



# Practice Session on Calculus - Part I

Revision Course on Engineering Mathematics - GATE, CS & IT

# Linear Algebra DPP

Use the code : BVREDDY, to get the maximum discount

1. The matrix  $A = \begin{bmatrix} a & 0 & 3 & 7 \\ 2 & 5 & 1 & 3 \\ 0 & 0 & 2 & 4 \\ 0 & 0 & 0 & b \end{bmatrix}$  has  $\det(A) = 100$  and  $\text{trace}(A) = 14$ . The value of  $|a - b|$  is \_\_\_\_\_.

**(GATE-16-EC)**

Use the code : BVREDDY, to get the maximum discount

2. The value of x for which the matrix

$$A = \begin{bmatrix} 3 & 2 & 4 \\ 9 & 7 & 13 \\ -6 & -4 & -9 + x \end{bmatrix}$$

has zero as an eigen value is \_\_\_\_\_.

(GATE-16-EC)

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3. Consider a  $2 \times 2$  square matrix

$$A = \begin{bmatrix} \sigma & x \\ \omega & \sigma \end{bmatrix}$$

Where  $x$  is unknown. If the eigen values of the matrix  $A$  are  $(\sigma + j\omega)$  and  $(\sigma - j\omega)$ , then  $x$  is equal to

- (a)  $+j\omega$
- (b)  $-j\omega$
- (c)  $+\omega$
- (d)  $-\omega$

**(GATE-16-EC)**

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4. Consider  $3 \times 3$  matrix with every element being equal to 1. Its only non-zero eigenvalue is

\_\_\_\_\_

(GATE-16-EE)

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**5.** A  $3 \times 3$  matrix P is such that,  $P^3 = P$ . Then the eigen values of P are

**(GATE-16-EE)**

- (a) 1, 1, -1
- (b) 1,  $0.5 + j0.866$ ,  $0.5 - j0.866$
- (c) 1,  $-0.5 + j0.866$ ,  $-0.5 - j0.866$
- (d) 0, 1, -1

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6. Consider the matrix  $A = \begin{pmatrix} 2 & 1 & 1 \\ 2 & 3 & 4 \\ -1 & -1 & -2 \end{pmatrix}$  whose eigen values are 1, -1 and 3. Then trace of  $(A^3 - 3A^2)$  is \_\_\_\_\_. **(GATE-16-IN)**

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7. The condition for which the eigen values of matrix  $A = \begin{bmatrix} 2 & 1 \\ 1 & k \end{bmatrix}$  are positive, is

- (a)  $k > \frac{1}{2}$       (b)  $k > -2$       (c)  $k > 0$       (d)  $k < -\frac{1}{2}$       (GATE-16-ME)

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8. A real square matrix A is called skew-symmetric if

- (a)  $A^T = A$
- (b)  $A^T = A^{-1}$
- (c)  $A^T = -A$
- (d)  $A^T = A + A^{-1}$

**(GATE-16-ME)**

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9. The eigen values of the matrix are  $\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$

- (a)  $i$  and  $-i$
- (b) 1 and -1
- (c) 0 and 1
- (d) 0 and -1

(GATE-16-PI)

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10. The number of solutions of the simultaneous algebraic equations  $y = 3x + 3$  and  $y = 3x + 5$  is

- (a) zero
- (b) 1
- (c) 2
- (d) infinite

**(GATE-16-PI)**

Use the code : BVREDDY, to get the maximum discount

11. Two eigen values of a  $3 \times 3$  real matrix P are  $(2 + \sqrt{-1})$  and 3. The determinant of P is \_\_\_\_\_.

**(GATE-16-CSE)**

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12. Suppose that the eigen values of matrix A are 1, 2, 4. The determinant of  $(A^{-1})^T$  is \_\_\_\_\_.

**(GATE-16-CSE)**

Use the code : BVREDDY, to get the maximum discount

13. Let  $A_1$ ,  $A_2$ ,  $A_3$  and  $A_4$  be four matrices of dimensions  $10 \times 5$ ,  $5 \times 20$ ,  $20 \times 10$  and  $10 \times 5$ , respectively. The minimum number of scalar multiplications required to find the product  $A_1A_2A_3A_4$  using the basic matrix multiplication method is \_\_\_\_\_.

(GATE-16-CSE)

Use the code : BVREDDY, to get the maximum discount

14. The eigen values of the matrix

$$A = \begin{bmatrix} 1 & -1 & 5 \\ 0 & 5 & 6 \\ 0 & -6 & 5 \end{bmatrix}$$
 are

(GATE-17-IN)

- (a) -1, 5, 6
- (b)  $1, -5 \pm j6$
- (c)  $1, 5 \pm j6$
- (d) 1, 5, 5

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15. The figure shows a shape ABC and its mirror image  $A_1B_1C_1$  across the horizontal axis (x-axis). The coordinate transformation matrix that maps ABC to  $A_1B_1C_1$  is

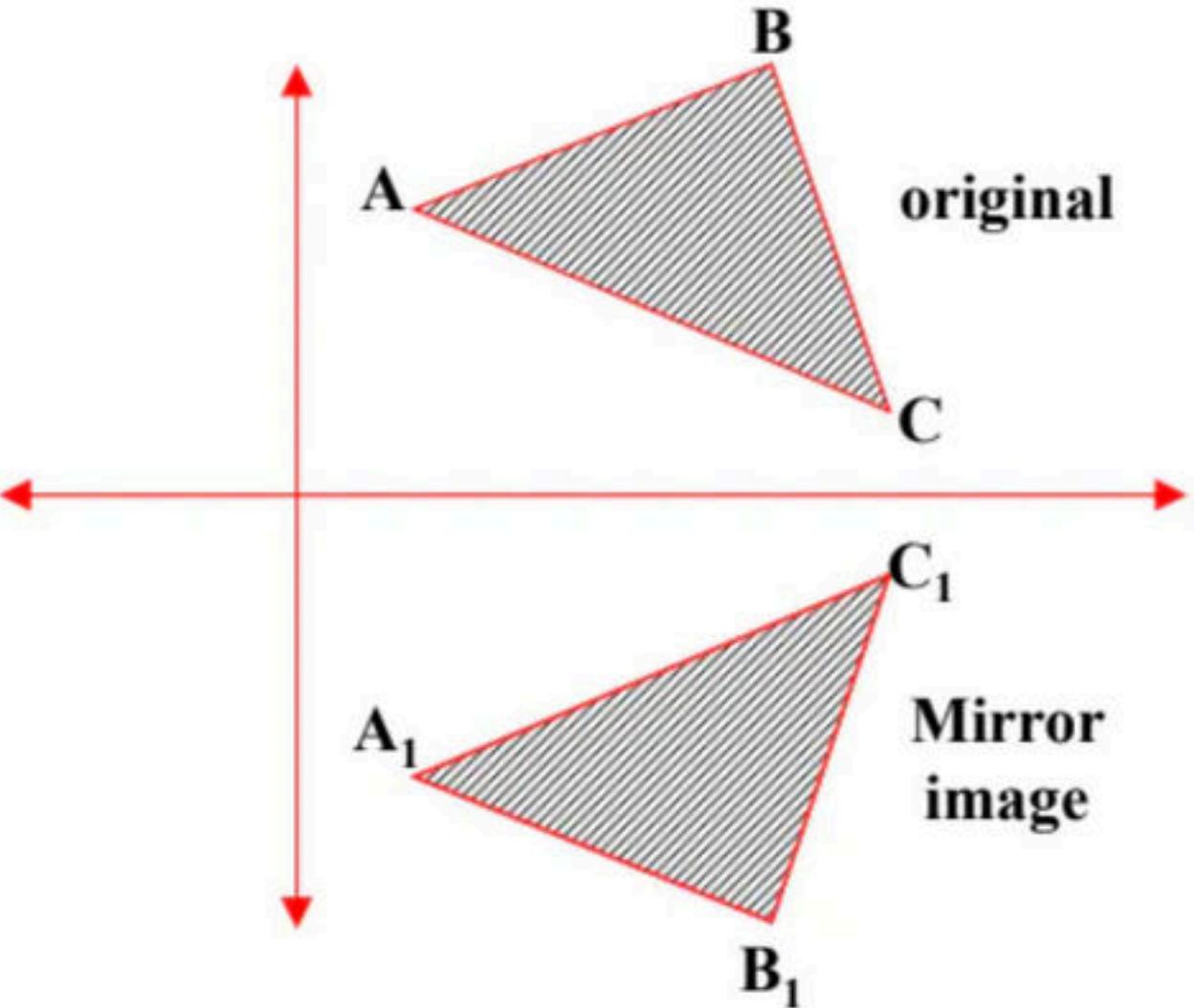
(GATE-17-IN)

(a)  $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$

(c)  $\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$

(b)  $\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$

(d)  $\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$



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16. Consider the  $5 \times 5$  matrix

$$\begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 5 & 1 & 2 & 3 & 4 \\ 4 & 5 & 1 & 2 & 3 \\ 3 & 4 & 5 & 1 & 2 \\ 2 & 3 & 4 & 5 & 1 \end{bmatrix}$$

It is given that A has only one real eigen value. Then the real eigen value of A is

- (a) -2.5
- (b) 0
- (c) 15
- (d) 25

(GATE-17-EC)

Use the code : BVREDDY, to get the maximum discount

17. The eigen values of the matrix given below

$$\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & -3 & -4 \end{bmatrix}$$
 are

- (a) (0, -1, -3)
- (b) (0, -2, -3)
- (c) (0, 2, 3)
- (d) (0, 1, 3)

**(GATE-17-EE)**

Use the code : BVREDDY, to get the maximum discount

18. The product of eigen values of the matrix P

$$P = \begin{bmatrix} 2 & 0 & 1 \\ 4 & -3 & 3 \\ 0 & 2 & -1 \end{bmatrix}$$
 is

- (a) -6
- (b) 2
- (c) 6
- (d) -2

**(GATE-17-ME)**

Use the code : BVREDDY, to get the maximum discount

19. The determinant of a  $2 \times 2$  matrix is 50. If one eigen value of the matrix is 10, the other eigen value is \_\_\_\_\_.

(GATE-17-ME)

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**20.** Consider the matrix  $A = \begin{bmatrix} 50 & 70 \\ 70 & 80 \end{bmatrix}$  whose eigen values  $\lambda_1$  and  $\lambda_2$  are  $x_1 = \begin{bmatrix} 70 \\ \lambda_1 - 50 \end{bmatrix}$  and  $x_2 = \begin{bmatrix} \lambda_2 - 80 \\ 70 \end{bmatrix}$ , respectively. The value of  $x_1^T x_2$  is \_\_\_\_\_

**(GATE-17-ME)**

Use the code : BVREDDY, to get the maximum discount

**21.** Consider the following simultaneous equations (with  $c_1$  and  $c_2$  being constants):

$$3x_1 + 2x_2 = c_1$$

$$4x_1 + x_2 = c_2$$

The characteristic equation for these simultaneous equations is

**(GATE-17-CE)**

(a)  $\lambda^2 - 4\lambda - 5 = 0$

(c)  $\lambda^2 + 4\lambda - 5 = 0$

(b)  $\lambda^2 - 4\lambda + 5 = 0$

(d)  $\lambda^2 + 4\lambda + 5 = 0$

Use the code : BVREDDY, to get the maximum discount

22. If  $A = \begin{bmatrix} 1 & 5 \\ 6 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 3 & 7 \\ 8 & 4 \end{bmatrix}$  then  $AB^T$  is equal to

(a)  $\begin{bmatrix} 38 & 28 \\ 32 & 56 \end{bmatrix}$

(b)  $\begin{bmatrix} 3 & 40 \\ 42 & 8 \end{bmatrix}$

(c)  $\begin{bmatrix} 43 & 27 \\ 34 & 50 \end{bmatrix}$

(d)  $\begin{bmatrix} 38 & 32 \\ 28 & 56 \end{bmatrix}$

(GATE-17-CE)

Use the code : BVREDDY, to get the maximum discount

**23.** The matrix P is the inverse of a matrix Q. If I denote the identity matrix, which one of the following options is correct?

- (a)  $PQ = I$  but  $QP \neq I$
- (b)  $QP = I$  but  $PQ \neq I$
- (c)  $PQ = I$  and  $QP = I$
- (d)  $PQ - QP = I$

**(GATE-17-CE)**

Use the code : BVREDDY, to get the maximum discount

**24.** Consider the matrix  $\begin{bmatrix} 5 & -1 \\ 4 & 1 \end{bmatrix}$ . Which one of the following statements is TRUE for the eigenvalues and eigenvectors of this matrix?

**(GATE-17-CE)**

- (a) eigenvalue 3 has a multiplicity of 2, and only one independent eigenvector exists.
- (b) eigenvalue 3 has a multiplicity of 2, and two independent eigenvectors exist.
- (c) eigenvalue 3 has a multiplicity of 2, and no independent eigenvector exists.
- (d) eigenvalues are 3 and -3, and two independent eigenvectors exist

**Use the code : BVREDDY, to get the maximum discount**

**25.** If the characteristic polynomial of a  $3 \times 3$  matrix M over R (the set of real numbers) is  $\lambda^3 - 4\lambda^2 + a\lambda + 30$ .  $a \in \mathbb{R}$ , and one eigenvalue of M is 2, then the largest among the absolute values of the eigenvalues of M is \_\_\_\_\_.

**(GATE-17-CSIT)**

Use the code : BVREDDY, to get the maximum discount

$$26. \text{ Consider the matrix } P = \begin{bmatrix} \frac{1}{\sqrt{2}} & 0 & \frac{1}{\sqrt{2}} \\ 0 & 1 & 0 \\ -\frac{1}{\sqrt{2}} & 0 & \frac{1}{\sqrt{2}} \end{bmatrix}.$$

Which one of the following statements about P is INCORRECT?

(GATE-17-ME)

- (a) Determinant of P is equal to 1
- (b) P is orthogonal
- (c) Inverse of P is equal to its transpose
- (d) All eigen values of P are real numbers

Use the code : BVREDDY, to get the maximum discount

27. For the given orthogonal matrix Q,

$$Q = \begin{bmatrix} 3/7 & 2/7 & 6/7 \\ -6/7 & 3/7 & 2/7 \\ 2/7 & 6/7 & -3/7 \end{bmatrix}$$

The inverse is

(GATE-18-CE)

$$(a) Q = \begin{bmatrix} 3/7 & 2/7 & 6/7 \\ -6/7 & 3/7 & 2/7 \\ 2/7 & 6/7 & -3/7 \end{bmatrix}$$

$$(b) Q = \begin{bmatrix} -3/7 & -2/7 & 6/7 \\ 6/7 & -3/7 & -2/7 \\ -2/7 & -6/7 & 3/7 \end{bmatrix}$$

$$(c) Q = \begin{bmatrix} 3/7 & -6/7 & 2/7 \\ 2/7 & 3/7 & 6/7 \\ 6/7 & 2/7 & -3/7 \end{bmatrix}$$

$$(d) Q = \begin{bmatrix} -3/7 & 6/7 & -2/7 \\ -2/7 & -3/7 & -6/7 \\ -6/7 & -2/7 & 3/7 \end{bmatrix}$$

Use the code : BVREDDY, to get the maximum discount

**28.** Which one of the following matrices is singular?

**(GATE-18-CE)**

(a)  $\begin{bmatrix} 2 & 5 \\ 1 & 3 \end{bmatrix}$

(b)  $\begin{bmatrix} 3 & 2 \\ 2 & 3 \end{bmatrix}$

(c)  $\begin{bmatrix} 2 & 4 \\ 3 & 6 \end{bmatrix}$

(d)  $\begin{bmatrix} 4 & 3 \\ 6 & 2 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

**29.** Consider matrix  $A = uv^T$

Where,  $u = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$ ,  $v = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ .

Note that  $v^T$  denotes the transpose of  $v$ . The largest eigen value of  $A$  is \_\_\_\_\_.

**(GATE-18-CSIT)**

**Use the code : BVREDDY, to get the maximum discount**

**30.** Consider a non-singular  $2 \times 2$  square matrix A. If  $\text{trace}(A) = 4$  and  $\text{trace}(A^2) = 5$ , the determinant of the matrix A is \_\_\_\_\_. (Up to 1 decimal place)

**(GATE-18-EC)**

Use the code : BVREDDY, to get the maximum discount

31. Let  $N$  be a 3 by 3 matrix with real number entries. The matrix  $N$  is such that  $N^2 = 0$ . The eigen values of  $N$  are

- (a) 0, 0, 0
- (b) 0, 0, 1
- (c) 0, 1, 1

**(GATE-18-IN)**

Use the code : BVREDDY, to get the maximum discount

32. If  $A = \begin{bmatrix} 1 & 2 & 3 \\ 0 & 4 & 5 \\ 0 & 0 & 1 \end{bmatrix}$  then  $\det(A^{-1})$  is \_\_\_\_\_ (correct to two decimal places).

(GATE-18-ME)

Use the code : BVREDDY, to get the maximum discount

33. The diagonal elements of a 3 by 3 matrix are -10, 5, and 0, respectively. If two of its eigenvalues are -15 each, the third eigen value is \_\_\_\_\_.

(GATE-18-PI)

Use the code : BVREDDY, to get the maximum discount

**34.** A  $3 \times 3$  matrix has eigen values 1, 2, and 5. The determinant of the matrix is \_\_\_\_\_.  
**(GATE-19-INST)**

Use the code : BVREDDY, to get the maximum discount

35. Consider the following matrix:  $R = \begin{bmatrix} 1 & 2 & 4 & 8 \\ 1 & 3 & 9 & 27 \\ 1 & 4 & 16 & 64 \\ 1 & 5 & 25 & 125 \end{bmatrix}$   
The absolute value of the product of Eigen values of R is \_\_\_\_\_. (GATE-19-CSIT)

Use the code : BVREDDY, to get the maximum discount

**36.** M is a  $2 \times 2$  matrix with eigen values 4 and 9. The eigen values of  $M^2$  are

**(GATE-19-EE)**

- (a) 2 and 3
- (b) -2 and -3
- (c) 4 and 9
- (d) 16 and 81

**Use the code : BVREDDY, to get the maximum discount**

37. Consider a  $2 \times 2$  matrix  $M = [v_1, v_2]$ , where,  $v_1$  and  $v_2$  are the column vectors.

Suppose  $M^{-1} = \begin{bmatrix} u_1^T \\ u_2^T \end{bmatrix}$ , where  $u_1^T$  and  $u_2^T$  are the row vectors.

Consider the following statements:

**Statement 1:**  $u_1^T v_1 = 1$  and  $u_2^T v_2 = 1$

**Statement 2:**  $u_1^T v_2 = 0$  and  $u_2^T v_1 = 0$

Which of the following options is correct?

