

# Evaluation of Weather Parameters for Renewable Energy Forecasting with Echo State Networks

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## Abstract

The abstract goes here. As a general guide, you should provide a concise (150-250 words) summary of your article - introduction, methodology, results, and conclusion. Avoid using abbreviations and acronyms unless the abbreviation/acronym is used repeatedly in the abstract. There should be no references in the abstract.

*Keywords:* FIXME, key words, go here, like:, simulation, spent nuclear fuel

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## 1. Introduction

### 1.1. Motivation

In response to the rising threat of climate change many countries have prioritized reducing carbon emissions. The goal set by the 2015 Paris Agreement  
5 is to prevent the global temperature from rising more than 1.5 °C above pre-industrial levels [1]. Virtually all current plans to reduce carbon emissions depend on increasing the share of energy production by renewable and clean energy sources, especially solar and wind [2, 3, 4, 5]. While solar and wind are low-carbon sources, these forms of electricity generation increase variability,  
10 which can lead to blackouts and power system failures [6]. Further, even modest penetrations of renewable energy negatively affect the economics of other types of clean energy, such as nuclear power [2, 7, 8]. This may force nuclear plants to shut down prematurely, at the precise moment all clean sources of energy are

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most needed. There has been some work done to quantify the economic benefit  
 15 of improving forecasts of renewable energy [9, 10, 11]. Improving renewable  
 energy forecasts can mitigate some of the negative side effects of variability. The  
 economic benefits of better forecasts include: reduced costs compared to building  
 storage devices [9]; curtailment reduction and more efficient use of non-renewable  
 sources [10]; and a slight, but important, amount of load-following from nuclear  
 20 and biomass generators, which are unable to follow rapid changes in demand [11].  
 Most proposed forecasting improvements involve new algorithms or machine  
 learning techniques. However, one of the simplest approaches to improving  
 forecasts is to improve the training data for such algorithms. There is a veritable  
 zoo of weather parameters that can supplement target training data, but we  
 25 don't know *a priori* which of these parameters will be helpful or detrimental to  
 model performance. In this paper, we evaluate several common parameters for  
 use in renewable energy forecasting with Echo State Networks (ESNs).

## 1.2. Why Echo State Networks

ESNs have several appealing features. They are simple, consisting only of a  
 30 large, sparse, reservoir and a single output layer [12]; flexible and generalizable,  
 while other network architectures require significant fine tuning [13]; and fast,  
 due to their simple structure and few trainable weights relative to other neural  
 networks. The ESN network architecture eliminates the need for complicated  
 data pre-processing, such as feature extraction, that is required for other machine  
 35 learning and statistical algorithms [14, 15]. ESNs can also outperform other  
 prediction techniques [16, 17, 18, 19, 20].

Classical ESNs have previously been used to forecast demand, wind energy,  
 and solar energy [21, 17, 20]. ESNs are typically used to make extreme short  
 term predictions, on the order of seconds or minutes [22, 23, 19], one-hour ahead  
 40 [18], and up to a single day ahead [21]. Forecasts must be multiple-hours to a  
 couple of days ahead to aid unit commitment and grid-scale energy economy  
 [9, 10, 11]. In this work we use a classic ESN architecture to forecast total  
 demand, wind production, and solar production, 4-hours and 48-hours ahead.

There has been a lot of work to improve the forecasting capability of the basic  
 45 ESN. Approaches include adding multiple reservoirs [20, 24, 25, 26]; including  
 non-linear units [27, 19]; combining with other network architecture [22, 28]; and  
 using a particle swarm approach [29, 23]. Some works mention that including  
 weather parameters may be useful for renewable energy forecasting [30, 19], but  
 none have demonstrated the effect each parameter has on model performance.  
 50 The primary goal of this work is to fill that gap.

### 1.3. Contributions

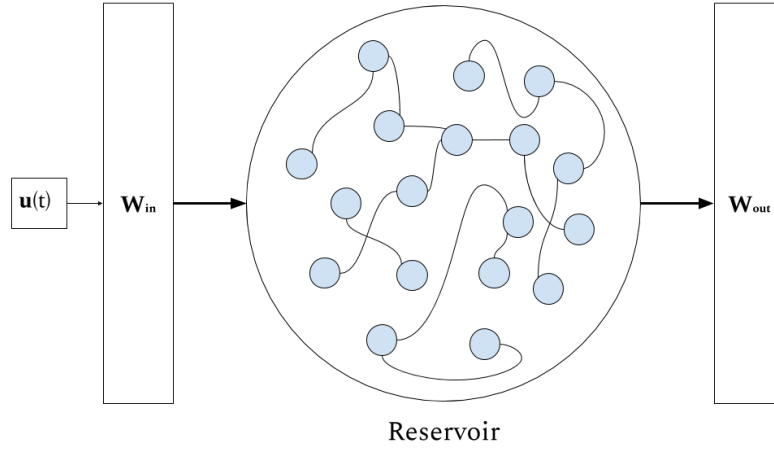
In this work, we use ESNs for three main prediction tasks: total electricity  
 demand, wind energy production, and solar energy production. We split these  
 tasks into further sub tasks; predicting 4-hours ahead and 48-hours ahead. These  
 55 predictions facilitate scheduling and grid planning because current market rules  
 put renewable energy on the grid first, forcing conventional power generators to  
 work around this variability [9]. Using ESNs to make predictions two-days ahead  
 is unique to this paper since the longest predictions by ESNs in the literature only  
 reach one-day ahead [21]. Finally, we repeat these tasks with several commonly  
 60 used weather parameters and evaluate their effect on model performance. The  
 need to consider exogenous meteorological inputs has been noted previously.  
 Suprisingly, sun elevation is seldom used as a correlated quantity for energy  
 demand and wind power.

The structure of the paper is as follows. In Section 2, we discuss how data were  
 65 selected and processed, and we review ESNs. Section 3 shows a benchmarking  
 exercise for our ESN implementation and presents the results. We discuss the  
 results and future implications in Section 4.

