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AUTOMATED ISOTOPE IDENTIFICATION USING ARTIFICIAL NEURAL NETWORKS

BY

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PRELIMINARY EXAMINATION

Submitted in partial fulfillment of the requirements  
for the degree of **Master of Science** in Nuclear Plasma and Radiological Engineering  
in the Graduate College of the  
University of Illinois at Urbana-Champaign, 2018

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*Adj. Assf. Res.*

*PhD*

*I am not totally  
sure about  
whether these  
caveats are  
necessary*

# ABSTRACT

There is a need to develop an algorithm that can identify and quantify isotopes in low-resolution gamma-ray spectra. Trained gamma-ray spectroscopists typically rely on intuition when identifying isotopes in spectra. Because they incorporate something similar to intuition, pattern recognition algorithms such as neural networks are prime candidates for automated isotope identification. Algorithms based on feature extraction such as peak finding or ROI algorithms work well for well-calibrated high resolution detectors. For low-resolution detectors, it may be more beneficial to use algorithms that incorporate more abstract features of the spectrum. To solve this, an artificial neural network (ANN) was trained to predict the presence and relative activities of isotopes from a mixture of many isotopes. The ANN is trained with simulated gamma-ray spectra, allowing easy expansion of the library of target isotopes. This proposal outlines extensions to this work including investigating new datasets and ANN structures.

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wrong dash type.

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It seems like you've using the wrong (long) dash type (the one intended to

# CHAPTER 1

## INTRODUCTION

separate clauses rather than words) where you want to use a normal hyphen.

The main question addressed in this work is: Can artificial neural networks (ANNs) using simulated spectra as training data automate isotope identification and quantification? Gamma-ray spectroscopists often use intuition when identifying isotopes in spectra. ANNs mimic this abstract analysis, synthesizing features of a gamma-ray spectrum in non-intuitive ways. Exploiting this intuition may overcome common hurdles encountered by other isotope identification algorithms.

The proposed work will demonstrate the performance of ANNs for automated gamma-ray spectroscopy in low-resolution spectra. The low-resolution detector of interest in this work is a 2-inch by 2-inch NaI(Tl) cylindrical scintillation detector. This detector is industry standard due to its ease of use, low cost, and acceptable resolution for gamma-ray spectroscopy.

The **algorithms** performance will be displayed on two different datasets. The first dataset will focus on identifying isotopes in ANSI N42-34-2006, the American national standard performance criteria for hand-held instruments for the detection and identification of radionuclides [1]. The second dataset will be built to perform uranium enrichment calculations.

In addition to isotope identification, this work will explore the ability of ANNs to quantify the count contribution from each isotope. The ANN's ability to extract count contribution information from gamma-ray spectra is important for nondestructive analysis (NDA). ~~An example of NDA is performing~~ <sup>such as</sup> uranium enrichment calculations. Knowing the enrichment of uranium is important in two scenarios. The first scenario is when uranium is identified at a border crossing. Typically the spectrum would need to be given to a trained spectroscopist to quantify the enrichment, but this process could be automated on the device first used to identify it. The second case would be in treaty verification technologies. Low-resolution NaI

need more info here... sensitive info what?  
Perhaps "revealed" "detected" "recorded"  
"captured" ?

This fact is brand new to the reader. Reorder the sentence to guide the reader.

gamma-ray detectors decrease the amount of possibly sensitive information while giving enough information to produce accurate enrichment quantification. The fact that ANNs can be taught to ignore certain patterns and only give information agreed upon by treaty signatories also makes them a good tool for treaty verification. The ability of ANNs to operate without knowing the shielding and background spectrum makes them better for zero knowledge scenarios. NaI detectors also have a higher efficiency than the higher resolution HPGe. This means that the counting times for NaI are smaller than would be required to get the same number of counts using an HPGe.

"Accordingly, ANNs may be a good tool for treaty verification because they can be taught to ignore certain patterns and only give information agreed upon by treaty signatories."

Similarly, because ANNs can operate without shielding and background spectrum information, they will perform better in "zero knowledge scenarios."

Consider beefing up this section. One page does not a "chapter" make. Explain what lies ahead in the document. Additionally, consider stating clearly how you will know when this work is complete...

(performance metric, benchmark, usable software tool)



Included or included? legacy or state of the art? Is this the contemporary art?

# CHAPTER 2

## LITERATURE REVIEW

### 2.1 Gamma-Ray Spectroscopy for Isotope Identification

Traditionally, isotope identification is conducted by a trained spectroscopist. Rawool-Sullivan et al. identified a common workflow performed by a group of gamma-ray spectroscopists [2]. This workflow included discriminating background and source photopeaks, adjusting the calibration using background photopeaks and checking for shielding effects in the low-energy photopeaks. Once photopeaks are identified, the spectroscopist would use their prior knowledge of isotope emissions (or consult a database of these emissions) to match isotopes to the spectrum. The researchers also noted that while spectroscopists used this book knowledge, they often would use intuition developed from analyzing tens or hundreds of gamma-ray spectrum. The researchers also noted the difficulty in incorporating this subjective analysis into an automated algorithm.

very good.

There are many automated radioisotope identification methods available, but few perform well given a low-resolution gamma-ray spectrum of a mixture of radioisotopes. Common methods include library comparison algorithms, region of interest (ROI) algorithms, principle component analysis (PCA), and template matching.

yes! here narrative!

Spectra

Library comparison algorithms attempt to match photopeak energies found in a gamma-ray spectrum with those found in a library of known isotope decay energies. Drifts and uncertainties in detector calibration can lead to misidentifying photopeaks, leading to incorrect isotope identifications [3]. To be automated, this method needs an algorithm to extract photopeak centroids from a spectrum. Photopeak extraction algorithms face difficulties when a large number of photopeaks overlap in a spectrum, such as when a mixture of radioisotopes are measured with a low-resolution detector [4].

It seems like you mean, explicitly, "extract photopeak centroids"

Metrics for performance?

despite drift & calibration error. True?

target  
radioisotope

perform

in this context,  
"different" is confusing.  
→ avoid "different" when you mean  
"various"

ROI algorithms search for elevated counts compared to background in a region where photopeaks are expected ~~to be for different radioisotopes~~. ROI algorithms may also operate poorly when photopeaks of different radioisotopes overlap [3]. For this reason, large isotope libraries will **perform** poorly using this method. Similarly to the library comparison algorithm, calibration drift may shift photopeaks into different neighboring ROIs, leading to incorrect identification. The ROI method has been used to differentiate normally occurring radioactive material (NORM) from special nuclear material (SNM) using plastic scintillators [5].

PCA can also be applied to radioisotope identification. The goal of PCA is to reduce the dimensionality of a dataset into uncorrelated variables [6]. Using a few of these principle components, the data may be represented in a reduced space that contains most of the information present in the original data. The transformed data can then be clustered based on isotope identity. Clustering algorithms may include K-means or Mahalanobis distance [7, 8]. PCA has been applied to isotope identification using plastic scintillators [9] and anomaly detection using both plastic scintillators and NaI detectors [10]. Despite the progress of PCA in some isotope identification problems, there has not been significant progress in applying PCA to separating mixtures of isotopes in gamma-ray spectra.

quantitatively

Template matching algorithms find an example in a database of gamma-ray spectra that most closely matches a measured spectrum [3]. The database of spectra can contain multiple detector calibration settings, shielding materials, and source-to-detector distances. Goodness of fit can be measured using a hypothesis test such as chi-squared test, euclidean distance, or Mahalanobis distance. While a sufficient amount of example spectra can be used to identify almost any measured spectrum, the drawback of this method is the time necessary to compare a measured spectrum to the library and the computer memory necessary to store said library. This method also may have difficulty when mixtures of isotopes are considered, although work is being done to correct this [11].

These algorithms largely incorporate book knowledge. By further incorporating the intuition identified by Rawool-Sullivan et al., these algorithms may be improved. A machine learning approach to automated gamma-ray spectroscopy may be able to marry book knowledge and a trained spectroscopists intuition.

## 2.2 Artificial Neural Networks

Artificial neural networks were first created to mimic biologic neurons. Since their creation, they have demonstrated promising results on a variety of different classification and regression tasks [12, ?, ?]. The following sections will give an overview of how ANNs learn and operate.

### 2.2.1 Architecture and Training

ANNs work by mapping arbitrary input spaces,  $\mathbb{R}^N$ , to arbitrary output space,  $\mathbb{R}^K$ . An example one hidden layer ANN mapping  $\mathbb{R}^N \mapsto \mathbb{R}^K$  is shown in Figure 2.1. Each circle represents a neuron, or node. The mathematical process governing each neuron in the ANN is shown in Figure 2.2. In Figure 2.2, the signal from the previous layer is propagated to the next by applying some function, typically sigmoidal, to the dot product of the signal from the previous layer and the weight vector going into a given node,  $B_j$  in Figure 2.2. Given a one-layer ANN with a finite number of hidden nodes, any function  $\mathbb{R}^N \mapsto \mathbb{R}^K$  can be described to arbitrary precision [?]. Additional hidden layers increase the representational power of an ANN, reducing the number of nodes and computational power required to represent a function. There is no direct method to compute the optimal number of hidden layers or nodes for a given problem. These, along with other hyperparameters, need to be optimized for a given dataset.

