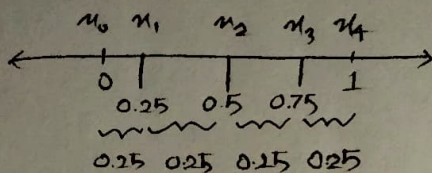


Q4 : Given, the domain of integration is  $[0, 1]$

①

Dividing it into 4 intervals, we get,



$$\Delta x = 0.25 = \frac{1}{4}$$

$$\begin{aligned} x_0 &= 0 \\ x_1 &= 0.25 \\ x_2 &= 0.5 \\ x_3 &= 0.75 \\ x_4 &= 1 \end{aligned}$$

② Given,  $\int_0^1 x e^{x^2} dx$

According to Simpson's rule,  $\int_a^b f(x) dx = \frac{\Delta x}{3} [f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + f(x_4)]$

$$\begin{aligned} \text{Now, } & \frac{\Delta x}{3} [f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + f(x_4)] \\ &= \frac{0.25}{3} \left[ 0e^{0^2} + 4(0.25)e^{(0.25)^2} + 2(0.5)e^{(0.5)^2} + 4(0.75)e^{(0.75)^2} + (1)e^{(1)^2} \right] \end{aligned}$$

$$= 0.7868026435 \approx 0.79$$

(Ans)