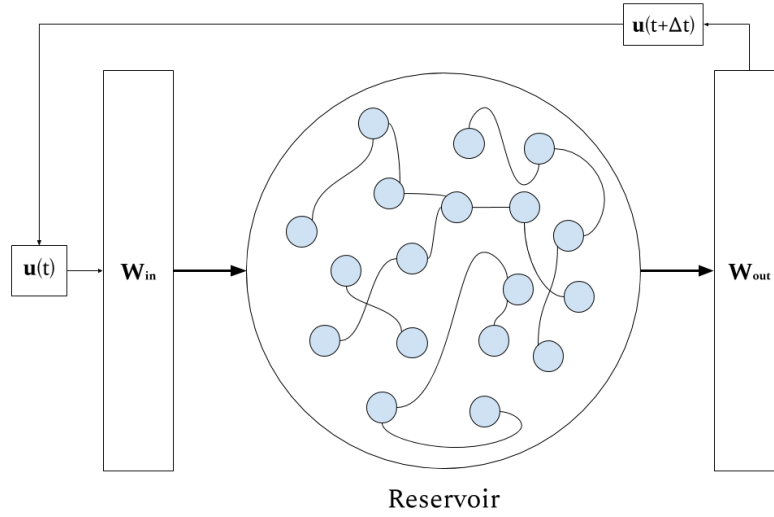
## 2. Methodology

### 2.1. Echo State Networks

70 An ESN, sometimes called a “reservoir computer,” [31, 32, 33] is a type of  
 recurrent neural network that replaces the many hidden layers of a conventional  
 feed-forward neural network with a reservoir that is:



(a) Training Flow



(b) Predicting Flow

Figure 1: (a) Shows the behavior of an ESN during the training phase. (b) Shows ESN behavior during the predicting phase. The output  $u(t + \Delta t)$  is used as the next input value.

1. sparse,
2. connected by uniformly random weights, centered at zero,
- 75 3. and large (i.e. has many neurons).

The reservoir is therefore a randomly instantiated adjacency matrix,  $\mathbf{W}$ , of size  $N \times N$ . The input vector,  $U(t)$ , of  $K$  units is mapped onto the reservoir by an input matrix,  $W^{in}$  of size  $N \times K$ . The activation states of the reservoir are calculated by

$$x(t) = \tanh(W^{in} \cdot U(t) + \mathbf{W}x(t-1)) \quad (1)$$

Where  $x(t)$  is the collection of reservoir activations [18, 32, 12]. The output is read by an output weight matrix,  $W^{out}$ .

$$U(t + \Delta t) = (W^{out})^T \cdot x(t) \quad (2)$$

In the training phase, the output,  $U(t + \Delta t)$ , is discarded and the next training input is passed to the network. During the prediction phase, the output is kept and used as the next input. Figure 1 illustrates this behavior. The speed of ESNs is owed to this structure— only  $W^{out}$  has tunable weights. Everything  
80 else is fixed. In this work, we adapted the open source Python package `pyESN` [34] to construct and train the network.

## 2.2. Hyper-Parameter Optimization

ESNs are fast because the hidden layer in a conventional feed-forward neural network is replaced by a large reservoir that does not require training. The  
85 trade off is that ESNs are sensitive to various hyper-parameters that need to be optimized [12]. These hyper-parameters are summarized in Table 1. The spectral radius ( $\rho$ ) should satisfy the “echo state property” which means that previous reservoir activations have a decaying influence on future states. This is usually guaranteed for  $\rho < 1$ , but is not a requirement [12].

90 The hyper-parameters are optimized by performing a grid search over the test values specified in Table 1. The following steps were taken for each prediction task:

Table 1: Description of Model Hyper-Parameters

Hyper-parameter	Purpose	Tested Values
<b>noise</b>	Neuron regularization	[0.0001, 0.0003, 0.0007, 0.001, 0.003, 0.005, 0.007, 0.01]
$\rho$	Spectral radius	[0.5, 0.7, 0.9, 1, 1.1, 1.2, 1.3, 1.5]
$N$	Size of reservoir, $\mathbf{W}$	[600, 800, 1000, 1500, 2000, 2500, 3000, 4000]
<b>sparsity</b>	The density of connections in $\mathbf{W}$	[0.005, 0.01, 0.03, 0.05, 0.1, 0.12, 0.15, 0.2]
Training Length	Size of the training set before prediction	$L \in [5000, 25000]$ , step size = 300

1. Select a hyper-parameter or pair of parameters.
2. Generate ESN prediction with the specified parameters.
- 95 3. Calculate and record the root mean squared error (RMSE).
4. Continue until last entry in the parameter set is reached.
5. Set the network parameters to hyper-parameter value that minimizes the RMSE.

This algorithm generates an error surface where the coordinates of the absolute  
100 minimum correspond to the indices of values in the hyper-parameter test sets  
that minimized the RMSE. Figure 2 shows an example heatmap that optimized  
the spectral radius and noise hyperparameters for the 4- hour ahead demand  
forecast and illustrates the sensitivity of ESNs to hyperparameter values.

### 2.3. Prediction Tasks

105 We first performed a benchmarking task by making a prediction for the  
Lorenz 1963 model [35]. Then we optimized predictions for univariate time-series  
representing total demand, solar energy, and wind energy 4-hours ahead and  
48-hours ahead. Finally, those same six tasks were repeated with an additional  
predictor. The tasks are summarized in Table 2.

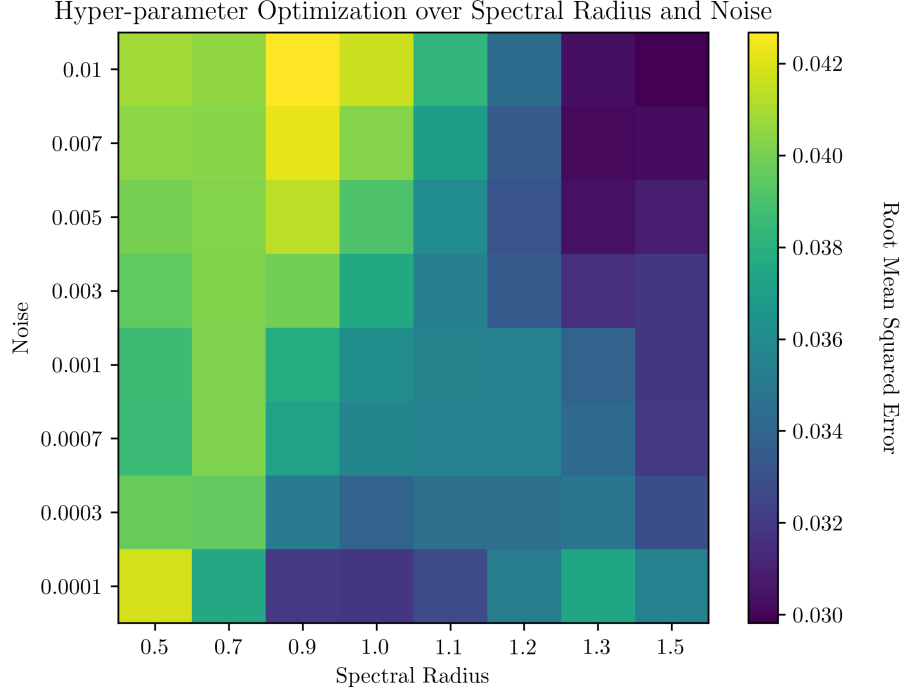


Figure 2: An example heatmap of the RMSE for 4-hour ahead demand prediction with different combinations of spectral radius,  $\rho$ , and noise.