- (a) Statement 2 is true and statement 1 is false
- (b) Both the statements are false
- (c) Statement 1 is true and statement 2 is false
- (d) Both the statements are true

**(GATE-19-EE)**

**Use the code : BVREDDY, to get the maximum discount**

**38.** For any real, square and non-singular matrix B, the  $\det B^{-1}$  is

- (a) zero
- (b)  $(\det B)^{-1}$
- (c)  $-(\det B)$
- (d)  $\det B$

**(GATE-19-ME)**

Use the code : BVREDDY, to get the maximum discount

39. Consider the matrix  $P = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$

The number of distinct eigen values of P is

- (a) 2
- (b) 1
- (c) 3
- (d) 0

**(GATE-19-ME)**

Use the code : BVREDDY, to get the maximum discount

40. The inverse of the matrix  $\begin{bmatrix} 2 & 3 & 4 \\ 4 & 3 & 1 \\ 1 & 2 & 4 \end{bmatrix}$  is

(GATE-19-CE)

(a)  $\begin{bmatrix} -10 & 4 & 9 \\ 15 & -4 & -14 \\ -5 & 1 & 6 \end{bmatrix}$

(b)  $\begin{bmatrix} 2 & -\frac{4}{5} & -\frac{9}{5} \\ -3 & \frac{4}{5} & \frac{14}{5} \\ 1 & -\frac{1}{5} & -\frac{6}{5} \end{bmatrix}$

(c)  $\begin{bmatrix} -2 & -\frac{4}{5} & \frac{9}{5} \\ 3 & -\frac{4}{5} & -\frac{14}{5} \\ -1 & \frac{1}{5} & \frac{6}{5} \end{bmatrix}$

(d)  $\begin{bmatrix} 10 & -4 & -9 \\ -15 & 4 & 14 \\ 5 & -1 & -6 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

41. Let  $A_1$ ,  $A_2$ ,  $A_3$  and  $A_4$  be four matrices of dimensions  $10 \times 5$ ,  $5 \times 20$ ,  $20 \times 10$  and  $10 \times 5$ , respectively. The minimum number of scalar multiplications required to find the product  $A_1A_2A_3A_4$  using the basic matrix multiplication method is \_\_\_\_\_.

(GATE-20-ME)

Use the code : BVREDDY, to get the maximum discount

42. A  $4 \times 4$  matrix [P] is given below

$$[P] = \begin{bmatrix} 0 & 1 & 3 & 0 \\ -2 & 3 & 0 & 4 \\ 0 & 0 & 6 & 1 \\ 0 & 0 & 1 & 6 \end{bmatrix}$$

The eigen values of [P] are

- (a) 0, 3, 6, 6
- (b) 1, 2, 3, 4
- (c) 1, 2, 5, 7
- (d) 3, 4, 5, 7

**(GATE-2020(CE))**

Use the code : BVREDDY, to get the maximum discount

43. If  $P = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$  and  $Q = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$  then  $Q^T P^T$  is

(GATE-21-CE)

(a)  $\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$

(c)  $\begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix}$

(b)  $\begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$

(d)  $\begin{bmatrix} 2 & 4 \\ 1 & 3 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

44. If A is a square matrix then orthogonality property mandates

(GATE-21-CE)

- (a)  $AA^T = I$
- (b)  $AA^T = 0$
- (c)  $AA^T = A^{-2}$
- (d)  $AA^T = A^2$

Use the code : BVREDDY, to get the maximum discount

45. Let p and q be real numbers such that  $p^2 + q^2 = 1$ . The eigenvalues of the matrix  $\begin{bmatrix} p & q \\ q & -p \end{bmatrix}$

are

- |                |              |              |
|----------------|--------------|--------------|
| (a) pq and -pq | (b) 1 and 1  | (GATE-21-EE) |
| (c) j and -j   | (d) 1 and -1 |              |

Use the code : BVREDDY, to get the maximum discount

**46.** Consider the following matrix :

$$\begin{pmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{pmatrix}$$

The largest eigenvalue of the above matrix is \_\_\_\_\_.

**(GATE-2021-cs)**

Use the code : BVREDDY, to get the maximum discount

47. A real  $2 \times 2$  non-singular matrix A with repeated eigenvalue is given as

$$A = \begin{bmatrix} x & -3.0 \\ 3.0 & 4.0 \end{bmatrix}$$

where x is a real positive number . The value of x ( rounded off to one decimal place ) is \_\_\_\_\_.

(GATE – 2021 – EC )

Use the code : BVREDDY, to get the maximum discount

48. The determinant of the matrix M shown below is \_\_\_\_\_.

$$M = \begin{bmatrix} 1 & 2 & 0 & 0 \\ 3 & 4 & 0 & 0 \\ 0 & 0 & 4 & 3 \\ 0 & 0 & 2 & 1 \end{bmatrix}$$

(GATE – 2021 – IN)

Use the code : BVREDDY, to get the maximum discount

49. The eigen vector (s) of the matrix

$$\begin{bmatrix} 0 & 0 & \alpha \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \alpha \neq 0 \text{ is (are)}$$

(GATE – 93)

- (a) (0, 0,  $\alpha$ )
- (b) ( $\alpha$ , 0, 0)
- (c) (0, 0, 1)
- (d) (0,  $\alpha$ , 0)

Use the code : BVREDDY, to get the maximum discount

50. If A and B are real symmetric matrices of order n then which of the following is true.

(GATE – 94[CS])

- (a)  $A A^T = I$
- (b)  $A = A - 1$
- (c)  $AB = BA$
- (d)  $(AB)^T = B^T A^T$

Use the code : BVREDDY, to get the maximum discount

51. The inverse of the matrix  $S = \begin{bmatrix} 1 & -1 & 0 \\ 1 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$

is

(GATE - 95[EE])

(a)  $\begin{bmatrix} 1 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 1 & 1 \end{bmatrix}$

(b)  $\begin{bmatrix} 0 & 1 & 1 \\ -1 & -1 & 1 \\ 1 & 0 & 1 \end{bmatrix}$

(c)  $\begin{bmatrix} 2 & 2 & -2 \\ -2 & 2 & -2 \\ 0 & 2 & 2 \end{bmatrix}$

(d)  $\begin{bmatrix} \frac{1}{2} & \frac{1}{2} & \frac{-1}{2} \\ \frac{-1}{2} & \frac{1}{2} & \frac{-1}{2} \\ 0 & 0 & 1 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

52. The eigen values of the matrix  $\begin{bmatrix} a & 1 \\ a & 1 \end{bmatrix}$  are

(GATE - 94[EE])

- (a)  $(a + 1), 0$
- (b)  $a, 0$
- (c)  $(a - 1), 0$
- (d)  $0, 0$

Use the code : BVREDDY, to get the maximum discount

53. The matrix  $\begin{bmatrix} 1 & -4 \\ 1 & -5 \end{bmatrix}$  is an inverse of the

matrix  $\begin{bmatrix} 5 & -4 \\ 1 & -1 \end{bmatrix}$  **(GATE – 94[PI])**

(a) True

(b) False

Use the code : BVREDDY, to get the maximum discount

54. The value of the following determinant

$$\begin{vmatrix} 1 & 4 & 9 \\ 4 & 9 & 16 \\ 9 & 16 & 25 \end{vmatrix}$$

is **(GATE - 94[PI])**

- (a) 8
- (b) 12
- (c) -12
- (d) -8

Use the code : BVREDDY, to get the maximum discount

55. For the following matrix  $\begin{bmatrix} 1 & -1 \\ 2 & 3 \end{bmatrix}$  the number of real positive characteristic roots is

(GATE - 94[PI])



**Use the code : BVREDDY, to get the maximum discount**

56. Given matrix  $L = \begin{bmatrix} 2 & 1 \\ 3 & 2 \\ 4 & 5 \end{bmatrix}$  and  $M = \begin{bmatrix} 3 & 2 \\ 0 & 1 \end{bmatrix}$

then  $L \times M$  is

(GATE - 95[PI])

(a)  $\begin{bmatrix} 8 & 1 \\ 13 & 2 \\ 22 & 5 \end{bmatrix}$

(b)  $\begin{bmatrix} 6 & 5 \\ 9 & 8 \\ 12 & 13 \end{bmatrix}$

(c)  $\begin{bmatrix} 1 & 8 \\ 2 & 13 \\ 5 & 22 \end{bmatrix}$

(d)  $\begin{bmatrix} 6 & 2 \\ 9 & 4 \\ 0 & 5 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

57.

Inverse of matrix  $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}$  is

(GATE – 97[CE])

(a)  $\begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$

(b)  $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$

(c)  $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

(d)  $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

58. Given the matrix  $A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}$ . Its eigen values are (GATE – 95[EE])

- a) 1, 2, 3
- b)-1, -2 , -3
- c)1 ,-2 , 3
- d)-1 ,-2 ,3

Use the code : BVREDDY, to get the maximum discount

59. The matrices  $\begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix}$  and  $\begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}$

commute under multiplication.

(GATE – 96[CS])

- (a) If  $a = b$  (or)  $\theta = n\pi$ ,  $n$  is an integer
- (b) always
- (c) never
- (d) If  $a \cos\theta \neq b \sin\theta$

Use the code : BVREDDY, to get the maximum discount

60. Let  $A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$  and  $B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}$  be two matrices such that  $AB = I$ .

Let  $C = A \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$  and  $CD = I$ .

Express the elements of D in terms of the elements of B.

Use the code : BVREDDY, to get the maximum discount

61. The eigen values of  $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$  are

(GATE – 96[ME])

- (a) 0, 0, 0
- (b) 0, 0, 1
- (c) 0, 0, 3
- (d) 1, 1, 1

Use the code : BVREDDY, to get the maximum discount

62. If the determinant of the matrix

$$\begin{bmatrix} 1 & 3 & 2 \\ 0 & 5 & -6 \\ 2 & 7 & 8 \end{bmatrix}$$
 is 26, then the determinant of

$$\text{the matrix } \begin{bmatrix} 2 & 7 & 8 \\ 0 & 5 & -6 \\ 1 & 3 & 2 \end{bmatrix}$$
 is

(GATE - 97[CE])

- (a) - 26
- (b) 26
- (c) 0
- (d) 52

Use the code : BVREDDY, to get the maximum discount

**63.** If A and B are two matrices if both AB and BA exists

- a) Only if A has as many rows as B has columns
- b) Only if the order of A and B are same
- c) Only if A and B are skew symmetric
- d) Only if both A and B are symmetric

**Use the code : BVREDDY, to get the maximum discount**

64. The determinant of the matrix

$$\begin{bmatrix} 6 & -8 & 1 & 1 \\ 0 & 2 & 4 & 6 \\ 0 & 0 & 4 & 8 \\ 0 & 0 & 0 & -1 \end{bmatrix}$$

is

(GATE - 97[CS])

- (a) 11
- (c) 0

- (b) - 48
- (d) - 24

Use the code : BVREDDY, to get the maximum discount

65. If  $\Delta = \begin{vmatrix} 1 & a & bc \\ 1 & b & ca \\ 1 & c & ab \end{vmatrix}$  then which of the following is a factor of  $\Delta$ .

(GATE - 98[CS])

- (a)  $a + b$
- (b)  $a - b$
- (c)  $abc$
- (d)  $a + b + c$

Use the code : BVREDDY, to get the maximum discount

66. If  $A$  is a real square matrix then  $AA^T$  is  
(GATE – 98[CE])

- (a) un symmetric
- (b) always symmetric
- (c) skew – symmetric
- (d) some times symmetric

Use the code : BVREDDY, to get the maximum discount

67. In matrix algebra  $AS = AT$  ( $A, S, T$ , are matrices of appropriate order) implies

$S = T$  only if

(GATE - 98[CE])

- (a)  $A$  is symmetric
- (b)  $A$  is singular
- (c)  $A$  is non-singular
- (d)  $A$  is skew-symmetric

Use the code : BVREDDY, to get the maximum discount

68. The eigen values of the matrix  $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$

are

(GATE - 98[EC])

- (a) 1, 1
- (b) -1, -1
- (c)  $j, -j$
- (d) 1, -1

Use the code : BVREDDY, to get the maximum discount

69.

$$A = \begin{bmatrix} 2 & 0 & 0 & -1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 3 & 0 \\ -1 & 0 & 0 & 4 \end{bmatrix}$$

The sum of the eigen

values of the matrix A is

(GATE – 98[EE])

- (a) 10
- (b) -10
- (c) 24
- (d) 22

Use the code : BVREDDY, to get the maximum discount

70.

$$\text{If } A = \begin{bmatrix} 5 & 0 & 2 \\ 0 & 3 & 0 \\ 2 & 0 & 1 \end{bmatrix} \text{ then } A^{-1} =$$

(GATE - 98[EE])

(a)  $\begin{bmatrix} 1 & 0 & -2 \\ 0 & 1/3 & 0 \\ -2 & 0 & 5 \end{bmatrix}$

(b)  $\begin{bmatrix} 5 & 0 & 2 \\ 0 & -1/3 & 0 \\ 2 & 0 & 1 \end{bmatrix}$

(c)  $\begin{bmatrix} 1/5 & 0 & 1/2 \\ 0 & 1/3 & 0 \\ 1/2 & 0 & 1 \end{bmatrix}$

(d)  $\begin{bmatrix} 1/5 & 0 & -1/2 \\ 0 & 1/3 & 0 \\ -1/2 & 0 & 1 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

71.

If  $A = \begin{bmatrix} 1 & -2 & -1 \\ 2 & 3 & 1 \\ 0 & 5 & -2 \end{bmatrix}$  and

$\text{adj}(A) = \begin{bmatrix} -11 & -9 & 1 \\ 4 & -2 & -3 \\ 10 & k & 7 \end{bmatrix}$  then  $k =$

(GATE - 99)

- |        |       |
|--------|-------|
| (a) -5 | (b) 3 |
| (c) -3 | (d) 5 |

Use the code : BVREDDY, to get the maximum discount

72.

If  $A$  is any  $n \times n$  matrix and  $k$  is a scalar then

$|kA| = \alpha |A|$  where  $\alpha$  is

(GATE-99[CE])

- (a)  $kn$
- (b)  $n^k$
- (c)  $k^n$
- (d)  $\frac{k}{n}$

Use the code : BVREDDY, to get the maximum discount

73. The number of terms in the expansion of general determinant of order  $n$  is

(GATE – 99[CE])

- (a)  $n^2$
- (b)  $n!$
- (c)  $n$
- (d)  $(n + 1)^2$

Use the code : BVREDDY, to get the maximum discount

74. The equation

$$\begin{vmatrix} 2 & 1 & 1 \\ 1 & 1 & -1 \\ y & x^2 & x \end{vmatrix} = 0$$

represents a parabola passing through the points.

(GATE – 99[CE])

- (a) (0, 1), (0, 2), (0, -1)
- (b) (0, 0), (-1, 1), (1, 2)
- (c) (1, 1), (0, 0), (2, 2)
- (d) (1, 2), (2, 1), (0, 0)

Use the code : BVREDDY, to get the maximum discount

75. An  $n \times n$  array  $V$  is defined as follows

$v[i,j] = i - j$  for all  $i, j$ ,  $1 \leq i, j \leq n$  then the sum of the elements of the array  $V$  is

(GATE-2000[CS])

- (a) 0
- (b)  $n - 1$
- (c)  $n^2 - 3n + 2$
- (d)  $n(n + 1)$

Use the code : BVREDDY, to get the maximum discount

76. The determinant of the matrix

$$\begin{bmatrix} 2 & 0 & 0 & 0 \\ 8 & 1 & 7 & 2 \\ 2 & 0 & 2 & 0 \\ 9 & 0 & 6 & 1 \end{bmatrix}$$

is **(GATE-2000[CS])**

- (a) 4      (b) 0      (c) 15      (d) 20

Use the code : BVREDDY, to get the maximum discount

77. If A, B, C are square matrices of the same order then  $(ABC)^{-1}$  is equal to

(GATE-2000[CE])

- (a)  $C^{-1} A^{-1} B^{-1}$
- (b)  $C^{-1} B^{-1} A^{-1}$
- (c)  $A^{-1} B^{-1} C^{-1}$
- (d)  $A^{-1} C^{-1} B^{-1}$

Use the code : BVREDDY, to get the maximum discount

78. The eigen values of the matrix

$$\begin{bmatrix} 2 & -1 & 0 & 0 \\ 0 & 3 & 0 & 0 \\ 0 & 0 & -2 & 0 \\ 0 & 0 & -1 & 4 \end{bmatrix} \text{ are}$$

(GATE-2000[EC])

- (a) 2, -2, 1, -1
- (b) 2, 3, -2, 4
- (c) 2, 3, 1, 4
- (d) None

Use the code : BVREDDY, to get the maximum discount

79. Consider the following statements

**S<sub>1</sub>:** The sum of two singular matrices may

be singular.

**S<sub>2</sub>:** The sum of two non-singular may be

non-singular.

Which of the following statements is true?

(GATE-01[CS])

- (a) S<sub>1</sub> & S<sub>2</sub> are both true
- (b) S<sub>1</sub> & S<sub>2</sub> are both false
- (c) S<sub>1</sub> is true and S<sub>2</sub> is false
- (d) S<sub>1</sub> is false and S<sub>2</sub> is true

Use the code : BVREDDY, to get the maximum discount

80. The determinant of the following matrix

$$\begin{bmatrix} 5 & 3 & 2 \\ 1 & 2 & 6 \\ 3 & 5 & 10 \end{bmatrix}$$

(GATE- 01[CE])

- (a) - 76
- (b) - 28
- (c) 28
- (d) 72

Use the code : BVREDDY, to get the maximum discount

81. The eigen values of the matrix  $\begin{bmatrix} 5 & 3 \\ 2 & 9 \end{bmatrix}$  are

(GATE-01[CE])

- (a) (5.13, 9.42)
- (b) (3.85, 2.93)
- (c) (9.00, 5.00)
- (d) (10.16, 3.84)

Use the code : BVREDDY, to get the maximum discount

82. The product  $[P][Q]^T$  of the following two matrices [P] and [Q]

where  $[P] = \begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix}$ ,  $[Q] = \begin{bmatrix} 4 & 8 \\ 9 & 2 \end{bmatrix}$  is

(GATE-01[CE])

(a)  $\begin{bmatrix} 32 & 24 \\ 56 & 46 \end{bmatrix}$

(b)  $\begin{bmatrix} 46 & 56 \\ 24 & 32 \end{bmatrix}$

(c)  $\begin{bmatrix} 35 & 22 \\ 61 & 42 \end{bmatrix}$

(d)  $\begin{bmatrix} 32 & 56 \\ 24 & 46 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

83. Obtain the eigen values of the matrix

$$A = \begin{bmatrix} 1 & 2 & 34 & 49 \\ 0 & 2 & 43 & 94 \\ 0 & 0 & -2 & 104 \\ 0 & 0 & 0 & -1 \end{bmatrix}$$

(GATE - 02[CS])

- (a) 1,2,-2,-1
- (b) -1,-2,-1,-2
- (c) 1,2,2,1
- (d) None

Use the code : BVREDDY, to get the maximum discount

84. The number of linearly independent eigen

vectors of  $\begin{bmatrix} 2 & 1 \\ 0 & 2 \end{bmatrix}$  is

(GATE-07[ME])

- (a) 0
- (b) 1
- (c) 2
- (d) infinite

Use the code : BVREDDY, to get the maximum discount

85. The determinant of the matrix

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 100 & 1 & 0 & 0 \\ 100 & 200 & 1 & 0 \\ 100 & 200 & 300 & 1 \end{bmatrix} \text{ is } (\text{GATE - 02[EE]})$$

- (a) 100
- (b) 200
- (c) 1
- (d) 300

Use the code : BVREDDY, to get the maximum discount

86. Eigen values of the following matrix are

$$\begin{bmatrix} -1 & 4 \\ 4 & -1 \end{bmatrix}$$

(GATE – 02|CE)

- (a) 3, -5
- (b) -3, 5
- (c) -3, -5
- (d) 3, 5

Use the code : BVREDDY, to get the maximum discount

87. If matrix  $X = \begin{bmatrix} a & 1 \\ -a^2 + a - 1 & 1-a \end{bmatrix}$  and  
 $X^2 - X + I = O$  then the inverse of  $X$  is  
**(GATE – 04)**

(a)  $\begin{bmatrix} 1-a & -1 \\ a^2 & a \end{bmatrix}$

(b)  $\begin{bmatrix} 1-a & -1 \\ a^2 - a + 1 & a \end{bmatrix}$

(c)  $\begin{bmatrix} -a & 1 \\ -a^2 + a - 1 & a - 1 \end{bmatrix}$

(d)  $\begin{bmatrix} a^2 - a + 1 & a \\ 1 & 1-a \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

88. The number of different  $n \times n$  symmetric matrices with each elements being either 0 or 1 is

(GATE-04[CS])

(a)  $2^n$

(b)  $2^{n^2}$

(c)  $2^{\frac{n^2+n}{2}}$

(d)  $2^{\frac{n^2-n}{2}}$

Use the code : BVREDDY, to get the maximum discount

89. Let A, B, C, D be  $n \times n$  matrices, each with non-zero determinant.  $ABCD = I$  then  $B^{-1} =$

(GATE-04[CS])

- (a)  $D^{-1}C^{-1}A^{-1}$
- (b) CDA
- (c) ABC
- (d) does not exist

Use the code : BVREDDY, to get the maximum discount

90. The sum of the eigen values of the matrix

$$\begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{bmatrix}$$

is **(GATE-04[ME])**

- (a) 5
- (b) 7
- (c) 9
- (d) 18

Use the code : BVREDDY, to get the maximum discount

91. For what value of x will the matrix given

below become singular?

$$\begin{bmatrix} 8 & x & 0 \\ 4 & 0 & 2 \\ 12 & 6 & 0 \end{bmatrix}$$

(GATE-04[ME])

- a) -4
- b) 4
- c) 2
- d)-2

Use the code : BVREDDY, to get the maximum discount

92. Real matrices  $[A]_{3 \times 1}$ ,  $[B]_{3 \times 3}$ ,  $[C]_{3 \times 5}$ ,  $[D]_{5 \times 3}$ ,  $[E]_{5 \times 5}$ ,  $[F]_{5 \times 1}$  are given. Matrices  $[B]$  and  $[E]$  are symmetric. Following statements are made with respect to their matrices.

