

# Practice Session on Calculus - Part V

Revision Course on Engineering Mathematics - GATE, CS & IT

# **CALCULUS DPP**

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$$1. \lim_{x \rightarrow 0} \frac{x(e^x - 1) + 2(\cos x - 1)}{x(1 - \cos x)} = \frac{0}{0} \quad (\text{GATE -ME- 1993})$$

$$\frac{x(e^x) + (e^x - 1)1 - 2\sin x}{x(0 + \sin x) + (1 - \cos x)} \quad (\frac{0}{0})$$

$$\frac{xe^x + e^x + e^x - 2\cos x}{x\cos x + \sin x + \sin x} \quad (\frac{0}{0})$$

$$\frac{xe^x + e^x + e^x + e^x + 2\sin x}{-x\sin x + \cos x + \cos x + \cos x} = \frac{3}{3} = 1.$$

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2. The integration of  $\int \log x \, dx$  has the value (GATE -EC- 1994)

- (a)  $(x \log x - 1)$   
~~(c)  $x(\log x - 1)$~~

- (b)  $\log x - x$   
(d) None of the above

I LATE

$$\int_{u}^{v} \log x \, dx = \log x(x) - \int \frac{1}{x} x \, dx$$

$$\int u v = u \int v - \int u' \int v$$

$$= \log x(x) - x.$$

$$= x(\log x - 1)$$

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3.  $\lim_{n \rightarrow \infty} (\sqrt{n^2 + n} - \sqrt{n^2 + 1})$  is \_\_\_\_\_.

(GATE-16-IN)

$$\frac{\sqrt{n^2+n} - \sqrt{n^2+1}}{\sqrt{n^2+n} + \sqrt{n^2+1}} \cdot \frac{\sqrt{n^2+n} + \sqrt{n^2+1}}{\sqrt{n^2+n} + \sqrt{n^2+1}}$$

$$\begin{aligned} \frac{n^2+n - n^2-1}{\sqrt{n^2+n} + \sqrt{n^2+1}} &= \frac{n(1-\frac{1}{n})}{n\left[\sqrt{1+\frac{1}{n}} + \sqrt{1+\frac{1}{n^2}}\right]} \\ &= \frac{1}{1+\frac{1}{n}} = \frac{1}{2}. \end{aligned}$$

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4.  $\lim_{x \rightarrow \infty} \frac{x^3 - \cos x}{x^2 + (\sin x)^2} = \underline{\hspace{2cm}}$  (GATE -CS- 1995)
- (a)  $\infty$       (b) 0      (c) 2      (d) Does not exist

$$\frac{x^3 \left(1 - \frac{\cos x}{x^3}\right)}{x^2 \left(1 + \left(\frac{\sin x}{x}\right)^2\right)} = \frac{x \left(1 - \frac{\cos x}{x^3}\right)}{1 + \left(\frac{\sin x}{x}\right)^2} = \frac{x (1 - 0)}{1 + 0} = \infty$$

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$$5. \lim_{x \rightarrow 0} x \sin \frac{1}{x} = \underline{\hspace{2cm}} \quad (\text{GATE -CS- 1995})$$

(a)  $\infty$

~~(b) 0~~

(c) 1

(d) Does not exist

$$\lim_{x \rightarrow 0} x \sin\left(\frac{1}{x}\right) = 0 \cdot \sin\left[\frac{1}{x}\right]$$

$$[-1 \leq \sin x \leq 1]$$

$$= 0 \cdot \text{finite} = 0$$

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6. The function  $f(x) = |x+1|$  on the interval  $[-2, 0]$  is \_\_\_\_\_

(GATE-EC- 1995)

- (a) continuous and differentiable
- ~~(b) continuous on the interval but not differentiable at all points~~
- (c) Neither continuous nor differentiable
- (d) Differentiable but not continuous

$$x = -1$$

$$f(x) = |x+1|$$

↳ Continuous  $\forall x$

↳ differentiable every where except  
at  $x = -1$

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7. If a function is continuous at a point its first derivative (GATE -EC- 1995)

- ~~(a) may or may not exist~~      (b) exists always  
(c) will not exist      (d) has a unique value

L  
↓  
C  
↓  
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L C D

10<sup>th</sup> 12<sup>th</sup>

B.Tech.

