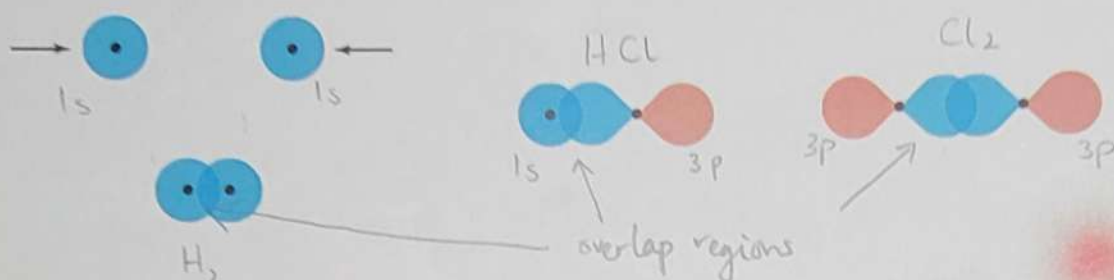# Valence bond theory
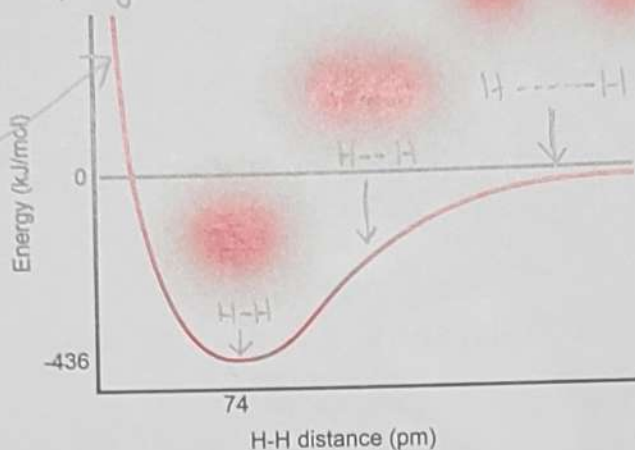
Covalent bonds form through sharing of electrons by adjacent atoms.

Can occur when orbitals on the two atoms overlap → valence bond theory

H_2

HCl

Cl_2

overlap regions

The energy of the system depends
on the quality of the overlap
between orbitals

If the distance is too close,
repulsive forces between nuclei increases
the energy of the system

H-H distance (pm)

Hybrid Orbitals

To apply the ideas of orbital overlap and valence-bond theory to polyatomic molecules, we
need to introduce the concept of **hybrid atomic orbitals (HAOs)**.

Mix (combine, hybridize) n atomic orbitals to make n hybrid orbitals

sp hybrid orbitals

Consider beryllium: in its ground electronic state, it would not be able to form bonds
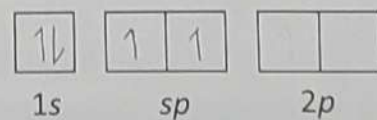because it has no singly-occupied orbitals:
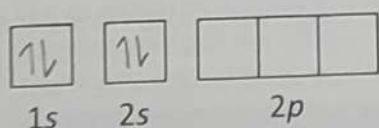
1s   2s   2p
     ground state
   no unpaired electrons
Mixing the s and p orbitals yields
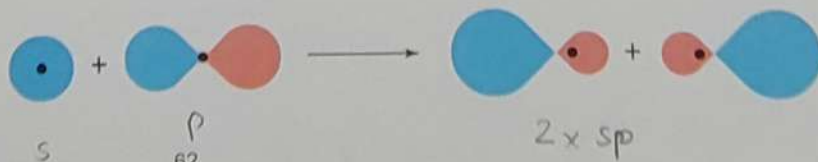two degenerate orbitals