- (I) Matrix product  $[F]^T [C]^T [B] [C] [F]$  is a scalar.
- (II) Matrix product  $[D]^T [F] [D]$  is always symmetric.

With reference to above statements which of the following applies?

(GATE-04[CE])

- (a) statement (I) is true but (II) is false
- (b) statement (I) is false but (II) is true
- (c) both the statements are true
- (d) both the statements are false

Use the code : BVREDDY, to get the maximum discount

93. The eigen values of the matrix  $\begin{bmatrix} 4 & -2 \\ -2 & 1 \end{bmatrix}$

are

(GATE-04[CE])

- (a) 1, 4
- (b) -1, 2
- (c) 0, 5
- (d) can not be determined

Use the code : BVREDDY, to get the maximum discount

94. What are the eigen values of the following

2 x 2 matrix  $\begin{bmatrix} 2 & -1 \\ -4 & 5 \end{bmatrix}$  (GATE-05[CS])

- (a) -1, 1
- (b) 1, 6
- (c) 2, 5
- (d) 4, -1

Use the code : BVREDDY, to get the maximum discount

95. Consider the matrices  $X_{4 \times 3}$ ,  $Y_{4 \times 3}$  and  $P_{2 \times 3}$ .

The order of  $[P (X^T Y)^{-1} P^T]^T$  will be

(GATE-05[CE])

- (a)  $2 \times 2$
- (b)  $3 \times 3$
- (c)  $4 \times 3$
- (d)  $3 \times 4$

Use the code : BVREDDY, to get the maximum discount

96. The determinant of the matrix given below

is 
$$\begin{bmatrix} 0 & 1 & 0 & 2 \\ -1 & 1 & 1 & 3 \\ 0 & 0 & 0 & 1 \\ 1 & -2 & 0 & 1 \end{bmatrix}$$

(GATE-05)

- (a) -1
- (b) 0
- (c) 1
- (d) 2

Use the code : BVREDDY, to get the maximum discount

97. For the matrix  $P = \begin{bmatrix} 3 & -2 & 2 \\ 0 & -2 & 1 \\ 0 & 0 & 1 \end{bmatrix}$ , one of the eigen values is -2. Which of the following is an eigen vector? (GATE-05[EE])

(a)  $\begin{pmatrix} 3 \\ -2 \\ 1 \end{pmatrix}$

(b)  $\begin{pmatrix} -3 \\ 2 \\ -1 \end{pmatrix}$

(c)  $\begin{pmatrix} 1 \\ -2 \\ 3 \end{pmatrix}$

(d)  $\begin{pmatrix} 2 \\ 5 \\ 0 \end{pmatrix}$

Use the code : BVREDDY, to get the maximum discount

98. If  $R = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 1 & -1 \\ 2 & 3 & 2 \end{bmatrix}$  then the top row of  $R^{-1}$

is **(GATE-05[EE])**

- (a) [5 6 4]      (b) [5 -3 1]
- (c) [2 0 -1]      (d) [2 -1 0]

Use the code : BVREDDY, to get the maximum discount

99. The eigen values of the matrix M given are  
15, 3 and 0.

$$M = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}, \text{the value of the determinant}$$

of a matrix is

(GATE-05[PI])

- (a) 20
- (b) 10
- (c) 0
- (d) -10

Use the code : BVREDDY, to get the maximum discount

100. Identify which one of the following is an

eigen vector of the matrix  $A = \begin{bmatrix} 1 & 0 \\ -1 & -2 \end{bmatrix}$

(GATE-05[IN])

- (a)  $[-1 \ 1]^T$
- (b)  $[3 \ -1]^T$
- (c)  $[1 \ -1]^T$
- (d)  $[-2 \ 1]^T$

Use the code : BVREDDY, to get the maximum discount

101. If  $A = \begin{bmatrix} 2 & -0.1 \\ 0 & 3 \end{bmatrix}$  and  $A^{-1} = \begin{bmatrix} \frac{1}{2} & a \\ 0 & b \end{bmatrix}$  then

$$a + b =$$

(GATE-05[EE])

(a)  $\frac{7}{20}$

(b)  $\frac{3}{20}$

(c)  $\frac{19}{60}$

(d)  $\frac{11}{20}$

Use the code : BVREDDY, to get the maximum discount

102. Given an orthogonal matrix

$$A = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & 1 & -1 \end{bmatrix}. (AA^T)^{-1} \text{ is}$$

(GATE-05[EC])

- (a)  $\frac{1}{4}I_4$
- (b)  $\frac{1}{2}I_4$
- (c)  $I$
- (d)  $\frac{1}{3}I_4$

Use the code : BVREDDY, to get the maximum discount

103. Given the matrix  $\begin{bmatrix} -4 & 2 \\ 4 & 3 \end{bmatrix}$ , the eigen vector

is

(GATE-05[EC])

(a)  $\begin{bmatrix} 3 \\ 2 \end{bmatrix}$

(b)  $\begin{bmatrix} 4 \\ 3 \end{bmatrix}$

(c)  $\begin{bmatrix} 2 \\ -1 \end{bmatrix}$

(d)  $\begin{bmatrix} -2 \\ 1 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

104. Eigen values of a matrix  $S = \begin{bmatrix} 3 & 2 \\ 2 & 3 \end{bmatrix}$  are

5 and 1. What are the eigen values of the matrix  $S^2 = SS$ ? **(GATE - 06[ME])**

- (a) 1 and 25
- (b) 6, 4
- (c) 5, 1
- (d) 2, 10

Use the code : BVREDDY, to get the maximum discount

105. Multiplication of matrices E and F is G.

Matrices E and G are

$$E = \begin{bmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \text{ and } G = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}.$$

What is the matrix F?

(GATE-06[ME])

(a)  $\begin{bmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$  (b)  $\begin{bmatrix} \cos\theta & \cos\theta & 0 \\ -\cos\theta & \sin\theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$

(c)  $\begin{bmatrix} \cos\theta & \sin\theta & 0 \\ -\sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$  (d)  $\begin{bmatrix} \sin\theta & -\cos\theta & 0 \\ \cos\theta & \sin\theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

106. For a given  $2 \times 2$  matrix A, it is observed that

$$A \begin{bmatrix} 1 \\ -1 \end{bmatrix} = -1 \begin{bmatrix} 1 \\ -1 \end{bmatrix} \text{ and } A \begin{bmatrix} 1 \\ -2 \end{bmatrix} = -2 \begin{bmatrix} 1 \\ -2 \end{bmatrix}$$

then the matrix A is      (GATE-06[IN])

(a)  $A = \begin{bmatrix} 2 & 1 \\ -1 & -1 \end{bmatrix} \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ -1 & -2 \end{bmatrix}$

(b)  $A = \begin{bmatrix} 1 & 1 \\ -1 & -2 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 1 & 2 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ -1 & -1 \end{bmatrix}$

(c)  $A = \begin{bmatrix} 1 & 1 \\ -1 & -2 \end{bmatrix} \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ -1 & -1 \end{bmatrix}$

(d)  $A = \begin{bmatrix} 0 & -2 \\ 1 & -3 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

**107.** The eigen values and the corresponding eigen vectors of a  $2 \times 2$  matrix are given by

**Eigen value**

$$\lambda_1 = 8$$

**Eigen vector**

$$V_1 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$\lambda_2 = 4$$

$$V_2 = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

The matrix is

**(GATE-06[EC])**

(a)  $\begin{bmatrix} 6 & 2 \\ 2 & 6 \end{bmatrix}$

(b)  $\begin{bmatrix} 4 & 6 \\ 6 & 4 \end{bmatrix}$

(c)  $\begin{bmatrix} 2 & 4 \\ 4 & 2 \end{bmatrix}$

(d)  $\begin{bmatrix} 4 & 8 \\ 8 & 4 \end{bmatrix}$

**Use the code : BVREDDY, to get the maximum discount**

108. For the matrix  $\begin{bmatrix} 4 & 2 \\ 2 & 4 \end{bmatrix}$ . The eigen value

corresponding to the eigen vector  $\begin{bmatrix} 1 & 0 & 1 \\ 1 & 0 & 1 \end{bmatrix}$  is

(GATE-06[EC])

- (a) 2
- (b) 4
- (c) 6
- (d) 8

Use the code : BVREDDY, to get the maximum discount

**109.** For a given matrix  $A = \begin{bmatrix} 2 & -2 & 3 \\ -2 & -1 & 6 \\ 1 & 2 & 0 \end{bmatrix}$ , one

of the eigen value is 3. The other two eigen values are

(GATE-06[CE])

- (a) 2, -5
- (b) 3, -5
- (c) 2, 5
- (d) 3, 5

Use the code : BVREDDY, to get the maximum discount

**110.** The minimum and maximum eigen values

of matrix  $\begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{bmatrix}$  are -2 and 6

respectively. What is the other eigen value?

**(GATE-07[CE])**

- (a) 5
- (b) 3
- (c) 1
- (d) -1

Use the code : BVREDDY, to get the maximum discount

111. The inverse of  $2 \times 2$  matrix  $\begin{bmatrix} 1 & 2 \\ 5 & 7 \end{bmatrix}$  is

(GATE - 07[CE])

(a)  $\frac{1}{3} \begin{bmatrix} -7 & 2 \\ 5 & -1 \end{bmatrix}$

(b)  $\frac{1}{3} \begin{bmatrix} 7 & 2 \\ 5 & 1 \end{bmatrix}$

(c)  $\frac{1}{3} \begin{bmatrix} 7 & -2 \\ -5 & 1 \end{bmatrix}$

(d)  $\frac{1}{3} \begin{bmatrix} -7 & -2 \\ -5 & -1 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

112. If a square matrix A is real and symmetric  
then the eigen values

(GATE – 07[ME])

- (a) are always real
- (b) are always real and positive
- (c) are always real and non-negative
- (d) occur in complex conjugate pairs

Use the code : BVREDDY, to get the maximum discount

113. The determinant  $\begin{vmatrix} 1+b & b & 1 \\ b & 1+b & 1 \\ 1 & 2b & 1 \end{vmatrix}$  equals to  
**(GATE-07[PI])**

- (a) 0
- (b)  $2b(b - 1)$
- (c)  $2(1 - b)(1 + 2b)$
- (d)  $3b(1 + b)$

Use the code : BVREDDY, to get the maximum discount

114. If  $A = \begin{bmatrix} -3 & 2 \\ -1 & 0 \end{bmatrix}$  then  $A^9$  equals

(GATE-07[EE])

- (a)  $511 A + 510 I$
- (b)  $309 A + 104 I$
- (c)  $154 A + 155 I$
- (d)  $e^{9A}$

Use the code : BVREDDY, to get the maximum discount

115. All the four entries of  $2 \times 2$  matrix

$P = \begin{bmatrix} P_{11} & P_{12} \\ P_{21} & P_{22} \end{bmatrix}$  are non - zero and one of

the eigen values is zero. Which of the following statement is true?

(GATE-08[EC])

- (a)  $P_{11}P_{22} - P_{12}P_{21} = 1$
- (b)  $P_{11}P_{22} - P_{12}P_{21} = -1$
- (c)  $P_{11}P_{22} - P_{21}P_{12} = 0$
- (d)  $P_{11}P_{22} + P_{12}P_{21} = 0$

Use the code : BVREDDY, to get the maximum discount

116. The matrix  $\begin{bmatrix} 1 & 2 & 4 \\ 3 & 0 & 6 \\ 1 & 1 & p \end{bmatrix}$  has one eigen value to 3. The sum of the other two eigen values is

(GATE-08[ME])

- (a) p
- (b) p - 1
- (c) p - 2
- (d) p - 3

Use the code : BVREDDY, to get the maximum discount

117. The eigen vectors of the matrix  $\begin{bmatrix} 1 & 2 \\ 0 & 2 \end{bmatrix}$  are

written in the form  $\begin{bmatrix} 1 \\ a \end{bmatrix}$  &  $\begin{bmatrix} 1 \\ b \end{bmatrix}$ . What is

$a + b$ ?

(GATE-08[ME])

- (a) 0
- (b)  $\frac{1}{2}$
- (c) 1
- (d) 2

Use the code : BVREDDY, to get the maximum discount

118. The eigen vector pair of the matrix

$$\begin{bmatrix} 3 & 4 \\ 4 & -3 \end{bmatrix}$$
 is

(GATE-08[PI])

(a)  $\begin{bmatrix} 2 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix}$

(b)  $\begin{bmatrix} 2 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \end{bmatrix}$

(c)  $\begin{bmatrix} -2 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix}$

(d)  $\begin{bmatrix} -2 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

119. The inverse of matrix  $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  is

(GATE-08[PI])

(a)  $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

(b)  $\begin{bmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{bmatrix}$

(c)  $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}$

(d)  $\begin{bmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

120. How many of the following matrices have an eigen value 1?

$$\begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}, \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}, \begin{bmatrix} 1 & -1 \\ 1 & 1 \end{bmatrix} \text{ & } \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$$

(GATE-08[CS])

- (a) one
- (b) two
- (c) three
- (d) four

Use the code : BVREDDY, to get the maximum discount

121 . The product of matrices  $(PQ)^{-1} P$  is

(GATE-08[CE])

- (a)  $P^{-1}$
- (b)  $Q^{-1}$
- (c)  $P^{-1} Q^{-1} P$
- (d)  $P Q P^{-1}$

Use the code : BVREDDY, to get the maximum discount

122. The eigen values of the matrix

$$[P] = \begin{bmatrix} 4 & 5 \\ 2 & -5 \end{bmatrix} \text{ are } \quad (\text{GATE-08[CE]})$$

- (a) -7 and 8
- (b) -6 and 5
- (c) 3 and 4
- (d) 1 and 2

Use the code : BVREDDY, to get the maximum discount

123. A square matrix B is symmetric if \_\_\_\_\_  
(GATE-09[CE])

- (a)  $B^T = -B$
- (b)  $B^T = B$
- (c)  $B^{-1} = B$
- (d)  $B^{-1} = B^T$

Use the code : BVREDDY, to get the maximum discount

124. The eigen values of the following matrix

$$\begin{bmatrix} -1 & 3 & 5 \\ -3 & -1 & 6 \\ 0 & 0 & 3 \end{bmatrix} \text{ are } \quad (\text{GATE-09[EC]})$$

- (a) 3, 3+5j, 6-j
- (b) -6+5j, 3+j, 3-j
- (c) 3+j, 3-j, 5+j
- (d) 3, -1+3j, -1-3j

Use the code : BVREDDY, to get the maximum discount

125. The characteristic equation of a  $3 \times 3$  matrix

P is defined as

$$\alpha(\lambda) = |\lambda I - P| = \lambda^3 + 2\lambda + \lambda^2 + 1 = 0.$$

If I denotes identity matrix then the inverse of P will be

(GATE-08[EE])

- |                       |                        |
|-----------------------|------------------------|
| (a) $P^2 + P + 2I$    | (b) $P^2 + P + I$      |
| (c) $- (P^2 + P + I)$ | (d) $- (P^2 + P + 2I)$ |

Use the code : BVREDDY, to get the maximum discount

126. The eigen values of a  $2 \times 2$  matrix X are -2 and -3. The eigen values of matrix  $(X+I)^{-1}(X+5I)$  are **(GATE-09[IN])**



Use the code : **BVREDDY**, to get the maximum discount

127.