Artificial ANNs learn a function by changing the weights connecting the layers so that some error function is minimized for a given dataset. One popular method to update the weights is through the process of gradient descent through the backpropagation of errors [?]. The update equation for a single weight,  $w_j$ , is shown in Equations 2.1 and 2.2. In these equations,  $E$  is the given error function to be minimized (commonly mean squared error or cross entropy) and  $\eta$  is the learning rate of the ANN.

$$\Delta w_j = -\eta \frac{dE}{dw_j} \quad (2.1)$$

*this jargon needs to be saved for a few sentences. Just say "An example ANN..." and explain hidden layers separately.*

*Separate the Fig 2.1 discussion into its own paragraph. Provide a shallower intro to the concept. Too steep.*

*Drop in explanation of hidden layers here? Most folks don't know what makes a function sigmoidal.*

*total? including hidden?*

*Corresponding*

*Number of layers & number of nodes?*

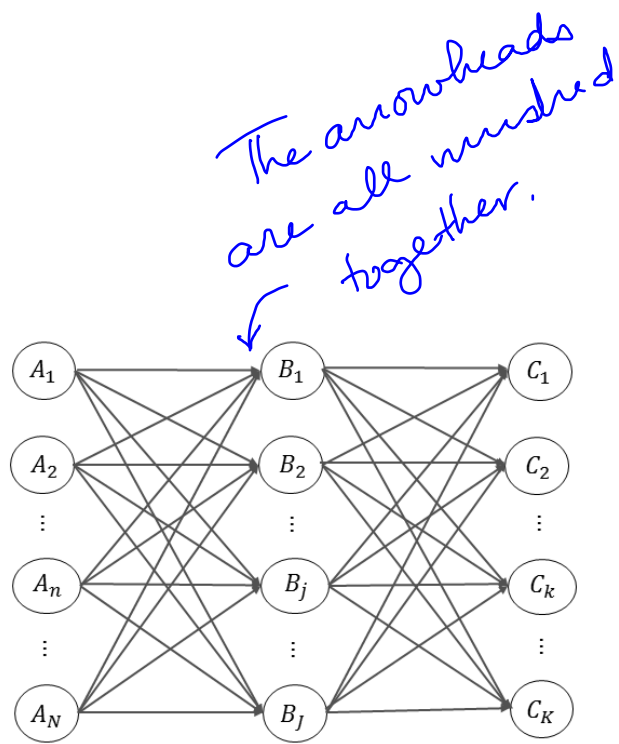


Figure 2.1: Example ANN with input layer A, hidden layer B, and output layer C.

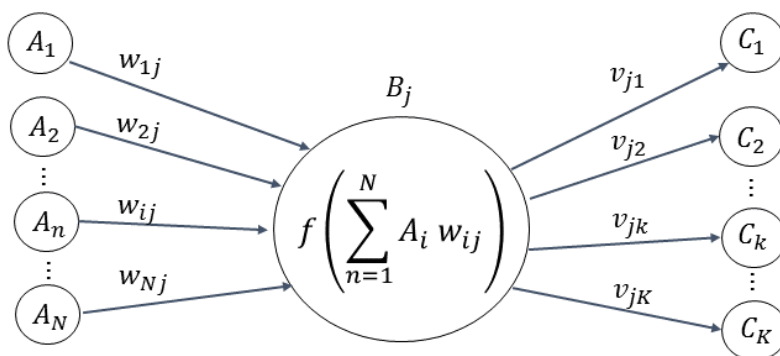


Figure 2.2: Summary of the operation of a single neuron.

Try to keep figures from breaking eqns. Use align?

$$w_j^{new} = w_j^{old} + \Delta w_j$$

← consider including eqn in sentence. (2.2)

Discuss where weight updates fit in the algorithm.

## 2.2.2 Hyperparameters

this is the first mention of training sets.

In general, ANNs have a tendency to memorize their training set in a process called over-training. An overtrained ANN will tend to incorrectly identify novel data. To prevent this, a number of hyperparameters were used to prevent overfitting and optimize performance.

Explain the algorithm procedure above.

Unfortunately, there is currently no known method to know which hyperparameters have an impact on model performance before training. Because of this, a number of popular hyperparameters are typically added to a model and a random hyperparameter search is used to identify those which are important. There is evidence that a random search in a given hyperparameter range finds better hyperparameters quicker than a grid search in the same range [?]. There is also a proof showing that given 60 points randomly sampled in some space with a finite minimum, the minimum of those 60 random samples is within 5% of the true minimum with 95% probability [?]. Training 60 ANNs is computationally feasible, making this a good method to find a close-to-optimal ANN for a given dataset.

Missing a word?

## 2.3 Automated Isotope Identification Using ANNs

There have been a number of published papers which apply ANNs to automated isotope identification. ANNs have been applied to peak fitting [?], isotope identification [?, ?], and activity estimation [?, ?]. Many of this work rely on ROI methods [?], feature extraction [?], high-resolution gamma-ray spectra as the input to the ANN [?], small libraries of isotopes, and assume perfectly calibrated detectors. ANN training methods created for high-resolution gamma-ray spectra may not perform well when trained using low-resolution spectra given the large discrepancy in resolution. ANN training that relies on ROI methods may not perform well when ROIs overlap significantly with large libraries of isotopes.

This is a tautology. Why won't they work?

It has been shown that an ANN may be trained to perform isotope identification and

quantification using low-resolution NaI gamma-ray spectrum using a library of six isotopes [?]. While promising, this study used a library too small to be of practical use. The American National Standards Institutes (ANSI) has identified 31 gamma-ray emitting isotopes that automated isotope identification algorithms should be able to identify [1].

Cliffhanger... need concluding paragraph for this chapter.

Perhaps reiterate what it is you will do to fill the gap. You mention the ANSI standard but then... what happened to saying you'd use it?

It may not be immediately clear that you did this work.

# CHAPTER 3

Use the intro section to introduce

## ARTIFICIAL NEURAL NETWORK APPROACH TO IDENTIFYING AND QUANTIFYING ISOTOPES IN GAMMA-RAY SPECTRA

the work as preliminary effort upon which the proposed thesis work is being built.

### 3.1 Introduction

of possible isotopes

The ANN presented here is trained to quantify the count contribution of each isotope from a library. Because the ANN trains using simulated gamma-ray spectra, additional datasets can be trivially created. The ANN structure, training details, and hyperparameter optimization are described.

evaluate an unknown spectrum and testing datasets

### 3.2 Artificial Neural Network Structure

The fully connected ANN explored in this work uses a rectified linear (*relu*) activation function, seen in Equation 3.1, with a *softmax* output function, seen in Equation 3.2.

uses it for what? refer back to fig 2.1 & 2.2.

$$relu(x) = \max(0, x)$$

only final period needed.

$$softmax(z_j; \mathbf{z}) = \frac{\exp(z_j)}{\sum_{k=1}^K \exp(z_k)}$$

Be clear about who did the showing. You right?

The *relu* function was chosen for the node activations because previous work has shown that it is easy to optimize and generally perform better than other non-linear functions [?, pg. 189]. While the *softmax* function is traditionally used in classification ANNs, using it here ensures the output from the ANN is normalized to unity. This allows the ANN to output relative count contributions from each isotope. This method was shown to perform well for quantifying isotopes in real and simulated spectra [?, ?].

where is this in the algorithm procedure?

By setting a **detection threshold** based on the highest count contribution, this method can also be used as an

Say that "I showed" or "The present work showed"

identification algorithm. For example, Table 3.1 shows the top five isotope outputs from an ANN that used the spectrum in Figure 3.1 as input. Using an arbitrary threshold of 15%, any isotope with a contribution below 15% of 0.441 can be ignored. This leads to a correct identification of  $^{60}\text{Co}$ ,  $^{137}\text{Cs}$ , and background. **The threshold used can be chosen to ensure a desired performance metric (false alarm rate, precision, recall) on an appropriate dataset.**

Table 3.1: Top five isotopes found by an ANN trained to quantify isotopes.