sp hybrid orbitals
have two lobes: 1 large, 1 small
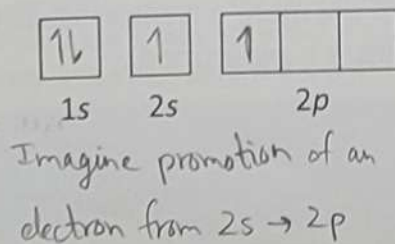
1s   2s   2p
Imagine promotion of an
electron from 2s → 2p
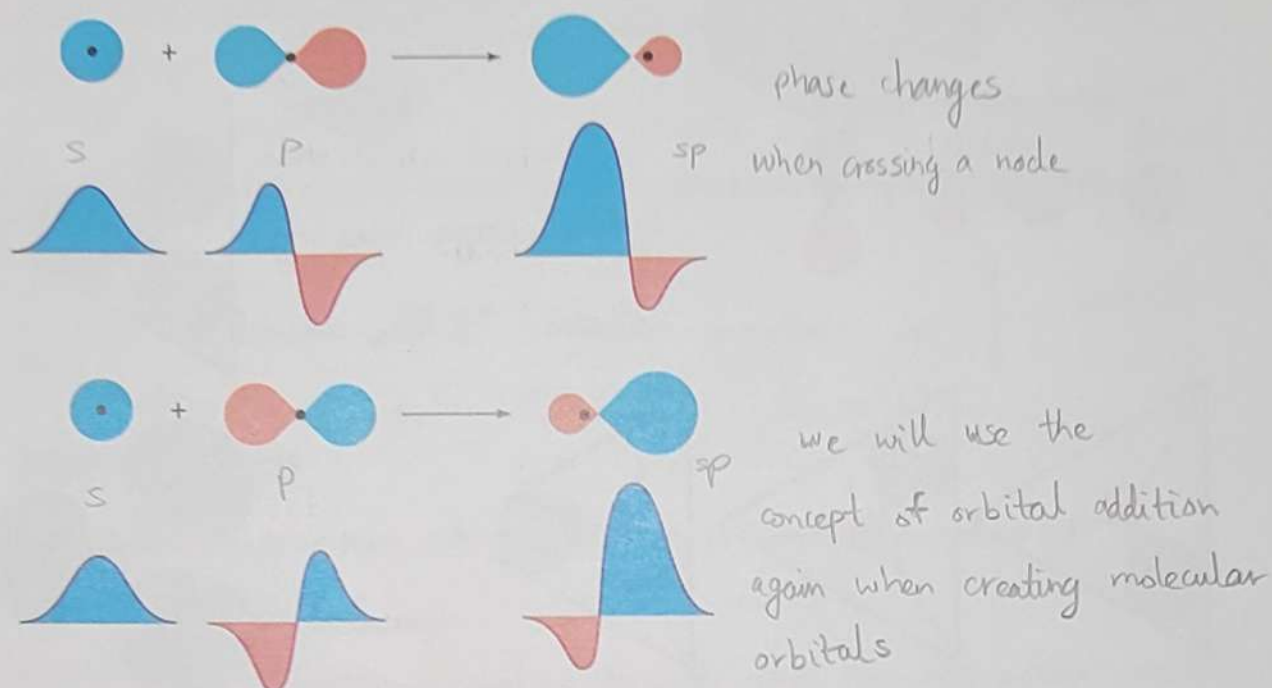
1s   sp   2p
rewrite orbital diagram
to show hybrid orbitals
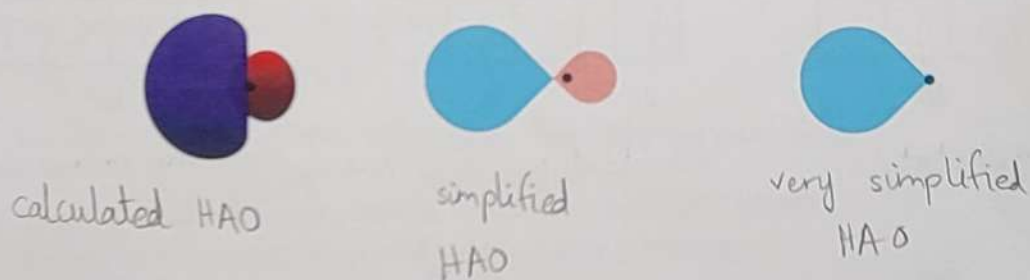

s   p
           62

2 x sp

Phase

Note that orbitals, atomic and hybrid alike, have lobes of different colours. This difference in **phase** arises from the wave nature of the electron. Regions where the wave function is positive are represented by one colour (here **blue**), negative by another (here **red**).

phase changes
when crossing a node

we will use the concept of orbital addition again when creating molecular orbitals

Orbitals are usually drawn in simplified form, and hybrid orbitals are no exception:

calculated HAO

simplified HAO

very simplified HAO

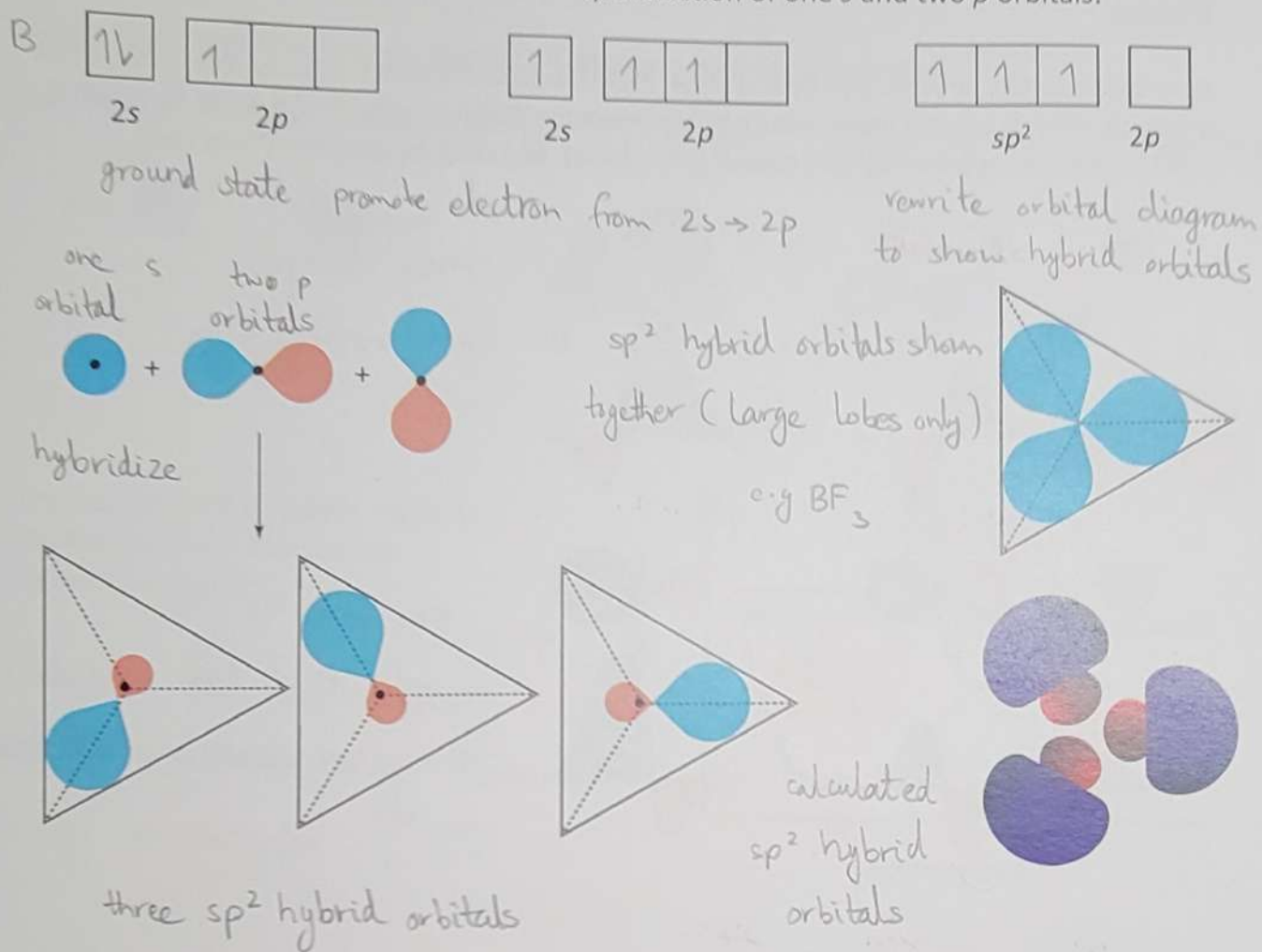These two degenerate *sp* orbitals align themselves 180° from each other, and 90° from the two remaining unhybridized *p* orbitals.

