Automatic Orthogonal Moments for Production Functions Estimation

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Introduction

- Models defined by conditional moment restrictions (CMRs) are ubiquitous in economics.
 - Regressions, quantile models, missing data, simultaneous equations, rational expectations, and production functions, among many others (Chen and Qiu, 2016).
 - Despite their popularity, there does not exists a general and automatic approach that can be used to construct Locally Robust (LR)/Orthogonal/Debiased Moments (Chernozhukov et al., 2022; Neyman, 1959) for CMRs.

This paper

- We introduce an automatic method to construct debiased moments in general semiparametric models defined by several CMRs, with possibly different conditioning variables and endogenous regressors.
- We specialize our results in a fundamental model in economics: production functions at the firm level.

Why production functions?

- Production functions have been at the core of economics since the early 1800's (Chambers, 1988).
- Learning production functions (and productivity measures) is essential to answer several relevant questions for designing policies.
 - Trade liberalization, exporting, foreign ownership, competition, investment climate, learning by doing, to name a few (Ackerberg et al., 2007, 2015, ACF hereafter).

The general model

- $W_i = (Y_i, Z_i), i = 1, \dots, n, \text{ is iid.}$
- Y is a random vector of endogenous variables taking values in $\mathcal{Y}\subseteq\mathbb{R}^{d_Y}$, and Z is random vector of exogenous variables taking values in $\mathcal{Z}\subseteq\mathbb{R}^{d_Z}$.
- Let $\theta \in \Theta \subset \mathbb{R}^{d_{\theta}}$ denote a finite-dimensional parameter vector.
- Let $\eta \in \mathbf{B}$ be a d_{η} -vector of real-valued measurable functions of W.

■ There is a vector of residual functions $m_i: \mathcal{Y} \times \Theta \times \boldsymbol{B} \mapsto \mathbb{R}$ of Y, θ , and η , such that:

$$\mathbb{E}\left[\left.m_{j}\left(Y,\theta_{0},\eta_{0}\right)\right|Z^{\left(j\right)}\right]=0,\quad\mu_{j}-a.s.,\quad j=1,2,\cdots,J,\quad \ \left(1\right)$$

- where $\mathbb{E}[\cdot]$ is expectation under the distribution of Y given $Z^{(j)}$,
- $\blacksquare \mu_i$ is probability measure of $Z^{(j)}$,
- lacksquare Z denotes the union of different random elements of $(Z^{(1)},\cdots,Z^{(J)})$
- \blacksquare m_i is known up to the parameters (θ_0, η_0) .

Specifically, when we write (1), we actually mean

 $\mathbb{E}\left[\left.m_{j}\left(Y,\eta_{0j}\right)\right|Z^{\left(j\right)}\right]=0,\quad\mu_{j}-a.s.,\quad j=1,2,\cdots,J_{\eta},$

$$\mathbb{E}\left[m_{j}(Y,\theta_{0},\eta_{0})|Z^{(j)}\right] = 0, \quad \mu_{j}-a.s., \quad j = J_{\eta}+1, J_{\eta}+2, \cdots, J, \quad (3)$$
where $m_{j} = (m_{j}, \dots, m_{j})$

where $\eta_0 = (\eta_{01}, \dots, \eta_{0J_n})$.

■ Hereafter, we assume that there exists a unique $(\theta_0, \eta_0) \in \Theta \times B$ such that (2) and (3) hold.

Learning Production Functions

- We observe a panel of n firms across T periods, where i and t index firms and periods, respectively. Note $W_i \equiv (W_{i1}, \dots, W_{iT})$.
- Variables in the model:
 - Y_{1it}: "value-added" output;
 - X_{it}: inputs;
 - $lacktriangleq M_{it}$: intermediate inputs.
- Output is determined by

$$Y_{1it} = p(X_{it}, \theta_{01}) + \omega_{it} + \epsilon_{it}, \tag{4}$$

where p is known up to θ_{01} , ω_{it} is firm i's productivity shock (anticipated productivity) in period t, which is allowed to be correlated with inputs X_{it} , and ϵ_{it} is noise in output.