Isotope	Count Contribution
$^{60}\text{Co}$	0.441
$^{137}\text{Cs}$	0.440
Background	0.068
$^{99}\text{Mo}$	0.019
$^{235}\text{U}$	0.017

*These metrics deserve more time. Perhaps later.*

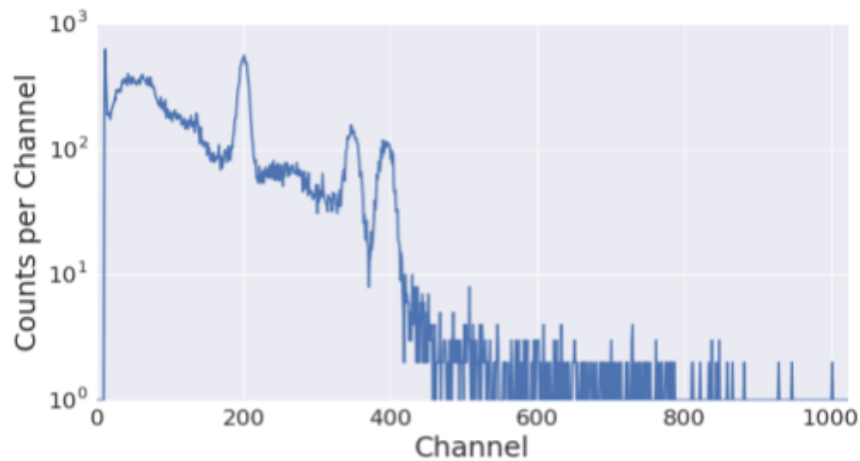


Figure 3.1: Gamma-ray spectrum of a  $0.288 \mu\text{Ci } ^{60}\text{Co}$  source and a  $0.890 \mu\text{Ci } ^{137}\text{Cs}$  source. Each source-to-detector distance was adjusted so their respective count rate on the detector was equal.



### 3.3 Dataset Construction

consider a flow chart  
image to accompany  
this paragraph.

In order to train an ANN, a training set and training key must be provided. The training set is a set of ANN input data and the training key is the correct ANN output for each input. Because creating a training set of real gamma-ray spectra is infeasible, the training set used in this work was simulated. The training set was created using a one-dimensional Monte Carlo radiation detector simulation program called GADRAS [?]. The simulation process began by simulating individual 1 mCi sources with no background. Each source was simulated at a distance of 30cm from a 2 inch by 2 inch Ortec 905-3 NaI spectrometer for 10 hours, ensuring each spectrum had low statistical noise. These single-isotope sources were then sampled using the inverse transform sampling method [?]. This allows the creation of arbitrary source combinations. The background isotopes were modeled using built-in GADRAS background sources for  $^{40}\text{K}$ , uranium and daughters in soil, and thorium and daughters in soil.

Because the calibration on NaI detectors shifts over time (due to voltage drift in the electronics and changes in crystal temperature), a method to change training spectra calibration was included. To mimic gain shift, the channels in each spectrum were linearly rebinned by some percent. The magnitude of each shift was uniformly chosen between a +/- 25% gain drift. After rebinning, the resulting spectrum was reconstructed using third order spline interpolation with the new bin positions.

Using this method, many training sets can be created depending on different algorithm goals. The training set and isotope library can be modified for specific problems like unknown source interdiction and uranium enrichment calculations. Methods of creating ANNs for these problems will be described in later sections.

### 3.4 Training Details and Hyperparameter Optimization

An optimization algorithm is needed to train the model. Optimization is necessary to choose good model parameters and hyperparameters. Model parameters are the weights connecting each layer in an ANN. Optimizing the model parameters is also known as training or learn-

Trying and seeing might need to be formalized a bit, ideally based on performance metrics.

ing. Hyperparameters are the variables that define the structure of the ANN (number of layers, nodes in each layer, non-linear function on each node) as well as the variables that control how the model learns (the learning rate, neuron dropout frequency, loss function).

Finding appropriate hyperparameters requires trying different hyperparameter combinations and seeing which gives the lowest validation error on a dataset. This can be done using either a manual or automated search.

The Adam optimizer was chosen as the training algorithm for this work due to its incorporation of parts of other successful optimization algorithms and its reported superior performance over these algorithms [?]. Another benefit of the Adam optimizer is the introduction of only one additional hyperparameter, the learning rate. Other optimizers require tuning more than one additional hyperparameter. During training, the ANN minimized the average cross entropy,

define  $N$ .

$$E = -\frac{1}{N} \sum_{n=1}^N y_n \log(\hat{y}_n) + (1 - y_n) \log(1 - \hat{y}_n), \quad (3.3)$$

between the correct labels,  $y_n$ , and the network predictions,  $\hat{y}_n$ . This cost function was chosen because it is traditionally used with ANNs whose output is the *softmax* function.

Raw data is typically preprocessed before being input to an ANN. For this work each spectrum was preprocessed by scaling the counts in each bin between [0,1]. Scaling the inputs improves numerical stability during training.

Hyperparameters are often necessary to properly train an ANN. The following hyperparameters are considered in this study are: the number of neurons in each layer, the number of layers used, initial learning rate for the training algorithm, the  $L_2$  weight regularization strength, and neuron dropout rate.

Adding  $L_2$  weight regularization allows the magnitude of the weights to increase only when there is a comparable reduction in the unmodified error function.

$$\tilde{E} = E + \sum_i \lambda w_i^2, \quad (3.4)$$

only one period needed

In Equation 3.4,  $w_i$  is the weight between each neuron in the ANN and  $\lambda$  is the regularization

delete one "are"

strength hyperparameter. A larger  $\lambda$  will force the ANN to prefer smaller weights connecting the neurons. This reduces the **models** capacity, or its ability to represent complicated or intricate functions. This is similar to putting a limit on the magnitude of the coefficients in a high order polynomial when fitting data. If  $\lambda$  is too small, the model will have a ~~greater~~ <sup>too much</sup> capacity. This will create a model that is more likely to overfit. If  $\lambda$  is too large, the ANN will preferentially minimize the  $L_n$  error, failing to learn the desired task.

Another method to reduce model capacity is neuron dropout. Neuron dropout is the process of temporarily removing a neuron from the ANN architecture during training [?]. The probability that a neuron is removed is called the neuron dropout rate, which is a hyperparameter. By applying dropout throughout training, the ANN's architecture changes every iteration. This makes neuron dropout a cost efficient way to average many different ANN architectures, improving performance.

## 3.5 Key Results

Two key results are described in the following section. The first result demonstrates the ANNs ability to correctly identify isotopes in the ANSI N42-34-2006 library with an unknown calibration. This demonstration also demonstrates how well the ANN operates when spectroscopic features such as photopeaks are unclear. The second result demonstrates the ANNs ability to **identify if an isotope that is shielded by lead.**

### 3.5.1 Single Isotope Identification

The isotope library chosen for this demonstration was 29 gamma-ray producing isotopes from the ANSI N42.34-2006 standard, as well as  $^{152}\text{Eu}$  [1]. **The reason for including will be described in a later section. because it is available in our lab.** Based on lab observations using an Ortec 905-3 NaI spectrometer, the average background count rate was set at 85 counts per second (cps). Each spectrum in the training set had a maximum of 5 different non-background isotopes included ~~in the spectrum~~. Each isotope had a count rate which was logarithmically distributed between 10 and 1000 cps. The exposure time was logarith-

Is this range/distribution representative of the target application?

Natural Th & U?

How strong?

mically distributed between 10 and 2000 seconds. Each non-background isotope had an equal probability of being included in each spectrum. The counts from background were distributed uniformly between background thorium, background uranium, and background  $^{40}\text{K}$ . To mimic calibration shift, the channels in each spectrum were linearly rebinned. The magnitude of each shift was uniformly chosen between a  $\pm 25\%$  calibration drift. The 0% gain shift setting corresponds to a detector with a maximum bin energy of 3 MeV. A calibration drift of  $\pm 25\%$  is an extreme case of incorrect calibration.

To demonstrate the performance of the algorithm on spectra with single isotopes where features were easily identifiable by eye versus spectra without obvious visible features, two simulated validation datasets were considered. Both datasets consisted of spectra with a single isotope simulated using the same process as the ANN training set with the rebinning randomly chosen between  $\pm 20\%$ . The rebinning magnitude was reduced to avoid testing the ANN near the edge of its training. A calibration drift of  $\pm 20\%$  is still an extremely incorrect calibration. A confusion matrix was used to compare the performance of the ANN on both datasets. For all the results, the count contribution cutoff was arbitrarily set at 15% of the largest count contribution calculated by the ANN.

For spectra in the first validation dataset, both the source and background contributed 85 counts per second with an integration time of 60 seconds. Each isotope in the training library was simulated one hundred times with this count distribution. Simulated  $^{60}\text{Co}$  spectra with the extreme calibration settings are shown in Figure 3.2.