large lobes of sp hybrid orbitals

H 1s orbital
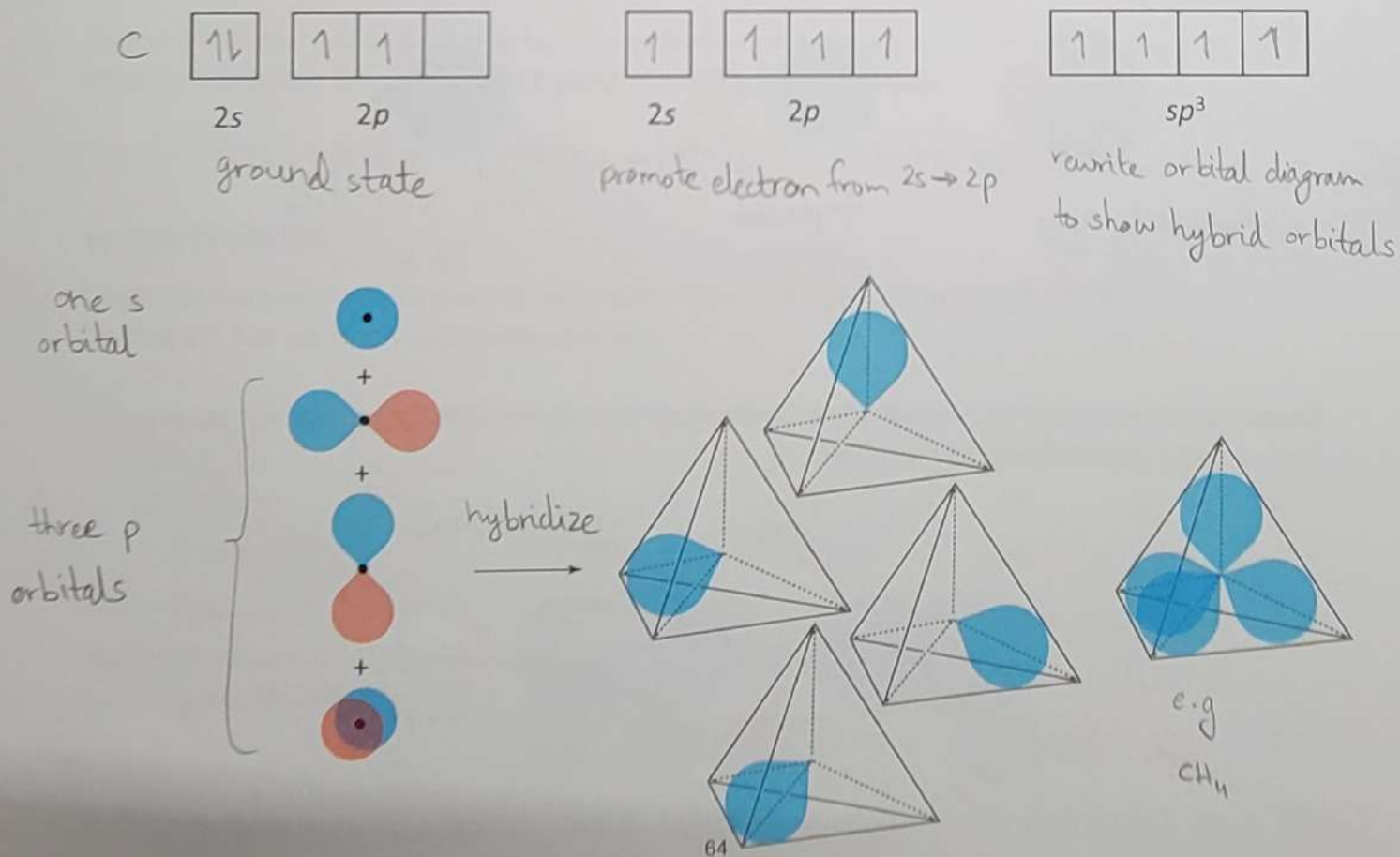
H

Be

H

H 1s orbital

overlap regions
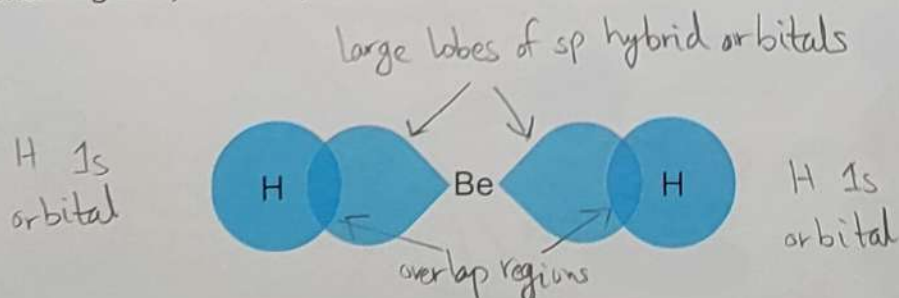
(the small back-lobes of hybrid orbitals and other p-orbitals are not shown)

