Table of Trigonometric Identities

Basic Identities

•
$$\cos^2(\theta) + \sin^2(\theta) = 1$$

•
$$\tan^2(\theta) + 1 = \sec^2(\theta)$$

•
$$\sin(2\theta) = 2\sin(\theta)\cos(\theta)$$

•
$$\cos(2\theta) = \cos^2(\theta) - \sin^2(\theta)$$

Half Angle Identities

•
$$\sin^2(\theta) = \frac{1 - \cos(2\theta)}{2}$$

•
$$\cos^2(\theta) = \frac{1 + \cos(2\theta)}{2}$$

Ptolemy's Identities

•
$$\sin(A+B) = \sin(A)\cos(B) + \cos(A)\sin(B)$$

•
$$cos(A + B) = cos(A)cos(B) - sin(A)sin(B)$$

•
$$\tan(A+B) = \frac{\tan(A) + \tan(B)}{1 - \tan(A)\tan(B)}$$

Product to Sum

•
$$\sin(A)\sin(B) = \frac{1}{2}\cos(A-B) - \frac{1}{2}\cos(A+B)$$

•
$$\cos(A)\cos(B) = \frac{1}{2}\cos(A-B) + \frac{1}{2}\cos(A+B)$$

•
$$\sin(A)\cos(B) = \frac{1}{2}\sin(A-B) + \frac{1}{2}\sin(A+B)$$

Even and Odd Properties

•
$$\sin(-\theta) = -\sin(\theta)$$

•
$$\cos(-\theta) = \cos(\theta)$$

•
$$\tan(-\theta) = -\tan(\theta)$$

Reflections

•
$$\sin\left(\frac{\pi}{2} - \theta\right) = \cos(\theta)$$
 and $\sin(\pi - \theta) = \sin(\theta)$

•
$$\cos\left(\frac{\pi}{2} - \theta\right) = \sin(\theta)$$
 and $\cos(\pi - \theta) = -\cos(\theta)$

•
$$\tan\left(\frac{\pi}{2} - \theta\right) = \cot(\theta)$$
 and $\tan(\pi - \theta) = -\tan(\theta)$