



Regular Expression - III

Complete Course on Theory of Computation

GRE $L = \{ \text{all strings of a's \& b's including } \epsilon \}$

$$(a+b)^0 = \epsilon, a, \underline{b}, aa, bbb, a^{10}b^{20}, \dots$$

$$(a+b)^1 = \epsilon, a^{10}, a^{10}b^{20}, \dots$$

$$(a+b)^2 = a^{10}b^{20}, \dots$$

$$b^2 (ab^2)^2$$

$$a^2 (ba^2)^2$$

~~$$a^0 + b^0 = \epsilon, a^{10}, a^{20}, a^{30}, a^5, b^5, b^{10}, b^{20}, ab$$~~

$$(ab^2)^2 = \epsilon, a^2, \underline{b^2}, \underline{a^2}, \underline{b^2}, \underline{a^2}, \dots$$

$$((a+b)^0)^2 = (a+b)^0$$

$$(b^2 a^2)^2, ((a+b)^2)^2$$

$$(a^2 b^2)^2$$

$$(b^2 a^2)^2$$

(13)

$$\left(\underline{ab^{\star}} + \underline{ba^{\star}} \right)^{\phi}$$

(14)

$$\left(\underline{b^{\star}a} + \underline{a^{\star}b} \right)^{\phi}$$

① 0^b
all

② $(0+)^b$
even

③ $(00)^b$
odd

④ $(00)^b (0+)^b \Rightarrow$ all

equal?

① 22 ④

16 R.E $0^*(10^*)^*$ Same as

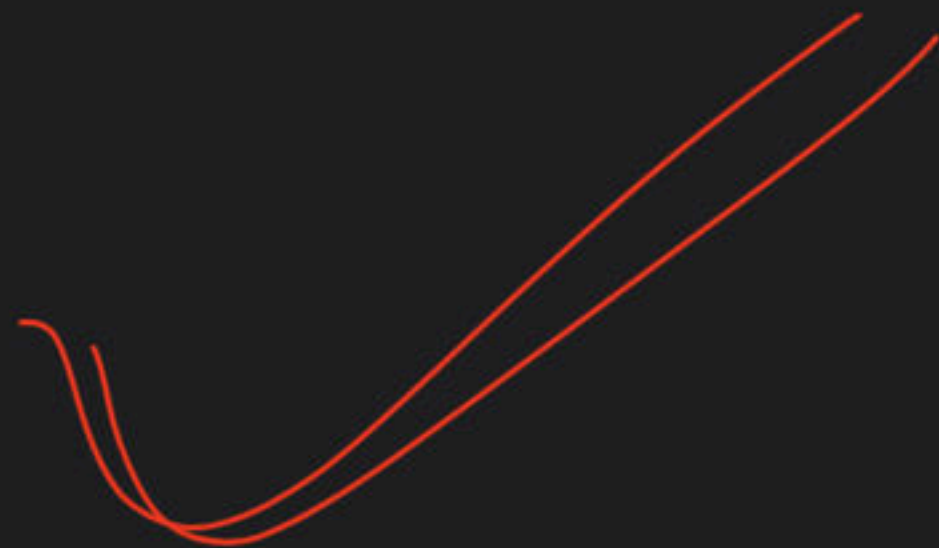
✓
(a) $(1^*0^*)^*1^*$

✓ ✓
(b) $0 + (0+10)^*$
✓

(c) $(0+1)^*10(0+1)^*$
0 ✓
1 ✓
∈ ✓

~~(d) none~~

(a)



GRE $L = \{ \text{set of all strings over its alphabet } \{0, 1, 2\} \text{ in which every 2 is immediately followed by exactly 2-0's or every 1 is immediately followed by 0 (or 20)} \}$.