#### 2.4. Data Selection and Processing

All data predicting demand, wind energy, and solar energy on the University of Illinois at Urbana-Champaign (UIUC) campus are from the UIUC Solar Farm 1.0 dashboard [36] and proprietary data shared with us courtesy of the UIUC Facilities and Services Department. All data had hourly resolution. Weather data was retrieved from the National Oceanic and Atmospheric Administration (NOAA)[37] for two locations: Champaign, IL, where UIUC is located, and Lincoln, IL, where Railsplitter Windfarm is located. UIUC has a power purchase agreement with Railsplitter Windfarm [38].

In the case of UIUC solar data, significant portions were missing due to instrument failure. In order to fill in this missing data, we calculated the theoretical solar energy production based on irradiance data from OpenEI [39].

Table 2: Summary of Prediction Tasks

Target	Future	Additional Predictor
Total Demand	4 hours ahead	None
		Solar Elevation
Solar Energy	48 hours ahead	Humidity
		Pressure
Wind Energy		Wet Bulb Temp.
		Dry Bulb Temp.
		Wind Speed

The solar output is given by [40]

$$P = G_T \eta_{ref} \tau_{pv} A [1 - \gamma (T - 25)] \quad [W] \quad (3)$$

where

$$G_T = P_{DNI} * \cos(\beta + \delta - lat) + P_{DHI} * \left( \frac{180 - \beta}{180} \right) \left[ \frac{W}{m^2} \right] \quad (4)$$

where

$$\delta = 23.44 \sin \left( \left( \frac{\pi}{180} \right) \left( \frac{360}{365} \right) (N + 284) \right) [\text{degrees}] \quad (5)$$

$\eta, \tau, \gamma$  are solar panel properties

$P_{DNI}$  is the direct normal irradiance

$P_{DHI}$  is the diffuse horizontal irradiance

$\beta$  is the tilt angle of the solar panels

The solar elevation angle,  $\alpha$ , was also calculated [41, 42] using coordinates for the UIUC Solar Farm 1.0.

$$\alpha = \sin^{-1} [\sin(\delta) \sin(\phi) + \cos(\delta) \cos(\phi) \cos(\omega)] \quad (6)$$



where

$\delta$  is the declination angle

$\phi$  is the latitude of interest

$\omega$  is the hour angle

Finally, we normalized all of the data using the infinity norm

$$\|\mathbf{x}\|_{\infty} \equiv \max |x_i|. \quad (7)$$

The infinity norm is equivalent to normalizing by the system capacity. This is useful because it simplifies the comparison of our results between tasks whose training data have vastly different magnitudes. This normalization also makes it possible to compare results with other works and is consistent with the recommendation from Kobylinski et al. (2020) [43]. The maximum value for each system is given in Table 3.

Table 3: Description of the size of the UIUC microgrid

System	Maximum Value
Electricity Load	81.6 [MW]
Solar Energy	4.7 [MW]
Wind Energy	8.8 [MW]

## 2.5. Performance Metrics

We measure the accuracy of the model using two error metrics: mean absolute error (MAE) and root mean squared error (RMSE). These are defined as

$$\text{MAE} = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i| \quad (8)$$

$$\text{RMSE} = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2} \quad (9)$$

where

$\hat{y}_i$  is the predicted output

$y_i$  is the true value

The MAE measures the expected error throughout the forecast horizon. The RMSE indicates the presence of large but infrequent errors. Since the data were normalized by system capacity [9], the error metrics are easily interpretable. In order to compare how each individual weather input either improved or worsened the forecast we calculated a “percent improvement” over the univariate case (i.e. a demand prediction based only on historical demand data). This percent improvement is calculated by

$$\% \text{ Improvement} = \frac{\hat{e} - e}{e} \times 100, [-] \quad (10)$$

where  $e$  is the error from the univariate forecast and  $\hat{e}$  is the error from the duovariate forecast. The sign indicates the direction of change in error. Finally, in order to facilitate comparison with other work, we calculated the normalized root mean squared error (NRMSE) by

$$NRMSE = \sqrt{\frac{\sum_{i=1}^N (y_i - \hat{y}_i)^2}{\sum_{i=1}^N (y_i - \tilde{y})^2}} \quad (11)$$

where

$\tilde{y}$  is the mean of the target set

### 3. Results

#### 3.1. Benchmark: Lorenz 1963

We first verified that our choice of implementation for a conventional ESN produced similar results to those found in the literature [31]. The hyper-parameters that minimized the RMSE of the model can be found in Table 4. Our optimized values are somewhat different from the literature, but our ESN implementation

successfully replicated the climate of the Lorenz Attractor similar to Pathak et. al 2017. Figure 3 shows the ESN forecast ten seconds into the future for Lorenz 1963 model.

Table 4: Hyper-parameters for the Lorenz 1963 Model. The random seed was generated by the open source package `numpy`.

Parameter	This paper	Literature [31]
$N$	2000	300
$\rho$	0.9	1.2
<b>sparsity</b>	0.1	0.1
<b>noise</b>	0.001	0
Training Length	3200	Not Specified
Random Seed	85	Not Specified

### 135 3.2. ESN Forecasting: Demand

We used ESNs to forecast electricity demand, or electric load, both 4 hour intervals and 48 hour intervals. Figure 4 shows the 48-hour ahead forecast that had the lowest RMSE. In this case, the forecast that used relative humidity as an additional input had the lowest error, as shown in Table 5. Table 5 also  
140 shows that the forecast was weakened by training with air temperature (both wet bulb and dry bulb), air pressure, and wind speed. Adding solar elevation angle performed about the same as the base case.

The 4-hour interval forecast with the lowest RMSE is shown in Figure 5. Solar elevation angle improved the forecast more than any other meteorological  
145 input. Table 6 shows that humidity, air pressure, dry bulb temperature, and wind speed made the forecast worse.