63

Three sp² hybrid orbitals are formed from hybridization of one s and two p orbitals:

B

↑↓			

2s   2p

↑	↑	↑

2s   2p

↑	↑	↑	

sp²   2p

ground state   promote electron from $2s \rightarrow 2p$ rewrite orbital diagram to show hybrid orbitals

one s orbital   two p orbitals

hybridize

sp² hybrid orbitals shown together (large lobes only)

e.g BF_3

three sp² hybrid orbitals

calculated sp² hybrid orbitals

Four sp³ hybrid orbitals are formed from hybridization of one s and three p orbitals:

C

↑↓	↑	↑	

2s   2p

↑	↑	↑	↑

2s   2p

↑	↑	↑	↑

sp³

ground state   promote electron from $2s \rightarrow 2p$ rewrite orbital diagram to show hybrid orbitals

one s orbital

three p orbitals

hybridize

e.g CH_4

64

For geometries involving expanded octets on the central atom, we use *d* orbitals in our hybrids:

s,p,p,p,d

trigonal bipyramidal

s,p,p,p,d,d

five sp^3d

six sp^3d^2

octahedral
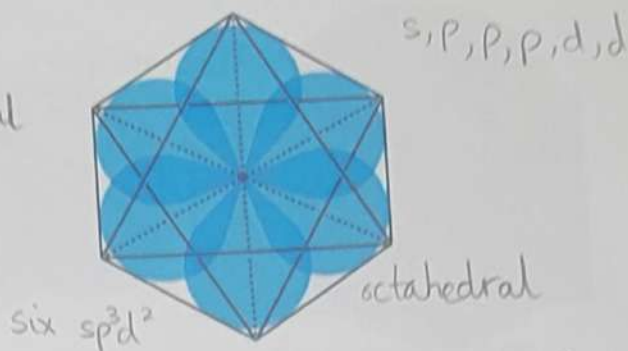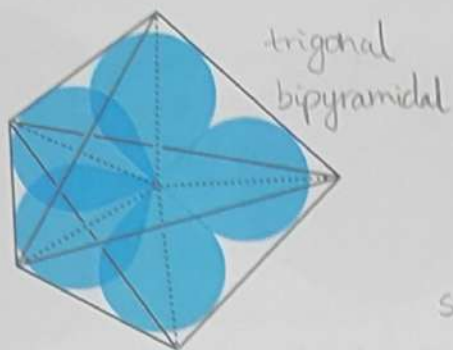
Once you know the electron-domain geometry, you know the hybridization state of the atom:

2 electron domains = sp   3 electron domains = sp^2

4 electron domains = sp^3 5 = sp^3d 6 = sp^3d^2

Multiple Bonds

The covalent bonds we have seen so far are **sigma** (σ) bonds, characterized by:

- head-to-head overlap
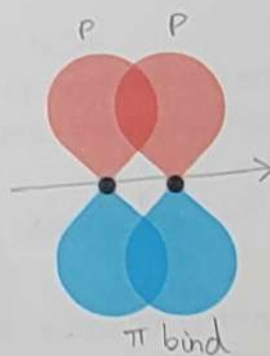- cylindrical symmetry of electron density about the internuclear axis

To describe multiple bonding, we must invoke **pi** (π) bonds.

Pi (π) bonds are characterized by:

side-to-side overlap
electron density above and below the internuclear axis

P   P

π bond

Single bonds are **always** σ bonds, because σ overlap is greater, resulting in a stronger bond and more energy lowering.
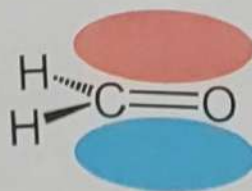
in a multiple bond, ONE of the bonds is a σ bond

and the rest are π bonds

In a molecule like formaldehyde an sp^2 orbital on carbon overlaps in σ fashion with the corresponding orbital on the oxygen.

$$H_2C=\ddot{O}:$$
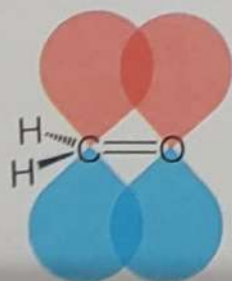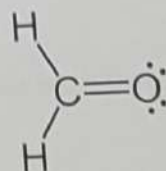
the unhybridized p orbitals overlap in π fashion

$H_2C=O$

one π bond

$- = 1\sigma$

$= = 1\sigma + 1\pi$

$\equiv = 1\sigma + 2\pi$

In triple bonds, e.g. acetylene, two *sp* orbitals form a σ bond between the carbons:
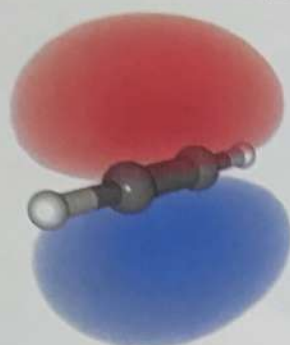
one pair of *p* orbitals
overlapping in π fashion
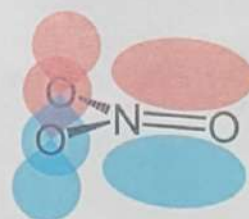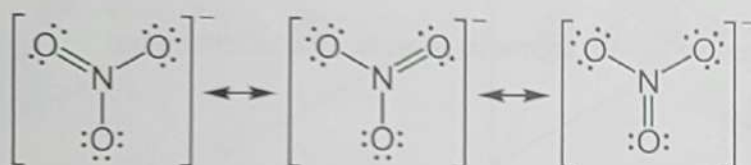above plane
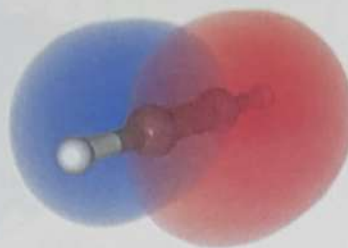
one pair of *p* orbitals
overlapping in π fashion
in plane

two π bonds

Delocalized π Bonding

When writing Lewis structures for species like the nitrate ion, we draw resonance structures to more accurately reflect the structure of the molecule or ion.