For a matrix  $[M] = \begin{bmatrix} \frac{3}{5} & \frac{4}{5} \\ \frac{5}{5} & \frac{5}{5} \\ x & \frac{3}{5} \end{bmatrix}$ . The

transpose of the matrix is equal to the inverse of the matrix,  $[M]^T = [M]^{-1}$ . The value of  $x$  is given by (GATE-09[ME])

(a)  $-\frac{4}{5}$

(b)  $-\frac{3}{5}$

(c)  $\frac{3}{5}$

(d)  $\frac{4}{5}$

Use the code : BVREDDY, to get the maximum discount

128. The trace and determinant of a  $2 \times 2$  matrix are shown to be  $-2$  and  $-35$  respectively. Its eigen values are

(GATE-09[EE])

- (a)  $-30, -5$
- (b)  $-37, -1$
- (c)  $-7, 5$
- (d)  $17.5, -2$

Use the code : BVREDDY, to get the maximum discount

129. The value of the determinant

$$\begin{vmatrix} 1 & 3 & 2 \\ 4 & 1 & 1 \\ 2 & 1 & 3 \end{vmatrix}$$

(GATE-09[PI])

is

- (a) - 28
- (b) - 24
- (c) 32
- (d) 36

Use the code : BVREDDY, to get the maximum discount

130. An eigen vector of  $p = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 2 & 2 \\ 0 & 0 & 3 \end{bmatrix}$  is

(GATE-10[EE])

- (a)  $[-1 \ 1 \ 1]^T$
- (b)  $[1 \ 2 \ 1]^T$
- (c)  $[1 \ -1 \ 2]^T$
- (d)  $[2 \ 1 \ -1]^T$

Use the code : BVREDDY, to get the maximum discount

131. The eigen values of a skew-symmetric matrix are **(GATE-10[EC])**

- (a) always zero
- (b) always pure imaginary
- (c) either zero (or) pure imaginary
- (d) always real

Use the code : BVREDDY, to get the maximum discount

132. One of the eigen vector of the matrix

$$A = \begin{bmatrix} 2 & 2 \\ 1 & 3 \end{bmatrix} \text{ is } \quad (\text{GATE-10[ME]})$$

(a)  $\begin{bmatrix} 2 \\ -1 \end{bmatrix}$

(b)  $\begin{bmatrix} 2 \\ 1 \end{bmatrix}$

(c)  $\begin{bmatrix} 4 \\ 1 \end{bmatrix}$

(d)  $\begin{bmatrix} 1 \\ -1 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

133. A real  $n \times n$  matrix  $A = [a_{ij}]$  is defined as

follows  $\begin{cases} a_{ij} = i, & \forall i = j \\ = 0, & \text{otherwise} \end{cases}$ .

The sum of all  $n$  eigen values of  $A$  is

(GATE 10[IN])

(a)  $\frac{n(n+1)}{2}$

(b)  $\frac{n(n-1)}{2}$

(c)  $\frac{n(n+1)(2n+1)}{2}$

(d)  $n^2$

Use the code : BVREDDY, to get the maximum discount

134. X and Y are non-zero square matrices of size  $n \times n$ . If  $XY = O_{n \times n}$  then

(GATE-10[IN])

- (a)  $|X| = 0$  and  $|Y| \neq 0$
- (b)  $|X| \neq 0$  and  $|Y| = 0$
- (c)  $|X| = 0$  and  $|Y| = 0$
- (d)  $|X| \neq 0$  and  $|Y| \neq 0$

Use the code : BVREDDY, to get the maximum discount

135. Consider the following matrix  $A = \begin{bmatrix} 2 & 3 \\ x & y \end{bmatrix}$ .

If the eigen values of A are 4 and 8 then

(GATE-10[CS])

- (a)  $x = 4, y = 10$
- (b)  $x = 5, y = 8$
- (c)  $x = -3, y = 9$
- (d)  $x = -4, y = 10$

Use the code : BVREDDY, to get the maximum discount

136. The inverse of the matrix  $\begin{bmatrix} 3+2i & i \\ -i & 3-2i \end{bmatrix}$  is  
(GATE-10[CE])

- (a)  $\frac{1}{2} \begin{bmatrix} 3+2i & -i \\ i & 3-2i \end{bmatrix}$
- (b)  $\frac{1}{12} \begin{bmatrix} 3-2i & -i \\ i & 3+2i \end{bmatrix}$
- (c)  $\frac{1}{14} \begin{bmatrix} 3+2i & -i \\ i & 3-2i \end{bmatrix}$
- (d)  $\frac{1}{14} \begin{bmatrix} 3-2i & -i \\ i & 3+2i \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

137. If  $(1, 0, -1)^T$  is an eigen vector of the

following matrix  $\begin{bmatrix} 1 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 1 \end{bmatrix}$  then the

corresponding eigen value is

(GATE-10[PI])

- (a) 1
- (b) 2
- (c) 3
- (d) 5

Use the code : BVREDDY, to get the maximum discount

138. The minimum eigenvalue of the following

matrix is  $\begin{bmatrix} 3 & 5 & 2 \\ 5 & 12 & 7 \\ 2 & 7 & 5 \end{bmatrix}$

(GATE – 13[EC])

- (a) 0
- (b) 1
- (c) 2
- (d) 3

Use the code : BVREDDY, to get the maximum discount

139. The matrix  $[A] = \begin{bmatrix} 2 & 1 \\ 4 & -1 \end{bmatrix}$  is decomposed into a product of lower triangular matrix  $[L]$  and an upper triangular  $[U]$ . The properly decomposed  $[L]$  and  $[U]$  matrices respectively are

(GATE-11[EE])

(a)  $\begin{bmatrix} 1 & 0 \\ 4 & -1 \end{bmatrix}$  and  $\begin{bmatrix} 1 & 1 \\ 0 & -2 \end{bmatrix}$

(b)  $\begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$  and  $\begin{bmatrix} 2 & 1 \\ 0 & -3 \end{bmatrix}$

(c)  $\begin{bmatrix} 1 & 0 \\ 4 & 1 \end{bmatrix}$  and  $\begin{bmatrix} 2 & 1 \\ 0 & -1 \end{bmatrix}$

(d)  $\begin{bmatrix} 2 & 0 \\ 4 & -3 \end{bmatrix}$  and  $\begin{bmatrix} 1 & 0.5 \\ 0 & 1 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

140. The matrix  $M = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & 6 \\ -1 & -2 & 0 \end{bmatrix}$  has eigen

values  $-3, -3, 5$ . An eigen vector corresponding to the eigen value  $5$  is  $[1 \ 2 \ -1]^T$ . One of the eigen vector of the matrix  $M^3$  is

(GATE-11[IN])

- (a)  $[1 \ 8 \ -1]^T$
- (b)  $[1 \ 2 \ -1]^T$
- (c)  $[1 \ \sqrt[3]{2} \ -1]^T$
- (d)  $[1 \ 1 \ -1]^T$

Use the code : BVREDDY, to get the maximum discount

141. The eigen values of the following matrix

$$\begin{bmatrix} 10 & -4 \\ 18 & -12 \end{bmatrix}$$
 are

(GATE-11[PI])

- (a) 4, 9
- ~~(b) 6, -8~~
- (c) 4, 8
- (d) -6, 8

$$\lambda_1 + \lambda_2 = -2$$

$$\begin{aligned}\lambda_1 \lambda_2 &= -120 + 72 \\ &= -48\end{aligned}$$

Use the code : BVREDDY, to get the maximum discount

142. If a matrix  $A = \begin{bmatrix} 2 & 4 \\ 1 & 3 \end{bmatrix}$  and matrix

$B = \begin{bmatrix} 4 & 6 \\ 5 & 9 \end{bmatrix}$  the transpose of product of

these two matrices i.e.,  $(AB)^T$  is equal to  
(GATE-11[PI])

(a)  $\begin{bmatrix} 28 & 19 \\ 34 & 47 \end{bmatrix}$

(b)  $\begin{bmatrix} 19 & 34 \\ 47 & 28 \end{bmatrix}$

(c)  $\begin{bmatrix} 48 & 33 \\ 28 & 19 \end{bmatrix}$

(d)  ~~$\begin{bmatrix} 28 & 19 \\ 48 & 33 \end{bmatrix}$~~

$$AB = \begin{bmatrix} 2 & 4 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} 4 & 6 \\ 5 & 9 \end{bmatrix}$$

$$= \begin{bmatrix} 8+20 & 12+36 \\ 4+15 & 6+27 \end{bmatrix}$$

$$= \begin{bmatrix} 28 & 48 \\ 19 & 33 \end{bmatrix}$$

$$(AB)^T = \begin{bmatrix} 28 & 19 \\ 48 & 33 \end{bmatrix}$$

Use the code : BVREDDY, to get the maximum discount

143. Eigen values of a real symmetric matrix are

always

(GATE-11[ME])

(a) positive

(b) negative

~~(c) real~~

(d) ~~square~~ is a square

Eigen values of real Symmetric matrix  $\rightarrow$  always Real

Eigen values of Skew Symmetric matrix  
= zero (or) purely img.

Use the code : BVREDDY, to get the maximum discount

144. [A] is a square matrix which is neither symmetric nor skew-symmetric and  $[A]^T$  is its transpose. The sum and differences of these matrices are defined as  
 $\checkmark$   $[S] = [A] + [A]^T$  and  $\checkmark$   $[D] = [A] - [A]^T$  respectively. Which of the following statements is true? **(GATE-11[CS])**

$$A = \frac{(A + A^T)}{2} + \frac{(A - A^T)}{2}$$

↓                              ↓

Symmetric                              Skew  
Symmetric

- (a) Both  $[S]$  and  $[D]$  are symmetric
  - (b) Both  $[S]$  and  $[D]$  are skew-symmetric
  - (c)  $[S]$  is skew-symmetric and  $[D]$  is symmetric
  - (d)  $[S]$  is symmetric and  $[D]$  is skew-symmetric

Use the code : BVREDDY, to get the maximum discount

145. Consider the matrix as given below

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 4 & 7 \\ 0 & 0 & 3 \end{bmatrix}$$

. Which one of the following options provides the correct values of the eigen values of the matrix? (GATE-11[CS])

- (a) 1, 4, 3
- (b) 3, 7, 3
- (c) 7, 3, 2
- (d) 1, 2, 3

UTM

$\lambda = 1, 4, 3$ .

Use the code : BVREDDY, to get the maximum discount

146. Given that  $A = \begin{bmatrix} -5 & -3 \\ 2 & 0 \end{bmatrix}$  and  $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ ,

$$|A - \lambda I| = 0$$

the value of  $A^3$  is

(GATE-12[EC, EE, IN])

- (a)  $15A + 12I$       ~~(b)  $19A + 30I$~~   
(c)  $17A + 15I$       (d)  $17A + 21I$

$$\begin{vmatrix} -5-\lambda & -3 \\ 2 & -\lambda \end{vmatrix} = 0$$

$$5\lambda + \lambda^2 + 6 = 0$$

$$\boxed{\lambda^2 + 5\lambda + 6 = 0}$$

$$A^2 + 5A + 6I = 0$$

$$A^2 = -5A - 6I$$

$$A^3 = -5A^2 - 6A$$

$$A^3 = -5(-5A - 6I) - 6A = 25A + 30I - 6A.$$

$$\boxed{A^3 = 19A + 30I}$$

Use the code : BVREDDY, to get the maximum discount

147. For the matrix  $A = \begin{bmatrix} 5 & 3 \\ 1 & 3 \end{bmatrix}$ , ONE of the normalized eigen vectors is given as

(GATE-12[ME, PI])

(a)  $\begin{pmatrix} \frac{1}{2} \\ \frac{\sqrt{3}}{2} \end{pmatrix}$

(c)  $\begin{pmatrix} \frac{3}{\sqrt{10}} \\ \frac{-1}{\sqrt{10}} \end{pmatrix}$

(b)  $\begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{-1}{\sqrt{2}} \end{pmatrix}$

(d)  $\begin{pmatrix} \frac{1}{5} \\ \frac{2}{\sqrt{5}} \end{pmatrix}$

$$\lambda_1 + \lambda_2 = 8$$

$$\lambda_1 \lambda_2 = 15 - 3 = 12$$

$$\underline{\lambda_1 = 2}, \quad \lambda_2 = 6.$$

$$A \times = \lambda \times$$

$$\begin{bmatrix} 5 & 3 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = 2 \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$5x_1 + 3x_2 = 2x_1$$

$$3x_1 = -3x_2$$

$$\boxed{x_1 = -x_2}$$

Use the code : BVREDDY, to get the maximum discount

148. The eigen values of matrix  $\begin{bmatrix} 9 & 5 \\ 5 & 8 \end{bmatrix}$  are

- (GATE-12[CE])
- (a) -2.42 and 6.86
  - (b) ~~3.48 and 13.53~~
  - (c) 4.70 and 6.86
  - (d) 6.86 and 9.50

$$\lambda_1 + \lambda_2 = 17$$

$$\lambda_1 \lambda_2 = 72 - 25 = 47$$

Use the code : BVREDDY, to get the maximum discount

149. A matrix has eigen values -1 and -2.

The corresponding eigenvectors are  $\begin{bmatrix} 1 \\ -1 \end{bmatrix}$

and  $\begin{bmatrix} 1 \\ -2 \end{bmatrix}$  respectively. The matrix is

(GATE - 13[EE])

(a)  $\begin{bmatrix} 1 & 1 \\ -1 & -2 \end{bmatrix}$

(b)  $\begin{bmatrix} 1 & 2 \\ -2 & -4 \end{bmatrix}$

(c)  $\begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix}$

(d)  $\begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}$

$$AP = PD$$

$$A = PDP^{-1}$$

$$A = \begin{bmatrix} 1 & 1 \\ -1 & -2 \end{bmatrix} \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix}^{-1} \begin{bmatrix} -2 & -1 \\ -1 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1+0 & -2 \\ -1+1 & +4 \end{bmatrix} \begin{bmatrix} 2 & +1 \\ -1 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} -2+2 & -1+2 \\ 2-4 & 1-4 \end{bmatrix}$$

$$= \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}$$

Use the code : BVREDDY, to get the maximum discount

150. The two vectors  $[1 \ 1 \ 1]$  and  $[1 \ a \ a^2]$

where  $a = -\frac{1}{2} + j\frac{\sqrt{3}}{2}$  and  $j = \sqrt{-1}$  are

- (a) orthonormal
- (b) orthogonal
- (c) parallel
- (d) collinear

(GATE-11[EE])

- (b) orthogonal
- (d) collinear

$$a = -\frac{1}{2} + j\frac{\sqrt{3}}{2}$$

$$1, \ a, \ a^2$$

$$x_1 \quad x_2$$

$$\begin{aligned} x_1 x_2^\top &= 0 \\ x_2 x_1^\top &= 0 \end{aligned} \quad \left. \right\} \text{orthogonal.}$$

$$\begin{aligned} x_1 x_1^\top &= 1 \\ x_2 x_2^\top &= 1 \end{aligned} \quad \left. \right\} \text{orthonormal.}$$

Use the code : BVREDDY, to get the maximum discount

$$x_1 = [1 \ 1 \ 1] \quad x_2 = [1 \ a \ a^2] \quad x_1 x_1^T = [1 \ 1 \ 1] \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$$

$$x_1 x_2^T = [1 \ 1 \ 1] \begin{bmatrix} 1 \\ a \\ a^2 \end{bmatrix}_{1 \times 3} \quad x_2 x_2^T = [1 \ a \ a^2] \begin{bmatrix} 1 \\ a \\ a^2 \end{bmatrix}_{3 \times 1}$$

$$x_1 x_2^T = 1 + a + a^2 = 0$$

$$= 1 + 1 + 1 = \underline{\underline{3}}$$

$$x_2 x_2^T = [1 \ a \ a^2] \begin{bmatrix} 1 \\ a \\ a^2 \end{bmatrix} = 1 + a^2 + a^4$$

$$= 1 + a^2 + a$$

$$= 0$$

$$x_2 x_1^T = [1 \ a \ a^2] \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$$

$$= 1 + a + a^2 = 0$$

Cube roots of unity.

$1,$	$\frac{-1}{2} + j\frac{\sqrt{3}}{2}$	$\frac{-1}{2} - j\frac{\sqrt{3}}{2}$
$1$	$\omega$	$\omega^2$
$1$	$a$	$a^2$ .

$$1 + a + a^2 = 0$$

$$(1)(a)(a^2) = 1$$

151. Let A be an  $m \times n$  matrix and B an  $n \times m$  matrix. It is given that determinant  $(I_m + AB) = \text{determinant}(I_n + BA)$ , where  $I_k$  is the  $k \times k$  identity matrix. Using the above property, the determinant of the matrix

$$\begin{bmatrix} 2 & 1 & 1 & 1 \\ 1 & 2 & 1 & 1 \\ 1 & 1 & 2 & 1 \\ 1 & 1 & 1 & 2 \end{bmatrix}$$

given below is

- (a) 2
- (b) 5
- (c) 8
- (d) 16

(GATE - 2013[EC])

$$C_1 \leftrightarrow C_1 + C_2 + C_3 + C_4$$

$$\begin{vmatrix} 5 & 1 & 1 & 1 \\ 5 & 2 & 1 & 1 \\ 5 & 1 & 2 & 1 \\ 5 & 1 & 1 & 2 \end{vmatrix} = 5 \begin{vmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & 1 & 1 \\ 1 & 1 & 2 & 1 \\ 1 & 1 & 1 & 2 \end{vmatrix}$$

$$= 5 \begin{vmatrix} 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

$$= (5) \begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{vmatrix} = 5(1) = 5$$

Use the code : BVREDDY, to get the maximum discount

$$A = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}_{4 \times 1}$$

$$B = \begin{bmatrix} 1 & 1 & 1 & 1 \end{bmatrix}_{1 \times 4}$$

$$m=4 \quad n=1$$

$$(I_4 + AB) = I_4 + \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}_{4 \times 1} \begin{bmatrix} 1 & 1 & 1 & 1 \end{bmatrix}_{1 \times 4}$$

$$= I_4 + \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 2 & 1 & 1 & 1 \\ 1 & 2 & 1 & 1 \\ 1 & 1 & 2 & 1 \\ 1 & 1 & 1 & 2 \end{bmatrix}$$

$$|I_4 + BA| = |I_1 + BA|.$$

$$I_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$BA = \begin{bmatrix} 1 & 1 & 1 & 1 \end{bmatrix}_{1 \times 4} \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}_{4 \times 1}.$$

$$I_1 = [1].$$

$$= 1+1+1+1 = 4$$

$$|I_1 + BA| = |1+4| = \underline{\underline{5}}$$

152. One pair of eigenvectors corresponding to the two eigen values of the matrix

$$\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$$

(GATE – 2013[IN])

(a)  $\begin{bmatrix} 1 \\ -j \end{bmatrix}, \begin{bmatrix} j \\ -1 \end{bmatrix}$

(b)  $\begin{bmatrix} 0 \\ 1 \end{bmatrix}, \begin{bmatrix} -1 \\ 0 \end{bmatrix}$

(c)  $\begin{bmatrix} 1 \\ j \end{bmatrix}, \begin{bmatrix} 0 \\ 1 \end{bmatrix}$

(d)  $\cancel{\begin{bmatrix} 1 \\ j \end{bmatrix}, \begin{bmatrix} j \\ 1 \end{bmatrix}}$

$$0 - x_2 = -j x_1.$$

$$x_1 = -j x_2$$

$$x_2 = j x_1.$$

$$\frac{x_2}{x_1} = j$$

$$\lambda_1 + \lambda_2 = 0$$

$$\lambda_1 \lambda_2 = +1$$

$$\lambda_1 = j \quad \lambda_2 = -j$$

$$A\mathbf{x} = \lambda \mathbf{x}$$

$$\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = j \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$0 - x_2 = j x_1.$$

$$x_1 = j x_2$$

$$\frac{x_1}{x_2} = +j$$

Use the code : BVREDDY, to get the maximum discount

153. The eigen values of a symmetric matrix are

all

(GATE – 2013[ME])

- (a) Complex with non-zero positive imaginary part.
- (b) Complex with non-zero negative imaginary part.
- (c) real ✓
- (d) Pure imaginary

Use the code : BVREDDY, to get the maximum discount

154. What is the minimum number of multiplications involved in computing the matrix product PQR? Matrix P has 4 rows and 2 columns, matrix Q has 2 rows and 4 columns and matrix R has 4 rows and 1 column \_\_\_\_\_.