The performance of this implementation is consistent with previous applications of ESNs to the task of predicting electric load [21]. Further, these results indicate that ESNs perform better than other machine learning techniques – long  
150 short term memory (LSTM)[44], Sequence to Sequence (S2S) [44], and support vector regression [15] – for predicting energy demand.

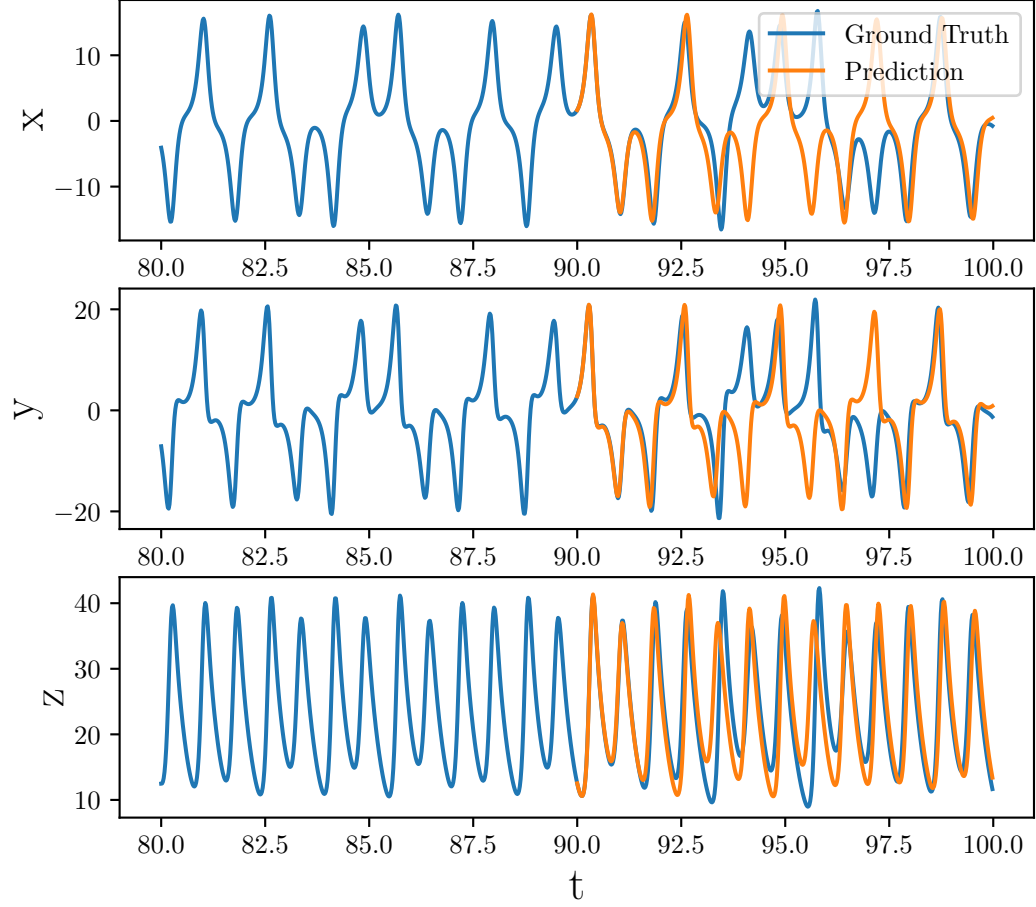


Figure 3: Using an ESN to replicate the climate of the Lorenz Attractor.

### 3.3. ESN Forecasting: Solar Energy

We repeated the 4-hour and 48-hour ahead forecasts for solar energy production on the UIUC campus. Figure 6 and Figure 7 show the best forecasts for 48-hours ahead and 4-hours ahead, respectively. The shaded gray regions emphasize where the predicted energy production dipped below zero. This should never occur in reality. Table 7 shows that relative humidity was the best additional feature for the 48-hour ahead prediction. While Table 8 shows that wet bulb temperature improved the forecast the most. In both cases, the predictions were

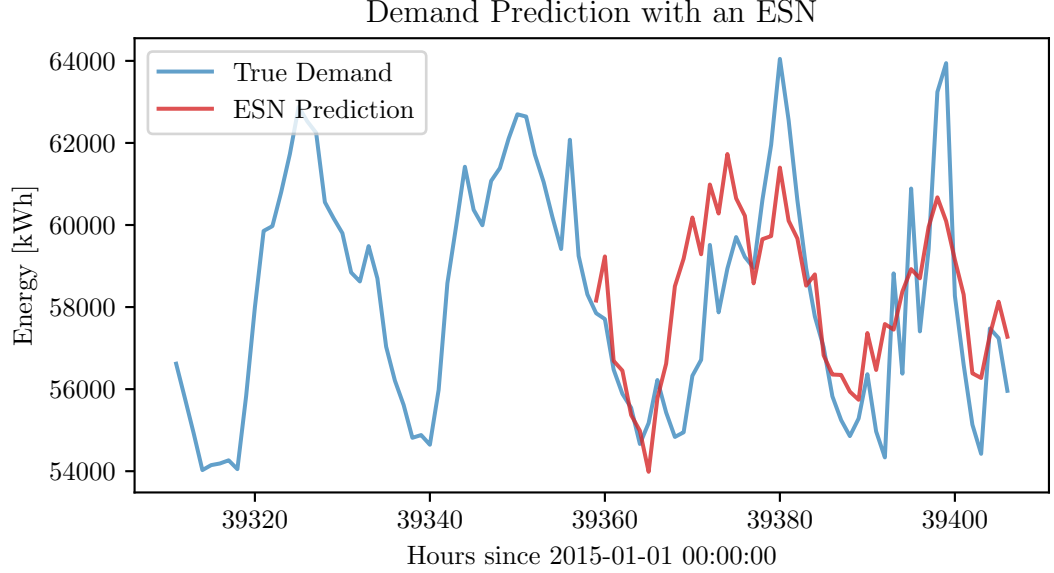


Figure 4: The optimized 48-hour ahead demand prediction. The inputs for this forecast were hourly demand and relative humidity. *Hyperparameters*: Reservoir Size:1500, Sparsity: 0.2, Spectral Radius: 1.5, Noise: 0.0007, Training Length: 5000, Prediction Window: 48, Random state: 85

improved by each feature, except for air pressure and wind speed.

Our results are comparable to other work that used ESNs to forecast solar energy [30]. However, these results show that conventional ESNs are insufficient for improving energy economics through day-ahead forecasting [11].