- Estimating production functions presents econometric challenges.
- Potential endogeneity between inputs and productivity (Marschak and Andrews, 1944).
- Several approaches have been proposed to solve this issue.
- Perhaps the most popular one in applied work is the proxy variable approach (Olley and Pakes, 1996; Levinsohn and Petrin, 2003; Ackerberg et al., 2015; Wooldridge, 2009).
- Ackerberg et al. (2015) (ACF, hereafter) have highlighted identification issues in LP's model, which also carries over OP's setting.

The Proxy Variable Approach

■ The assumptions of the model implies

$$\mathbb{E}\left[\omega_t|\Omega_{t-1}\right] = h(\omega_{t-1},\theta_{02}),$$

- where h is known up to θ_{02} .
- The "trick" relies on

$$\omega_{it} = \mathcal{M}^{-1}(X_{it}, M_{it}). \tag{5}$$

(SS)

Then, we naturally obtain

$$\mathbb{E}\left[\left.Y_{1t} - \eta_0\left(X_t, M_t\right)\right| \Omega_t\right] = 0, \ \ a.s.,$$
 (FS)

$$\mathbb{E}[Y_{1t} - p(X_t, \theta_{01}) - h(\eta_0(X_{t-1}, M_{t-1}) - p(X_{t-1}, \theta_{01}), \theta_{02}) | \Omega_{t-1}]$$
= 0, a.s.,

• where Ω_t is the firm's information set at t.

Debiased moments for CMRs

- Recall that $\eta_0 \in \mathbf{B}$. Let \mathbf{B} be some Hilbert space with norm $||\cdot||_{\mathbf{B}}$ of measurable d_{η} -functions of W and inner product $\langle \cdot, \cdot \rangle_{\mathbf{B}}$.
- We assume that

$$g_{j}\left(Z^{(j)},\theta_{0},\eta\right)=\mathbb{E}\left[m_{j}\left(Y,\theta_{0},\eta\right)|Z^{(j)}\right]$$
 (6)

- is "smooth" (at η_0).
- We assume that $g_j\left(Z^{(j)},\theta_0,\cdot\right): \mathbf{B} \mapsto L^2\left(Z^{(j)}\right)$ is Fréchet differentiable, where the derivative is given by

$$\left[\nabla g_{j}\left(Z^{(j)},\theta_{0},\eta_{0}\right)\right](b) \equiv \frac{d}{d\tau}g_{j}\left(Z^{(j)},\theta_{0},\eta_{0}+\tau b\right)
= \left[S_{\theta_{0},\eta_{0}}^{(j)}b\right]\left(Z^{(j)}\right),$$
(7)

• for some $b \in \mathbf{B}$, where $\frac{d}{d\tau}$ denotes derivative from the right.

lacksquare We introduce the operator $S_{ heta_0,\eta_0}$ that is defined as follows

$$S_{ heta_0,\eta_0}b:=\left(S_{ heta_0,\eta_0}^{(1)}b,\cdots,S_{ heta_0,\eta_0}^{(J)}b
ight).$$

Under suitable assumptions, results in Argañaraz and Escanciano
 (2023) imply that in our setting, LR moments are of the form

$$\psi\left(W,\theta_{0},\eta_{0},\kappa_{0}\right)=\sum_{j=1}^{J}m_{j}\left(Y,\theta_{0},\eta_{0}\right)\kappa_{0j}\left(Z^{\left(j\right)}\right),$$

(8)

• where $\kappa_0=(\kappa_{01},\cdots,\kappa_{0J})\in\overline{\mathcal{R}}(S_{\theta_0,\eta_0})^\perp$. We denote them as Orthogonal Instruments (O-IVs). Note

$$\overline{\mathcal{R}}\left(S_{ heta_0,\eta_0}
ight)^{\perp} = \left\{f_1 \in igotimes_{j=1}^J L^2\left(Z^{(j)}
ight) : \mathbb{E}\left[f_1'f_2
ight] = 0, f_2 \in \overline{\mathcal{R}}\left(S_{ heta_0,\eta_0}
ight)
ight\}.$$

■ How can we get those O-IVs?