In reality, each of the four atoms in the nitrate ion has a *p* orbital

The *p* orbitals on all three oxygens overlap with the
p orbital on the central nitrogen

→ the π electrons are delocalized throughout the ion
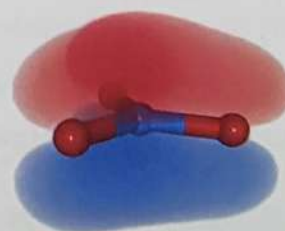
Similarly for benzene, we can
write two resonance forms:

Neither resonance structure completely describes the electrons in the π bonds.

→ the π electrons
are delocalized throughout
the ring

Molecular Orbitals

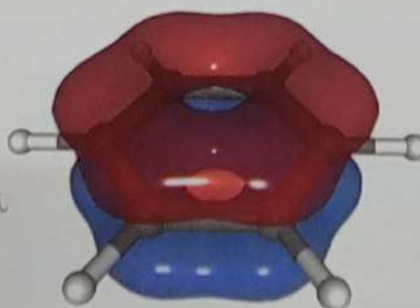Some aspects of bonding are not explained by Lewis structures, VSEPR theory, and hybridization (valence bond theory), for example:

- why does O_2 interact with magnetic field?

- why are some molecules coloured?

- how do we explain metallic bonding?

We can use molecular orbital (MO) theory to explain some of these observations.

electrons in atoms are found in _atomic orbitals_

electrons in molecules are found in _molecular orbitals_

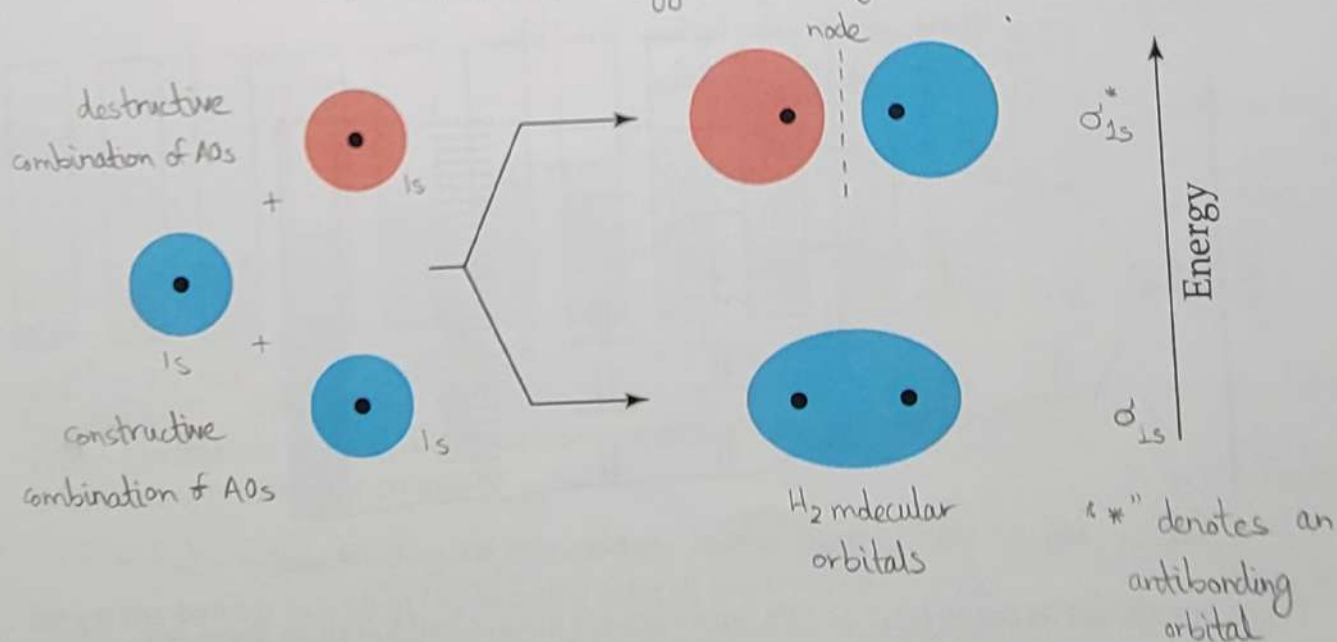Molecular orbitals have some characteristics are similar to those of atomic orbitals.