### 3.4. ESN Forecasting: Wind Energy

Finally, we performed the same prediction tasks ask before, for wind energy. Figure 8 and Figure 9 show the best forecasts that minimized the RMSE for 48 and 4-hours ahead, respectively. All features except air pressure improved the forecast. Including solar elevation angle improved the 48-hour ahead forecast the most, while adding windspeed improved the 4-hour ahead the most. Those results are shown in Table 9 and 10 respectively. Qualitatively, our conventional ESN achieved results comparable to a more complex algorithm by simply adding

Table 5: Tabulated error for 48-hour ahead total electricity demand forecasts with various coupled quantities. Improvement indicates the percentage improvement over the base case of forecasting electricity demand alone.

Scenario	NRMSE	MAE	RMSE	Improvement MAE (%)	Improvement RMSE (%)
Total Demand	0.76691	0.0189	0.0241	[-]	[-]
Demand + Sun Elevation	0.76351	0.0191	0.0240	+1.0582	-0.4149
Demand + Humidity	0.70799	0.0180	0.0223	-4.7619	-7.4689
Demand + Pressure	0.77769	0.0176	0.0245	-6.8783	+1.6600
Demand + Wet Bulb Temp.	0.99886	0.0241	0.0314	+27.5132	+30.2904
Demand + Dry Bulb Temp.	0.86634	0.0218	0.0273	+15.3439	+13.2780
Demand + Wind Speed	0.77958	0.0197	0.0245	+4.2328	+1.6600

a single meteorological predictor [28]. The results for a 48-hour ahead forecast from a more complex algorithm are shown in Figure 10.

However, the state-of-the-art Weather Research and Forecasting model [45],  
175 a numerical weather prediction model, far outperforms our best results. Thus, conventional ESNs are insufficient for applications in grid planning [9].

#### 4. Discussion

The forecast accuracy of our ESN for the Lorenz model does not persist for quite as long as in other works [31]. However, our model successfully replicates the  
180 environment that produces the Lorenz Attractor. Further, optimal parameters may be unique for each randomly instantiated reservoir. It is impossible to replicate the exact conditions of other works without information about a seed for the random state. We have included this information for future work to compare with our results.

185 Chitsazan et al. 2017 compared wind speed forecasting with a conventional ESN to an ESN with nonlinear readouts and achieved better results with the base model than we did [46]. However, this could be attributed to the fact that

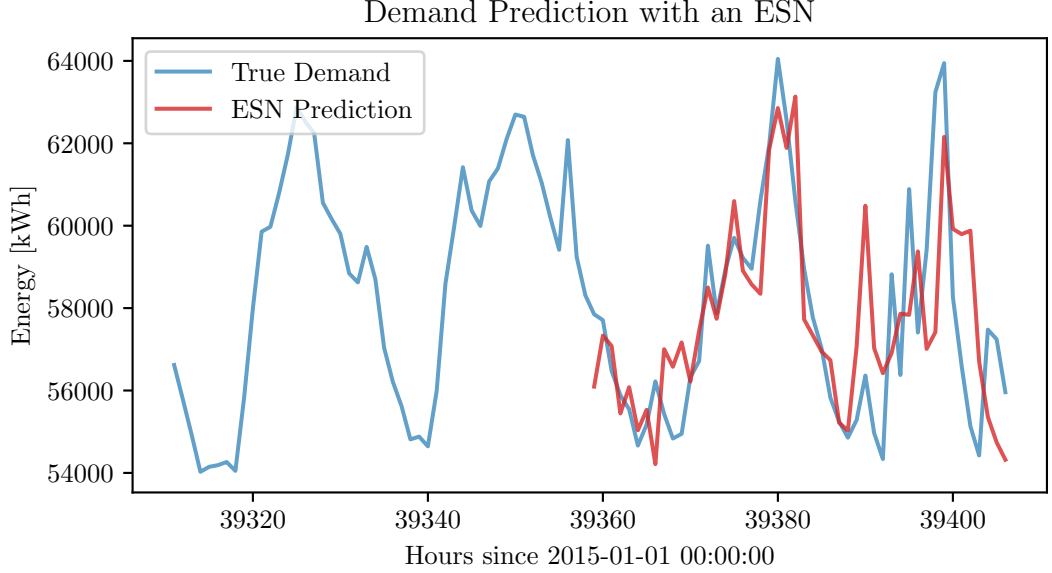


Figure 5: The optimized 4 hour ahead demand prediction. The inputs for this forecast were hourly demand and solar elevation angle. *Hyperparameters*: Reservoir Size:2500, Sparsity: 0.01, Spectral Radius: 1.5, Noise: 0.003, Training Length: 5000, Prediction Window: 4, Random state: 85

For each target variable – demand, wind, and solar – we found that sun elevation angle, while not always the best, was the only meteorological factor that improved the forecast error in every case. We hypothesize that the effect of additional weather features on model performance is related to the temporal complexity of that feature relative to the target variable. Electricity demand, for example, is quite “predictable,” and therefore has low complexity. Air temperature and other weather related variables are less predictable. Thus, adding air temperature as a model input increases the total complexity of the system and weakens performance. Further, solar elevation angle is completely deterministic and perfectly predictable and was the only feature that improved, or had a neutral effect on, model performance. Like electricity demand, solar elevation angle has both diurnal and annual periodicity, but has lower complexity than air temperature and electricity demand itself. Conversely, solar and wind

Table 6: Tabulated error for 4-hour ahead electricity demand forecasts with various coupled quantities. Improvement indicates the percentage improvement over the base case of forecasting electricity demand alone.

Scenario	NRMSE	MAE	RMSE	Improvement MAE (%)	Improvement RMSE (%)
Total Demand	0.83634	0.0193	0.0263	[-]	[-]
Demand + Sun Elevation	0.75855	0.0183	0.0239	-5.1831	-9.1255
Demand + Humidity	0.92245	0.0219	0.0290	+13.4715	+10.2662
Demand + Pressure	0.86714	0.0186	0.0273	-3.6269	+3.8023
Demand + Wet Bulb Temp.	0.80366	0.0196	0.0253	+1.5544	-3.8023
Demand + Dry Bulb Temp.	0.85662	0.0208	0.0270	+7.7720	+2.6616
Demand + Wind Speed	0.85152	0.0201	0.0268	+4.1451	+1.9011

energy are both nonlinear functions of many weather variables and consequently have greater complexity than air temperature. This means that adding a temperature feature as a model input will likely decrease the total complexity of the system and improve the forecast. Including wind speed only improved the wind energy forecasts, likely because it has greater complexity than solar energy and less than wind energy. Relative humidity has an inconsistent and poorly understood effect on model performance. It improved the forecast for 48-hour ahead electricity demand but worsened it for the 4- hour ahead forecast, as shown in Table 5 and Table 6. The opposite trend occurred for solar energy. Quantifying the predictability and complexity of these systems is in progress. A good measure for this type of complexity is the *weighted permutation entropy* [47, 48, 49].