(A)<sub>m×n</sub> (B)<sub>n×p</sub>

$$\text{No. of Multiplications} = m n p$$

$$\text{No. of additions} = m (n-1) p$$

(GATE – 2013[CE])

16

Use the code : BVREDDY, to get the maximum discount

155. Which one of the following does NOT

equal  $\begin{vmatrix} 1 & x & x^2 \\ 1 & y & y^2 \\ 1 & z & z^2 \end{vmatrix}$ ?

(GATE - 2013[CS])

(a)  $\begin{vmatrix} 1 & x(x+1) & x+1 \\ 1 & y(y+1) & y+1 \\ 1 & z(z+1) & z+1 \end{vmatrix}$

(b)  $\begin{vmatrix} 1 & x+1 & x^2+1 \\ 1 & y+1 & y^2+1 \\ 1 & z+1 & z^2+1 \end{vmatrix}$

(c)  $\begin{vmatrix} 0 & x-y & x^2-y^2 \\ 0 & y-z & y^2-z^2 \\ 1 & z & z^2 \end{vmatrix}$

(d)  $\begin{vmatrix} 2 & x+y & x^2+y^2 \\ 2 & y+z & y^2+z^2 \\ 1 & z & z^2 \end{vmatrix}$

$C_2 \rightarrow C_2 + C_1$

$C_3 \rightarrow C_3 + C_1$

(b)

$R_1 \rightarrow R_1 - R_2$

$R_2 \rightarrow R_2 - R_3$

(c)

$R_1 \rightarrow R_1 + R_2$

$R_2 \rightarrow R_2 + R_3$

(d)

Use the code : BVREDDY, to get the maximum discount

156. For matrices of same dimension M, N and scalar c, which one of these properties DOES NOT ALWAYS hold?

(GATE-14-EC-SET1)

- (a)  $(M^T)^T = M$  ✓
- (b)  $(cM)^T = c(M)^T$  ✓
- (c)  $(M + N)^T = M^T + N^T$  ✓
- (d)  $MN = NM$  ✗

Use the code : BVREDDY, to get the maximum discount

157. A real  $(4 \times 4)$  matrix A satisfies the equation  $A^2 = I$ , where I is the  $(4 \times 4)$  identity matrix. The positive eigen value of A is \_\_\_\_\_.

(GATE-14-EC-SET1)

$$A^2 = I$$

$$\lambda^2 = 1$$

$$(\lambda - 1)(\lambda + 1) = 0$$

$$\lambda = +1, -1$$

Use the code : BVREDDY, to get the maximum discount

158. Consider the matrix

$$J_6 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & \alpha \\ 0 & 0 & 0 & 0 & \alpha & 0 \\ 0 & 0 & 0 & \alpha & 0 & 0 \\ 0 & 0 & \alpha & 0 & 0 & 0 \\ 0 & \alpha & 0 & 0 & 0 & 0 \\ \alpha & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$P = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & \alpha \\ 0 & 1 & 0 & 0 & \alpha & 0 \\ 0 & 0 & 1 & \alpha & 0 & 0 \\ 0 & 0 & \alpha & 1 & 0 & 0 \\ 0 & \alpha & 0 & 0 & 1 & 0 \\ \alpha & 0 & 0 & 0 & 0 & 1 \end{bmatrix}_{6 \times 6}$$

Which is obtained by reversing the order of the columns of the identity matrix  $I_6$ . Let  $P = I_6 + \alpha J_6$ , where  $\alpha$  is a non-negative real number. The value of  $\alpha$  for which  $\det(P) = 0$  is \_\_\_\_\_.

(GATE-14-EC-SETI)

$$|P| = (-\alpha^2)^3 = 0$$

$$\boxed{\alpha = \pm 1}$$

$$\alpha = +1 \checkmark$$

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$$\begin{vmatrix} 1 & \alpha \\ \alpha & 1 \end{vmatrix}_{2 \times 2} = (1 - \alpha^2)^1$$

$$\begin{vmatrix} 1 & 0 & 0 & \alpha \\ 0 & 1 & \alpha & 0 \\ 0 & \alpha & 1 & 0 \\ \alpha & 0 & 0 & 1 \end{vmatrix}_{4 \times 4} = (1 - \alpha^2)^2.$$

159. The determinant of matrix A is 5 and the determinant of matrix B is 40. The determinant of matrix AB is \_\_\_\_\_.

(GATE-14-EC-SET2)

$$\begin{aligned}|AB| &= |A| |B| \\&= (5)(40) = 200\end{aligned}$$

Use the code : BVREDDY, to get the maximum discount

160. The maximum value of the determinant among all  $2 \times 2$  real symmetric matrices with trace 14 is 49.

(GATE-14-EC-SET2)

$$\frac{\lambda_1 + \lambda_2}{2} = ?$$

$$AM \geq GM.$$

$$? \geq \sqrt{\lambda_1 \lambda_2}$$

$$\boxed{\lambda_1 \lambda_2 \leq 49}$$

$$\lambda_1 + \lambda_2 = 14$$

$$|A| = \lambda_1 \lambda_2$$

$$AM =$$

$$GM = \sqrt{\lambda_1 \lambda_2}.$$

Use the code : BVREDDY, to get the maximum discount

161. Which one of the following statements is  
NOT true for a square matrix A?

(GATE-14-EC-SET3)

- (a) If A is upper triangular, the eigen values of A are the diagonal elements of it ✓
- (b) If A is real symmetric, the eigen values of A are always real and positive ~~positive~~
- (c) If A is real, the eigen values of A and  $A^T$  are always the same
- (d) If all the principal minors of A are positive, all the eigen values of A are also positive

Use the code : BVREDDY, to get the maximum discount

162. A system matrix is given as follows

$$A = \begin{bmatrix} 0 & 1 & -1 \\ -6 & -11 & 6 \\ -6 & -11 & 5 \end{bmatrix}.$$

The absolute value of the ratio of the maximum eigen value to the minimum eigen value is 3.

(GATE-14-EE-SET1)

3

$$\lambda_1 + \lambda_2 + \lambda_3 = -6.$$

$$\lambda_1 \lambda_2 \lambda_3 = -6 [1] = \underline{-6}$$

$$\lambda_1 = -1$$

$$\lambda_2 = -2$$

$$\lambda_3 = -3.$$

Use the code : BVREDDY, to get the maximum discount

163. Which one of the following statements is true for all real symmetric matrices?

(GATE-14-EE-SET2)

- (a) All the eigen values are real ✓
- (b) All the eigen values are positive
- (c) All the eigen values are distinct
- (d) Sum of all the eigen values is zero

Use the code : BVREDDY, to get the maximum discount

164. A scalar valued function is defined as  
 $f(x) = x^T Ax + b^T x + c$ , where A is a  
symmetric positive definite matrix with  
dimension  $n \times n$ ; b and x are vectors of  
dimension  $n \times 1$ . The minimum value of  $f(x)$   
will occur when  $x$  equals.

(GATE-14-IN-SET1)

(a)  $(A^T A)^{-1} B$

(b)  $- (A^T A)^{-1} B$

(c)  $- \left( \frac{A^{-1} B}{2} \right)$

(d)  $\frac{A^{-1} B}{2}$

$x = -\frac{1}{2} A^{-1} B$

$(A)_{l \times 1}$

$f(x) = x A x + B x + C$ .

$f(x) = A x^2 + B x + C$ .

$f'(x) = 2Ax + B = 0$

$2Ax + B = 0$ .

$2Ax = -B$ .

$x = -\frac{1}{2} \frac{B}{A}$ .

Use the code : BVREDDY, to get the maximum discount

$$A = \begin{bmatrix} p & q \\ q & s \end{bmatrix}_{2 \times 2}$$

$$B = \begin{bmatrix} b_1 \\ b_2 \end{bmatrix}.$$

$$X = \begin{bmatrix} x \\ y \end{bmatrix}_{2 \times 1}.$$

$$f(x) = [x \ y] \begin{bmatrix} px+qy \\ qx+sy \end{bmatrix} + b_1x + b_2y + c$$

$$f(x) = px^2 + qxy + qxy + sy^2 + b_1x + b_2y + c.$$

$$f(x) = X^T A X + B^T X + C$$

$$= [x \ y] \begin{bmatrix} p & q \\ q & s \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + [b_1 \ b_2] \begin{bmatrix} x \\ y \end{bmatrix} + C.$$

$$f(x) = px^2 + 2qxy + sy^2 + b_1x + b_2y + c$$

$$P = \frac{\partial f}{\partial x} = 2px + 2qy + b_1.$$

$$Q = \frac{\partial f}{\partial y} = 2qx + 2sy + b_2.$$

$$2 \begin{bmatrix} P & Q \\ Q & S \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = 0$$

$$2Ax + B = 0$$

$$\boxed{x = -\frac{1}{2} \bar{A}^{-1} B}$$

165. For the matrix A satisfying the equation given below, the eigen values are

$$[A] \begin{bmatrix} 1 & 2 & 3 \\ 7 & 8 & 9 \\ 4 & 5 & 6 \end{bmatrix} = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

(GATE-14-IN-SET1)

- (a) (1, -j, j)
- (b) (1, 1, 0)
- ~~(c) (1, 1, -1)~~
- (d) (1, 0, 0)

$$A = I$$

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

$$\lambda_1 + \lambda_2 + \lambda_3 = 1.$$

$$\lambda_1 \lambda_2 \lambda_3 = -1$$

Use the code : BVREDDY, to get the maximum discount

$$R_1 \rightarrow \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 & x_2 \\ x_3 & x_4 \end{bmatrix} = \begin{bmatrix} x_1 & x_2 \\ x_3 & x_4 \end{bmatrix}$$

$$R_2 \rightarrow \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 & x_2 \\ x_3 & x_4 \end{bmatrix} = \begin{bmatrix} x_3 & x_4 \\ x_1 & x_2 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 & x_2 \\ x_3 & x_4 \end{bmatrix} = \begin{bmatrix} x_3 & x_4 \\ x_1 & x_2 \end{bmatrix}$$

$$\begin{bmatrix} x_1 & x_2 \\ x_3 & x_4 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} = \begin{bmatrix} x_2 & x_1 \\ x_4 & x_3 \end{bmatrix}$$

**166.** Given that the determinant of the matrix

$\begin{bmatrix} 1 & 3 & 0 \\ 2 & 6 & 4 \\ -1 & 0 & 2 \end{bmatrix}$  is -12, the determinant of the

matrix  $\begin{bmatrix} 2 & 6 & 0 \\ 4 & 12 & 8 \\ -2 & 0 & 4 \end{bmatrix}$  is (GATE-14-ME-SET1)



$$A = \begin{bmatrix} 1 & 3 & 0 \\ 2 & 6 & 4 \\ -1 & 0 & 2 \end{bmatrix}$$

$$B = \begin{bmatrix} 2 & 6 & 0 \\ 4 & 12 & 8 \\ -2 & 0 & 4 \end{bmatrix}$$

$$B = 2A.$$

$$|B| = 2^n |A| = 2^3 (-1^2) \equiv -96.$$

Use the code : BVREDDY, to get the maximum discount

167. One of the eigen vectors of the matrix

$$\begin{bmatrix} -5 & 2 \\ -9 & 6 \end{bmatrix}$$

is

(GATE-14-ME-SET2)

(a)  $\begin{Bmatrix} -1 \\ 1 \end{Bmatrix}$

(b)  $\begin{Bmatrix} -2 \\ 9 \end{Bmatrix}$

(c)  $\begin{Bmatrix} 2 \\ -1 \end{Bmatrix}$

(d)  $\begin{Bmatrix} 1 \\ 1 \end{Bmatrix}$

$$-5x_1 + 2x_2 = -3x_1.$$

$$2x_2 = 2x_1$$

$$x_2 = x_1$$

$$\lambda_1 + \lambda_2 = 1$$

$$\lambda_1 \lambda_2 = -30 + 18 = -12.$$

$$\lambda_1 = 4, -3$$

$$Ax = \lambda x.$$

$$\begin{bmatrix} -5 & 2 \\ -9 & 6 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = 4 \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$-5x_1 + 2x_2 = 4x_1.$$

$$2x_2 = 9x_1$$

Use the code : BVREDDY, to get the maximum discount

168. Consider a  $3 \times 3$  real symmetric matrix S such that two of its eigen values are  $a \neq 0$ ,  $b \neq 0$  with respective eigen vectors

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}, \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}. \text{ If } a \neq b \text{ then } x_1y_1 + x_2y_2 + x_3y_3$$

equals

- (a) a
- (b) b
- (c) ab
- (d) 0

(GATE-14-ME-SET3)

- (b) b
- (d) 0

Eigen vectors of Symmetric matrix are orthogonal to each other.

$$x_1 x_2^T = 0$$

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} [y_1 \ y_2 \ y_3] = 0$$

$$x_1 y_1 + x_2 y_2 + x_3 y_3 = 0$$

Use the code : BVREDDY, to get the maximum discount

169. Which one of the following equations is a correct identity for arbitrary  $3 \times 3$  real matrices P, Q and R?

(GATE-14-ME-SET4)

- (a)  $\underline{P(Q+R)} = PQ + RP$  ✗
- (b)  $(P-Q)^2 = P^2 - 2PQ + Q^2$  ✗
- (c)  $\det(P+Q) = \det P + \det Q$  ✗
- (d)  $(P+Q)^2 = P^2 + PQ + QP + Q^2$  ✓

$$|A+B| \neq |A| + |B|.$$

$$|AB| = |A| |B|.$$

Use the code : BVREDDY, to get the maximum discount

170.

Given the matrices  $J = \begin{bmatrix} 3 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 6 \end{bmatrix}$  and

$K = \begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix}$ , the product  $K^T J K$  is \_\_\_\_\_.

(GATE-14-CE-SET1)

$$= [1 \ 2 \ -1] \begin{bmatrix} 3 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 6 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix}$$

$$= [1 \ 2 \ -1] \begin{bmatrix} 3+4-1 \\ 2+8-2 \\ 1+4-6 \end{bmatrix}$$

$$= [1 \ 2 \ -1] \begin{bmatrix} 6 \\ 8 \\ -1 \end{bmatrix}$$

$$= 6 + 16 + 1 = \underline{\underline{23}}$$

Use the code : BVREDDY, to get the maximum discount

171. The sum of Eigen values of the matrix, [M]

is where  $[M] = \begin{bmatrix} 215 & 650 & 795 \\ 655 & 150 & 835 \\ 485 & 355 & 550 \end{bmatrix}$

$$\lambda_1 + \lambda_2 + \lambda_3 = 215 + 150 + 550 \\ = \underline{\underline{915}}$$

(GATE-14-CE-SET1)

- (a) 915
- (b) 1355
- (c) 1640
- (d) 2180

Use the code : BVREDDY, to get the maximum discount

172. The determinant of matrix  $\begin{bmatrix} 0 & 1 & 2 & 3 \\ 1 & 0 & 3 & 0 \\ 2 & 3 & 0 & 1 \\ 3 & 0 & 1 & 2 \end{bmatrix}$  is

$$R_3 \rightarrow R_3 - 3R_1.$$

(GATE-14-CE-SET2)

$$\begin{vmatrix} 0 & 1 & 2 & 3 \\ 1 & 0 & 3 & 0 \\ 2 & 3 & 0 & 1 \\ 3 & 0 & 1 & 2 \end{vmatrix} = - \begin{vmatrix} 1 & 3 & 0 \\ 2 & -6 & -8 \\ 3 & 1 & 2 \end{vmatrix} = - [1(-12+8) - 3(4+24)] \\ = -[-4 - 3(28)] \\ = \underline{\underline{88}}$$

Use the code : BVREDDY, to get the maximum discount

▲ 1 • Asked by Rupnarayan

Please help me with this doubt



← Solutions

Unanswered

All Sections

All Tr

Question 11

YOU DIDN'T ATTEMPT

Your time taken: 44s

Avg time taken by others: 1m 40s

Attempt accuracy: 49% Basics of Matrix

Which of the following elementary operations may affect  
the rank of a matrix?

Scalar multiplication

Adding two rows

Adding a row with the scalar multiple of another row

None of the above

CORRECT ANSWER

Row operations

▲ 1 • Asked by Shashank

Please help me with this doubt

Your Time Taken: 2m 41s

Probability Distribution

$X_1$  is a normal random variable with  $E(X_1) = 0$  and  $V(X_1) = 1$ . If  $X_2 = X_1^2$  then which of the following statement(s) is/are INCORRECT?

$X_1$  and  $X_2$  are dependent

Correlation coefficient,  $r_{X_1 X_2} = 0$

INCORRECT

$X_1$  and  $X_2$  are independent

YOUR ANSWER

$X_1$  and  $X_2$  are linearly correlated

CORRECT ANSWER

$$f(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}}$$

$$E[X_1] = E[X_1^2]$$

$$E[X_2] = 1$$

$$\text{Var}(X_2) = \text{Var}(X_1^2)$$

=

173. The value of the dot product of the eigenvectors corresponding to any pair of different eigen values of a  $4 \times 4$  symmetric positive definite matrix is \_\_\_\_\_.

(GATE-14-CS-SET1)

Use the code : BVREDDY, to get the maximum discount

174. The product of the non-zero eigen values of

the matrix  $\begin{bmatrix} 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 \\ 1 & 0 & 0 & 0 & 1 \end{bmatrix}$  is \_\_\_\_\_.

(GATE-14-CS-SET2)

Use the code : BVREDDY, to get the maximum discount

175. Which one of the following statements is TRUE about every  $n \times n$  matrix with only real eigen values? **(GATE-14-CS-SET3)**

- (a) If the trace of the matrix is positive and the determinant is negative, at least one of its eigen values is negative.
- (b) If the trace of the matrix is positive, all its eigen values are positive.
- (c) If the determinant of the matrix is positive, all its eigen values are positive.
- (d) If the product of the trace and determinant of the matrix is positive, all its eigen values are positive.

Use the code : BVREDDY, to get the maximum discount

176. The value of 'P' such that the vector  $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$  is

an eigenvector of the matrix  $\begin{bmatrix} 4 & 1 & 2 \\ P & 2 & 1 \\ 14 & -4 & 10 \end{bmatrix}$

is \_\_\_\_\_. (GATE-15-EC-SET1)

Use the code : BVREDDY, to get the maximum discount

177. The value of 'x' for which all the eigenvalues of the matrix given below are real is

$$\begin{bmatrix} 10 & 5+j & 4 \\ x & 20 & 2 \\ 4 & 2 & -10 \end{bmatrix}$$

(GATE-15-EC- SET2)

- (a)  $5 + j$
- (b)  $5 - j$
- (c)  $1 - 5j$
- (d)  $1 + 5j$

Use the code : BVREDDY, to get the maximum discount

178. For  $A = \begin{bmatrix} 1 & \tan x \\ -\tan x & 1 \end{bmatrix}$ , the determinant of  $A^T A^{-1}$  is

(GATE-15-EC-SET3)

- (a)  $\sec^2 x$
- (b)  $\cos 4x$
- (c) 1
- (d) 0

Use the code : BVREDDY, to get the maximum discount

179. If the sum of the diagonal elements of a  $2 \times 2$  matrix is  $-6$ , then the maximum possible value of determinant of the matrix is \_\_\_\_\_.