Figure 3.3.1

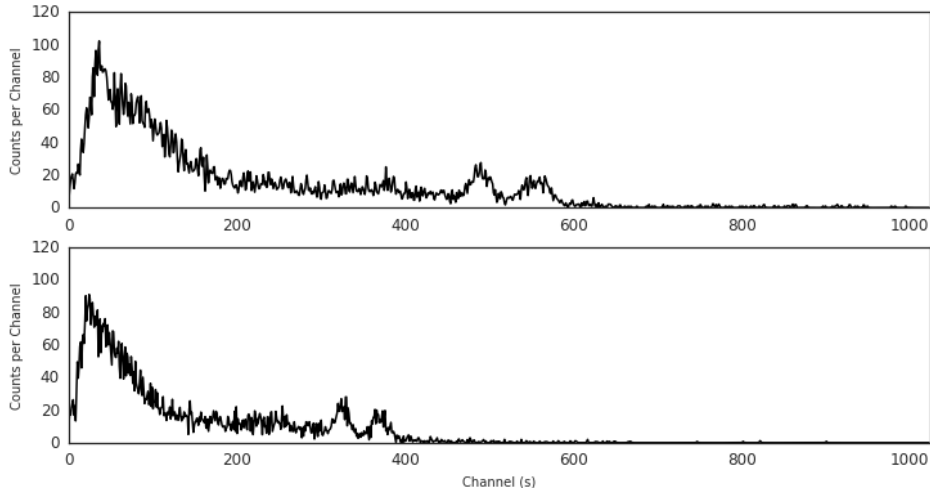


Figure 3.2: Two simulated  $^{60}\text{Co}$  spectra. In each spectrum, the  $^{60}\text{Co}$  and background contribute 5100 counts to the spectrum. The bottom spectrum's gain was offset by  $-20\%$  while the top spectrum's gain was offset by  $+20\%$ .

The confusion matrix generated using an ANN is displayed in Figure 3.3. In this confusion matrix, the largest count contributing isotope was used to identify the spectrum. The ANN exhibited a low false positive rate with this simulated dataset. False positives occurred mainly with sources that primarily emit only a few low-energy photons. This is especially notable when  $^{99m}\text{Tc}$ , which primarily emits a 141 keV gamma-ray, is misidentified as  $^{57}\text{Co}$ , which emits a 122 keV gamma-ray. A  $-13\%$  calibration shifted  $^{99m}\text{Tc}$  spectrum looks almost identical to a  $^{57}\text{Co}$  spectrum without a calibration shift. Incorrect identification occurred due to the proximity of the photopeaks of these isotopes. Incorrect identification also occurred due to a lack of other prominent spectral features such as the Compton continuum for low-energy gamma-rays. This effect can also be seen in Figure 3.3 when  $^{204}\text{Tl}$  is misidentified as  $^{201}\text{Tl}$ . Both  $^{204}\text{Tl}$  and  $^{201}\text{Tl}$  primarily emit photons around 70 and 80 keV.

Perhaps explain how to read a matrix. This will be new to most readers.

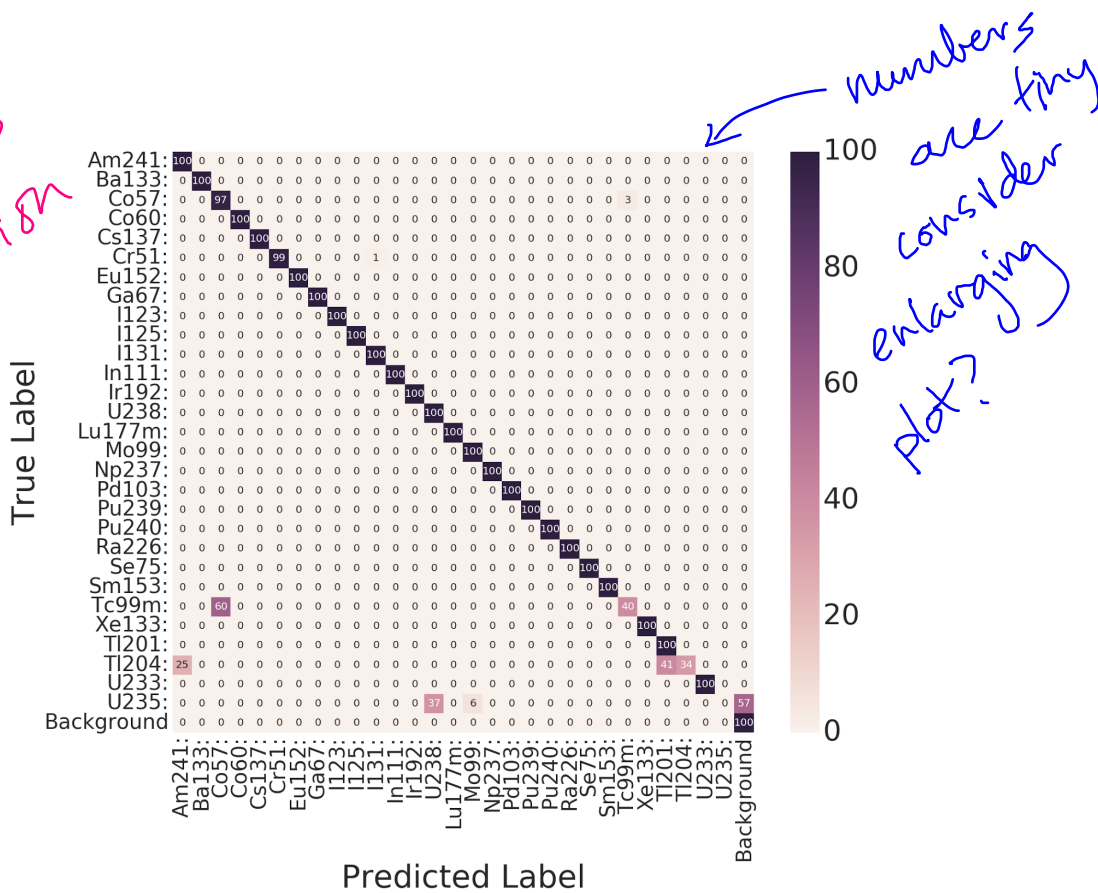


Figure 3.3: The confusion matrix for a single isotope dataset. Both the source and background contribute 5100 counts to the spectrum.

Simulated?

In the second validation dataset, the source and background were **measured** for 10 seconds and the source count rate was reduced to half the strength of background. Example simulated  $^{60}\text{Co}$  spectra with the extreme calibration settings are shown in Figure 3.4. Note that compared to figure 3.2, the photopeaks of  $^{60}\text{Co}$  are more difficult to identify by eye. The lack of clear spectral features in these spectra may present extra difficulty to algorithms that rely solely on feature extraction methods. Also, the lack of prominent background peaks would make these spectra difficult to calibrate.

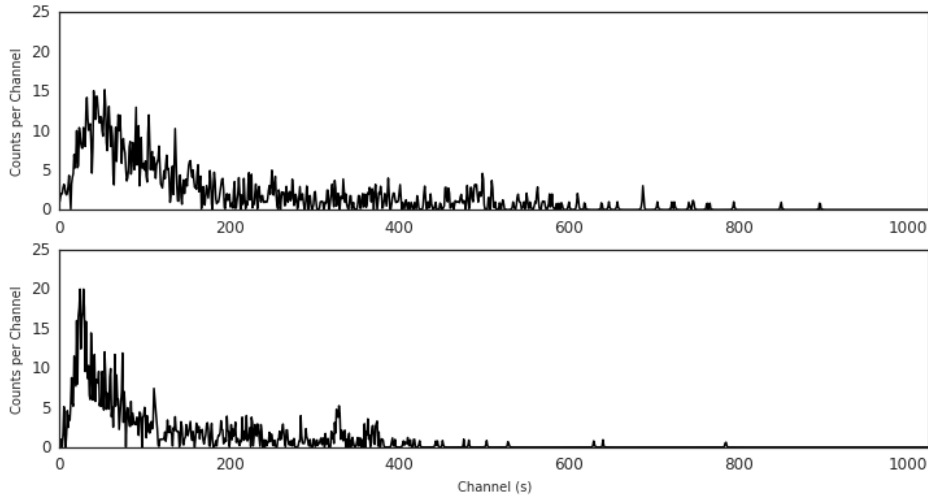


Figure 3.4: Two simulated  $^{60}\text{Co}$  spectra. In each spectrum, the  $^{60}\text{Co}$  source contributes 425 counts and background contribute 850 counts. The red spectrum's gain is offset by  $-20\%$ , while the blue spectrum's gain is offset by  $+20\%$ .

The confusion matrix for this dataset is shown in Figure 3.5. Note that the false positive rate increases, but often there was enough information in each spectrum to correctly identify the isotope. This implies that the ANN trained in this way can be effective in non-ideal measurement situations (low signal-to-noise spectrum, short measurement time, incorrectly calibrated detector).

*perhaps say  $^{60}\text{Co}$  with extreme gain shift*

Numbers are tiny,  
consider enlarging plot.