- each contain 2 electrons with opposite spin

- each has a definite energy

- electron density distribution can be visualized with contour diagrams

However, unlike atomic orbitals, molecular orbitals

are associated with an _entire molecule_

The hydrogen molecule

When n AOs overlap, n MOs form. For H_2, $1s$ (H) + $1s$ (H) must result in 2 MOs:

A molecular orbital energy level diagram:

destructive combination of AOs

$1s$

+

$1s$

+

constructive combination of AOs

node

σ_{1s}^*

σ_{1s}

Energy

H_2 molecular orbitals

"*" denotes an antibonding orbital

Both bonding and antibonding molecular orbitals have electron density centered around the internuclear axis

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→ sigma (σ) bonds

H_2 molecule

more stable than separate
H atoms → molecule forms

antibonding orbital

He_2 molecule
bonding orbital

less stable than separate He
atoms → molecule does not form
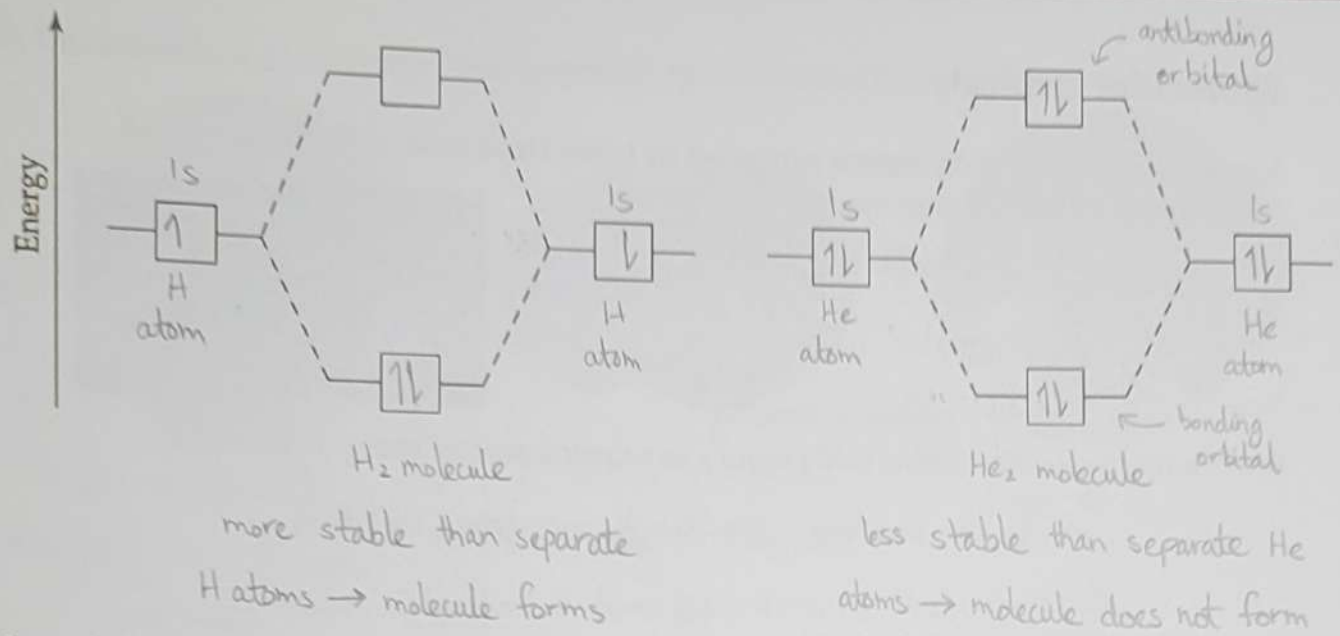
Note similarity to mixing of atomic orbitals to make hybrid atomic orbitals: the difference here is that the orbitals used are on two different nuclei.

Bond order

Bond order $= \frac{1}{2}$ (no. of bonding electrons − no. of antibonding electrons)

$$B.O. \quad H_2 = \frac{1}{2}(2-0) = 1$$

$$B.O. \quad He_2 = \frac{1}{2}(2-2) = 0$$

Band theory

We can apply the same reasoning to the combination of other orbitals to generate molecular orbitals for any molecule, but we are going to use MO theory to help us understand the bonding in metals, an important class of materials.