Debiased moments for production functions

- Let us assume that $(X_t, M_t) \subset \Omega_t$. Let $C_t = (X_t, M_t, X_{t-1}, M_{t-1})$.
- A simple derivation indicates that $S_{\theta_0,\eta_0}: \mathbf{B} \mapsto L^2(C_t) \times L^2(C_t)$ is as follows

$$S_{\theta_{0},\eta_{0}}b = (-b(C_{t}), -h_{\omega}(\eta_{0}(X_{t-1}, M_{t-1}) - p(X_{t-1}, \theta_{01}), \theta_{02})b(C_{t})),$$
(9)

• where h_{ω} is the derivative of h with respect to ω_{t-1} .

Proposition

A LR moment for the model of production function estimation, introduced by Olley and Pakes (1996), is given by

$$\psi(W, \theta_0, \eta_0, \kappa_0) = (Y_{1t} - \eta_0(X_t, M_t)) \kappa_{01}(C_t) + (Y_{1t} - p(X_t, \theta_{01}) - (10)$$

$$\psi(W, \theta_0, \eta_0, \kappa_0) = (Y_{1t} - \eta_0(X_t, M_t)) \kappa_{01}(C_t) + (Y_{1t} - \rho(X_t, \theta_{01}) - (10)$$

where $\kappa_0 = (\kappa_{01}(C_t), \kappa_{02}(C_t)) \in \overline{\mathcal{R}}(S_{\theta_0, \eta_0})^{\perp}$.

Estimation of the O-IVs

■ Suppose that there exists a function ν_j such that the Fréchet derivative of $\mathbb{E}\left[\psi\left(W,\theta_0,\eta,\kappa_0\right)\right]$ in the direction b is

$$\frac{d}{d\tau}\mathbb{E}\left[\psi\left(W,\theta_{0},\eta_{0}+\tau b,\kappa_{0}\right)\right] = \frac{d}{d\tau}\mathbb{E}\left[\sum_{j=1}^{J}m_{j}\left(Y,\theta_{0},\eta_{0}+\tau b\right)\kappa_{0j}\left(Z^{(j)}\right)\right]$$

$$=\sum_{j=1}^{J}\mathbb{E}\left[\nu_{j}\left(Y,\theta_{0},\eta_{0},b\right)\kappa_{0j}\left(Z^{(j)}\right)\right]$$

$$=0,$$

(11)

- for any $b \in \mathbf{B}$.
- Typically, ν_j will be obtained by direct calculation.

- Let us assume that for all $1 \le j \le J$, the estimator $\hat{\kappa}_j$ is of the form $\hat{\kappa}_j\left(Z^{(j)}\right) = \gamma_j\left(Z^{(j)}\right)'\hat{\beta}_j$, where $\gamma_j\left(Z^{(j)}\right)$ is a r_j -dimensional vector of basis functions.
- Let D(W) be a $d_{\eta} \times q_1$ matrix of basis functions for deviations b.
- Let $d_s \equiv d_s(W)$ be the s-column of D(W). Note that d_s belongs to B.
- We can construct a sample analog of the derivative in (11) by replacing b for d_s and κ_{0j} for $\gamma\left(Z^{(j)}\right)'\beta_j$, leading to

$$\hat{\psi}_{\eta\ell}\left(d_{s},\beta_{\ell}\right) = \frac{1}{n-n_{\ell}} \sum_{\ell' \neq \ell} \sum_{i \in I_{J'}} \sum_{j=1}^{J} \nu_{j}\left(Y,\tilde{\theta},\hat{\eta}_{\ell\ell'},d_{s}\right) \gamma_{j}\left(Z_{i}^{(j)}\right)' \beta_{j\ell},$$

$$s=1,\cdots,q_1.$$

- ► PGMM
- ► Coordinate Descent Algorithm
- ► Estimator of parameter

Monte Carlo

- To produce output, firms employ three inputs, namely, L_1 , L_2 , and K, with a Cobb-Douglas technology.
- The parameters θ_{0l_1} , θ_{0l_2} , and θ_{0k} are the corresponding input elasticities.
- The level of capital is generated by the perpetual inventory method.
- Productivity ω_t follows an AR(1) process with persistence parameter given by θ_{02} .
- There exists an intermediate input that is assumed to follow:

$$M_{it} = \exp\left\{-0.5u_{it}u'_{it} + \omega_{it}\right\},\,$$

- where $u_{it} = (L'_{it}, K_{it})'$.
- We consider the data from the steady state distribution implied by the model.

