## Fall 2012 CENG 355

## Solution 3

1.

(a) Direct-mapped: 3-bit **Block = A\_{5-3}**, 1-bit **Word = A\_2**; miss rate = 10/12.

| Tag | Word 1 | Word 0 | _       |
|-----|--------|--------|---------|
| 00  | [04]   | [00]   | Block 0 |
| 00  | [OC]   | [80]   | Block 1 |
|     |        |        | Block 2 |
|     |        |        | Block 3 |
| 10  | [A4]   | [AO]   | Block 4 |
| 10  | [AC]   | [A8]   | Block 5 |
|     |        |        | Block 6 |
|     |        |        | Block 7 |

(b) 4-way set-associative: 1-bit  $\mathbf{Set} = \mathbf{A_3}$ , 1-bit  $\mathbf{Word} = \mathbf{A_2}$ ; miss rate = 6/12.

| Tag  | Word 1 | Word 0 |       |
|------|--------|--------|-------|
| 1000 | [84]   | [80]   | Set 0 |
| 1010 | [A4]   | [A0]   | Set 0 |
| 0000 | [04]   | [00]   | Set 0 |
|      |        |        | Set 0 |
| 1000 | [8C]   | [88]   | Set 1 |
| 1010 | [AC]   | [A8]   | Set 1 |
| 0000 | [OC]   | [80]   | Set 1 |
|      |        |        | Set 1 |

(c) Fully-associative: 1-bit **Word = A\_2**; miss rate = 6/12.

| Tag   | Word 1 | Word 0 |
|-------|--------|--------|
| 10001 | [8C]   | [88]   |
| 10000 | [84]   | [80]   |
| 10100 | [A4]   | [A0]   |
| 10101 | [AC]   | [A8]   |
| 00001 | [OC]   | [80]   |
| 00000 | [04]   | [00]   |
|       |        |        |
|       |        |        |

2.

(a)

| Tag | Word 3 | Word 2 | Word 1 | Word 0 | _       |
|-----|--------|--------|--------|--------|---------|
| 10  | [8C]   | [88]   | [84]   | [80]   | Block 0 |
| 00  | [1C]   | [18]   | [14]   | [10]   | Block 1 |
| 10  | [AC]   | [A8]   | [A4]   | [AO]   | Block 2 |
|     |        |        |        |        | Block 3 |

Miss rate = 6/16

(b)

| Tag | Word 3 | Word 2 | Word 1 | Word 0 | _     |
|-----|--------|--------|--------|--------|-------|
| 101 | [AC]   | [A8]   | [A4]   | [AO]   | Set 0 |
| 100 | [8C]   | [88]   | [84]   | [80]   | Set 0 |
| 000 | [1C]   | [18]   | [14]   | [10]   | Set 1 |
|     |        |        |        |        | Set 1 |

Miss rate = 7/16

(c)

| Tag  | Word 3 | Word 2 | Word 1 | Word 0 |
|------|--------|--------|--------|--------|
| 0000 | [OC]   | [80]   | [04]   | [00]   |
| 1010 | [AC]   | [A8]   | [A4]   | [A0]   |
| 1000 | [8C]   | [88]   | [84]   | [80]   |
| 0001 | [1C]   | [18]   | [14]   | [10]   |

Miss rate = 4/16

3.

$$T_{ave} = h_1C_1 + (1-h_1)C_2 + (1-h_1)(1-h_2)M = 7.2\tau - 4.8h_2.$$

If  $h_2 = 1$  (i.e., 100% hit rate), then  $T_{ave} = 2.4\tau$  (minimum).

If  $T_{ave}$  =  $4\tau$ , then  $h_2$  = 2/3 (i.e., 67% hit rate).