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8.  $\lim_{\theta \rightarrow 0} \frac{\sin m\theta}{\theta}$ , where  $m$  is an integer, is one of the following:

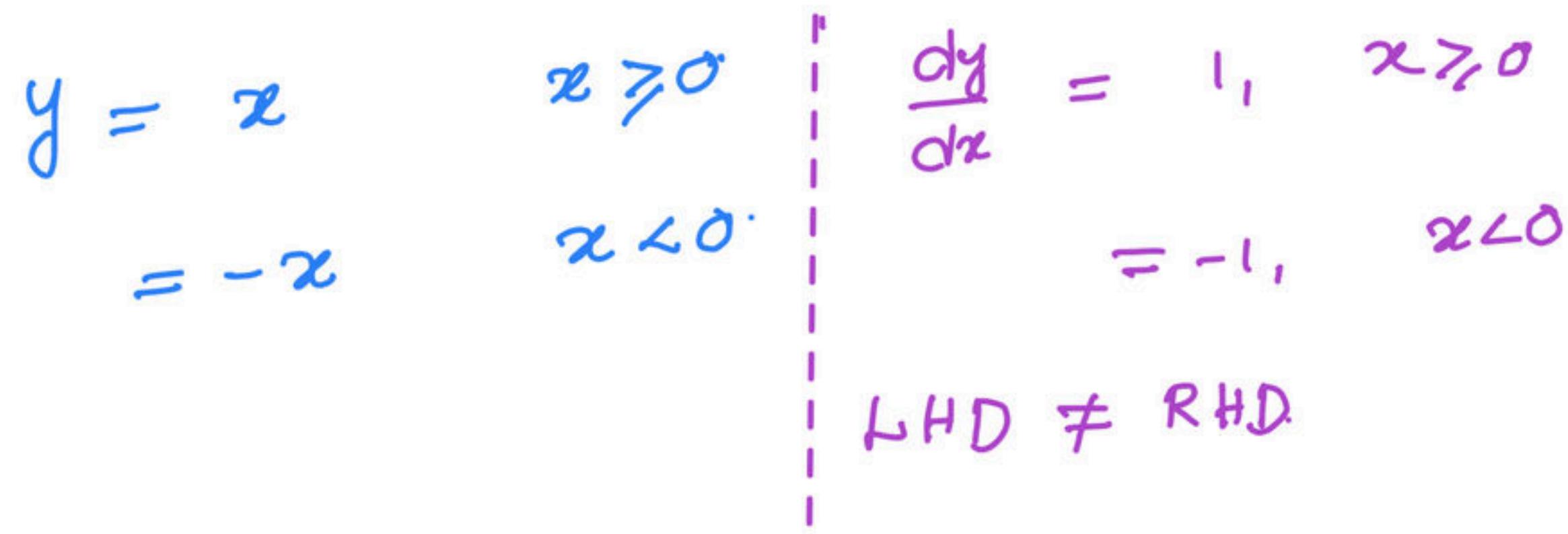
(GATE -CS- 1997)

- (a)  ~~$m$~~       (b)  $m\pi$       (c)  $m\theta$       (d) 1

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9. If  $y = |x|$  for  $x < 0$  and  $y = x$  for  $x \geq 0$  then  
(GATE -EC- 1997)

- (a)  $\frac{dy}{dx}$  is discontinuous at  $x = 0$       (b)  $y$  is discontinuous at  $x = 0$
- (c)  $y$  is not defined at  $x = 0$
- (d) Both  $y$  and  $\frac{dy}{dx}$  are discontinuous at  $x = 0$