$\Rightarrow \epsilon, 0, 00, 000, \dots, 0^k, 200, \cancel{2000}, 10, 100$

~~120~~, 1200, \dots , 10000000

$$0^k (200 + 100^k + 1200)^k$$

40D
 40R

NFA construction

NFA construction much easier than DFA construction. But NFA will cover only strings present in L but DFA will cover every string present in Σ^*

DFA: $\delta: \underline{Q} \times \underline{\Sigma} \rightarrow \underline{Q}$ $\begin{bmatrix} \checkmark & \checkmark \\ \text{I} & \checkmark \end{bmatrix}$

~~ϵ -free-NFA~~

NFA: $\delta: \underline{Q} \times \underline{\Sigma} \rightarrow P(Q) \text{ (or) } 2^Q$ $\begin{bmatrix} \checkmark & \checkmark \end{bmatrix}$

$$Q = \{1, 2\}$$

$$\delta(Q) = \begin{bmatrix} \{1\} \\ \{1, 2\} \end{bmatrix}$$

$$\{1\}$$

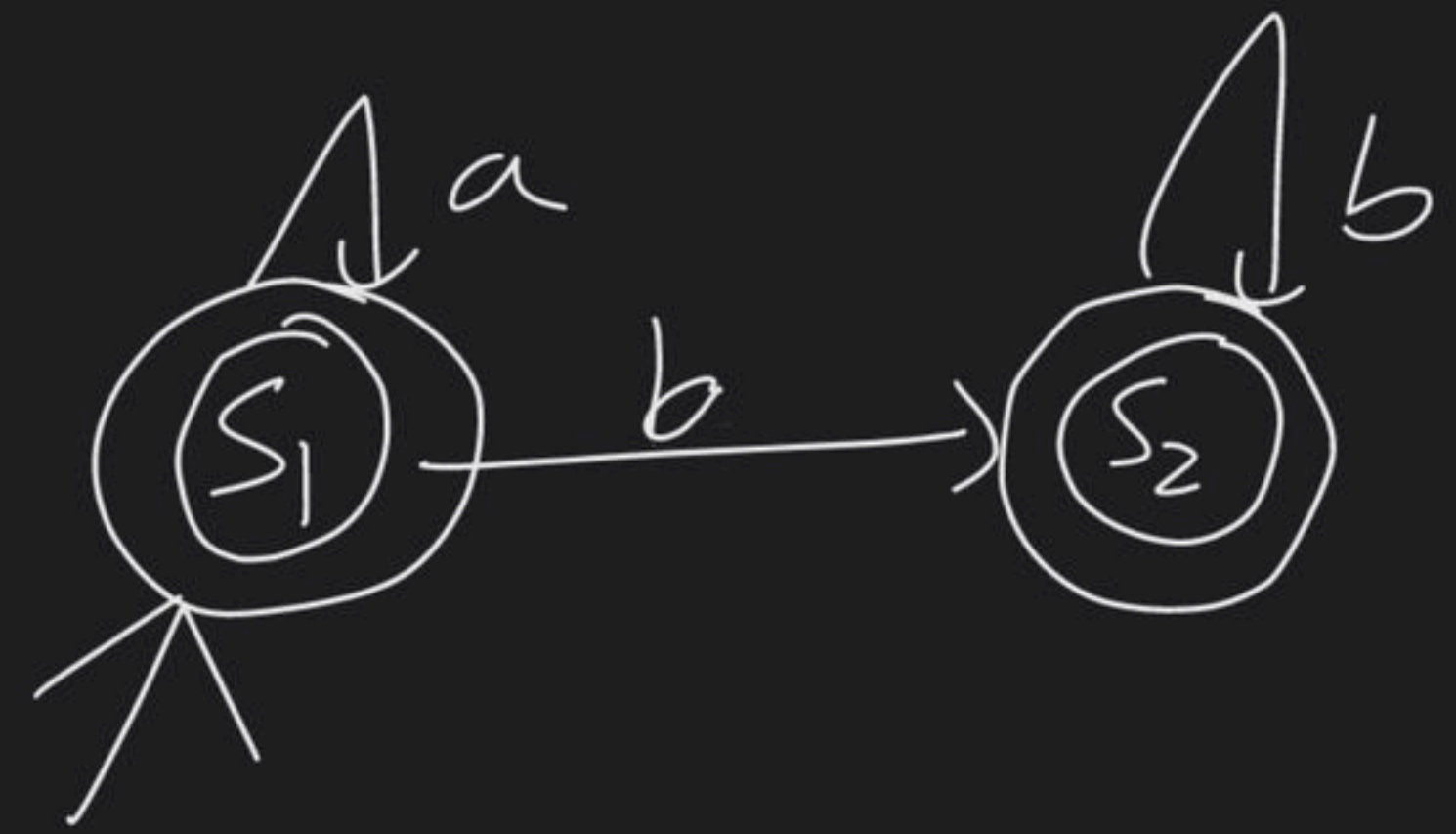
$$\{2\}$$

$$\{1, 2\}$$

$\epsilon\text{-NFA} : \delta : Q \times \{\Sigma, \epsilon\} \rightarrow P(Q) \text{ (or) } 2^Q$