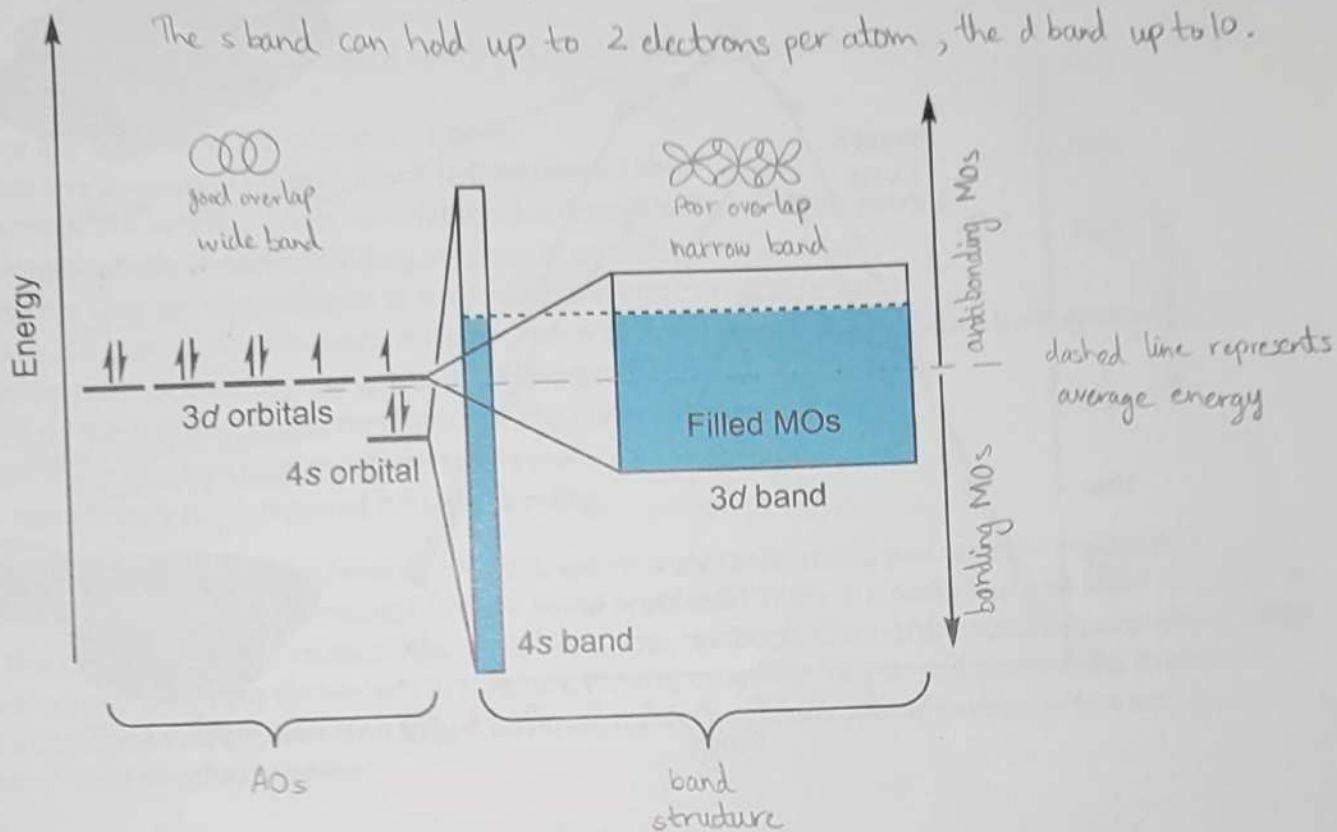Imagine a linear chain of sodium (Na) atoms, which overlap via 3s orbitals:
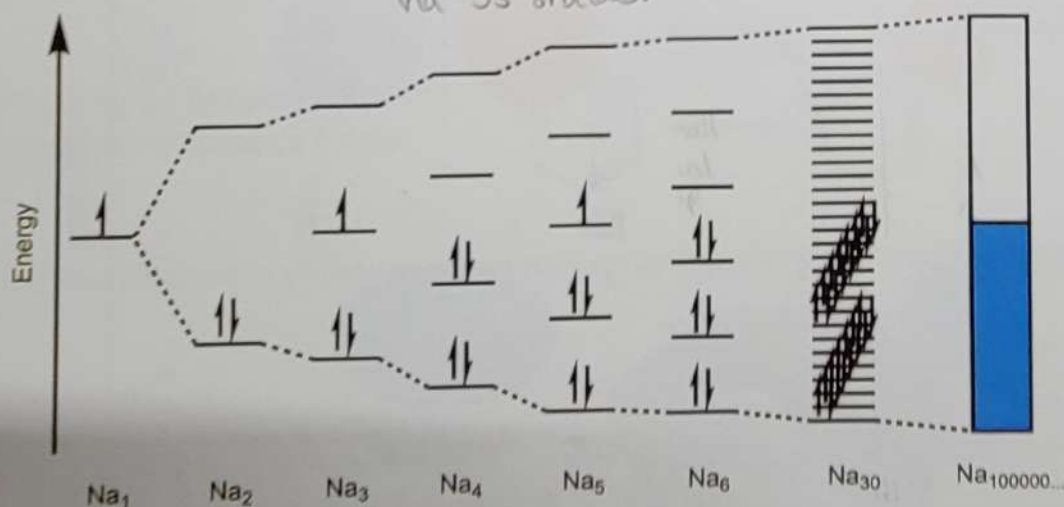
There are always as many MOs as AOs, and they are always half full since there is 1 3s electron per sodium atom.

Spacing between orbitals gets closer as we add atoms until they became effectively continuous: a band

68

The energy differences between orbitals within a band are tiny, so electrons can readily move through the metal. Metals are hence excellent **conductors**.
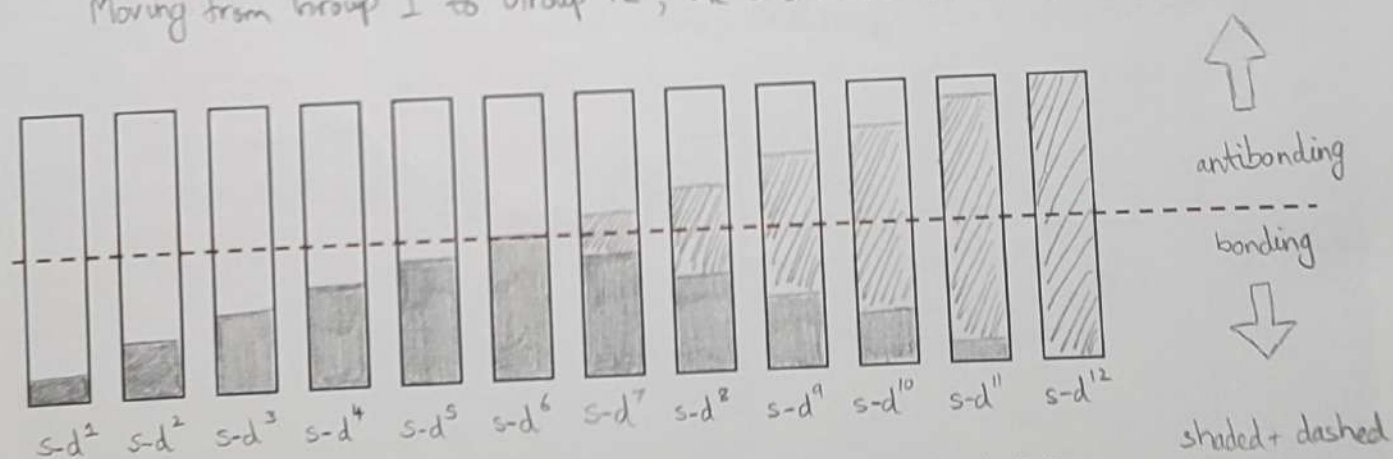
For metals in groups 1-12, the s and d bands overlap.
The s band can hold up to 2 electrons per atom, the d band up to 10.

good overlap
wide band

Poor overlap
narrow band

dashed line represents average energy

Energy

3d orbitals

4s orbital

4s band

Filled MOs

3d band

antibonding MOs

bonding MOs

AOs

band structure

We can simplify the picture by imagining metals to have a single band that can accommodate 12 electrons per atom, the s-d band.