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10. The value of

$$\lim_{x \rightarrow 1} \frac{x^3 - 3x + 2}{x^3 - x^2 - x + 1}$$

Is \_\_\_\_\_ [round off to one decimal place]

(GATE-2022-PI)

$$\begin{aligned}\frac{3x^2 - 3}{3x^2 - 2x - 1} &= \frac{6x}{6x - 2} \\ &= \frac{6}{4} = \frac{3}{2}.\end{aligned}$$

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$$11. \lim_{x \rightarrow 0} \frac{1}{10} \frac{1 - e^{-j5x}}{1 - e^{-jx}} = \underline{\hspace{2cm}}$$

(GATE -IN-1998)

(a) 0

(b) 1.1

(c) 0.5

(d) 1

$$\frac{1}{10} \cdot \frac{\sigma + j5}{\sigma + je^{-jx}} e^{-j5x} = \frac{1}{2}$$

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12. Limit of the function,  $\lim_{n \rightarrow \infty} \frac{n}{\sqrt{n^2 + n}}$  is \_\_\_\_\_

(GATE -EC-1999)

(a)  $\frac{1}{2}$

(b) 0

(c)  $\infty$

(d) 1

$$\begin{aligned} n \sqrt{1 + \frac{1}{n}} &= \sqrt{\frac{1}{1 + \frac{1}{n}}} \\ &= \frac{1}{\sqrt{1 + \frac{1}{n}}} \end{aligned}$$

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13. Value of the function  $\lim_{x \rightarrow a} (x-a)^{x-a}$  is \_\_\_\_\_ (GATE -CS-1999)

(a) 1

(b) 0

(c)  $\infty$

(d) a

$$y = (x-a)^{x-a}$$

$$\log y = (x-a) \log(x-a).$$

$$(x-a) \log(x-a).$$

$$y = e$$

$$y =$$

$$e^{\infty}$$

$$\log_0 = \infty$$

$$\log_1 = 0$$

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$$\log y = (x-a) \log(x-a)$$

$$\log y = \frac{\log(x-a)}{1/(x-a)}$$

$$\log y = \frac{1/x-a}{-1/(x-a)^2}$$

$$\log y = - (x-a)$$

$$\log y = 0$$

$$y = e^0 = 1$$

14. The function  $f(x) = e^x$  is \_\_\_\_\_ (GATE -EC-1999)

- (a) Even      (b) Odd      ~~(c) Neither even nor odd~~      (d) None

$$f(x) = e^x$$

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15. Consider the following integral  $\lim_{a \rightarrow \infty} \int_1^a x^{-4} dx$  \_\_\_\_\_ (GATE -CS-2000)

- (a) diverges
- ~~(b) converges to  $1/3$~~
- (c) converges to  $-\frac{1}{a^3}$
- (d) converges to 0

$$\begin{aligned}\int_1^a \frac{1}{x^4} dx &= \left. \frac{x^{-4+1}}{-4+1} \right|_1^a = \frac{-1}{3} \left[ a^{-3} - 1 \right] \\ &= \frac{-1}{3} \left[ \frac{1}{a^3} - 1 \right] \\ &= +\frac{1}{3}.\end{aligned}$$

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16. Limit of the function  $f(x) = \frac{1-a^4}{x^4}$  as  $x \rightarrow \infty$  is given by

(GATE -CS-2000)

(a) 1

(b)  $e^{-a^4}$

(c)  $\infty$

(d) 0

$$f(x) = \frac{1}{x^4} (1 - a^4)$$

$x \rightarrow \infty$

$$= 0 \underset{\substack{\downarrow \\ \text{finite}}}{(1 - a^4)} = 0$$

$\frac{1}{x} \rightarrow 0$

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$$17. \lim_{x \rightarrow \frac{\pi}{4}} \frac{\sin 2\left(x - \frac{\pi}{4}\right)}{x - \frac{\pi}{4}} = \underline{\hspace{2cm}}$$

(GATE -IN-2001)

