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import numpy as np
import pandas as pd

def f(x): return np.sin(5*x) + np.cos(2*x)

def bisec2(f,a,b):
    xi = (a + b)/2
    if f(a)*f(b) > 0: return [xi, a, b, "Root Not Bracketed"]
    elif f(xi) == 0: return [xi, a, b, "Root Found"]
    elif f(xi)*f(a) < 0: return [xi, a, xi, "Root between a and xi"]
    elif f(xi)*f(b) < 0: return [xi, xi, b, "Root between xi and b"]

def bisection(ErrorTable,ErrorNoteTable,atable,btable,xtable):
    MaxIter = 20
    eps = 0.0005
    Stopcode = "NoStopping"
    i = 0
    while i <= MaxIter and Stopcode == "NoStopping":
        ri = bisec2(f, atable[i], btable[i])
        if ri[3] == "Root Not Bracketed":
            xtable.append(ri[0])
            ErrorNoteTable.append(ri[3])
            break
        if ri[3] == "Root Found":
            xtable.append(ri[0])
            ErrorTable.append(0)
            ErrorNoteTable.append(ri[3])
            break
        atable.append(ri[1])
        btable.append(ri[2])
        xtable.append(ri[0])
        ErrorNoteTable.append(ri[3])
        if i != 0:
            ei = (xtable[i] - xtable[i - 1])/xtable[i]
            ErrorTable.append(ei)
        if abs(ErrorTable[i]) > eps:
            Stopcode = "NoStopping"
        else:
            Stopcode = "Stop"
        i+=1
    T2 = ([[i, atable[i], btable[i], xtable[i], f(atable[i]),
            f(btable[i]), f(xtable[i]), ErrorTable[i],
            ErrorNoteTable[i]] for i in range(len(xtable))])
    T2 = pd.DataFrame(T2, columns=["Iteration", "a", "b", "x_i", "f[a]", "f[b]", "f[x_i]", "er",
    "ErrorNote"])
    display(T2)

# First Root
ErrorTable = [1]
ErrorNoteTable = []
atable = [-0.6]
btable = [-0.5]
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xtable = []

print("First Root")

bisection(ErrorTable,ErrorNoteTable,atable,btable,xtable)


# Second Root

ErrorTable = [1]

ErrorNoteTable = []

atable = [-0.3]

btable = [-0.2]

xtable = []

print("Second Root")

bisection(ErrorTable,ErrorNoteTable,atable,btable,xtable)


# Third Root

ErrorTable = [1]

ErrorNoteTable = []

atable = [0.1]

btable = [0.9]

xtable = []

print("Third Root")

bisection(ErrorTable,ErrorNoteTable,atable,btable,xtable)
```