cdot N) l_d + m_s (R_l \cdot V)^{\alpha} l_s \right) + \sum_{l \in D} \frac{\left(m_d (S_l \cdot N) l_d + m_s (R_l \cdot V)^{\alpha} l_s \right)}{\max(r_l^2, 1)}$$

- if m_s , m_d and m_a are (RGB) vectors, use the Hadamard product to multiply them by other vectors
- otherwise, just use scalar multiplication

FragColor: color displayed from illiumination I on surface with color C

- if material components are single constants: $FragColor = (I_rC_r, I_qC_q, I_bC_b)$
- if material components are colors: FragColor = I