Table 1: Monte Carlo Results

True Parameters: $\theta_{0k}=0.4,\theta_{0l_1}=0.3,\theta_{0l_2}=0.3,\theta_{02}=0.7$													
	n = 100												
Est.	Coef.	Bias	Std. Err.	Coef.	Bias	Std. Err.							
	(CMRs-D-ML)	(CMRs-D-ML)	(CMRs-D-ML)	(ACF)	(ACF)	(ACF)							
$\hat{ heta}_{m{k}}$	0.428	0.028	0.018	0.281	-0.119	1.109							
$\hat{ heta}_{l_1}$	0.311	0.011	0.024	0.335	0.035	0.539							
$\hat{ heta}_{l_2}$	0.310	0.010	0.024	0.322	0.022	0.516							
$\hat{ heta}_2$	0.666	-0.034	0.053	0.905	0.205	0.101							
	n = 500												
Est.	Coef.	Coef. Bias		Coef.	Bias	Std. Err.							
	$({\rm CMRs\text{-}D\text{-}ML}) ({\rm CMRs\text{-}D\text{-}ML})$		(CMRs-D-ML)	(ACF)	(ACF)	(ACF)							
$\hat{\theta}_k$	0.424	0.024	0.012	0.360	-0.040	0.542							
$\hat{\theta}_{l_1}$	0.310	0.010	0.013	0.289	-0.011	0.277							
$\hat{ heta}_{l_2}$	0.306	0.006	0.016	0.316	0.016	0.284							
$\hat{ heta}_2$	0.676	-0.024	0.025	0.863	0.163	0.097							
		n = 1,000											
Est.	Coef.	Bias	Std. Err.	Coef.	Bias	Std. Err.							
	(CMRs-D-ML)	(CMRs-D-ML)	(CMRs-D-ML)	(ACF)	(ACF)	(ACF)							
$\hat{ heta}_{m{k}}$	0.422	0.022	0.011	0.348	-0.052	0.385							
$\hat{ heta}_{l_1}$	0.309	0.009	0.013	0.303	0.003	0.178							
$\hat{ heta}_{l_2}$	0.305	0.005	0.014	0.303	0.003	0.164							
$\hat{ heta}_2$	0.680	-0.020	0.019	0.833	0.133	0.097							

Final Rermarks

- We have introduced an automatic construction of debiased moments for general models defined by several conditioning moment restrictions, with possible different conditioning variables and endogenous regressors.
- We have leveraged the generality of our theory to derive orthogonal moments in the context of production functions estimation at the firm level, following the approach of ACF.



PGMM

- Implement the penalized GMM (PGMM) framework, following Caner and Kock (2019) and Bakhitov (2022).
- Let us define, with some abuse of notation, the $q_1 imes r$ matrix \hat{G}_ℓ as follows:

$$\hat{G}_{\ell} := \begin{bmatrix} \frac{1}{n-n_{\ell}} \sum_{i} \nu_{1} \left(Y_{i}, \tilde{\theta}, \hat{\eta}_{\ell\ell'}, d_{1} \right) \gamma_{1}' & \cdots & \frac{1}{n-n_{\ell}} \sum_{i} \nu_{J} \left(Y_{i}, \tilde{\theta}, \hat{\eta}_{\ell\ell'}, d_{1} \right) \gamma_{J}' \\ & \cdots \\ \frac{1}{n-n_{\ell}} \sum_{i} \nu_{1} \left(Y_{i}, \tilde{\theta}, \hat{\eta}_{\ell\ell'}, d_{q_{1}} \right) \gamma_{1}' & \cdots & \frac{1}{n-n_{\ell}} \sum_{i} \nu_{J} \left(Y_{i}, \tilde{\theta}, \hat{\eta}_{\ell\ell'}, d_{q_{1}} \right) \gamma_{J}' \end{bmatrix}$$