**(GATE-15-EE- SET1)**

Use the code : BVREDDY, to get the maximum discount

180. The necessary condition to diagonalize a matrix is that

(GATE - 01[IN])

- (a) all its eigen values should be distinct
- (b) its eigen vectors should be independent
- (c) its eigen values should be real
- (d) the matrix is non-singular

Use the code : BVREDDY, to get the maximum discount

181. The smallest and largest Eigen values of the

following matrix are:

$$\begin{bmatrix} 3 & -2 & 2 \\ 4 & -4 & 6 \\ 2 & -3 & 5 \end{bmatrix}$$

(GATE – 15 – CE – Set 1)

- (a) 1.5 and 2.5
- (b) 0.5 and 2.5
- (c) 1.0 and 3.0
- (d) 1.0 and 2.0

Use the code : BVREDDY, to get the maximum discount

182. The two Eigen Values of the matrix  $\begin{bmatrix} 2 & 1 \\ 1 & p \end{bmatrix}$

have a ratio of 3:1 for  $p = 2$ . What is another value of 'p' for which the Eigen values have the same ratio of 3:1?

(GATE – 15 – CE – Set 2)

- (a) -2
- (b) 1
- (c)  $7/3$
- (d)  $14/3$

Use the code : BVREDDY, to get the maximum discount

**183.** If any two columns of a determinant

$$P = \begin{vmatrix} 4 & 7 & 8 \\ 3 & 1 & 5 \\ 9 & 6 & 2 \end{vmatrix}$$

are interchanged, which one

of the following statements regarding the value of the determinant is CORRECT?

**(GATE – 15 – ME – Set 1)**

- (a) Absolute value remains unchanged but sign will change.
- (b) Both absolute value and sign will change.
- (c) Absolute value will change but sign will not change.
- (d) Both absolute value and sign will remain unchanged.

**Use the code : BVREDDY, to get the maximum discount**

184. At least one eigenvalue of a singular matrix is (GATE – 15 – ME – Set 2)



**Use the code : BVREDDY, to get the maximum discount**

185. The lowest eigen value of the  $2 \times 2$  matrix

$$\begin{bmatrix} 4 & 2 \\ 1 & 3 \end{bmatrix}$$
 is \_\_\_\_\_. (GATE - 15 - ME - Set 3)

Use the code : BVREDDY, to get the maximum discount

186. For a given matrix  $P = \begin{bmatrix} 4+3i & -i \\ i & 4-3i \end{bmatrix}$ ,

where  $i = \sqrt{-1}$ , the inverse of matrix P is

(GATE – 15 – ME – Set 3)

(a)  $\frac{1}{24} \begin{bmatrix} 4-3i & i \\ -i & 4+3i \end{bmatrix}$

(b)  $\frac{1}{25} \begin{bmatrix} i & 4-3i \\ 4+3i & -i \end{bmatrix}$

(c)  $\frac{1}{24} \begin{bmatrix} 4+3i & -i \\ i & 4-3i \end{bmatrix}$

(d)  $\frac{1}{25} \begin{bmatrix} 4+3i & -i \\ i & 4-3i \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

187. Consider the following  $2 \times 2$  matrix A where two elements are unknown and are marked by a and b. The eigenvalues of this matrix are -1 and 7. What are the values of a and b?

$$A = \begin{pmatrix} 1 & 4 \\ b & a \end{pmatrix} \quad (\text{GATE} - 15 - \text{CS} - \text{Set 1})$$

- (a) a = 6, b = 4
- (b) a = 4, b = 6
- (c) a = 3, b = 5
- (d) a = 5, b = 3

Use the code : BVREDDY, to get the maximum discount

188. The larger of the two eigenvalues of the matrix  $\begin{bmatrix} 4 & 5 \\ 2 & 1 \end{bmatrix}$  is \_\_\_\_\_.

(GATE – 15 – CS – Set 2)

Use the code : BVREDDY, to get the maximum discount

**189.** Perform the following operations on the

matrix 
$$\begin{bmatrix} 3 & 4 & 45 \\ 7 & 9 & 105 \\ 13 & 2 & 195 \end{bmatrix}$$

- (i) Add the third row to the second row
- (ii) Subtract the third column from the first column.

The determinant of the resultant matrix  
is \_\_\_\_\_. **(GATE – 15 – CS – Set 2)**

Use the code : BVREDDY, to get the maximum discount

190. In the given matrix  $\begin{bmatrix} 1 & -1 & 2 \\ 0 & 1 & 0 \\ 1 & 2 & 1 \end{bmatrix}$ , one of the eigen values is 1. The eigen vectors corresponding to the eigen value 1 are

(GATE – 15 – CS – Set 3)

- (a)  $\{\alpha(4, 2, 1) | \alpha \neq 0, \alpha \in \mathbb{R}\}$
- (b)  $\{\alpha(-4, 2, 1) | \alpha \neq 0, \alpha \in \mathbb{R}\}$
- (c)  $\{\alpha(\sqrt{2}, 0, 1) | \alpha \neq 0, \alpha \in \mathbb{R}\}$
- (d)  $\{\alpha(-\sqrt{2}, 0, 1) | \alpha \neq 0, \alpha \in \mathbb{R}\}$

Use the code : BVREDDY, to get the maximum discount

**191.** In matrix equation  $[A]\{X\} = \{R\}$ .

$$[A] = \begin{bmatrix} 4 & 8 & 4 \\ 8 & 16 & -4 \\ 4 & -4 & 15 \end{bmatrix}, \{X\} = \begin{Bmatrix} 2 \\ 1 \\ 4 \end{Bmatrix} \text{ and } \{R\} = \begin{Bmatrix} 32 \\ 16 \\ 64 \end{Bmatrix}$$

One of the eigen values of matrix [A] is

- |        |        |       |       |                     |
|--------|--------|-------|-------|---------------------|
| (a) 16 | (b) 15 | (c) 4 | (d) 8 | <b>(GATE-19-ME)</b> |
|--------|--------|-------|-------|---------------------|

**Use the code : BVREDDY, to get the maximum discount**

192. Let  $A = \begin{bmatrix} 1 & 0 & 1 \\ -1 & 2 & 0 \\ 0 & 0 & -2 \end{bmatrix}$  and  $B = A^3 - A^2 - 4A + 5I$ , where I is the  $3 \times 3$  identity matrix.  
The determinant of B is \_\_\_\_\_ (up to 1 decimal place)

(GATE-18-EC)

Use the code : BVREDDY, to get the maximum discount

193. Consider a matrix P whose only eigenvectors are the multiples of  $\begin{bmatrix} 1 \\ 4 \end{bmatrix}$

Consider the following statements.

- (I) P does not have an inverse
- (II) P has a repeated eigenvalue
- (III) P cannot be diagonalized

Which one of the following options is correct?

- (a) Only I and III are necessarily true
- (b) Only II is necessarily true
- (c) Only I and II are necessarily true
- (d) Only II and III are necessarily true

**(GATE-18-CSIT)**

Use the code : BVREDDY, to get the maximum discount

**194.** Let  $A$  be  $n \times n$  real valued square symmetric matrix of rank 2 with  $\sum_{i=1}^n \sum_{j=1}^n A_{ij}^2 = 50$ .

Consider the following statements.

- (I) One eigenvalue must be in  $[-5, 5]$
- (II) The eigenvalue with the largest magnitude must be strictly greater than 5

Which of the above statements about eigenvalues of  $A$  is/are necessarily *correct*?

**(GATE-17-CSIT)**

- (a) Both (I) and (II)
- (b) (I) only
- (c) (II) only
- (d) Neither (I) nor (II)

**Use the code : BVREDDY, to get the maximum discount**

195. The matrix  $A = \begin{bmatrix} \frac{3}{2} & 0 & \frac{1}{2} \\ 0 & -1 & 0 \\ \frac{1}{2} & 0 & \frac{3}{2} \end{bmatrix}$  has three distinct eigen values and one of its eigen vectors is  $\begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$ . Which one of the following can be another eigen vector of A?

(GATE-17-EE)

(a)  $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$

(b)  $\begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}$

(c)  $\begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix}$

(d)  $\begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

**196.** If the entries in each column of a square matrix M add up to 1, then an eigen value of M is

- (a) 4
- (b) 3
- (c) 2
- (d) 1

**(GATE-16-CE)**

Use the code : BVREDDY, to get the maximum discount

197. Among the following, the pair of vectors orthogonal to each other is

(GATE – 95[ME])

- (a) [3, 4, 7], [3, 4, 7]
- (b) [1, 0, 0], [1, 1, 0]
- (c) [1, 0, 2], [0, 5, 0]
- (d) [1, 1, 1], [-1, -1, -1]

Use the code : BVREDDY, to get the maximum discount

198. Let  $M^4 = I$  (where  $I$  denotes the identity matrix) and  $M \neq I$ ,  $M^2 \neq I$  and  $M^3 \neq I$ . Then, for any natural number  $k$ ,  $M^{-1}$  equals:

(GATE – 16 – EC – Set 1)

- (a)  $M^{4k+1}$
- (b)  $M^{4k+2}$
- (c)  $M^{4k+3}$
- (d)  $M^{4k}$

Use the code : BVREDDY, to get the maximum discount

199. Let  $A_{n \times n}$  be matrix of order  $n$  and  $I_{12}$  be the matrix obtained by interchanging the first and second rows of  $I_n$ . Then  $A I_{12}$  is such that its first. **(GATE – 97[CS])**

- (a) row is the same as its second row
- (b) row is the same as second row of  $A$
- (c) column is the same as the second column of  $A$
- (d) row is a zero row.

Use the code : BVREDDY, to get the maximum discount

200. If the vector  $\begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix}$  is an eigen vector of

$$A = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{bmatrix}$$
 then one of the eigen

value of A is **(GATE – 98[EE])**

- (a) 1
- (b) 2
- (c) 5
- (d) -1

Use the code : BVREDDY, to get the maximum discount

201. If  $A = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & -1 & 0 & -1 \\ 0 & 0 & i & i \\ 0 & 0 & 0 & -i \end{bmatrix}$  the matrix  $A^4$ ,  
calculated by the use of Cayley – Hamilton  
theorem **(GATE – 93)**

Use the code : BVREDDY, to get the maximum discount

202. A  $5 \times 7$  matrix has all its entries equal to 1.

Then the rank of a matrix is

(GATE – 94[EE])

- (a) 7
- (b) 5
- (c) 1
- (d) Zero

Use the code : BVREDDY, to get the maximum discount

203. The rank of  $(m \times n)$  matrix ( $m < n$ ) cannot be more than

**(GATE - 94[EC])**

- (a) m
- (b) n
- (c)  $mn$
- (d) None

Use the code : BVREDDY, to get the maximum discount

**204.** The rank of the matrix  $\begin{bmatrix} 0 & 0 & -3 \\ 9 & 3 & 5 \\ 3 & 1 & 1 \end{bmatrix}$  is

(GATE – 94[CS])

- (a) 0
- (b) 1
- (c) 2
- (d) 3

Use the code : BVREDDY, to get the maximum discount

**205.** If for a matrix, rank equals both the number of rows and number of columns, then the matrix is called

(GATE – 94[PI])

- (a) Non-singular
- (b) singular
- (c) transpose
- (d) minor

Use the code : BVREDDY, to get the maximum discount

206. Rank of the matrix  $\begin{bmatrix} 0 & 2 & 2 \\ 7 & 4 & 8 \\ -7 & 0 & -4 \end{bmatrix}$  is 3

(GATE - 94[ME])

- (a) True
- (b) False

Use the code : BVREDDY, to get the maximum discount

207. The rank of the following  $(n+1) \times (n+1)$  matrix, where 'a' is a real number is

$$\begin{bmatrix} 1 & a & a^2 & \dots & \dots & a^n \\ 1 & a & a^2 & \dots & \dots & a^n \\ \vdots & & & & & \\ \vdots & & & & & \\ 1 & a & a^2 & \dots & \dots & a^n \end{bmatrix}$$

(GATE - 95[EE])

- (a) 1      (b) 2
- (c) n      (d) depends on the value of a

Use the code : BVREDDY, to get the maximum discount

208. The rank of the matrix

$$\begin{bmatrix} 1 & 4 & 8 & 7 \\ 0 & 0 & 3 & 0 \\ 4 & 2 & 3 & 1 \\ 3 & 12 & 24 & 2 \end{bmatrix}$$

is

(GATE - 98[CS])

- (a) 3
- (b) 1
- (c) 2
- (d) 4

Use the code : BVREDDY, to get the maximum discount

**209.** Consider the following two statements.

**(GATE-2000[CE])**

- (I) The maximum number of linearly independent column vectors of a matrix  $A$  is called the rank of  $A$ .
  - (II) If  $A$  is  $n \times n$  square matrix then it will be non-singular if rank of  $A = n$
- (a) Both the statements are false
  - (b) Both the statements are true
  - (c) (I) is true but (II) is false
  - (d) (I) is false but (II) is true

**Use the code : BVREDDY, to get the maximum discount**

210. The rank of matrix  $A = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 4 & 5 \\ 4 & 6 & 8 \end{bmatrix}$  is

(GATE–2000[IN])

- (a) 0
- (b) 1
- (c) 2
- (d) 3

Use the code : BVREDDY, to get the maximum discount

211. The rank of the matrix  $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$  is

(GATE – 02[CS])

- (a) 4
- (b) 2
- (c) 1
- (d) 0

Use the code : BVREDDY, to get the maximum discount

212. Given matrix  $[A] = \begin{bmatrix} 4 & 2 & 1 & 3 \\ 6 & 3 & 4 & 7 \\ 2 & 1 & 0 & 1 \end{bmatrix}$ , the rank

of the matrix is **(GATE – 03[CE])**



Use the code : BVREDDY, to get the maximum discount

213. Let  $A = [a_{ij}]$ ,  $1 \leq i, j \leq n$  with  $n \geq 3$  and  $a_{ij} = i \cdot j$ . Then the rank of A is

(GATE-07[IN])

- (a) 0
- (b) 1
- (c)  $n - 1$
- (d) n

Use the code : BVREDDY, to get the maximum discount

$$214. \quad A = \begin{bmatrix} p & q \\ r & s \end{bmatrix}; \quad B = \begin{bmatrix} p^2 + q^2 & pr + qs \\ pr + qs & r^2 + s^2 \end{bmatrix}$$

If the rank of matrix A is N, then the rank of matrix B is

(GATE-14-EE-SET3)

- (a)  $N/2$
- (b)  $N - 1$
- (c)  $N$
- (d)  $2N$

Use the code : BVREDDY, to get the maximum discount

215. The following system of equations

$$x_1 + x_2 + x_3 = 3$$

$$x_1 - x_3 = 0$$

$$x_1 - x_2 + x_3 = 1 \text{ has}$$

(GATE – 94[EC])

- (a) Unique solution
- (b) No solution
- (c) Infinite number of solutions
- (d) Only one solution

Use the code : BVREDDY, to get the maximum discount

216. Let  $AX = B$  be a system of linear equations where  $A$  is an  $m \times n$  matrix  $B$  is an  $n \times 1$  column matrix which of the following is false?

(GATE - 96[CS])

- (a) The system has a solution,  
if  $\rho(A) = \rho(A/B)$
- (b) If  $m = n$  and  $B$  is a non - zero vector  
then the system has a unique solution.
- (c) If  $m < n$  and  $B$  is a zero vector then the  
system has infinitely many solutions.
- (d) The system will have a trivial solution  
when  $m = n$ ,  $B$  is the zero vector and  
rank of  $A$  is  $n$ .

Use the code : BVREDDY, to get the maximum discount

**217.** In the Gauss – elimination for a solving system of linear algebraic equations, triangularization leads to

**(GATE – 96[ME])**

- (a) diagonal matrix
- (b) lower triangular matrix
- (c) upper triangular matrix
- (d) singular matrix

**Use the code : BVREDDY, to get the maximum discount**

218. For the following set of simultaneous equations **(GATE - 97[ME])**

$$1.5x - 0.5y + z = 2$$

$$4x + 2y + 3z = 9$$

$$7x + y + 5z = 10$$

- (a) the solution is unique
- (b) infinitely many solutions exist
- (c) the equations are incompatible
- (d) finite many solutions exist

Use the code : BVREDDY, to get the maximum discount

219. Consider the following set of equations

$$x + 2y = 5,$$

$$4x + 8y = 12,$$

$3x + 6y + 3z = 15$ . This set

(GATE ~ 98[CS])

- (a) has unique solution
- (b) has no solution
- (c) has infinite number of solutions
- (d) has 3 solutions

Use the code : BVREDDY, to get the maximum discount

220. Consider the following system of linear equations **(GATE – 03[CS])**

$$\begin{bmatrix} 2 & 1 & -4 \\ 4 & 3 & -12 \\ 1 & 2 & -8 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} \alpha \\ 5 \\ 7 \end{bmatrix}$$

Notice that the 2<sup>nd</sup> and 3<sup>rd</sup> columns of the coefficient matrix are linearly dependent.

For how many value of  $\alpha$ , does systems of equations have infinitely many solutions.



Use the code : BVREDDY, to get the maximum discount

221. A system of equations represented by  $AX = 0$  where X is a column vector of unknown and A is a square matrix containing coefficients has a non-trivial solution when A is.

(GATE – 03)

- (a) non-singular
- (b) singular
- (c) symmetric
- (d) Hermitian

Use the code : BVREDDY, to get the maximum discount

**222.** What values of x, y, z satisfy the following system of linear equations

$$\begin{bmatrix} 1 & 2 & 3 \\ 1 & 3 & 4 \\ 2 & 2 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 6 \\ 8 \\ 12 \end{bmatrix}$$

**(GATE – 04)**

- (a) x = 6, y = 3, z = 2
- (b) x = 12, y = 3, z = -4
- (c) x = 6, y = 6, z = -4
- (d) x = 12, y = -3, z = 4

**Use the code : BVREDDY, to get the maximum discount**

223. How many solutions does the following system of linear equations have

$$-x + 5y = -1$$

$$x - y = 2$$

$$x + 3y = 3$$

**(GATE-04[CS])**

- (a) infinitely many
- (b) two distinct solutions
- (c) unique
- (d) none

Use the code : BVREDDY, to get the maximum discount

224. Consider the following system of equations  
in three real variable  $x_1$ ,  $x_2$  and  $x_3$ :

$$2x_1 - x_2 + 3x_3 = 1$$

$$3x_1 + 2x_2 + 5x_3 = 2$$

$$-x_1 + 4x_2 + x_3 = 3$$

This system of equations has

(GATE-05[CE])

- (a) no solution
- (b) a unique solution
- (c) more than one but a finite number of solutions.
- (d) an infinite number of solutions.