These results point to an important disadvantage of using ESNs to forecast renewable energy. This network architecture is simple and fast, but remains a black box. We assume that there exists some underlying dynamics that can be “learned” but cannot observe the learning process nor extract important features from ESNs.



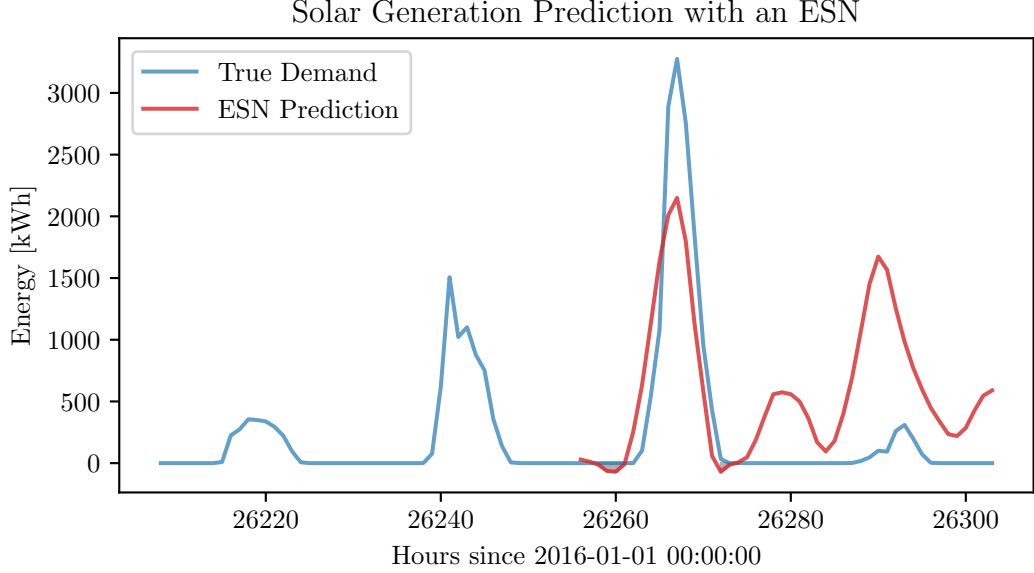


Figure 6: The optimized 48-hour ahead solar energy prediction. The inputs for this forecast were solar energy and relative humidity. Hyperparameters: Reservoir Size:800, Sparsity: 0.2, Spectral Radius: 1.5, Noise: 0.0001, Training Length: 5000, Prediction Window: 48, Random state: 85

The forecast lengths were decided based on the requirements for improved economics and planning mentioned in the literature [9, 10, 11]. The ESN model performed reasonably well at predicting four hours ahead but is not an improvement over the state-of-the-art [9, 45]. The model did not perform well at the 48-hour ahead forecasts. This could be due to the lack of higher resolution data. ESNs are known for their ability to predict highly non- linear systems [50, 51] yet using hourly data could add spurious complexity that confounds the model [48]

#### 4.1. Future Work

One appealing avenue of continued work is to leverage ESNs to generate synthetic data that respects real dynamics. Sythetic data is often useful for other machine learning or optimization algorithms. Typically, these data are

Table 7: Tabulated error for 48-hour ahead solar energy forecasts with various coupled quantities. Improvement indicates the percentage improvement over the base case of forecasting solar energy alone.

Scenario	NRMSE	MAE	RMSE	Improvement MAE (%)	Improvement RMSE (%)
Solar Energy	1.27301	0.1433	0.2062	[-]	[-]
Solar + Sun Elevation	0.84908	0.0957	0.1375	-33.2170	-33.3172
Solar + Humidity	0.80107	0.1001	0.1297	-30.1465	-37.1000
Solar + Pressure	1.33226	0.1910	0.2158	+33.2868	+4.6557
Solar + Wet Bulb Temp.	1.16352	0.1519	0.1884	+6.0014	-8.6324
Solar + Dry Bulb Temp.	0.93376	0.1080	0.1512	-24.6336	-26.6731
Solar + Wind Speed	1.54306	0.2136	0.2500	+49.0579	+21.2415

230 produced by sampling from an Auto-Regressive Moving Average (ARMA) model  
[52, 53], which tacitly assumes the training data can be made stationary. ESNs  
have been shown to replicate the environment of a dynamical system, although  
it remains to be seen how far in the future this behavior persists [31, 32]. Future  
work will also explore the effect of data resolution on model performance, as well  
235 as evaluate some of the improvements to the ESN algorithm.

## 5. Conclusion

Improving renewable energy forecasting is important for grid-planning and  
unit commitment. Especially as the share of variable renewable resources  
increases, challenging the baseload power from nuclear plants. We first demon-  
240 strated that our implementation of the ESN algorithm is consistent with the  
literature. Then we applied this model to prediction tasks for total demand, solar  
energy, and wind energy, and evaluated the influence of several meteorological  
factors on model performance. Our results show that additional inputs must be  
chosen carefully to avoid increasing the system complexity. The conventional  
245 ESN used here did not demonstrate an improvement over the state-of-the-art.

