

Exercise A.7**L Answer (a).**

We are given the function

$$x_1(t) = e^{jat} + e^{jbt},$$

where a and b are real constants. The right-hand side of this equation can be expressed in terms of the cosine function by pulling out a factor of e^{jct} , where c is the **average of a and b** (i.e., $c = \frac{1}{2}(a+b)$). We have

$$\begin{aligned} x_1(t) &= e^{jat} + e^{jbt} \\ &= e^{j[(a+b)/2]t} \left(e^{j[(a-b)/2]t} + e^{-j[(a-b)/2]t} \right) \\ &= e^{j[(a+b)/2]t} \left(2 \cos \left[\frac{1}{2}(a-b)t \right] \right) \\ &= 2e^{j(a+b)t/2} \cos \left[\frac{1}{2}(a-b)t \right]. \end{aligned}$$

factor out $e^{j(a+b)/2}$
 $e^{j\theta} + e^{-j\theta} = 2 \cos \theta$
 move 2 out front