

practice final 2a

prove that  $\log^2(n) \in o(n^{1/2})$

if  $\lim_{n \rightarrow \infty} \frac{f(n)}{g(n)} = 0$ , then  $f(n) \in o(g(n))$

$$\lim_{n \rightarrow \infty} \frac{\log^2(n)}{n^{1/2}} = \lim_{n \rightarrow \infty} \frac{2 \log(n) \cdot \frac{1}{n \ln 2}}{\frac{1}{2n^{1/2}}}$$

$$= \lim_{n \rightarrow \infty} 4 \log n \cdot \frac{n^{1/2}}{n \ln 2}$$

$$= \lim_{n \rightarrow \infty} \frac{4}{\ln 2} \cdot \frac{\log n}{n^{1/2}}$$

$$= \lim_{n \rightarrow \infty} \frac{4}{\ln 2} \cdot \frac{\frac{1}{n \ln 2}}{\frac{1}{2n^{1/2}}}$$

$$= \lim_{n \rightarrow \infty} \frac{8n^{1/2}}{n(\ln 2)^2} = \lim_{n \rightarrow \infty} \frac{8}{(\ln 2)^2} \cdot \frac{1}{n^{1/2}} = \underline{0}$$

So  $\log^2(n) \in o(n^{1/2})$

Practice exam q3

# of edges + # nodes even in a forest  
is this possible

forest:  $T_1$   $T_2$   
• •

# nodes : 2

# edges : 0

So edges + nodes : 2 → even

double nested loop invariant

"no invariants on final"

practice Final 6a

	0	1	2	3	4	5	6
0	0	0	0	0	1	1	1
1	0	0	1	1	0	0	0
2	0	1	0	1	1	1	0
3	0	1	1	0	1	0	1
4	1	0	1	1	0	1	1
5	1	0	1	0	1	0	0
6	1	0	0	1	1	0	0

practice Final 3b

1 node



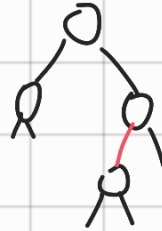
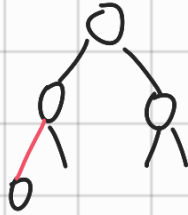
2:



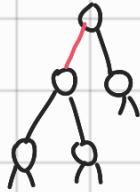
3:



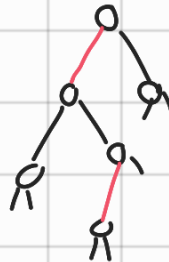
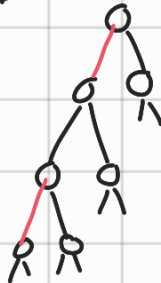
4:



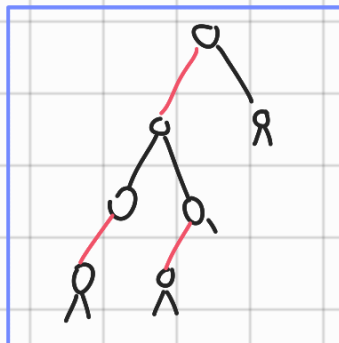
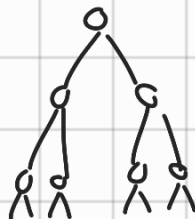
5:



6:

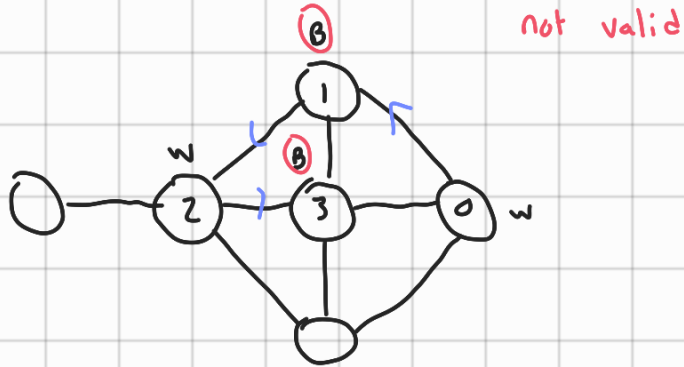


7:



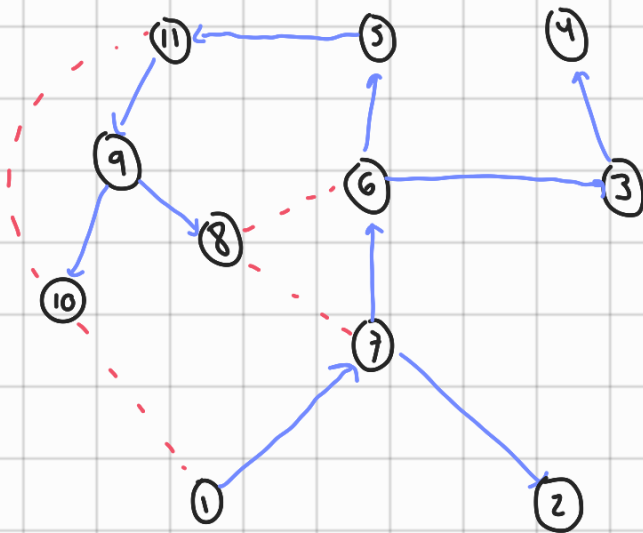
practice Final 8

DFS, BFS  $\in O(n \cdot m)$

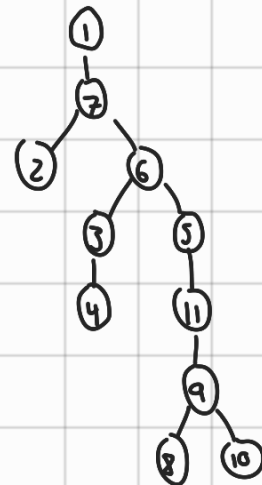


practice Final 7c

postorder: [2 4 3 8 10 9 11 5 6 7 1]



corresponding tree:



practice final 7a

bfs: [ 1 7 10 2 6 8 9 11 3 5 4 ]