- (a) 0
- (b)  $\frac{1}{2}$
- (c) 1
- (d) 2

$$y = x - \frac{\pi}{4}$$

$$\lim_{y \rightarrow 0} \frac{2 \left( \frac{\sin 2y}{2y} \right)}{2y} = 2.$$

$$\lim_{f(x) \rightarrow 0} \frac{\sin[f(x)]}{f(x)} = 1$$

$$\lim_{f(x) \rightarrow 0} \frac{\sin k f(x)}{f(x)} = k.$$

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18. Limit of the following sequence as  $n \rightarrow \infty$  is \_\_\_\_\_  $x_n = n^{\frac{1}{n}}$

(a) 0

(b) 1

(c)  $\infty$

(d)  $-\infty$

(GATE -CE-2002)

$$x(n) = n^{\frac{1}{n}}$$

$$\log x = \frac{1}{n} \log(n)$$

$$\log x = \frac{\log(n)}{n}$$

$$\log x = \frac{1/n}{1}$$

$$\log x = \frac{1}{n}$$

$$\log x = 0$$

$$x = 1$$

$\infty^0$

5

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19. Which of the following functions is not differentiable in the domain [-1, 1]?

(a)  $f(x) = x^2$  ✓

(b)  $f(x) = x - 1$  ✓

(c)  $f(x) = 2$  ✓

(d)  ~~$f(x) = \max(x, -x)$~~

(GATE -EC-2002)

$$f(x) = \max(x, -x)$$

$$f(x) = |x|$$

$$\begin{aligned} f(x) &= -x & x < 0 \\ &= x. & x > 0 \end{aligned}$$

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$$20. \lim_{x \rightarrow 0} \frac{\sin^2 x}{x} = \underline{\hspace{2cm}}$$

(GATE-CS-2003)

(a) 0

(b)  $\infty$

(c) 1

(d) -1

$$\begin{aligned} x \frac{\sin^2 x}{x^2} &= x \left( \frac{\sin x}{x} \right)^2 \\ &= x (1) = o(1) = 0 \end{aligned}$$

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21. The value of the function,  $f(x) = \lim_{x \rightarrow 0} \frac{x^3 + x^2}{2x^3 - 7x^2}$  is \_\_\_\_\_ (GATE-CS-2004)

(a) 0

(b)  $\frac{-1}{7}$

(c)  $\frac{1}{7}$

(d)  $\infty$

$$\frac{x^2(x+1)}{x^2(2x-7)} = \frac{x+1}{2x-7} = -\frac{1}{7}$$

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22. Consider the function  $f(x) = |x|^3$ , where  $x$  is real.

Then the function  $f(x)$  at  $\underline{x=0}$  is

(GATE -IN-2007)

- (a) continuous but not differentiable  
(c) twice differentiable but not thrice

- (b) once differentiable but not twice  
(d) thrice differentiable

$$\begin{aligned}f(x) &= -x^3 & x < 0 \\&= x^3 & x \geq 0\end{aligned}$$

$$\begin{aligned}f'(x) &= -3x^2, & x < 0 \\&= 3x^2, & x \geq 0.\end{aligned}$$

$$LHD = RHD = 0$$

$$\begin{aligned}f''(x) &= -6x, & x < 0 \\&= 6x, & x \geq 0\end{aligned}$$

$$LHD = RHD = 0$$

$$\begin{aligned}f'''(x) &= -6, & x < 0 \\&= 6, & x \geq 0.\end{aligned}$$

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at  $x = \bar{0}_+$ ,  $LHD = -6$

at  $x = 0^+$ ,  $RHD = 6$ .

