201909 M122 A01 Q6 Solns.

1. No. If $y = \frac{1}{x} + 2$ then we must have $x = \frac{1}{(y-2)}$.

There is no x such that f(x) = 2.

2. a) By inspection, f is 1-1 and into . :. f is invertible

b) α 1 2 3 4 5 6 f(f(x)) 6 4 1 5 2 3 f(f(x)) We have $f(\alpha) = y \iff f(f(x)) = x$ i. $f^{-1} = f(x)$.

- 3. Since R is reflexive (1,1), (2,2), $(3,3) \in \mathbb{R}$ Since (2,1), $(1,3) \in \mathbb{R}$ we have $(2,3) \in \mathbb{R}$ by transitivity: (1,2), (3,1), $(3,2) \notin \mathbb{R}$ by anti-symmetry. $\mathbb{R} = \{(1,1), (2,2), (3,3), (2,1), (1,3), (2,3)\}$.
- 4. a) reflexive: the product of the digits of x is the same as the product of the digits of x: R is reflexive
 - Symmetric: Suppose the product of the digits of x is the same as the product of the digits of y. Then the product of the digits of y is the same as the product of the digits of x i. R is symmetric.

transitive: Suppose the product of the digits of x equals the product of the digits of y and the product of the digits of y equals the product of the digits of X equals the product of the digits of X equals the product of the digits of X equals the product of the digits of Z. R is transitive.

is R 13 an equivalence relation

b) # equivalence classes = # different products
[20] [21], [29], [34], [35], [39] [44], [45], [47],
[48], [49], [55], [56], [57] cover the possible products

:. 24 défférent équisalence classes

gof is the identity function, :. it is i-1. but g is not i-1 because g(z) = g(3) and $z \neq 3$.

b. True. A= Zt, which is countable

c. True (0,1) is un countable, so any set that contains (0,1) as a subset is un countable.

d. True. For example of is always a subset, and