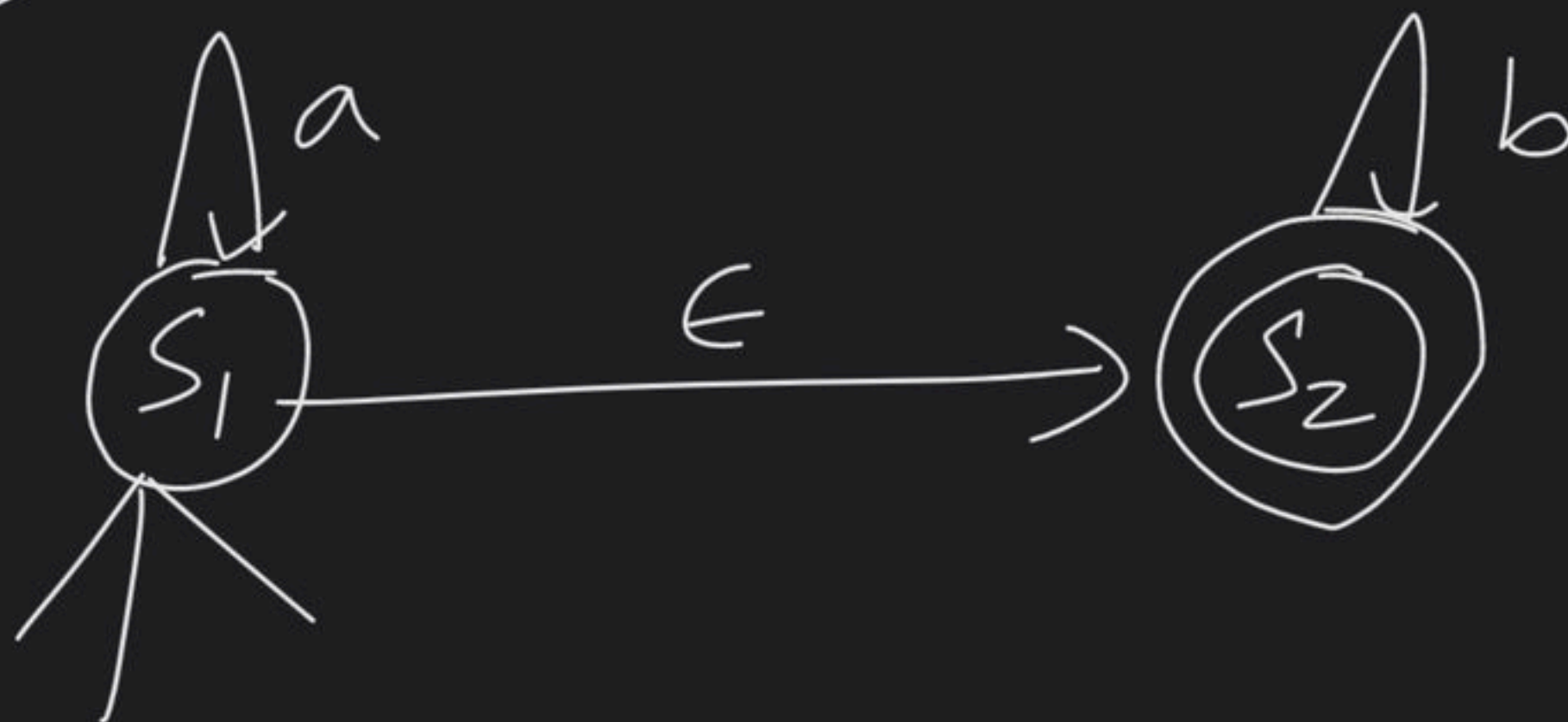
NFA $L = \{ a^m b^n \mid m, n \geq 0 \}$

$\Rightarrow \epsilon, a, aa, aaa, \dots, b, bb, bbb, \dots, ab, aabbb, \dots$



E.V ✓
I.I.V ✓
also ✓

E-NEA



Thanks All

Dedicate Hdp