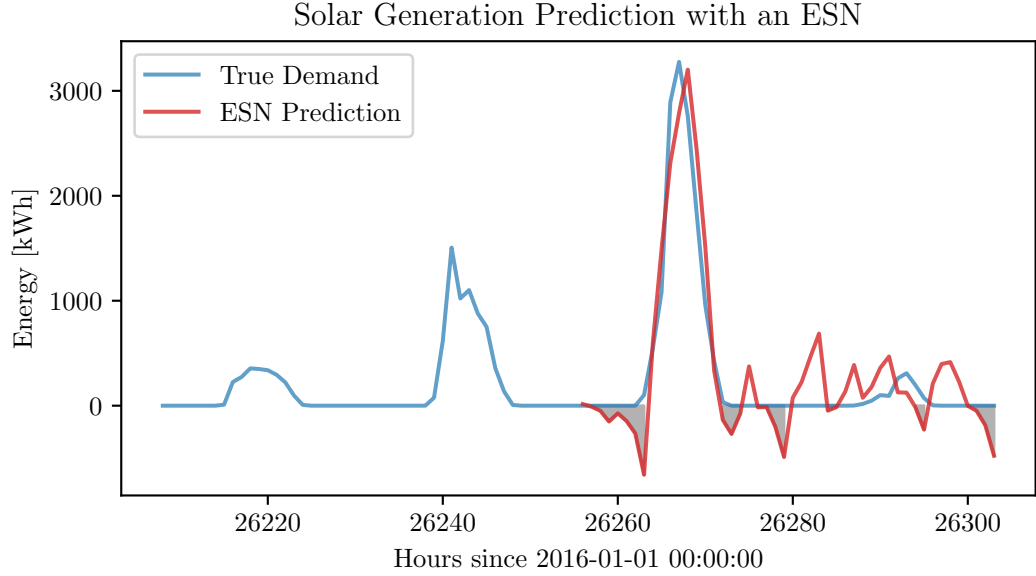


Figure 7: The optimized 4 hour ahead solar energy prediction. The inputs for this forecast were solar energy and hourly wet bulb temperature. *Hyperparameters*: Reservoir Size:800, Sparsity: 0.01, Spectral Radius: 0.9, Noise: 0.0001, Training Length: 5000, Prediction Window: 4, Random state: 85

Nor was it accurate enough to improve grid-scale energy economy. Future work will explore other applications of ESNs and evaluate improvements to the model algorithm.

## 6. Acknowledgments

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Table 8: Tabulated error for 4-hour ahead solar energy forecasts with various coupled quantities. Improvement indicates the percentage improvement over the base case of forecasting solar energy alone.

Scenario	NRMSE	MAE	RMSE	Improvement MAE (%)	Improvement RMSE (%)
Solar Energy	0.59151	0.0614	0.0958	[-]	[-]
Solar + Sun Elevation	0.51383	0.0554	0.0832	-9.7720	-13.1524
Solar + Humidity	0.59943	0.0663	0.0971	+7.9804	+1.3570
Solar + Pressure	0.77968	0.0925	0.1263	+50.6515	+31.8372
Solar + Wet Bulb Temp.	0.41541	0.0526	0.0673	-14.3322	-29.7954
Solar + Dry Bulb Temp.	0.61334	0.0682	0.0993	+11.0749	+3.6534
Solar + Wind Speed	0.70216	0.0723	0.1137	+17.7524	+18.6848

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260 the DOE H2@Scale Program (Award Number: DE-EE0008832)

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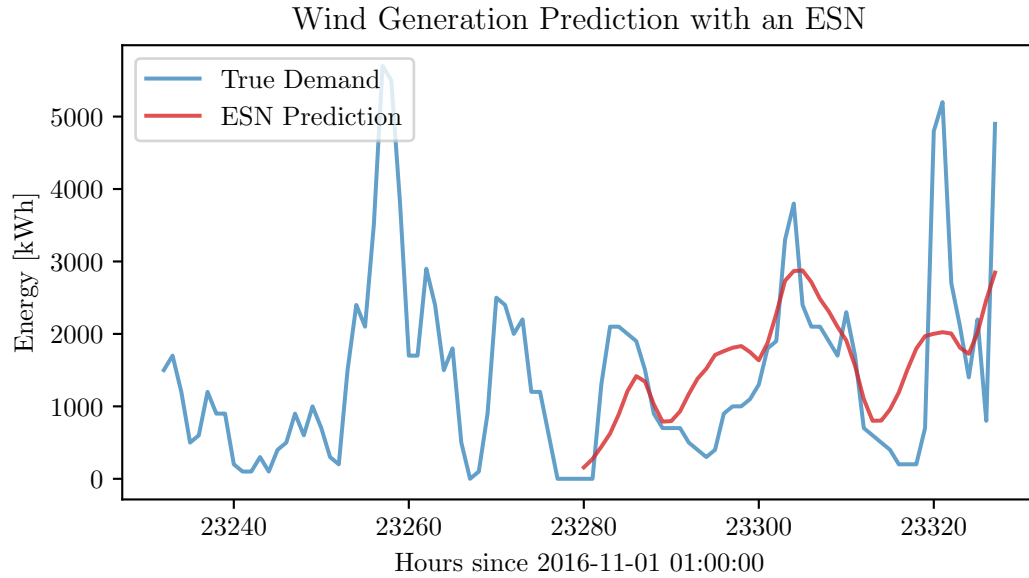


Figure 8: The optimized 48-hour ahead wind energy prediction that minimized the RMSE. The inputs for this forecast were wind energy and solar elevation angle. *Hyperparameters:* Reservoir Size:1000, Sparsity: 0.1, Spectral Radius: 0.9, Noise: 0.0001, Training Length: 19100, Prediction Window: 48, Random state: 85

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Table 9: Tabulated error for 48-hour ahead wind forecasts with various coupled quantities. Improvement indicates the percentage improvement over the base case of forecasting wind energy alone.

Scenario	NRMSE	MAE	RMSE	Improvement MAE (%)	Improvement RMSE (%)
Wind Energy	0.93167	0.1035	0.1308	[-]	[-]
Wind + Sun Elevation	0.81220	0.0857	0.1141	-17.1981	-12.7676
Wind + Humidity	0.84950	0.0952	0.1193	-8.0193	-8.7620
Wind + Pressure	0.98345	0.1076	0.1381	+3.9614	+5.5810
Wind + Wet Bulb Temp.	0.84323	0.0886	0.1184	-14.3961	-9.4801
Wind + Dry Bulb Temp.	0.86365	0.0815	0.1213	-21.2560	-7.2630
Wind + Wind Speed	0.84180	0.0763	0.1182	-26.2802	-9.6330