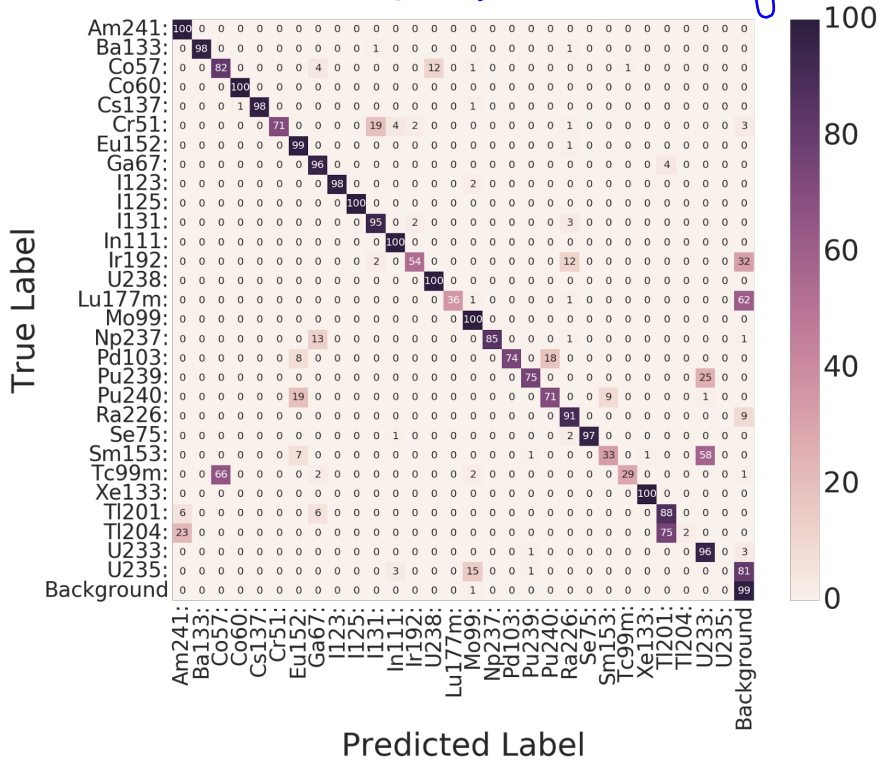


Figure 3.5: The confusion matrix for a single isotope dataset. In each case, the source contributes 425 counts and background contributes 850 counts to the spectrum.

### 3.5.2 Identifying Bare and Shielded $^{152}\text{Eu}$

An ANN was trained to identify bare and shielded isotopes. The ANN used a training dataset composed of bare and shielded sources from the ANSI N42–34–2006 library.

The ANNs performance is displayed by identifying a bare and shielded  $^{152}\text{Eu}$  source. The  $^{152}\text{Eu}$  isotope emits gamma-rays in a large range of energies. Because lower-energy gamma-rays are attenuated more strongly than higher-energy gamma-rays, the shielded  $^{152}\text{Eu}$  spectrum, shown in Figure 3.6, is significantly distorted compared to an unshielded  $^{152}\text{Eu}$  spectrum, shown in Figure 3.7. The effect of shielding can be seen by observing that the photopeaks below channel 100 observed in the bare source spectrum are not present in the shielded spectrum. In addition to distorting the spectrum, the shielding also reduced the number of counts in the spectrum, decreasing the signal-to-noise ratio.

good



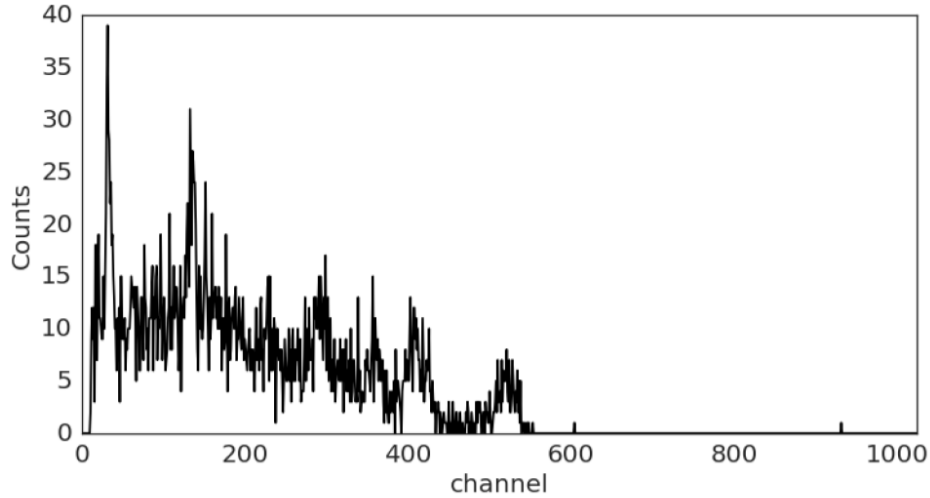


Figure 3.6: Spectrum of a Eu152 10 $\mu$ Ci source shielded by 8mm of lead. The collection time for this was 10s.

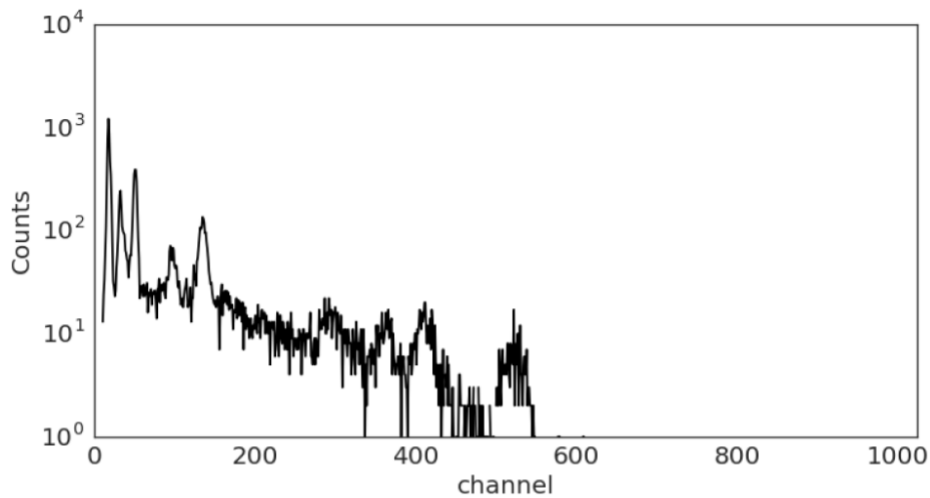


Figure 3.7: Spectrum of a Eu152 10  $\mu$ Ci source. The collection time for this was 10s.

*Varying by collection time or source strength?*

Despite the distortion and lower signal-to-noise ratio in the shielded example, the ANN was able to differentiate a bare and shielded  $^{152}\text{Eu}$  source. The average ANN output from 5 bare  $^{152}\text{Eu}$  spectra is shown in Table 3.2. Note that the ANN calculated that the vast majority of counts came from  $^{152}\text{Eu}$  and background. Table 3.3 shows the average ANN output for 5  $^{152}\text{Eu}$  spectra shielded by 8mm of lead. While the top count contributor was shielded  $^{152}\text{Eu}$ , the ANN included a number of incorrect sources with high count contributions. The extra identifications are likely due to the low signal-to-noise ratio in the shielded spectrum.

Table 3.2: Average ANN output from five spectra. Each spectrum was collected like the one in Figure 3.7. Only the top five isotopes are shown.

Isotope	Count Contribution
$^{152}\text{Eu}$	0.496
Background $^{40}\text{K}$	0.090
Background Uranium	0.072
Background Thorium	0.056
$^{60}\text{Co}$	0.051

*"simulated"*

Table 3.3: Average ANN output from five spectra. Each spectrum was **collected** like the one in Figure 3.6. Only the top five isotopes are shown.

Isotope	Count Contribution
Shielded $^{152}\text{Eu}$	0.303
Shielded $^{238}\text{U}$	0.234
$^{137}\text{Cs}$	0.182
$^{131}\text{I}$	0.084
$^{60}\text{Co}$	0.074

# CHAPTER 4

*motivation is given to establish that*

## FUTURE WORK AND PROPOSED EXPERIMENTS

For the proposed work, ~~there are~~ a number of experiments ~~that~~ will explore applying ANNs to gamma-ray spectroscopy. An outline of this work can be seen in Figure 4.1. Section 4.1 details two proposed **simulated** gamma-ray spectra datasets: **Arguments are given for why** these datasets represent important problems in gamma-ray spectroscopy. In addition to ANNs that use the full spectrum as input, ANNs that are trained to perform feature extraction will also be considered. Section 4.2 describes how autoencoders can be trained to extract key features from a gamma-ray spectrum. Section 4.3 **describes the how the** random hyperparameter search will be performed using K-folds cross validation. Once an appropriate ANN is found, a method called bagging (bootstrap aggregating) will be used to construct an ensemble of ANNs. Bagging is described in Section 4.4. Finally, the ANN performance on each **datasets** will be evaluated. Performance metrics are based on the ANN error in testing datasets, described in section 4.1.