■ The PGMM program is

$$\min_{\beta \in \mathbb{R}^r} \left(\hat{G}_{\ell} \beta \right)' \hat{\Lambda}_{q_1} \left(\hat{G}_{\ell} \beta \right) \quad \text{s.t.} \ ||\beta||_1 \le c_1 \ \text{and} \ ||\beta||_1 \ge c_2, \quad (13)$$

• where $\hat{\Lambda}_{q_1} = \hat{\Lambda}/q_1$, $\hat{\Lambda}$ is a $q_1 \times q_1$ positive semi-definite matrix, and c_1 and c_2 are positive constants.

■ The solution can be written as

$$\hat{\beta}_{\ell} := \operatorname*{arg\ min}_{\beta \in \mathbb{R}'} \ \left(\hat{G}_{\ell} \beta \right)' \hat{\Lambda}_{q_1} \left(\hat{G}_{\ell} \beta \right) + 2 \lambda_{1n} \left| \left| \beta \right| \right|_1 - 2 \lambda_{2n} \left| \left| \beta \right| \right|_1.$$

- where λ_{1n} and λ_{2n} are tuning parameters that depend on n and should satisfy $\lambda_{1n} \geq \lambda_{2n}$.
- ▶ Back

What is PGMM doing?

- Coordinate Descent Algorithm.
- The solution is

$$\hat{\beta} = \operatorname*{arg\;min}_{\beta \in \mathbb{R}^r} \frac{1}{2} \left(\left. G \beta \right)' \Lambda_{q_1} \left(\left. G \beta \right) + \lambda_n \left| \left| \beta \right| \right|_1,$$

- where we define $\lambda_n := \lambda_{1n} \lambda_{2n}$.
- The derivative of the first term of the objective function with respect to β_i is

$$\frac{\partial}{\partial \beta_j} \left[\frac{1}{2} (G\beta)' \Lambda_{q_1} (G\beta) \right] = e'_j G' \Lambda_{q_1} (G\beta - Ge_j \beta_j + Ge_j \beta_j)$$
$$= A_j + B_j \beta_j.$$

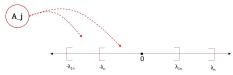
■ The subgradient of the penalty term is

$$\frac{\partial}{\partial \beta_j} \lambda_n ||\beta||_1 = \begin{cases} -\lambda_n & \text{if } \beta_j < 0 \\ [-\lambda_n, \lambda_n] & \text{if } \beta_j = 0 \\ \lambda_n & \text{if } \beta_j > 0 \end{cases}$$

■ The coordinate solution can be computed as

$$\beta_{j} = \begin{cases} \frac{\lambda_{n} - A_{j}}{B_{j}} & \text{if } \lambda_{n} < A_{j} \\ 0 & \text{if } A_{j} \in [-\lambda_{n}, \lambda_{n}] \\ \frac{-(\lambda_{n} + A_{j})}{B_{j}} & \text{if } -\lambda_{n} > A_{j} \end{cases}$$

- Our implementation does not prevent the trivial solution if tuning parameters are not properly chosen.
- There are two reasons why we still might end up with a trivial solution.
 - 1 When the rest of the coordinates tend to the trivial solution, A_j approaches zero, and β_j will be set to zero, and thus between $-\lambda_n$ and λ_n .
 - 2 If λ_{1n} is large enough. This is typical in any "Lasso" problem".
- To avoid the above from happening, the second tuning parameter, λ_{2n} , reduces λ_{1n} , making it more plausible to pick up a solution different from the trivial one.