$LHD \neq RHD$

$$23. \lim_{x \rightarrow 0} \frac{e^x - \left(1 + x + \frac{x^2}{2}\right)}{x^3} =$$

(GATE-ME-2007)

(a) 0

(b)  $\frac{1}{6}$

(c)  $\frac{1}{3}$

(d) 1

$$\begin{aligned} \frac{e^x - (1 + 1 + \frac{x^2}{2})}{3x^2} &= \frac{e^x - (0+0+1)}{6x} \\ &= \frac{e^x}{6} = \frac{1}{6}. \end{aligned}$$

$$\begin{aligned} e^x &= 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} \\ \frac{e^x - 1 - x - \frac{x^2}{2}}{x^3} &= \frac{\frac{x^3}{6}}{x^3} \\ &= \frac{1}{6} \end{aligned}$$

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24. If  $y = x + \sqrt{x + \sqrt{x + \sqrt{x + \dots}}}$  then  $y(2) = \dots$  (GATE-ME-2007)

$$y = 2 + \sqrt{\dots}$$

↑

$$\boxed{x=2}$$

- (a) 4 (or) 1  
(c) 1 only  
~~(b) 4 only~~  
(d) Undefined

$$y - x = \sqrt{x + \sqrt{x + \sqrt{x}}}$$

$$(y - x)^2 = x + \sqrt{x + \sqrt{x + \dots}}$$

$$(y - x)^2 = y$$

$$y^2 + x^2 - 2xy = y$$

$$y^2 + 4 - 4y = y$$

$$y^2 - 5y + 4 = 0$$

$$(y-4)(y-1) = 0$$

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$$y = 4.$$

$$y = 1.$$

$$y = 4$$

25.What is the value of  $\lim_{x \rightarrow \pi/4} \frac{\cos x - \sin x}{x - \pi/4}$

2007)

(a)  $\sqrt{2}$

(b) 0

(c)  $-\sqrt{2}$

(d) Limit does not exist

$$\begin{aligned}\frac{-\sin x - \cos x}{1.} &= \frac{-1}{\sqrt{2}} - \frac{1}{\sqrt{2}} = \frac{-2}{\sqrt{2}} \\ &= -\sqrt{2}\end{aligned}$$

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26.  $\lim_{\theta \rightarrow 0} \frac{\sin(\theta/2)}{\theta}$  is

(GATE-EC-2007)

(a) 0.5

(b) 1

(c) 2

(d) not defined

It  $\lim_{x \rightarrow 0} \frac{\sin kx}{x} = k$

$$k = \frac{1}{2}$$

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$$27. \lim_{x \rightarrow \infty} \frac{x - \sin x}{x + \cos x} = \underline{\hspace{2cm}}$$

(GATE-EC-2008)

- ~~(a) 1~~      (b) -1      (c)  $\infty$       (d)  $-\infty$

$$\frac{x(1 - \frac{\sin x}{x})}{x(1 + \frac{\cos x}{x})} = \frac{1 - 0}{1 + 0} = 1$$

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28. Given  $y = x^2 + 2x + 10$  the value of  $\left. \frac{dy}{dx} \right|_{x=1}$  is equal to (GATE-IN-2008)

(a) 0

~~(b) 4~~

(c) 12

(d) 13

$$\frac{dy}{dx} = 2x + 2$$

$$\left. \frac{dy}{dx} \right|_{x=1} = 4$$

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29.  $\lim_{x \rightarrow 0} \frac{\sin x}{x}$  is

(GATE-IN-2008)

(a) indeterminate

(b) 0

(c) 1

(d)  $\infty$

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30. The value of  $\lim_{x \rightarrow 8} \frac{x^{1/3} - 2}{x - 8}$  is

(GATE-ME-2008)

(a)  $\frac{1}{16}$

(b)  ~~$\frac{1}{12}$~~

(c)  $\frac{1}{8}$

(d)  $\frac{1}{4}$

$$\begin{aligned}\frac{\frac{1}{3}(x)^{-\frac{2}{3}}}{= \frac{1}{3}(2^3)^{-\frac{2}{3}}} \\ = \frac{1}{3} 2^{-2} = \frac{1}{12}\end{aligned}$$

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31. The value of the expression  $\lim_{x \rightarrow 0} \left[ \frac{\sin(x)}{e^x x} \right]$  is **(GATE-PI-2008)**

