

University of Victoria Exam 1 Fall 2021

Course Name: ECE 260

Course Title: Continuous-Time Signals and Systems

Section(s): A01, A02

CRN(s): A01 (CRN 10971), A02 (CRN 10972)

Instructor: Michael Adams

Duration: 50 minutes

Family Name: DRAIL

Given Name(s): STEPHEN

Student Number: V00 717907

63

25

This examination paper has 8 pages, all of which are numbered.

Students must count the number of pages in this examination paper before beginning to write, and report any discrepancy immediately to the invigilator.

All questions are to be answered on the examination paper in the space provided.

Total Marks: 25

This examination is closed book.

The use of a crib sheet is not permitted.

The use of a calculator is not permitted.

You must show all of your work!

You must clearly define any new quantities introduced in your answers (such as variables, functions, operators, and so on).

Question 1.

Consider the function f given by $f(z) = \frac{(z^2 - 2z)^2}{(z^2 + 2z + 1)^4}$, where z is complex.

(A) Find the (finite) poles and zeros of f as well as their corresponding orders. Show all of your work and do not skip any steps in your answer. [3 marks]

$$f(z) = \frac{(z - 2)^2}{((z+1)^2)^4} = \frac{z^2 (z-2)^2}{(z+1)^8}$$



(B) Determine the points at which f is analytic. [1 mark]

Since f is a cational function, it is order every whose except where the denominator is 0, is 25-1

Question 2. Using the MATLAB programming language, write a function called my func that takes a single real value x as a parameter and returns the real value y, where

$$y = \begin{cases} \sum_{n=0}^{50} (-1)^n x^n & \text{if } -1 < x < 1\\ 0 & \text{otherwise.} \end{cases}$$

Your code must use proper indentation and must not exceed 15 lines in length. Be sure to use correct syntax in your answer, since syntax clearly matters here. [2 marks]

Line #	Line of Code
1	function my func.
2	if((×21)/1(×4-1))
3	return o j
4	ebe.
5	for NO ! 1 : 56 4-00
6	y=y+(1).1(n).x.1(n),
7	
8	1 / 27
9	
10	
11	
12	
13	
14	
15	40

Question 3. Consider the (single-input single-output) system associated with the operator \mathcal{H} .

(A) State, in mathematical terms, the condition that must be satisfied for \mathcal{H} to be linear. You must use operator notation (e.g., do not use arrow notation). You must fully define all quantities (e.g., variables and constants) appearing in your answer and be specific about what values they can take. Failure to do so will likely result in a mark of zero on this question. [2 marks]

H{a,x, +a,x,}(t) = a,)-|x,(t) + a, H x, (t)

a, a, a, ane 3 calar valuer, ta, a, a & R

tin He independent variable

X, y, are need functions f, for & R

H system applied or RR -> RR

(B) Suppose now that $\Re x(t) = 2x(t) - 1$. Using the condition stated in your answer to part (a) of this question, determine whether \Re is linear. [2 marks]

$$\frac{\mathcal{H}_{q,X,+} + a_{2} \times_{2} \mathcal{J}(f) = 2 (a_{1} \times_{1} + a_{2} \times_{2})(f) - 1}{= 2a_{1} \times_{1}(f) + 2a_{2} \times_{2}(f) - 1}$$

$$= 2a_{1} \times_{1}(f) + 2a_{2} \times_{2}(f) - 1$$

$$+ \alpha_{1} \mathcal{H}_{x_{1}}(f) + 2a_{2} \mathcal{H}_{x_{1}}(f) = a_{1} (2 \times_{1}(f) - 1) + a_{2} (2 \times_{2}(f) - 1)$$

$$= 2a_{1} \times_{1}(f) - a_{1} + 2a_{2} \times_{2}(f) - a_{1}$$

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$$= 2a_{1} \times_{1}(f) - a_{2} \times_{2}(f) - a_{2}$$

$$= 2a_{1} \times_{1}(f) -$$

stion 4. Consider the function x, given by

$$x(t) = \int_{-\infty}^{t+1} e^{-\tau} \delta(\tau) d\tau + \int_{0}^{20} \tan(\tau) \delta(\tau+1) d\tau + \int_{-\infty}^{\infty} t^{2} \sin(\tau) \delta\left(\tau - \frac{\pi}{2}\right) d\tau.$$

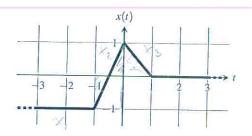
If a fully-simplified expression for x(t). Show all of your work and do not skip any steps in your answer. [4 marks]

$$X(f) = X_1(f) + X_2(f) + X_2(f)$$

= $1 + t^2 + t \ge -1$
= $t^2 + t \le -1$

Question 5.

Consider the function x shown in the figure. Write an expression for x(t) that consists of only a single case and is valid for all t. [Note that x(t) = -1 for all t < -1 and x(t) = 0 for all t > 1.] Show all of your work and do not skip any steps in your answer. [4 marks]



$$X(t) = X_{1}(t) + X_{2}(t) + X_{5}(t)$$

 $X_{1}(t) = (-1)(1 - u(t+1))$

$$(x_3(t)) = (-x+i)(u(t) - u(t-i))$$

Ouestion 6.

A function x (of a real variable) has the following properties:

- 2. the function ν is causal, where $\nu(t) = x(t-1)$; and $\nu(t) = 0$, $\nu(t) = 0$
- 3. the function w is odd, where w(t) = x(t) + 1.

Find x(t) for all t. You must make clear how you arrived at your answer. Show all of your work and do not skip any steps in your answer. [5 marks]

21 V is convel =
$$V(t)=0$$
, $t<0$
 $\Rightarrow x(t-1)=0$, $f<0$
 $\Rightarrow x(t)=0$, $f<0$
 $\Rightarrow x(t)=0$, $f<0$
 $\Rightarrow x(t)=0$
 $\Rightarrow x(t)=0$

$$X(t) = (t-1)(u(t) - u(t-1))$$
 $+ (t)(u(t+1 - u(t)))$
 $\times (t)(u(t+1 - u(t)))$
 $\times (t)(u(t+1 - u(t)))$

Question 7.

A system \mathcal{H} is defined by the equation $\mathcal{H}x(t) = \mathcal{D}x(t)$, where \mathcal{D} denotes the derivative operator (e.g., for $y(t) = t^2$, $\mathcal{D}y(t) = 2t$). For each function x given below, determine if x is an eigenfunction of \mathcal{H} , and if it is, state its corresponding eigenvalue.

(a) $x(t) = \cos(t)$; and

(b) $x(t) = \pi$.

Show all of your work and do not skip any steps in your answer. [2 marks]

21 evilo

 $\mathcal{H} = \lambda \times$

a) $H_{X(I)}^{-} = \sin(t) = \chi(t) \cdot (-\tan(t))$, since $-\tan(t)$ is not constant χ is not on Eugenfunction

(b) Tr(x(t) = 0 = 0 x(t) =) x is an eigenfunction with corresponds eigenvalue 0.

(2)