Use the code : BVREDDY, to get the maximum discount

**225.** Consider the system of equations,

$$A_{n \times n} X_{n \times 1} = \lambda X_{n \times 1} \text{ where } \lambda \text{ is a scalar.}$$

Let  $(\lambda_i, X_i)$  be an eigen value and its corresponding eigen vector for real matrix

A. Let  $I_{n \times n}$  be unit matrix. Which one of the following statement is not correct?

**(GATE-05[CE])**

- (a) For a homogeneous  $n \times n$  system of linear equations  $(A - \lambda I)X = 0$ , having a non trivial solution, the rank of  $(A - \lambda I)$  is less than n.
- (b) For matrix  $A^m$ , m being a positive integer,  $(\lambda_i^m, X_i^m)$  will be eigen pair for all i.
- (c) If  $A^T = A^{-1}$  then  $|\lambda_i| = 1$  for all i.
- (d) If  $A^T = A$  then  $\lambda_i$  are real for all i.

**Use the code : BVREDDY, to get the maximum discount**

226. The number of linearly independent solutions of the system of equations

$$\begin{bmatrix} 1 & 0 & 2 \\ 1 & -1 & 0 \\ 2 & -2 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = 0 \text{ is equal to}$$

(GATE – 94[EE])

- (a) 1
- (b) 2
- (c) 3
- (d) 0

Use the code : BVREDDY, to get the maximum discount

227. In the matrix equation  $PX = Q$  which of the following is a necessary condition for the existence of atleast one solution for the unknown vector  $X$ .

(GATE-05[EE])

- (a) Augmented matrix  $[P|Q]$  must have the same rank as matrix P.
- (b) vector Q must have only non-zero elements.
- (c) matrix P must be singular
- (d) matrix P must be square

Use the code : BVREDDY, to get the maximum discount

228. A is a  $3 \times 4$  matrix and  $AX = B$  is an inconsistent system of equations. The highest possible rank of A is

(GATE-05[ME])

- (a) 1      (b) 2      (c) 3      (d) 4

Use the code : BVREDDY, to get the maximum discount

229. Let A be  $3 \times 3$  matrix with rank 2.

Then  $AX = 0$  has

(GATE - 05[IN])

- (a) only the trivial solution  $X = 0$
- (b) one independent solution
- (c) two independent solutions
- (d) three independent solutions

Use the code : BVREDDY, to get the maximum discount

230. A system of linear simultaneous equations is given as  $Ax = b$

where  $A = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$  &  $b = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$

Then the rank of matrix A is

(GATE-06[IN])

- (a) 1
- (b) 2
- (c) 3
- (d) 4

Use the code : BVREDDY, to get the maximum discount

231. A system of linear simultaneous equations is given as  $Ax = b$

Where  $A = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$  and  $b = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$

Which of the following statement is true?

(GATE-06[IN])

- (a)  $x$  is a null vector
- (b)  $x$  is unique
- (c)  $x$  does not exist
- (d)  $x$  has infinitely many values

Use the code : BVREDDY, to get the maximum discount

232. Solution for the system defined by the set of equations  $4y + 3z = 8$ ,  $2x - z = 2$  &  $3x + 2y = 5$  is  
**(GATE-06[CE])**

- (a)  $x = 0, y = 1, z = 4/5$
- (b)  $x = 0, y = 1/2, z = 2$
- (c)  $x = 1, y = 1/2, z = 2$
- (d) non existent

Use the code : BVREDDY, to get the maximum discount

233. Let  $A$  be an  $n \times n$  real matrix such that  $A^2 = I$  and  $\mathbf{Y}$  be an  $n$ -dimensional vector. Then the linear system of equations  $Ax = \mathbf{Y}$  has

(GATE-07[IN])

- (a) no solution
- (b) unique solution
- (c) more than one but infinitely many dependent solutions.
- (d) infinitely many dependent solutions

Use the code : BVREDDY, to get the maximum discount

234. For what values of  $\alpha$  and  $\beta$  the following simultaneous equations have an infinite number of solutions

$$x + y + z = 5,$$

$$x + 3y + 3z = 9,$$

$$x + 2y + \alpha z = \beta$$

(GATE-07[CE])

- (a) 2, 7
- (c) 8, 3

- (b) 3, 8
- (d) 7, 2

Use the code : BVREDDY, to get the maximum discount

235. The number of linearly independent eigen

vectors of  $\begin{bmatrix} 2 & 1 \\ 0 & 2 \end{bmatrix}$  is

(GATE-07[ME])

- (a) 0
- (b) 1
- (c) 2
- (d) infinite

Use the code : BVREDDY, to get the maximum discount

236. If A is square symmetric real valued matrix of dimension  $2n$ , then the eigen values of A are

(GATE – 07[PI])

- (a)  $2n$  distinct real values
- (b)  $2n$  real values not necessarily distinct
- (c)  $n$  distinct pairs of complex conjugate numbers
- (d)  $n$  pairs of complex conjugate numbers, not necessarily distinct

Use the code : BVREDDY, to get the maximum discount

237.  $q_1, q_2, q_3, \dots, q_m$  are n-dimensional vectors with  $m < n$ . This set of vectors is linearly dependent. Q is the matrix with  $q_1, q_2, q_3, \dots, q_m$  as the columns. The rank of Q is

(GATE-07[EE])

- (a) less than m
- (b) m
- (c) between m and n
- (d) n

Use the code : BVREDDY, to get the maximum discount

238.  $X = [x_1 \ x_2 \ \dots \ x_n]^T$  is an n-tuple non-zero vector. The  $n \times n$  matrix  $V = XX^T$   
**(GATE-07[CE])**

- (a) has rank zero
- (b) has rank 1
- (c) is orthogonal
- (d) has rank n

Use the code : BVREDDY, to get the maximum discount

239. Let  $x$  and  $y$  be two vectors in a 3-dimensional space and  $\langle x, y \rangle$  denote their dot product. Then the determinant  $\det$

$$\begin{bmatrix} \langle x, x \rangle & \langle x, y \rangle \\ \langle y, x \rangle & \langle y, y \rangle \end{bmatrix} = \text{_____}.$$

(GATE-07[EE])

- (a) is zero when  $x$  and  $y$  are linearly independent
- (b) is positive when  $x$  and  $y$  are linearly independent
- (c) is non-zero for all non-zero  $x$  and  $y$
- (d) is zero only when either  $x$  (or)  $y$  is zero

Use the code : BVREDDY, to get the maximum discount

240. If the rank of a  $5 \times 6$  matrix  $Q$  is 4 then which one of the following statements is correct?

(GATE-08[EE])

- (a)  $Q$  will have four linearly independent rows and four linearly independent columns
- (b)  $Q$  will have four linearly independent rows and five linearly independent columns
- (c)  $Q Q^T$  will be invertible.
- (d)  $Q^T Q$  will be invertible.

Use the code : BVREDDY, to get the maximum discount

241. A is  $m \times n$  full rank matrix with  $m > n$  and I is an identity matrix.

Let matrix  $A^+ = (A^T A)^{-1} A^T$ . Then which one of the following statement is false?

(GATE-08[EE])

- (a)  $AA^+A = A$
- (b)  $(AA^+)^2 = AA^+$
- (c)  $A^+A = I$
- (d)  $AA^+A = A^+$

Use the code : BVREDDY, to get the maximum discount

**242. The system of linear equations**

$$\left. \begin{array}{l} 4x + 2y = 7 \\ 2x + y = 6 \end{array} \right\} \text{has } \quad (\text{GATE-08[EC]})$$

- (a) a unique solution
- (b) no solution
- (c) an infinite no. of solutions
- (d) exactly two distinct solution.

**Use the code : BVREDDY, to get the maximum discount**

243. For what values of 'a' if any will the following system of equations in x, y and z have a solution?

$$2x + 3y = 4,$$

$$x + y + z = 4,$$

$$x + 2y - z = a \quad (\text{GATE-08[ME]})$$

- (a) any real number
- (b) 0
- (c) 1
- (d) there is no such value

Use the code : BVREDDY, to get the maximum discount

244. The following system of equations

$$x_1 + x_2 + 2x_3 = 1, \quad x_1 + 2x_2 + 3x_3 = 2,$$

$$x_1 + 4x_2 + \alpha x_3 = 4 \text{ has a unique solution.}$$

The only possible value(s) for  $\alpha$  is/are

(GATE-08[CS])

- (a) 0
- (b) either 0 (or) 1
- (c) one of 0, 1 (or) -1
- (d) any real value expect 5

Use the code : BVREDDY, to get the maximum discount

**245.** The following system of equations

$$x + y + z = 3,$$

$$x + 2y + 3z = 4,$$

$$x + 4y + kz = 6$$

will not have a unique solution for  $k$  equal

to (GATE-08[CE])



Use the code : BVREDDY, to get the maximum discount

246. The value of  $x_3$  obtained by solving the following system of linear equations is

$$x_1 + 2x_2 - 2x_3 = 4$$

$$2x_1 + x_2 + x_3 = -2$$

$$-x_1 + x_2 - x_3 = 2$$

(GATE-09[PI])

- (a) -12      (b) -2      (c) 0      (d) 12

Use the code : BVREDDY, to get the maximum discount

247. For the set of equations

$$x_1 + 2x_2 + x_3 + 4x_4 = 2,$$

$$3x_1 + 6x_2 + 3x_3 + 12x_4 = 6.$$

The following statement is true

(GATE-10[EE])

- (a) only the trivial solution

$x_1 = x_2 = x_3 = x_4 = 0$  exist

- (b) there are no solutions

- (c) a unique non-trivial solution exist

- (d) multiple non-trivial solution exist

Use the code : BVREDDY, to get the maximum discount

248. The value of q for which the following set of linear equations  $2x + 3y = 0$ ,  $6x + qy = 0$  can have non-trivial solution is

(GATE-10[PI])

- (a) 2
- (b) 7
- (c) 9
- (d) 11

Use the code : BVREDDY, to get the maximum discount

249. The system of equations  $x + y + z = 6$ ,  
 $x + 4y + 6z = 20$ ,  $x + 4y + \lambda z = \mu$  has no  
solution for values of  $\lambda$  and  $\mu$  given by

(GATE-11[EC])

- |                                |                                   |
|--------------------------------|-----------------------------------|
| (a) $\lambda = 6, \mu = 20$    | (b) $\lambda = 6, \mu \neq 20$    |
| (c) $\lambda \neq 6, \mu = 20$ | (d) $\lambda \neq 6, \mu \neq 20$ |

Use the code : BVREDDY, to get the maximum discount

250. Consider the following system of equations

$$2x_1 + x_2 + x_3 = 0, \quad x_2 - x_3 = 0 \text{ and } x_1 + x_2 = 0.$$

This system has **(GATE-11[ME])**

- (a) a unique solution
- (b) no solution
- (c) infinite number of solutions
- (d) five solutions

Use the code : BVREDDY, to get the maximum discount

251.  $x + 2y + z = 4$ ,  $2x + y + 2z = 5$ ,  $x - y + z = 1$

The system of algebraic equations given above has

(GATE-12[ME, PI])

- (a) a unique solution of  $x=1$ ,  $y=1$  and  $z=1$
- (b) only the two solutions of  $x=1$ ,  $y=1$ ,  $z=1$   
and  $x=2$ ,  $y=1$ ,  $z=0$
- (c) infinite number of solutions.
- (d) no feasible solution.

Use the code : BVREDDY, to get the maximum discount

252. The equation

$$\begin{bmatrix} 2 & -2 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \text{ has}$$

(GATE – 13[EE])

- (a) no solution
- (b) only one solution
- (c) non-zero unique solution
- (d) multiple solutions

Use the code : BVREDDY, to get the maximum discount

253. Choose the CORRECT set of functions, which are linearly dependent.

(GATE – 2013[ME])

- (a)  $\sin x$ ,  $\sin^2 x$  and  $\cos^2 x$
- (b)  $\cos x$ ,  $\sin x$  and  $\tan x$
- (c)  $\cos 2x$ ,  $\sin^2 x$  and  $\cos^2 x$
- (d)  $\cos 2x$ ,  $\sin x$  and  $\cos x$

Use the code : BVREDDY, to get the maximum discount

**254.** The system of linear equations

$$\begin{pmatrix} 2 & 1 & 3 \\ 3 & 0 & 1 \\ 1 & 2 & 5 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} 5 \\ -4 \\ 14 \end{pmatrix} \text{ has}$$

**(GATE-14-EC-SET2)**

- (a) a unique solution
- (b) infinitely many solutions
- (c) no solution
- (d) exactly two solutions

**Use the code : BVREDDY, to get the maximum discount**

255. Which one of the following statements is NOT true for a square matrix A?

(GATE-14-EC-SET3)

- (a) If A is upper triangular, the eigen values of A are the diagonal elements of it
- (b) If A is real symmetric, the eigen values of A are always real and positive
- (c) If A is real, the eigen values of A and  $A^T$  are always the same
- (d) If all the principal minors of A are positive, all the eigen values of A are also positive

Use the code : BVREDDY, to get the maximum discount

**256. Given a system of equations**

$$x + 2y + 2z = b_1$$

$$5x + y + 3z = b_2$$

**Which of the following is true its solutions**

**(GATE-14-EE-SET1)**

- (a) The system has a unique solution for any given  $b_1$  and  $b_2$
- (b) The system will have infinitely many solutions for any given  $b_1$  and  $b_2$
- (c) Whether or not a solution exists depends on the given  $b_1$  and  $b_2$
- (d) The system would have no solution for any values of  $b_1$  and  $b_2$

**Use the code : BVREDDY, to get the maximum discount**

257.Which one of the following describes the relationship among the three vectors,  
 $\hat{i} + \hat{j} + \hat{k}$ ,  $2\hat{i} + 3\hat{j} + \hat{k}$  and  $5\hat{i} + 6\hat{j} + 4\hat{k}$ ?

(GATE-14-ME-SET1)

- (a) The vectors are mutually perpendicular
- (b) The vectors are linearly dependent
- (c) The vectors are linearly independent
- (d) The vectors are unit vectors

Use the code : BVREDDY, to get the maximum discount

258. The rank of the matrix  $\begin{bmatrix} 6 & 0 & 4 & 4 \\ -2 & 14 & 8 & 18 \\ 14 & -14 & 0 & -10 \end{bmatrix}$  is  
**(GATE-14-CE-SET2)**

Use the code : BVREDDY, to get the maximum discount

259. The system of equations, given below, has

$$x + 2y + 4z = 2$$

$$4x + 3y + z = 5$$

$$3x + 2y + 3z = 1$$

(GATE-14-PI-SET1)

- (a) a unique solution
- (b) Two solution
- (c) no solution
- (d) more than two solutions

Use the code : BVREDDY, to get the maximum discount

**260.** Consider the following system of equations:

$$3x + 2y = 1$$

$$4x + 7z = 1$$

$$x + y + z = 3$$

$$x - 2y + 7z = 0$$

The number of solutions for this system is

**(GATE-14-CS-SET1)**

Use the code : BVREDDY, to get the maximum discount

**261.** Consider the system of linear equations:

$$x - 2y + 3z = -1$$

$$x - 3y + 4z = 1 \text{ and}$$

$$-2x + 4y - 6z = k,$$

The value of 'k' for which the system has infinitely many solutions is \_\_\_\_\_.

**(GATE-15-EC-SET1)**

Use the code : BVREDDY, to get the maximum discount

262. The maximum value of 'a' such that the

matrix  $\begin{bmatrix} -3 & 0 & -2 \\ 1 & -1 & 0 \\ 0 & a & -2 \end{bmatrix}$  has three linearly

independent real eigenvectors is

(GATE 15-EE-SET1)

(a)  $\frac{2}{3\sqrt{3}}$

(b)  $\frac{1}{3\sqrt{3}}$

(c)  $\frac{1+2\sqrt{3}}{3\sqrt{3}}$

(d)  $\frac{1+\sqrt{3}}{3\sqrt{3}}$

Use the code : BVREDDY, to get the maximum discount

**263.** We have a set of 3 linear equations in 3 unknowns. ' $X \equiv Y$ ' means X and Y are equivalent statements and ' $X \not\equiv Y$ ' means X and Y are not equivalent statements.

**P:** There is a unique solution.

**Q:** The equations are linearly independent.

**R:** All eigen values of the coefficient matrix are non zero.

**S:** The determinant of the coefficient matrix is nonzero.

Which one of the following is TRUE?

**(GATE-15-EE-SET2)**

- (a)  $P \equiv Q \equiv R \equiv S$
- (b)  $P \equiv R \not\equiv Q \equiv S$
- (c)  $P \equiv Q \not\equiv R \equiv S$
- (d)  $P \not\equiv Q \not\equiv R \not\equiv S$

Use the code : BVREDDY, to get the maximum discount

264. Let  $A$  be an  $n \times n$  matrix with rank  $r$  ( $0 < r < n$ ). Then  $AX = 0$  has  $p$  independent solutions, where  $p$  is

(GATE - 15 - IN)

- (a)  $r$
- (b)  $n$
- (c)  $n - r$
- (d)  $n + r$

Use the code : BVREDDY, to get the maximum discount

265. For what value of 'p' the following set of equations will have no solution?

$$2x + 3y = 5$$

$$3x + py = 10 \quad (\text{GATE - 15 - CE - Set 1})$$

Use the code : BVREDDY, to get the maximum discount

266. Let  $A = [a_{ij}]$ ,  $1 \leq i, j \leq n$  with  $n \geq 3$  and  $a_{ij} = i \cdot j$ .

The rank of A is :

(GATE – 15 – CE – Set 2)



**Use the code : BVREDDY, to get the maximum discount**

**267.** If the following system has non – trivial solution

$$px + qy + rz = 0$$

$$qx + ry + pz = 0$$

$$rx + py + qz = 0$$

Then which one of the following Options is  
**TRUE?**                   **(GATE – 15 – CS – Set 3)**

- (a)  $p - q + r = 0$  or  $p = q = -r$
- (b)  $p + q - r = 0$  or  $p = -q = r$
- (c)  $p + q + r = 0$  or  $p = q = r$
- (d)  $p - q + r = 0$  or  $p = -q = -r$

Use the code : BVREDDY, to get the maximum discount

**268.** Let the eigen values of a  $2 \times 2$  matrix A be 1, -2 with eigen vectors  $x_1$  and  $x_2$  respectively. Then the eigen values and eigen vectors of the matrix  $A^2 - 3A + 4I$  would respectively, be

- (a) 2, 14;  $x_1, x_2$
- (c) 2, 0;  $x_1, x_2$

- (b) 2, 14;  $x_1, x_2$ ;  $x_1 - x_2$
- (d) 2, 0;  $x_1 + x_2, x_1 - x_2$

**(GATE-16-EE)**

Use the code : BVREDDY, to get the maximum discount

**269.** Let  $A$  be a  $4 \times 3$  real matrix which rank 2. Which one of the following statement is **TRUE**?

- (a) Rank of  $A^T$  is less than 2
- (b) Rank of  $A^T A$  is equal to 2
- (c) Rank of  $A^T A$  is greater than 2
- (d) Rank of  $A^T A$  can be any number between 1 and 3

**(GATE-16-EE)**

Use the code : BVREDDY, to get the maximum discount

**270.** The solution to the system of equations is

$$\begin{bmatrix} 2 & 5 \\ -4 & 3 \end{bmatrix} \begin{Bmatrix} x \\ y \end{Bmatrix} = \begin{Bmatrix} 2 \\ -30 \end{Bmatrix}$$

- (a) 6, 2  
(c) -6, -2

- (b) -6, 2  
(d) 6, -2

**(GATE-16-ME)**

Use the code : BVREDDY, to get the maximum discount

271. The number of linear independent eigenvectors of matrix  $A = \begin{bmatrix} 2 & 1 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$  is \_\_\_\_\_.

