ELEC360 Control Theory & Systems I

Midterm Exam

Date: 20-October-2017 Time: 09:30 to 10:20 AM

Venue: ECS 125 Duration: 50 minutes

Instructions:

- 1) Please write your V number in the answer booklet.
- 2) Please verify if your question paper has 4 pages including this page.
- 3) Please use only non-programmable scientific calculators.
- 4) No formula sheet or aid sheet is allowed.
- 5) Please refrain from writing anything on the question paper.
- 6) Please return only the answer sheet at the end of the exam. You can carry the question paper with you.
- 7) Please be seated in your place (even after submitting your answer sheet) until an announcement is made to disperse.
- 8) Please answer all questions given in the three sections.
 - (i) Section A comprises of six questions each of 1 mark.
 - (ii) Section B comprises of two questions each of 4 marks.
 - (iii) Section C comprises of one question of 6 marks.
- 9) For Section A, please write only the question number and the option letter

Section A $\underline{6 \times 1 = 6 \text{ marks}}$

1) Unit step response of a first order system is shown in Figure 1. The transfer function of the system is in the form $\frac{K}{sT+1}$, where K is the gain and T is the time constant of the system. Then the approximate value of time constant T is:

(1 mark)

(a) T = 1 second;

(b) T = 4 seconds;

(c) T = 18 seconds;

(d) T = 6 seconds;

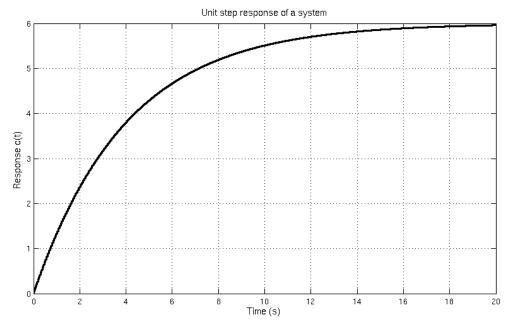


Figure 1. Unit step response of a system

2) Unit impulse response of a linear time invariant system for $t \ge 0$ is given by the equation $c(t) = \frac{1}{T}e^{-t/T}$, where T is the time constant of the system. Then the unit step (unit step input is the integral of unit impulse input) response of the system is:

(1 mark)

(a)
$$1 - e^{-t/T}$$

(b)
$$1 - Te^{-t/T}$$

(c)
$$e^{-t/T}$$

(d)
$$1 - \frac{1}{T}e^{-t/T}$$

3) The characteristic polynomial of a closed loop system is found to be $s^5 + 2s^4 + 3s^2 + 4s + K$. Find the range of K for which the system is stable

(1 mark)

(a) K > 0

(b) 2 > K > 0

(c) 2 < K < 0

- (d) None of the above
- 4) Unit step responses of a second order system for different damping ratio are given in Figure 2. If ζ_1 and ζ_2 correspond to damping ratio 1 and damping ratio 2 respectively, then which of the following is true?

(1 mark)

(a) $\zeta_1 > 0$; $\zeta_2 > 0$; $\zeta_2 > \zeta_1$

(b) $\zeta_1 > 0$; $\zeta_2 > 0$; $\zeta_1 > \zeta_2$

(c) $\zeta_1 > 0$; $\zeta_2 > 0$; $\zeta_2 = \zeta_1$

(d) None of the above

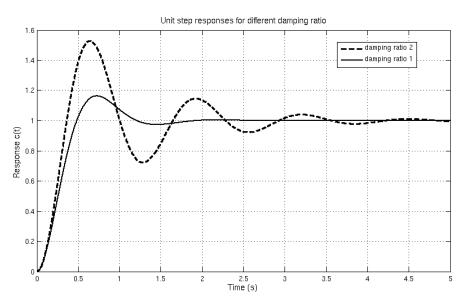


Figure 2. Unit step responses of a system for different damping ratio

5) Closed loop transfer function of a system is given by the equation

$$\frac{C(s)}{R(s)} = \frac{s+3}{(s+1)(s+2)}$$

If it is known that the Laplace transform of impulse signal is unity and the Laplace transform of $e^{-at} = \frac{1}{s+a}$ then the unit impulse response c(t) is given by:

(1 mark)

(a)
$$e^{-2t} - 2e^{-t}$$

(b)
$$e^{-t} - 2e^{-2t}$$

(c)
$$2e^{-t} - e^{-2t}$$

(d)
$$2e^{-2t} - e^{-t}$$

6) Differential equation representation of a spring-mass-dashpot system is given below $m\frac{d^2y}{dt^2} + b\frac{dy}{dt} - b\frac{du}{dt} + ky - ku = 0$

Symbols m, b, k are system constants while y is the desired output and u is the input. Then the transfer function representation of the system assuming zero initial conditions is given by

(1 mark)

(a)
$$\frac{ks+b}{ms^2+ks+b}$$

(b)
$$\frac{ms^2+ks+b}{ks+b}$$

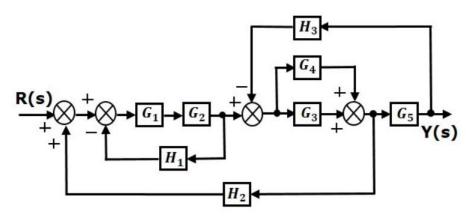
(c)
$$\frac{ms^2+ks+b}{bs+k}$$

(d)
$$\frac{bs+k}{ms^2+bs+k}$$

Section B $2 \times 4 = 8 \text{ marks}$

7) Reduce the block diagram to obtain the transfer function Y(s)/R(s)

(4 marks)



8) Feedforward transfer function of a system is given as $G(s) = \frac{k(s+3.15)}{s(s+1.5)(s+0.5)}$. Compute the steady state error for unit ramp input assuming unity negative feedback. (4 marks)

Section C $1 \times 6 = 6 \text{ marks}$

9) Plot the root locus of a system whose open-loop transfer function is given by the expression $G(s)H(s) = \frac{K(s+0.5)}{(s+2)(s+4)(s+6)}$. Also, mark the breakaway or break-in points, intersection point of asymptotes and angles of asymptotes. Further, from the root locus, comment on the range of K for which the closed loop system would be stable.