*"dataset"*

*good!*

*verbs*

*nouns*

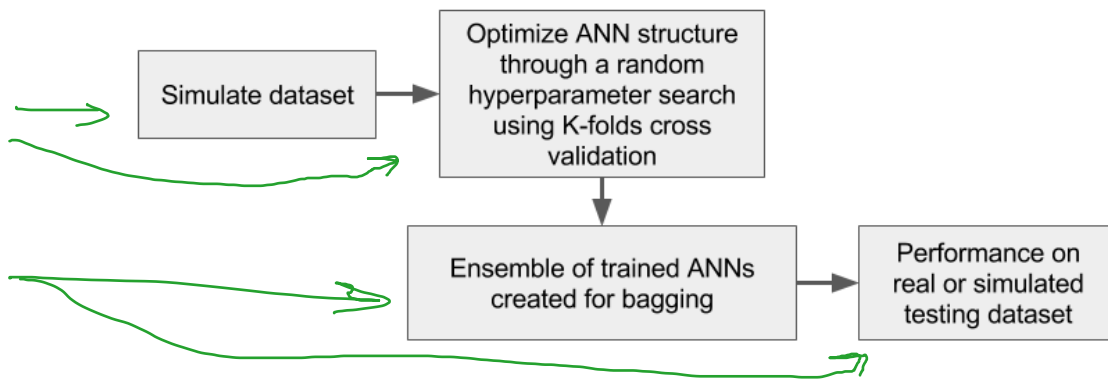


Figure 4.1: Workflow for the experiments proposed in this work.

## 4.1 Proposed Datasets

The proposed datasets represent important problems in automated gamma-ray spectroscopy. These include unknown source interdiction, uranium enrichment calculations, and isotope mixture analysis.

### 4.1.1 Unknown Source Interdiction

*This sentence seems to be missing a verb.*

One important problem in automated gamma-ray spectroscopy giving untrained operators the ability to identify an unknown source. Performance requirements for this task are outlined in ANSI N42-34-2006 standard. For this reason, this standard will guide the requirements in this section. Issues addressed by the ANSI standard include unknown shielding, unknown detector calibration, and unknown source combination. Methods to address these issues by using an ANN are described below. A way to validate the results is also described.

Typically, a source will be shielded, producing a weaker signals and distorting the spectrum. To address this, the training dataset will be sampled from a library of bare and shielded spectra. Because different materials have different shielding properties, a number of shielding materials and thicknesses will be included in the library. The materials included will be common shields, including aluminum, iron, and lead. The thicknesses will correspond to the amount needed to attenuate 662 keV gamma-rays by 20%, 40%, 60%, and 80%. These thicknesses can be seen in Table 4.1.

*how many?*

*Perhaps something very strongly shielded also? (95%)*

Table 4.1: Different amounts of aluminum, iron, and lead shield included in the training library.

	20%	40%	60%	80%
Aluminum	1.0 cm	2.3 cm	4.1 cm	7.2 cm
Iron	0.38 cm	0.87 cm	1.6 cm	2.8 cm
Lead	0.18 cm	0.42 cm	0.76 cm	1.3 cm

Because untrained operators would be using these algorithms, the detector calibration cannot be trusted. To address this, in each training batch the channels in each spectrum

will be rebinned. This rebinning will be based on the calibration <sup>of</sup> real detectors in our lab have at different photomultiplier tube (PMT) voltages. Typically these will be set at 750 V, corresponding to an energy range between 40 keV - 3000 keV. This energy range includes the gamma-rays required to identify isotopes in the ANSI library. The range of incorrect calibration will include 700 V - 800 V. *why not 20% as in the examples before?*

The ANSI standard also includes the ability to identify isotope mixtures in their requirements. The ANSI standard is primarily interested in combinations of special nuclear material (weapons grade plutonium (WGPu), high enriched uranium (HEU)) with medical isotopes (e.g.,  $^{99m}\text{Tc}$ ,  $^{201}\text{Tl}$ , or  $^{67}\text{Ga}$ ). To address this, random mixtures of one, two, and three isotopes will be included in the training dataset.

To fit the source interdiction scenario, count rate and source measurement time for spectra in the simulated training set will be kept within a range. The count rate on the detector will range from 10 counts per second (cps) to  $10^4$  cps. Below 10 cps the signal-to-background ratio will be too low for an identification. Above  $10^4$  cps deadtime effects will distort the spectrum. Sources above this count rate are easy to detect and would receive additional scrutiny. Source measurement times will range from 10 s - 1 hr. This is a typical range of measurements for source interdiction.

The performance of the ANN on this dataset will be reported in several ways. The ability to detect isotopes behind shielding will be tested by observing how the ANN identifies various laboratory isotopes behind shielding. Sources for this will include  $^{60}\text{Co}$ ,  $^{137}\text{Cs}$ ,  $^{152}\text{Eu}$ , and  $^{133}\text{Ba}$ . These sources are chosen because they represent isotopes with simple gamma-ray spectra ( $^{60}\text{Co}$  and  $^{137}\text{Cs}$  have two identifiable photopeaks) and more complicated spectra ( $^{152}\text{Eu}$  and  $^{133}\text{Ba}$  have multiple photopeaks). The amount of lead, iron, and aluminum included in **this experiment will depend on thickness of these materials available in our laboratory.** In addition to laboratory sources, real and simulated spectra of shielded HEU and WGPu will be included in this analysis. The mean ANN outputs and their variances will be presented for a number of spectra.

The ANNs ability to identify spectra with various calibrations will also use  $^{60}\text{Co}$ ,  $^{137}\text{Cs}$ ,  $^{152}\text{Eu}$ , and  $^{133}\text{Ba}$ . Spectra of individual sources will be measured using various calibrations. The calibration will be changed by changing the PMT voltage from 700 V to 800 V in 10 V

*and also presumably b/c they are available?*  
*i'm sure we can buy some common metals for you.*

*already said this?*

steps. The mean ANN outputs and variances will be presented for a number of spectra.

The ANNs ability to identify mixtures of less than three isotopes will be addressed. Mixtures of  $^{60}\text{Co}$ ,  $^{137}\text{Cs}$ ,  $^{152}\text{Eu}$ , and  $^{133}\text{Ba}$  will be recorded. The mean ANN outputs and their variances will be reported. In addition to these, mixtures in required by the ANSI standard,

- $^{137}\text{Cs}$  + depleted uranium (DU)
- $^{99m}\text{Tc}$  + HEU
- $^{201}\text{Tl}$  + HEU
- $^{67}\text{Ga}$  + HEU
- $^{131}\text{I}$  + WGPu
- Naturally occurring radioactive material (NORM) + HEU
- NORM + WGPu

will be simulated and their mean ANN output and variance will be reported.

#### 4.1.2 Uranium Enrichment Calculations

*Good* Measuring the enrichment of uranium is important for treaty verification purposes. These measurements are performed in uranium enrichment facilities and to verify warhead disarmament. Due to treaty conditions limiting the amount of sensitive information released to inspectors, information barriers are required. Information barriers can include removing regions in gamma-ray spectra or giving no information about shielding between the source and detector.

ANNs are a good candidate as an information barrier for three reasons. First, their output can be constrained, only outputting the enrichment given a gamma-ray spectrum. Restricting the output ensures potentially sensitive details of the sample are not known. Second, ANNs can be trained to use spectra with unknown background radiation and calibration drift. Because the inspector will have a time constraint, it is assumed a separate background

I thought a background spectrum wouldn't be available? Confusing sentence.

spectrum will not be taken. A background spectrum can be subtracted from a background and source spectrum, making analysis easier. ANNs can be taught to operate in areas with different background radiation. The other unknown, possible calibration drift, is typically corrected manually. Because the inspector will not have access to the spectrum, manual calibration adjustments cannot be performed. It has been shown that ANNs can be taught to identify isotopes in detectors with different calibration. A few technical hurdles need to be addressed when constructing an ANN to perform uranium enrichment. These hurdles and methods to address them are described below.

Because uranium emits relatively low energy gamma-rays, it's spectrum is especially susceptible to corruption by shielding. To address this, a shielding library will be included in the dataset simulation. This will be constructed using the same method described in section 4.1.1 using the material thicknesses shown in Table 4.1.

Treaty verification inspectors typically have under an hour to collect data for an enrichment measurement. For this reason source measurement times will range from 5 mins to 1 hr. Collection times shorter than 5 mins may produce ANNs with high variance outputs. To demonstrate the ANNs performance versus collection time, a graph of the measurement time versus ANN accuracy on a simulated verification dataset will be included. It is expected that collecting times less than 10 mins will result in an ANN accuracy too low to be of practical use. For reference, Analytically chemical techniques can measure uranium enrichment to 0.1–0.2% accuracy [?]. Comparing the areas of photopeaks in HPGe spectra, an accuracy of about 1% is possible [?]. Also due to the time constraint, it is assumed that background data cannot be collected. To address this, each training sample will include a random combination of background isotopes. The background count rate will range from 10–120 cps. ← typical?

Because trained inspectors are performing these measurements, large calibration drifts are not included in the training data. Small calibration drifts of less than 5% will be included to account for temperature changes and electronic drift.