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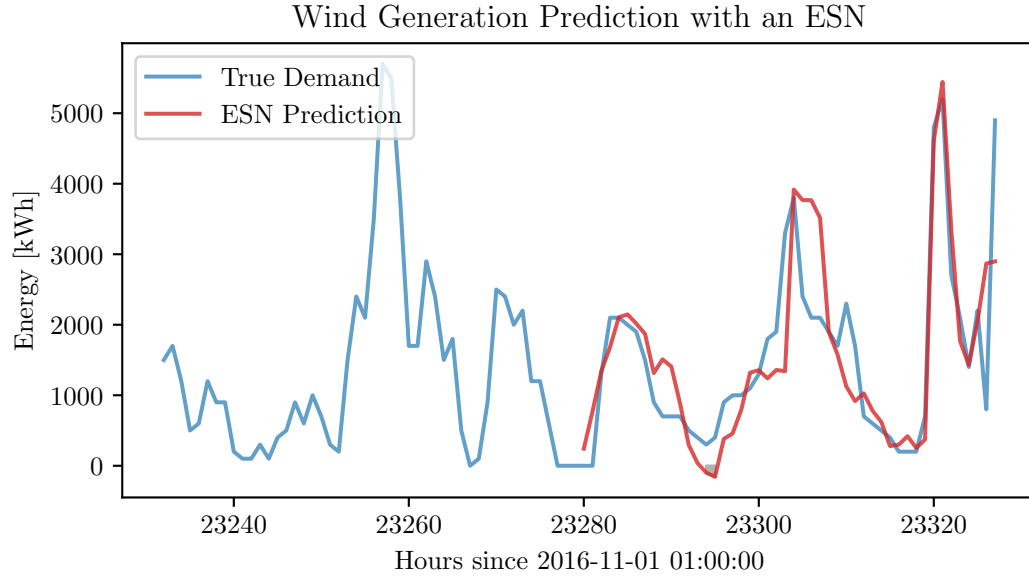


Figure 9: The optimized 4 hour ahead wind energy prediction. The inputs for this forecast were wind energy and hourly windspeed. *Hyperparameters*: Reservoir Size:1000, Sparsity: 0.15, Spectral Radius: 0.9, Noise: 0.001, Training Length: 14300, Prediction Window: 4, Random state: 85

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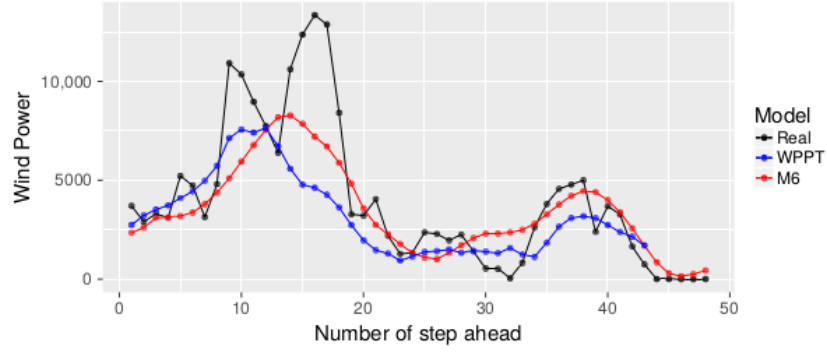
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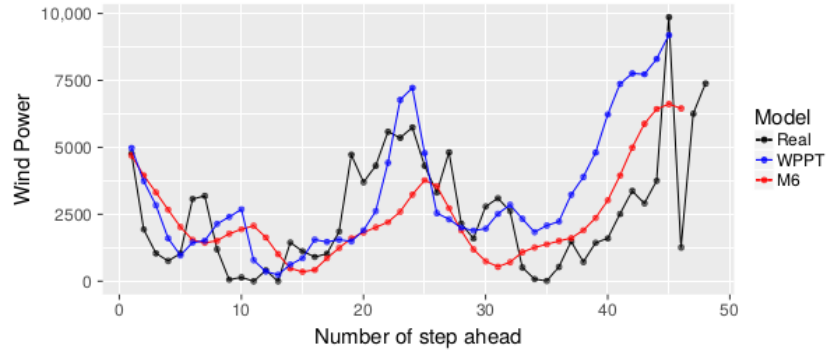
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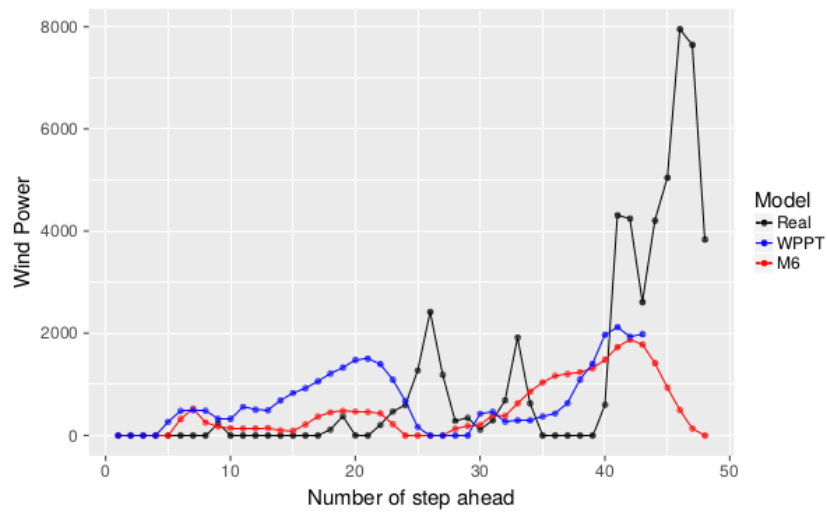
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**Figure 9.** Forecasting using subseries  $r = 1$ .



**Figure 10.** Forecasting using subseries  $r = 5$ .



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**Figure 11.** Forecasting using subseries  $r = 10$ .

Figure 10: The results of 48-hour ahead predictions from a forecasting algorithm combining ESN and long short term memory algorithms (“M6”). Compared to the Wind Power Prediction Tool (WPPT). Figure reproduced from López et al. 2018 [28].



Table 10: Tabulated error for 4-hour ahead wind forecasts with various coupled quantities. Improvement indicates the percentage improvement over the base case of forecasting wind energy alone.

Scenario	NRMSE	MAE	RMSE	Improvement MAE (%)	Improvement RMSE (%)
Wind Energy	0.88507	0.0903	0.1243	[-]	[-]
Wind + Sun Elevation	0.83394	0.0705	0.1171	-21.9269	-5.7924
Wind + Humidity	0.85522	0.0813	0.1201	-9.9668	-3.3789
Wind + Pressure	0.88587	0.0866	0.1244	-4.0974	+0.0804
Wind + Wet Bulb Temp.	0.76203	0.0731	0.1070	-19.0476	-13.9179
Wind + Dry Bulb Temp.	0.79939	0.0747	0.1123	-17.2757	-9.9654
Wind + Wind Speed	0.59596	0.0571	0.0837	-36.7663	-32.6629

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