Moving from Group 1 to Group 12, the s-d bands fill with electrons:


antibonding

bonding

s-d¹ s-d² s-d³ s-d⁴ s-d⁵ s-d⁶ s-d⁷ s-d⁸ s-d⁹ s-d¹⁰ s-d¹¹ s-d¹²

shaded + dashed
=
total electrons

When the band is half full, all of the bonding orbitals are full and all of the antibonding orbitals are empty.

⟹ metal-metal bonding is maximized and metals are very hard

shaded
=
bonding electrons

When the band is full, all of the bonding orbitals are full and all of the antibonding orbitals are also full, so the effects cancel each other out.

⟹ metal-metal bonding is minimized and metals are very soft

We can see this effect if we plot melting point against Group number:
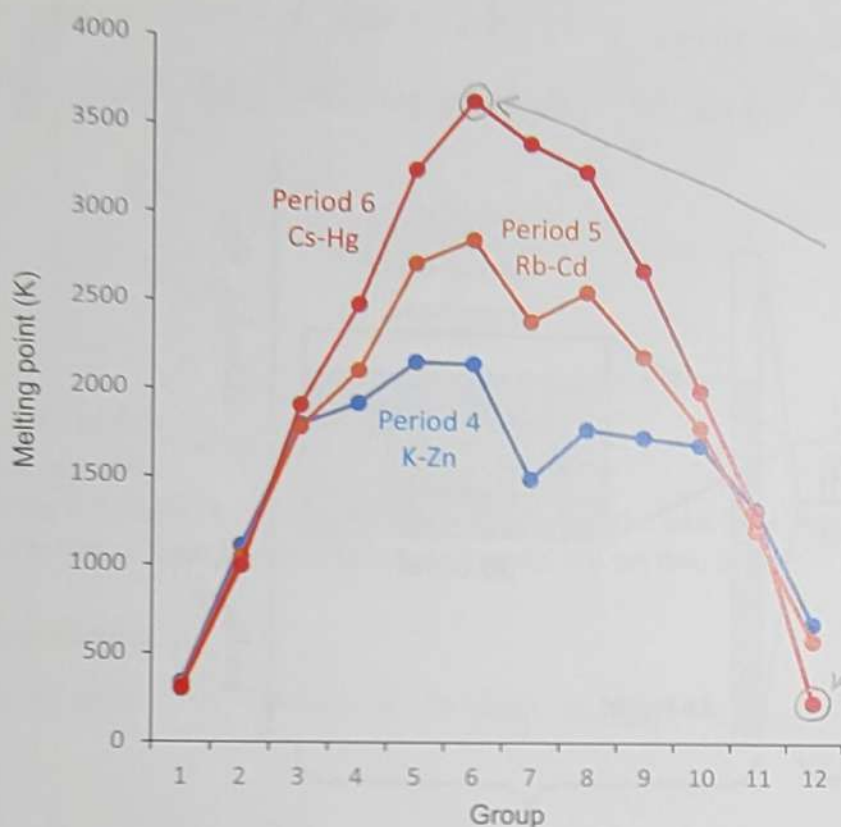
metal-metal bonding is maximized in tungsten s-d^6, mp 3422°C.

minimal metal-metal bonding in mercury, s-d^{12}, mp -39°C

liquid at RT

Metals, semiconductors and insulators

Materials can conduct electricity if electrons can move easily from an occupied orbital to an unoccupied one. In metals, there is no gap between the **valence band** and the **conduction band**. **Semiconductors** have a small band gap and **insulators** have a large band gap:

no band gap

small band gap

large band gap

conduction band

valence band
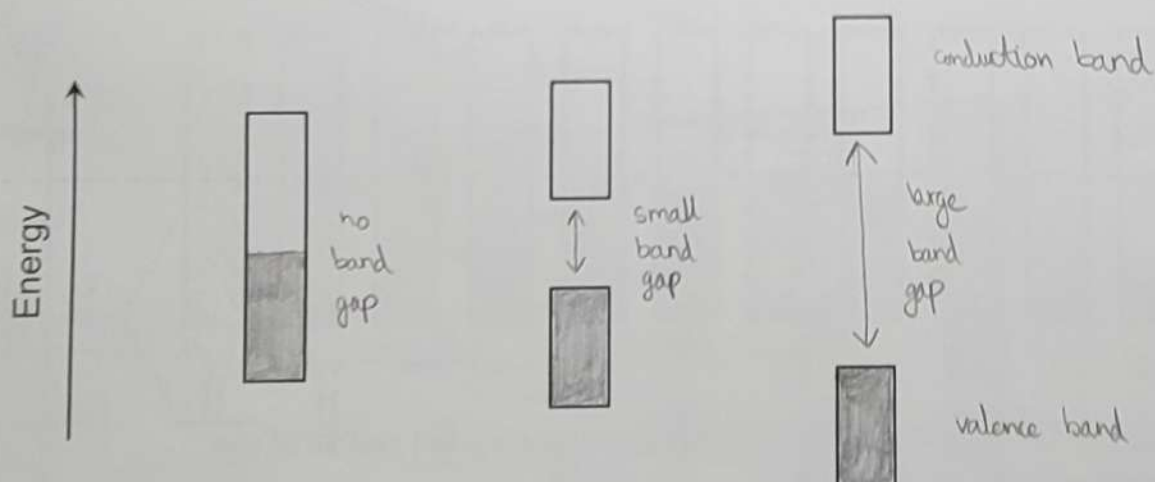
conductor

semi-conductor

insulator