The isotope library necessary for uranium enrichment consists of only six isotopes:  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{234}\text{U}$ ,  $^{234}\text{Th}$ ,  $^{231}\text{Th}$ , and  $^{234m}\text{Pa}$ . These are the main gamma-ray producing isotopes in a sample of uranium. The training set will be simulated using combinations of all of

these isotopes in pseudo-random combinations. Random sampling does not guarantee the training space is evenly sampled and often produces clusters. The presence of clusters in the training set may lead the ANN to learn a bias for certain combinations of isotopes. A way to reduce the chances of clusters and more uniformly sample the input space is using Latin hypercube sampling (LHS). LHS partitions each dimension of a space into  $N$  equal parts. The space is then sampled using  $N$  points, ensuring that there is only one point along each partition in each dimension. An example of this sampling method for a two-dimension space is shown in Figure 4.2.

X				
				X
		X		
	X			
			X	

Figure 4.2: An example of LHS sampling. Seen here is a square sampled using five points.

*using the metric mentioned before?*

To quantify how much LHS helps identification, datasets will be constructed using random sampling and LHS. The number of samples in each dataset will be 1k, 5k, 10k, 50k, 100k. ANNs will be trained using these datasets and their performance on a simulated validation dataset will then be measured and compared. It is expected that at a certain number of samples the ANN performance will reach an asymptote. It is also expected that the LHS datasets will reach a higher-accuracy asymptote quicker than the randomly sampled datasets.

To test the ability for ANNs to measure uranium enrichment, depleted, low-enriched, medium-enriched, and high-enriched uranium spectra will be simulated. for each enrichment level, 100 spectra will be simulated using collection times of 5, 10, 60, 300, 600, 1800, and 3600 s. Each of these spectra will contain an unknown background and calibration similar to the training set. Separate validation sets will be constructed for a small amount of shielding (0.1 cm of lead) and a large amount of shielding (1 cm of lead).



### 4.1.3 Additional Simulated Detector Models

Simulating additional NaI detectors using GADRAS may help the ANN generalize to different detectors. To begin this process, two 2-inch by 2-inch NaI detectors will be modeled using GADRAS and their properties will be changed. These changes will include changing the calibration and changing the shape of the photopeaks. The calibration changes will be based on laboratory NaI detectors. The shape of photopeaks will be changed based on laboratory NaI detectors' full-width-at-half-max (FWHM). Ten different models will be included.

Initial hyperparameter searches will be based on datasets simulated using a single detector. After an optimal ANN structure is found using the hyperparameter search, two new training datasets will be constructed with additional detector models. The two datasets will be constructed from five models and ten models. Two ANNs will be trained using both datasets. The performance of the ANNs on a dataset constructed using five new detector models will be reported. It is expected that the ANN trained using more detector models will have a higher accuracy on the new testing dataset.

## 4.2 Autoencoders

*Should define this as it is jargon-y to nuclear engineers -*

An autoencoder is an unsupervised ANN whose goal is to learn a representation of the input. This is accomplished by simultaneously training an encoding ANN and a decoding ANN. An example of this can be seen in Figure 4.3. As seen in this figure, the encoding ANN reduces an  $n$ -dimension input signal,  $X$ , to a  $m$ -dimension signal,  $z$ , where  $m < n$ . The decoding ANN takes the encoded signal,  $z$ , and outputs a reproduction of the input signal,  $X'$ .

Without an autoencoder, a single ANN has to learn multiple tasks to identify isotopes. An ANN would have to simultaneously identify the detector calibration, background signal, and possible source signal. By training an autoencoder to reconstruct a background-subtracted and correctly calibrated spectrum, the task of isotope identification is simplified for the ANN. This may result in more accurate identifications. To test this, for each dataset a single autoencoder and three ANNs will be trained. The first will be trained without an

autoencoder. The second will be trained using the encoder as input. The third will be trained using the full autoencoder as input. A random hyperparameter search will be used to find an appropriately structured autoencoder. The testing and validation error for these ANNs will be compared for each respective dataset.

In addition to using fully connected autoencoders, a 1-D convolutional autoencoder will also be explored. Fully connected ANNs do not assume the input has local spatial structure, while convolution ANNs do. Because gamma-ray spectra have local spatial structure in the form of photopeaks and Compton continua, it may be better to use a convolutional ANN over a fully connected ANN. To test this, the experiment described above will be repeated using a 1-D convolutional autoencoder.

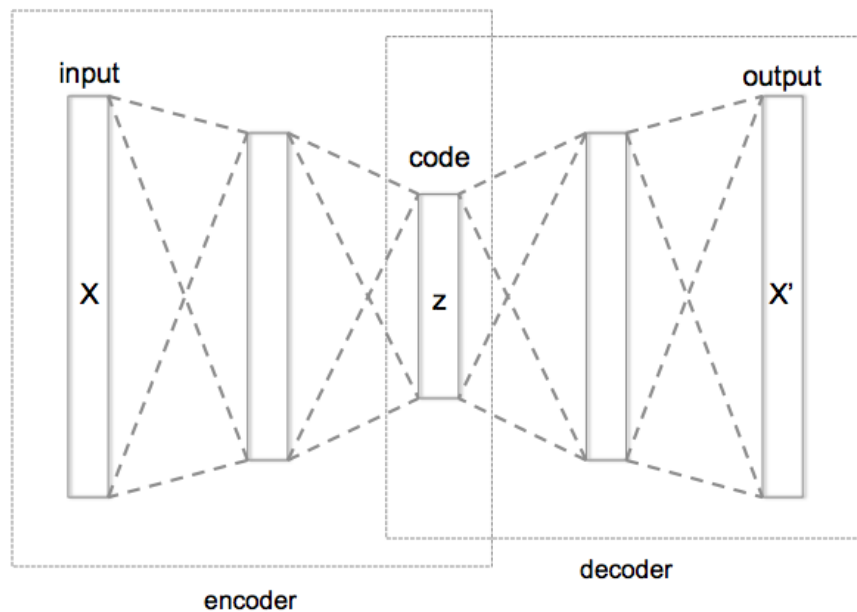


Figure 4.3: An example of an autoencoder [?].

### 4.3 K-folds Cross Validation

K-folds cross validation will be included in the hyperparameter search for each dataset. Cross validation is the general method of determining how well a model will generalize to

novel data. K-folds cross validation does this by splitting the available data into  $k$  subsets. From these,  $k-1$  subsets are used to train the ANN and the remaining subset is used as the validation dataset. Typical values for  $k$  are either 5 or 10. This process is repeated, using each subset once as the validation dataset. This process is illustrated in Figure 4.4 for 5-folds cross validation.

For each different hyperparameter combination, a new set of cross validation ANNs will be trained. The average of the final validation dataset errors will be used to pick the optimal ANN. Performing cross validation will more accurately demonstrate how well a given set of hyperparameters will generalize to new data. For each dataset the error and hyperparameter structure will be compared for ANNs trained with no cross validation, 5-folds cross validation, and 10-folds cross validation.

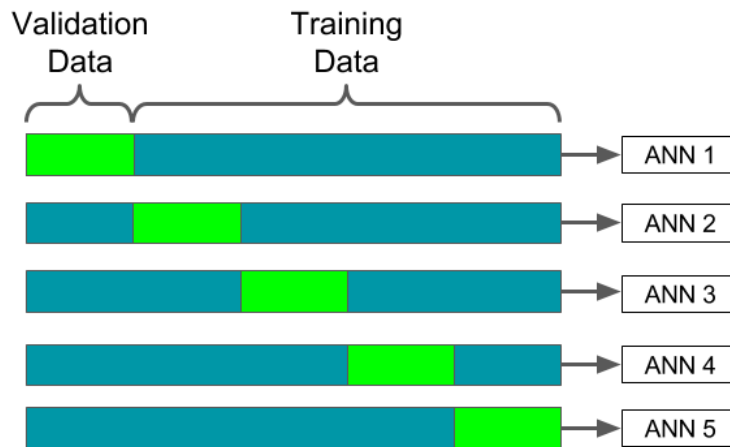


Figure 4.4: An example of 5-folds cross validation. In each fold, the same dataset is partitioned into training data, in blue, and validation data, in green. Each training dataset is used to train a separate ANN. Each ANNs respective validation dataset is used to stop the ANNs training.

## 4.4 Bagging

Each time the ANN trains, it produces slightly different identification results and performance. Bagging, or the process of averaging the outputs of many ANNs, can reduce the variance in the output [?]. In addition to this, bagging more accurately displays the true performance of a given ANN structure.

maybe  
a diagram  
or  
math?  
Needs  
to be  
something  
more than  
words.

Is there no mention  
of this figure?  
All figures should  
be called out in  
the text.

Analyzing the performance of bagging begins once the ANN structure is found from the random hyperparameter search. Using this structure, ten models will be trained. Each model will use the entire training dataset, ending training at the average iteration used for the cross validation step. The accuracy and variance in the output as more models are averaged will be reported. The accuracy and variance are expected to plateau with enough models being averaged. If the accuracy or variance do not plateau after ten models, additional will be created until the effect is observed.

Need to wrap up this chapter ...

The proposed datasets and ANN methods will directly serve key needs in verification technology ...

