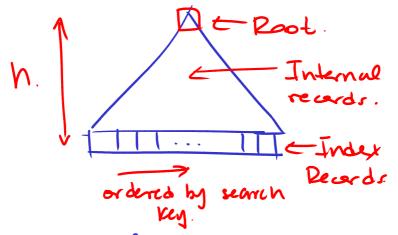
Indexer.

B+-tree

- · Atomakically Balanud
- · Finder reards are at the leaves

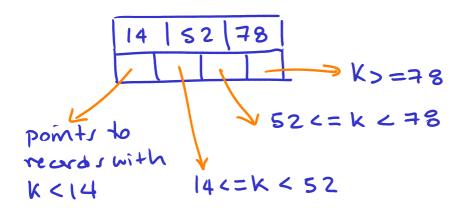


- · Every record is a block.
- · Index records form a list
- . They can be traversed in the order of the search key

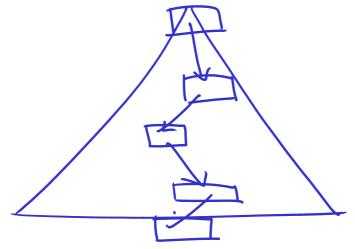
Internal records

 Example.

Assume n = 3



Index is traversed from not to leaf



We assume noot is always in memory hence, to reach the leaf we read h blocks. Cost of index:

· Cost of reaching the leafs

· Cost of reading the matching records.

Example:

1) Asame Pla, b)

To = 5 R

Only one or zero matching tyle:

⇒ We must traverse the index h

rhe leaf either cantains a = 5 or not

Got of index = h of index.

2) Jazo R

What if all types match?

· We traverse index (cast h)

Reads first leaf.

· We must read all leaves of index

Cost of index = h + # leaver -1

To be able to compute the cost of an index we need:

Calalate # of leaf blocks of index proportional to # index records per block.

of index records depends your a) type of index Sparse ss. Dense

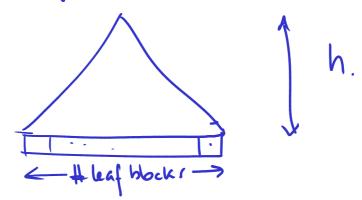
b) Number of types in Rel.

index reards per block depends upon:

- a) size of search lay
- b) occupancy rate =) How much waste space is there in the index (to keep it balanced).

We assume that occupancy rate of inner rodes and leaves is the same as internal nodes.

Hence, height of tree depends upon # of leaf records.



n = max number of Keys per record.

fill = occupancy rate (between 0-1,
but usally around 1/2 to 3/4)

#leaf blocks = # index records

no fill

For h, we simplify calculations:

h = logn.fill (#Index records)

Example:

Assume
$$n = 150$$
, $fill = \frac{2}{3}$

How many index records can we store in an index of height 1,2,3,4,5,6.

Let is wary about max # index leards

h # index Pecard (

1 100 =
$$10^2$$

2 100² = 10^4

3 100³ = 10^6

4 100⁵ = 10^{10}

With 5 block reads we can find a leaf with a given search key in an index of 10 giga-records!!

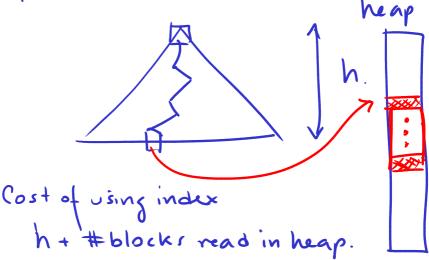
How many search lays do we need to store?

- · Sparse index: B(R)
- · Dense index: [R]

Sparse index is marginally shorter than dense index.

Cost of Using an Index

Sparce Index.



- · We only read one record in index
- · We read 1 or more blocks from heap

Example.

a)
$$\sigma_{a=s} R$$

if type exists: cost = h+1.

if type does not exist: cost = h.

b) $\sigma_{a>10} R$

Assume 50% of tiples match avery:

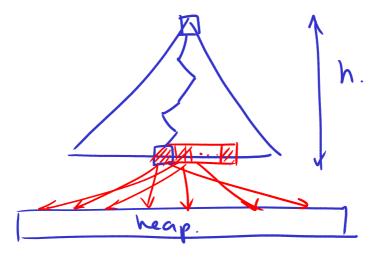
$$\Rightarrow$$
 We must scan 50% of sorted heap.
Cost = h + $\frac{B(R)}{R}$

$$B(R) = \frac{10^6}{10} = \frac{10^5}{2}$$

Cost = 3 + 10 ≥ bb cks. ≈ 105/2

8

Dense Index.



Cost:

- · Traverse tree to first leaf: h · Might need to read Ø or more leafs.
- · For every type in result, read one block.

Example.

$$R(a,b)$$
 $|R| = 10^6$ tuples.
heap: 10 tuples per block
Dense index on $R(a)$
Effective index records per block: 100
 $h = 4$ $|B| = 10^5$ blocks.

a)
$$\int_{a=s}^{a} R$$

if type exists: cost = h+1.

if type does not exist: cost = h.

Same as sparse!!.

b) Ta>10 R Assume 50% of types match.



We need to scan 50% of them.

#bbck/ in index =
$$\left[\frac{\# \text{ matching types}}{\text{n. fill}}\right]$$

= $\frac{.5 \cdot 10^6}{10^2} = .5 \cdot 10^4$

Cost =
$$h - 1 + 0.5 \cdot 10^4 + 10^6$$

 $\approx 10^6!!$

Approximately 10 times more than Sparse index!!

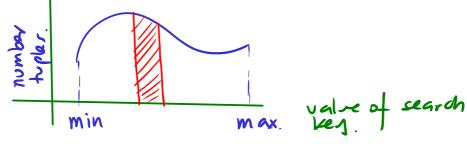
How do we know how many tipler match a given greny?

selectivity (p) = probability that a type in R matches predicate P.

Selectivity of matching a primary key:

Selection of matching a nonprimary vey:

We need a distribution.



We need to compute proportion of the tuples that match the predicate.

Example:

a mitem distribution at · Assume valer of b, min 1, max 100.

Selection (6>20) =
$$\frac{79}{100}$$

Selection (b>20 and b<30) =
$$\frac{9}{100}$$

Selection (b>200) = \emptyset