- Thus, we are able to find a feasible solution to the original problem (13), if the tuning parameters are suitable.
- We recommend selecting them by cross-validation and studying the general shape of the objective function.
- ► Back

Estimation of the parameter of interest

- To estimate the parameter of interest θ_0 , we follow Chernozhukov et al. (2018) and use cross-fitting.
- Let l_{ℓ} , $\ell=1,\cdots,L$, be a random partition of the observation index set $\{1,\cdots,n\}$ into L distinct subsets of about the same size.
- Let $\hat{\eta}_{\ell}$ and $\hat{\kappa}_{\ell}$ be given estimators of η_0 and κ_0 , respectively, based on observations that are not in I_{ℓ} .
- The CMRs Debiased Machine Learning Estimator (CMRs-D-ML) is

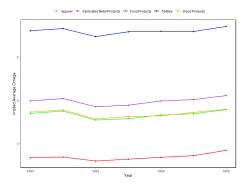
$$\hat{\theta} := \underset{\theta \in \Theta}{\operatorname{arg \, min}} \left(\frac{1}{n} \sum_{\ell=1}^{L} \sum_{i \in I_{\ell}} \psi \left(W_{i}, \theta, \hat{\eta}_{\ell}, \hat{\kappa}_{\ell} \right) \right)^{2}. \tag{14}$$

Data

- Data from Instituto Nacional de Estadistica de Chile.
- Information on all Chilean manufacturing plants with at least ten employees in the period 1979-1986.
- We focus on the five largest three-digit (ISIC codes) manufacturing industries in Chile: food products (311), textiles (321), apparel (322), wood products (331), and fabricated metal products (381).
- Plant variables are collected annually and they include revenues, investment, capital formation, different types of labor (blue and white collar), and measures of intermediate inputs (materials, services, electricity, and fuels).

Table 3: Empirical Results by 3-digit sector							
All $(n = 1,223)$							
Est.	Coef.	Std. Err.	Coef.	Std. Err.			
	(CMRs-D-ML)	(CMRs-D-ML)	(ACF)	(ACF)			
$\hat{\theta}_k$	0.800	0.018	0.488	0.000			
$\hat{\theta}\iota$	0.200	0.007	0.457	0.001			
$\hat{\theta}_2$	0.901	0.004	1.005	0.001			
Food products $(n = 689)$							
Est.	Coef.	Std. Err.	Coef.	Std. Err.			
	(CMRs-D-ML)	(CMRs-D-ML)	(ACF)	(ACF)			
$\hat{\theta}_k$	0.546	0.001	0.451	0.000			
$\hat{\theta}_t$	0.519	0.001	0.619	0.000			
$\hat{\theta}_2$	0.996	0.005	1.006	0.001			
	7	Textiles $(n = 158)$					
Est.	Coef.	Std. Err.	Coef.	Std. Err.			
	(CMRs-D-ML)	(CMRs-D-ML)	(ACF)	(ACF)			
$\hat{\theta}_k$	0.098	0.297	0.272	0.000			
$\hat{\theta}_l$	0.899	0.188	0.826	0.000			
$\hat{\theta}_2$	0.823	0.192	1.003	0.001			
		Apparel $(n = 116)$					
Est.	Coef.	Std. Err.	Coef.	Std. Err.			
	(CMRs-D-ML)	(CMRs-D-ML)	(ACF)	(ACF)			
$\hat{\theta}_k$	0.505	2.714	0.231	0.000			
$\hat{\theta}_{l}$	0.513	1.829	1.034	0.000			
$\hat{\theta}_2$	0.317	0.310	0.998	0.002			
		Products $(n = 118)$	3)				
Est.	Coef.	Std. Err.	Coef.	Std. Err.			
	(CMRs-D-ML)	(CMRs-D-ML)	(ACF)	(ACF)			
$\hat{\theta}_k$	0.400	2.616	0.080	0.000			
$\hat{\theta}_t$	0.600	1.487	1.243	0.000			
$\hat{\theta}_2$	0.116	0.031	0.996	0.002			
	Fabrica	ted Metal Produc	ets $(n = 1)$	142)			
Est.	Coef.	Std. Err.	Coef.	Std. Err.			
	(CMRs-D-ML)	(CMRs-D-ML)	(ACF)	(ACF)			
$\hat{\theta}_k$	0.401	1.569	0.274	0.000			
$\hat{\theta}_l$ $\hat{\theta}_2$	0.602 0.551	0.742 0.258	0.902 1.002	0.000			

Figure: Implied productivity





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