# CHAPTER 5

## CONCLUSION

Good conclusion  
with flesh out  
(with reference to  
more than just Ch4)  
or combine with

Because of their flexibility and their ability to train using simulated data, ANNs are well suited to solving different problems in gamma-ray spectroscopy. Because ANNs incorporate fuzzy logic, they mimic the intuition a trained spectroscopist uses when identifying spectra. This is in contrast to other identification algorithms that use rigid rules which may struggle to identify spectra that are poorly calibrated, have insufficient counts to form obvious features, or are in an unknown background.

To better understand what scenarios the ANN can operate in, two datasets will be investigated. The goal of the first dataset is to perform source interdiction using the ANSI N42-34-2006 library. The second dataset corresponds to performing uranium enrichment calculations for treaty verification purposes.

In addition to these datasets, a number of ANN experiments are suggested to improve on past work. The first improvement is adding additional detector models to the training set. The additional models should increase the generalization performance of the ANN. The second improvement will focus on how autoencoders can improve performance by keeping the calibration correction and background subtraction step separate from an ANN used for identification. This will include investigating the use of a 1-D convolution ANN as an autoencoder. To more accurately display the performance of a given ANN structure, k-folds cross validation will be added to the hyperparameter search for each dataset. After training, bagging will be added to the model. Bagging lowers the variance on the outputs of a given ANN structure and more accurately displays its performance.

# CHAPTER 6

## REFERENCES

- [1] *American National Standard Performance Criteria for Hand-Held Instruments for the Detection and Identification of Radionuclides, ANSI N42.34-2006*, IEEE Std., Rev. ANSI N42.34-2006, 2007.
- [2] M. Rawool-Sullivan, J. Bounds, S. Brumby, L. Prasad, and J. Sullivan, “Steps toward automated gamma ray spectroscopy steps toward automated gamma ray spectroscopy: How a spectroscopist deciphers an unknown spectrum to reveal the radioactive source,” 02 2010.
- [3] T. Burr and M. Hamada, “Radio-isotope algorithms for NaI gamma spectra,” *Algorithms*, vol. 2, pp. 339–360, March 2009.
- [4] H. Xiong, “Automated wavelet analysis of low resolution gamma-ray spectra and peak area uncertainty,” Master’s thesis, University of Illinois at Urbana-Champaign, 2015.
- [5] J. Ely, R. Kouzes, J. Schweppe, E. Siciliano, D. Strachan, and D. Weier, “The use of energy windowing to discriminate SNM from NORM in radiation portal monitors,” *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment*, vol. 560, no. 2, pp. 373 – 387, 2006.
- [6] J. I. T., *Principal Component Analysis*. Springer New York, 2002.
- [7] T. Kanungo, D. M. Mount, N. S. Netanyahu, C. D. Piatko, R. Silverman, and A. Y. Wu, “An efficient k-means clustering algorithm: analysis and implementation,” *IEEE Transactions on Pattern Analysis and Machine Intelligence*, vol. 24, no. 7, pp. 881–892, Jul 2002.
- [8] V. V. Kumari, B. R. Raju, and A. Naik, “Hybrid clustering algorithm based on mahalnobis distance and mst,” *International Journal of Applied Information Systems*, vol. 3, no. 5, pp. 60–63, Jul 2012.
- [9] D. Boardman, M. Reinhard, and A. Flynn, “Principal component analysis of gamma-ray spectra for radiation portal monitors,” *IEEE Transactions on Nuclear Science*, vol. 59, no. 1, pp. 154–160, Feb 2012.
- [10] R. Runkle, “Analysis of spectroscopic radiation portal monitor data using principal components analysis,” *IEEE Transactions on Nuclear Science*, vol. 53, no. 3, pp. 1418–1423, 2006.

- [11] J. Mattingly and D. Mitchell, "A framework for the solution of inverse radiation transport problems," *IEEE Transactions on Nuclear Science*, vol. 57, no. 6, pp. 3734–3743, 2010.
- [12] S. Jeyanthia, N. Maheswaria, and R. Venkatesh, "Neural network based automatic fingerprint recognition system for overlapped latent images," *Journal of Intelligent Fuzzy Systems*, vol. 28, 2015.
- [13] A. Krizhevsky, I. Sutskever, and G. Hinton, "Imagenet classification with deep convolutional neural networks," *Annual Conference on Neural Information Processing Systems*, pp. 1097–1105, 2012.
- [14] A. Rababaah and S. D., "Integration of two different signal processing techniques with artificial neural network for stock market forecasting," *Academy of Information Management Sciences Journal*, vol. 18, pp. 63–80, 2015.
- [15] K. Hornik, "Approximation capabilities of multilayer feedforward networks," *Neural Networks*, vol. 4, pp. 251–257, 1991.
- [16] D. E. Rumelhart, G. E. Hinton, and R. J. Williams, "Learning representations by back-propagating errors," *Nature*, vol. 323, pp. 533–536, 1986.
- [17] J. Bergstra and Y. Bengio, "Random search for hyper-parameter optimization," *Journal of Machine Learning Research*, vol. 13, pp. 281–305, 2012.
- [18] A. Zheng, *Evaluating Machine Learning Models*. O'Reilly Media, Inc., 2015.
- [19] R. Abdel-Aal, "Comparison of algorithmic and machine learning approaches for the automatic fitting of gaussian peaks," *Neural Computing and Applications*, vol. 11, no. 1, pp. 17–29, 2002.
- [20] R. Abdel-Aal and M. Al-Haddad, "Determination of radioisotopes in gamma-ray spectroscopy using abductive machine learning," *Nuclear Instruments and Methods in Physics Research A*, vol. 391, pp. 275–288, 1996.
- [21] M. Medhat, "Artificial intelligence methods applied for quantitative analysis of natural radioactive sources," *Annals of Nuclear Energy*, vol. 45, pp. 73 – 79, 2012.
- [22] V. Vigneron, J. Morel, M. Lepy, and J. Martinez, "Statistical modelling of neural networks in  $\gamma$ -spectrometry," *Nuclear Instruments and Methods in Physics Research A*, vol. 396, p. 642647, 1996.
- [23] V. Pilato, F. Tola, J. Martinex, and M. Huver, "Application of neural networks to quantitative spectrometry analysis," *Nuclear Instruments and Methods in Physics Research A*, vol. 422, pp. 423–427, 1999.
- [24] L. Chen and Y.-X. Wei, "Nuclide identification algorithm based on KL transform and neural networks," *Nuclear Instruments and Methods in Physics Research A*, vol. 598, pp. 450–453, 2009.

- [25] E. Yoshida, K. Shizuma, S. Endo, and T. Oka, “Application of neural networks for the analysis of gamma-ray spectra measured with a Ge spectrometer,” *Nuclear Instruments and Methods in Physics Research A*, vol. 484, pp. 557–563, 2002.
- [26] P. Olmos, J. C. Diaz, J. M. Perez, P. Gomez, V. Rodellar, P. Aguayo, A. Bru, G. Garcia-Belmonte, and J. L. Pablos, “A new approach to automatic radiation spectrum analysis,” *IEEE Transactions on Nuclear Science*, vol. 38, pp. 971–975, August 1991.
- [27] I. Goodfellow, Y. Bengio, and A. Courville, *Deep Learning*. MIT Press, 2016, <http://www.deeplearningbook.org>.
- [28] M. Kamuda, “Automated isotope identification algorithm using artificial neural networks,” Master’s thesis, University of Illinois at Urbana-Champaign, 2017.
- [29] M. Kamuda, J. Stinnett, and C. J. Sullivan, “Automated isotope identification algorithm using artificial neural networks,” *IEEE Transactions on Nuclear Science*, vol. 64, pp. 1858 – 1864, 2017.
- [30] D. J. Mitchell and L. T. Harding, “GADRAS isotope ID user’s manual for analysis of gamma-ray measurements and api for linux and android,” *SAND2014-3933*, May 2014.
- [31] L. Devroye, *Non-Uniform Random Variate Generation*. Springer-Verlag New York Inc., 1986.
- [32] D. Kingma and J. Ba, “Adam: A method for stochastic optimization,” *International Conference for Learning Representations*, 2015.
- [33] N. Srivastava, G. Hinton, A. Krizhevsky, I. Sutskever, and R. Salakhutdinov, “Dropout: A simple way to prevent neural networks from overfitting,” *Journal of Machine Learning Research*, vol. 15, pp. 1929–1958, 2014.
- [34] G. Nelson and D. Reilly, *Passive Nondestructive Assay of Nuclear Materials*. Los Alamos National Lab, 1991, ch. The Measurment of Uranium Enrichment.
- [35] W. contributor Chervinskii, “Autoencoder structure,” 2015. [Online]. Available: [https://commons.wikimedia.org/wiki/File:Autoencoder\\_structure.png](https://commons.wikimedia.org/wiki/File:Autoencoder_structure.png)
- [36] L. Breiman, “Bagging predictors,” *Machine Learning*, vol. 24, no. 2, pp. 123–140, Aug 1996. [Online]. Available: <https://doi.org/10.1007/BF00058655>