(GATE-16-ME)

Use the code : BVREDDY, to get the maximum discount

**272.** The number of solutions of the simultaneous algebraic equations  $y = 3x + 3$  and  $y = 3x + 5$  is

- (a) zero
- (b) 1
- (c) 2
- (d) infinite

**(GATE-16-PI)**

Use the code : BVREDDY, to get the maximum discount

**273.** Consider the following linear system

$$x + 2y - 3z = a$$

$$2x + 3y + 3z = b$$

$$5x + 9y - 6z = c$$

This system is consistent if a, b, c satisfies the equation

**(GATE-16-CE)**

- (a)  $7a - b - c = 0$   
(c)  $3a - b + c = 0$

- (b)  $3a + b - c = 0$   
(d)  $7a - b + c = 0$

**Use the code : BVREDDY, to get the maximum discount**

**274.** Consider the systems, each consisting of  $m$  linear equations in  $n$  variables.

- I.** If  $m < n$ , then all such systems have a solution
- II.** If  $m > n$ , then none of these systems has a solution
- III.** If  $m = n$ , then there exists a system which has a solution

Which one of the following is **CORRECT**?

- (a) **I, II and III** are true
- (b) Only **II and III** are true
- (c) Only **III** is true
- (d) None of them is true

**(GATE-16-CSE)**

**Use the code : BVREDDY, to get the maximum discount**

**275.** If  $V$  is a non-zero vector of dimension  $3 \times 1$ , then the matrix  $A = VV^T$  has a rank = \_\_\_\_\_  
**(GATE-17-IN)**

Use the code : BVREDDY, to get the maximum discount

**276.** The rank of the matrix  $\begin{bmatrix} 1 & -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & -1 & 0 \\ 0 & 1 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & -1 \end{bmatrix}$  is \_\_\_\_\_

**(GATE-17-EC)**

Use the code : BVREDDY, to get the maximum discount

277. The rank of the matrix  $M = \begin{bmatrix} 5 & 10 & 10 \\ 1 & 0 & 2 \\ 3 & 6 & 6 \end{bmatrix}$  is

- (a) 0
- (b) 1
- (c) 2
- (d) 3

**(GATE-17-EC)**

Use the code : BVREDDY, to get the maximum discount

**278.** Consider the following simultaneous equations (with  $c_1$  and  $c_2$  being constants):

$$3x_1 + 2x_2 = c_1$$

$$4x_1 + x_2 = c_2$$

The characteristic equation for these simultaneous equations is

**(GATE-17-CE)**

(a)  $\lambda^2 - 4\lambda - 5 = 0$

(c)  $\lambda^2 + 4\lambda - 5 = 0$

(b)  $\lambda^2 - 4\lambda + 5 = 0$

(d)  $\lambda^2 + 4\lambda + 5 = 0$

Use the code : BVREDDY, to get the maximum discount

279. The rank of the following matrix is

$$\begin{bmatrix} 1 & 1 & 0 & -2 \\ 2 & 0 & 2 & 2 \\ 4 & 1 & 3 & 1 \end{bmatrix}$$

- (a) 1
- (b) 2
- (c) 3
- (d) 4

Use the code : BVREDDY, to get the maximum discount

**280.** Consider matrix  $A = \begin{bmatrix} k & 2k \\ k^2 - k & k^2 \end{bmatrix}$  and vector  $x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$ . The number of distinct real values of  $k$  for which the equation  $Ax = 0$  has infinitely many solutions is \_\_\_\_\_.

**(GATE-18-EC)**

Use the code : BVREDDY, to get the maximum discount

**281.** Let  $M$  be a real  $4 \times 4$  matrix. Consider the following statements:

$S_1$ :  $M$  has 4 linearly independent eigenvectors

$S_2$ :  $M$  has 4 distinct eigen values.

$S_3$ :  $M$  is non-singular (invertible).

Which one among the following is TRUE?

- (a)  $S_1$  implies  $S_2$   
(c)  $S_2$  implies  $S_1$

- (b)  $S_1$  implies  $S_3$   
(d)  $S_3$  implies  $S_2$

**(GATE-18-EC)**

Use the code : BVREDDY, to get the maximum discount

**282.** Consider the following system of linear equation

$$3x + 2ky = -2$$

$$kx + 6y = 2$$

Here x and y are the unknowns and k is a real constant. The value of k for which there are infinite number of solutions is

- |        |        |
|--------|--------|
| (a) 3  | (b) 1  |
| (b) -3 | (d) -6 |
- (GATE-18-IN)**

**Use the code : BVREDDY, to get the maximum discount**

**283.** The rank of the matrix  $\begin{bmatrix} -4 & 1 & -1 \\ -1 & -1 & -1 \\ 7 & -3 & 1 \end{bmatrix}$  is

(GATE-18-ME)

**Use the code : BVREDDY, to get the maximum discount**

**284.** The rank of the matrix,  $M = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$ , is \_\_\_\_\_.

**(GATE-19-EE)**

Use the code : BVREDDY, to get the maximum discount

**285.** The set of equations  $x + y + z = 1$ ,  $ax - ay + 3z = 5$ ,  $5x - 3y + az = 6$  has infinite solutions, if  $a =$

- (a) 4
- (b) 3
- (c) -4
- (d) -3

**(GATE-19-ME)**

Use the code : BVREDDY, to get the maximum discount

**286.** Euclidean norm (length) of the vector  $[4 \quad -2 \quad -6]^T$  is

- (a)  $\sqrt{56}$
- (c)  $\sqrt{48}$

- (b)  $\sqrt{24}$
- (d)  $\sqrt{12}$

**(GATE-19-CE)**

Use the code : BVREDDY, to get the maximum discount

**287.** Consider the system of equations

$$\begin{bmatrix} 1 & 3 & 2 \\ 2 & 2 & -3 \\ 4 & 4 & -6 \\ 2 & 5 & 2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 2 \\ 1 \end{bmatrix}$$

The value of  $x_3$  (round off to the nearest integer), is \_\_\_\_\_.

**(GATE-2020(CE))**

**Use the code : BVREDDY, to get the maximum discount**

**288.** Let A and B be two  $n \times n$  matrices over real numbers. Let  $\text{rank}(M)$  and  $\det(M)$  denote the rank and determinant of a matrix M, respectively. Consider the following statements:

- I.  $\text{rank}(AB) = \text{rank}(A) \text{rank}(B)$
- II.  $\det(AB) = \det(A) \det(B)$
- III.  $\text{rank}(A + B) \leq \text{rank}(A) + \text{rank}(B)$
- IV.  $\det(A + B) \leq \det(A) + \det(B)$

Which of the above statements are TRUE?

- (a) III and IV only      (b) II and III only  
(c) I and IV only      (d) I and II only

**(GATE-2020 (CS))**

**Use the code : BVREDDY, to get the maximum discount**

**289.** The rank of the matrix  $\begin{bmatrix} 1 & 2 & 2 & 3 \\ 3 & 4 & 2 & 5 \\ 5 & 6 & 2 & 7 \\ 7 & 8 & 2 & 9 \end{bmatrix}$  is

**(GATE-21-CE)**

- (a) 4
- (b) 2
- (c) 1
- (d) 3

Use the code : BVREDDY, to get the maximum discount

**290.** The rank of the matrix  $\begin{bmatrix} 5 & 0 & -5 & 0 \\ 0 & 2 & 0 & 1 \\ -5 & 0 & 5 & 0 \\ 0 & 1 & 0 & 2 \end{bmatrix}$  is

**(GATE-21-CE)**

- (a) 1
- (b) 2
- (c) 3
- (d) 4

Use the code : BVREDDY, to get the maximum discount

**291.** Consider an  $n \times n$  matrix  $A$  and a non-zero  $n \times 1$  vector  $p$ . Their product  $Ap = \alpha^2 p$ , where  $\alpha \in \mathbb{R}$  and  $\alpha \notin \{-1, 0, 1\}$ . Based on the given information, the eigen value of  $A^2$  is:  
**(GATE-21-ME)**

- (a)  $\alpha$
- (b)  $\alpha^2$
- (c)  $\sqrt{\alpha}$
- (d)  $\alpha^4$

Use the code : BVREDDY, to get the maximum discount

**292.** Suppose that P is a  $4 \times 5$  matrix such that every solution of the equation  $Px = 0$  is a scalar multiple of  $[ 2 \ 5 \ 4 \ 3 \ 1 ]^T$ . The rank of P is **(GATE-2021-cs)**

Use the code : BVREDDY, to get the maximum discount

**293.** Consider the rows vectors  $v = (1, 0)$  and  $w = (2, 0)$ . The rank of the matrix  $M = 2v^T v + 3w^T w$ , where the superscript T denotes the transpose , is

**(GATE – 2021 – IN)**

- (a) 3
- (b) 2
- (c) 4
- (d) 1

Use the code : BVREDDY, to get the maximum discount

**294.** Let  $c_1, \dots, c_n$  be scalars, not all zero, such that  $\sum_{i=1}^n c_i a_i = 0$  where  $a_i$  are column vectors in  $R^n$ . Consider the set of linear equations  $Ax = b$

Where  $A = [a_1, \dots, a_n]$  and  $b = \sum_{i=1}^n a_i$ . The set of equations has

**(GATE-17-CSIT)**

- (a) A unique solution at  $x = j_n$  where  $j_n$  denotes a  $n$ -dimensional vector of all 1
- (b) no solution
- (c) infinitely many solutions
- (d) finitely many solutions

**Use the code : BVREDDY, to get the maximum discount**

**295.** P and Q are two square matrices of the same order. Which of the following statement(s) is/are correct?

**(GATE-2022-CE)**

- (a) If P and Q are invertible, then  $[PQ]^{-1} = Q^{-1}P^{-1}$
- (b) If P and Q are invertible, then  $[QP]^{-1} = P^{-1}Q^{-1}$
- (c) If P and Q are invertible, then  $[PQ]^{-1} = P^{-1}Q^{-1}$
- (d) If P and Q are not invertible, then  $[PQ]^{-1} = Q^{-1}P^{-1}$

**Use the code : BVREDDY, to get the maximum discount**

**296.** The matrix M is defined as

$$M = \begin{bmatrix} 1 & 3 \\ 4 & 2 \end{bmatrix}$$

and has eigenvalues 5 and 2. The matrix Q is formed as

$$Q = M^3 - 4M^2 - 2M$$

Which of the following is/are the eigenvalue(s) of matrix Q

**(GATE-2022-CE)**

- (a) 15
- (b) 25
- (c)-20
- (d) -30

**Use the code : BVREDDY, to get the maximum discount**

**297.** Consider the following two statements with respect to the matrices  $A_{m \times n}$ ,  $B_{n \times m}$ ,  $C_{n \times n}$ ,  $D_{n \times n}$

Statement 1:  $\text{tr}(AB) = \text{tr}(BA)$

Statement 2:  $\text{tr}(CD) = \text{tr}(DC)$

where  $\text{tr}()$  represents the trace of a matrix. Which one of the following holds?

**(GATE-2022-CSE)**

- (a) Statement 1 is correct and Statement 2 is wrong.
- (b) Statement 1 is wrong and Statement 2 is correct.
- (c) Both Statement 1 and Statement 2 are correct.
- (d) Both Statement 1 and Statement 2 are wrong.

**Use the code : BVREDDY, to get the maximum discount**

**298.** Consider solving the following system of simultaneous equations using LU decomposition.

$$x_1 + x_2 - 2x_3 = 4$$

$$x_2 + 3x_3 - x_1 = 7$$

$$2x_1 + x_2 - 5x_3 = 7$$

Where L and U are denoted as

$$L = \begin{bmatrix} L_{11} & 0 & 0 \\ L_{21} & L_{22} & 0 \\ L_{31} & L_{32} & L_{33} \end{bmatrix}, \quad U = \begin{bmatrix} U_{11} & U_{12} & U_{13} \\ 0 & U_{22} & U_{23} \\ 0 & 0 & L_{33} \end{bmatrix}$$

Which one of the following is the correct combination of values for  $L_{32}$ ,  $U_{33}$ , and  $x_1$ ?

**(GATE-2022-CSE)**

- (a)  $L_{32} = 2$ ,  $U_{33} = -\frac{1}{2}$ ,  $x_1 = -1$
- (b)  $L_{32} = 2$ ,  $U_{33} = 2$ ,  $x_1 = -1$
- (c)  $L_{32} = -\frac{1}{2}$ ,  $U_{33} = 2$ ,  $x_1 = 0$
- (d)  $L_{32} = -\frac{1}{2}$ ,  $U_{33} = -\frac{1}{2}$ ,  $x_1 = 0$

**Use the code : BVREDDY, to get the maximum discount**

**299.** Which of the following is/are the eigenvector(s) for the matrix given below?

$$\begin{bmatrix} -9 & -6 & -2 & -4 \\ -8 & -6 & -3 & -1 \\ 20 & 15 & 8 & 5 \\ 32 & 21 & 7 & 12 \end{bmatrix}$$

**(GATE-2022-CSE)**

(a)  $\begin{bmatrix} -1 \\ 1 \\ 0 \\ 1 \end{bmatrix}$

(b)  $\begin{bmatrix} 1 \\ 0 \\ -1 \\ 0 \end{bmatrix}$

(c)  $\begin{bmatrix} -1 \\ 0 \\ 2 \\ 2 \end{bmatrix}$

(d)  $\begin{bmatrix} 0 \\ 1 \\ -3 \\ 0 \end{bmatrix}$

**Use the code : BVREDDY, to get the maximum discount**

**300.** Consider a system of linear equations  $Ax=b$ , where

$$A = \begin{bmatrix} 1 - \sqrt{2} & 3 \\ -1 & \sqrt{2} - 3 \end{bmatrix}, b = \begin{bmatrix} 1 \\ 3 \end{bmatrix}$$

This system of equations admits \_\_\_\_\_

**(GATE-2022-ECE)**

- (a) a unique solution for  $x$
- (b) infinitely many solutions for  $x$
- (c) no solutions for  $x$
- (d) exactly two solutions for  $x$

**Use the code : BVREDDY, to get the maximum discount**

**301.** Consider a matrix  $3 \times 3$  A whose  $(i, j)^{\text{th}}$  element =  $(i - j)^3$ , then the matrix A will be  
**(GATE-2022-EEE)**

- (a) Symmetric
- (b) Skew symmetric
- (c) Unitary
- (d) Null

**Use the code : BVREDDY, to get the maximum discount**

**302.** Consider matrix  $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 4 & -2 \\ 0 & 1 & 1 \end{bmatrix}$ , the matrix A is satisfy the equation  $6A^{-1} = A^2 + cA + dI$  where c and d are scalars and I is the identity matrix, the  $(c + d)$  is equal to

**(GATE-2022-EEE)**

- (a) 5
- (b) 17
- (c) -6
- (d) 11

**Use the code : BVREDDY, to get the maximum discount**

**303.**  $e^A$  denotes the exponential of a square matrix A. Suppose  $\lambda$  is an eigen value and v is the corresponding eigen vector of matrix A.

Consider the following two statement

Statement 1:  $e^\lambda$  is an eigen value of  $e^A$

Statement 2: v is an eigen vector of  $e^A$ .

Which one of the following option is correct.?

**(GATE-2022-EEE)**

- (a) Statement 1 is true and Statement 2 is false
- (b) Statement 1 is false and Statement 2 is true
- (c) Both the statements are correct
- (d) Both statements are false

**Use the code : BVREDDY, to get the maximum discount**

**304.** Given  $M = \begin{bmatrix} 2 & 3 & 7 \\ 6 & 4 & 7 \\ 4 & 6 & 14 \end{bmatrix}$ , which of the following statement(s) is/are correct?

**(GATE-2022-IN)**

- (a) The rank of M is 2
- (b) The rank of M is 3
- (c) The rows of M are linearly independent
- (d) The determinant of M is 0

**Use the code : BVREDDY, to get the maximum discount**

**305.** The matrix  $A = \begin{bmatrix} 4 & 3 \\ 9 & -2 \end{bmatrix}$  has eigen values - 5 and 7.

The eigenvector(s) is/are \_\_\_\_\_

**(GATE-2022-IN)**

- (a)  $\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
- (b)  $\begin{bmatrix} 13 \\ 4 \end{bmatrix}$
- (c)  $\begin{bmatrix} 2 \\ -6 \end{bmatrix}$
- (d)  $\begin{bmatrix} 2 \\ 8 \end{bmatrix}$

Use the code : BVREDDY, to get the maximum discount

**306.** If  $A = \begin{bmatrix} 10 & 2k+5 \\ 3k-5 & k+5 \end{bmatrix}$  is a symmetric matrix, the value of  $k$  is \_\_\_\_\_ (GATE-2022-ME)

- (a) 8
- (b) 10
- (c) -0.4
- (d)  $\frac{1+\sqrt{1561}}{12}$

Use the code : BVREDDY, to get the maximum discount

**307.** The system of linear equations in real  $(x, y)$  given by

$$(x \ y) \begin{bmatrix} 2 & 5 - 2\alpha \\ \alpha & 1 \end{bmatrix} = (0 \ 0)$$

involves a real parameter  $\alpha$  and has infinitely many non-trivial solutions for special value(s) of  $\alpha$ . Which one or more among the following options is/are non-trivial solution(s) of  $(x, y)$  for such special value(s) of  $\alpha$ ?

**(GATE-2022-ME)**

- (a)  $x = 2, y = -2$
- (b)  $x = -1, y = 4$
- (c)  $x = 1, y = 1$
- (d)  $x = 4, y = -2$

**Use the code : BVREDDY, to get the maximum discount**

**308.** A is a  $3 \times 5$  real matrix of rank 2. For the set of homogeneous equations  $Ax = 0$ , where 0 is a zero vector and x is a vector of unknown variables, which of the following is/are true?

**(GATE-2022-ME)**

- (a) The given set of equations will have a unique solution.
- (b) The given set of equations will be satisfied by a zero vector of appropriate size.
- (c) The given set of equations will have infinitely many solutions.
- (d) The given set of equations will have many but a finite number of solutions.

**Use the code : BVREDDY, to get the maximum discount**

**309.** If the sum and product of eigen values of a  $2 \times 2$  matrix  $\begin{bmatrix} 3 & p \\ p & q \end{bmatrix}$  are 4 and -1 respectively, then  $|p|$  is \_\_\_\_\_ (in integer).

**(GATE-2022-ME)**

Use the code : BVREDDY, to get the maximum discount

**310.** Matrix A as product of two other matrices is given by

$$A = \begin{bmatrix} 3 \\ 2 \end{bmatrix} [1 \quad 4]$$

The value of  $\det(A)$  is \_\_\_\_\_ [round off to nearest integer]

**(GATE-2022-PI)**

Use the code : BVREDDY, to get the maximum discount

**311.** If a matrix is squared, then

**(GATE-2022-PI)**

- (a) both eigenvalues and eigenvectors are retained.
- (b) eigenvalues get squared but eigenvectors are retained.
- (c) both eigenvalues and eigenvectors must change.
- (d) eigenvalues are retained but eigenvectors change.

**Use the code : BVREDDY, to get the maximum discount**