Math 101 Tutorial Worksheet 7

There is an associated quiz due on BrightSpace on Tuesday, March 8 at 10:00 PM

1. Which of the following series converge, and which diverge?

(a)
$$\sum_{n=1}^{\infty} \frac{2^n + 3^n}{3^n + 4^n}$$

(b)
$$\sum_{n=1}^{\infty} (-1)^n \left(\sqrt{n^2 + n} - n \right)$$

(c)
$$\sum_{n=1}^{\infty} \frac{\sqrt{n}}{n^2 + 1}$$

(d)
$$\sum_{n=1}^{\infty} (-1)^n \frac{n^n}{(2^n)^3}$$

(e)
$$\sum_{n=1}^{\infty} \frac{(-100)^n}{n!}$$

(f)
$$\sum_{n=1}^{\infty} \left(1 - \frac{1}{3n}\right)^n$$

(g)
$$\sum_{n=1}^{\infty} \frac{n2^n(n+1)!}{(3^n) \, n!}$$

(h)
$$\sum_{n=1}^{\infty} \frac{1}{1+2^2+3^2+\cdots+n^2}$$

2. Do the following series $\sum_{n=1}^{\infty} a_n$ converge or diverge?

(a)
$$a_1 = 3, a_{n+1} = \left(\frac{n}{n+1}\right) a_n$$

(b)
$$a_1 = 1, a_{n+1} = \left(\frac{1 + \tan^{-1} n}{n}\right) a_n$$