(a) 0

(b)  $\frac{1}{2}$

(c) 1

(d)  $\frac{1}{1+e}$

$$\frac{\sin x}{x} \cdot \frac{1}{e^x} = (1)(1) = 1.$$

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32. The total derivative of the function 'xy' is

(GATE-PI-2009)

- (a)  $x \, dy + y \, dx$  (b)  $x \, dx + y \, dy$  (c)  $dx + dy$

- (d)  $dx \, dy$

$$xdy + ydx.$$

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33. If  $f(x) = \sin|x|$  then the value of  $\frac{df}{dx}$  at  $x = -\frac{\pi}{4}$  is **(GATE-PI-2010)**

- (a) 0      (b)  $\frac{1}{\sqrt{2}}$

~~(c)  $-\frac{1}{\sqrt{2}}$~~

- (d) 1

$$f(x) = \sin|x|.$$

$$\begin{aligned} f(x) &= -\sin x & x < 0 \\ &= \sin x. & , x > 0 \end{aligned}$$

$$f'(x) = -\cos x, \quad x < 0$$

$$= \cos x, \quad x > 0$$

$$f'\left(x = -\frac{\pi}{4}\right) = -\frac{1}{\sqrt{2}}.$$

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34. What is the value of  $\lim_{n \rightarrow \infty} \left(1 - \frac{1}{n}\right)^{2n}$  ?

$e^{-2}$

(GATE-CS-2010)

(a) 0

~~(b)  $e^{-2}$~~

(c)  $e^{-t/2}$

(d) 1

$$\begin{aligned}
 & f(x) \quad g(x) \\
 & \underset{x \rightarrow \infty}{\text{It}} \quad g(x)[f(x) - 1] \\
 = & e^{\underset{x \rightarrow \infty}{\text{It}}} \quad 2n \left[ 1 - \frac{1}{n} - 1 \right] \\
 = & e^{\underset{x \rightarrow \infty}{\text{It}}} - 2 \\
 = & e^{-2}
 \end{aligned}$$

$\frac{1}{\infty}$  ✓ log  
 $0^\infty \}$  log  
 $\infty^0 \}$  log

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$$\lim_{x \rightarrow \infty} \left(1 + \frac{a}{x}\right)^{bx} = e^{ab}$$

(1)

$$\lim_{x \rightarrow 0} \left(1 + ax\right)^{\frac{b}{x}} = e^{ab}.$$

35. The  $\lim_{x \rightarrow 0} \frac{\sin\left(\frac{2}{3}x\right)}{x}$  is

(GATE-CE-2010)

(a)  $\frac{2}{3}$

(b) 1

(c)  $\frac{3}{2}$

(d)  $\infty$

It  $\lim_{x \rightarrow 0} \frac{\sin kx}{x} = k = \frac{2}{3}$

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36. The function  $y = \underline{|2-3x|}$

(GATE-ME-2010)

- (a) is continuous  $\forall x \in R$  and differentiable  $\forall x \in R$
- (b) is continuous  $\forall x \in R$  and differentiable  $\forall x \in R$  except at  $x = \frac{3}{2}$
- (c) is continuous  $\forall x \in R$  and differentiable  $\forall x \in R$  except at  $x = \frac{2}{3}$
- (d) is continuous  $\forall x \in R$  and except at  $x = 3$  and differentiable  $\forall x \in R$

$$2 - 3x = 0$$

$$x = \frac{2}{3} \checkmark$$

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37. What should be the value of  $\lambda$  such that the function defined below is continuous at  $x = \frac{\pi}{2}$ ? (GATE-CE-2011)

$$f(x) = \begin{cases} \frac{\lambda \cos x}{\frac{\pi}{2} - x}, & \text{if } x \neq \frac{\pi}{2} \\ 1, & \text{if } x = \frac{\pi}{2} \end{cases}$$

It  
 $x \rightarrow \frac{\pi}{2}$

$$\frac{\lambda \cos x}{\frac{\pi}{2} - x} = \frac{-\lambda \sin x}{-1} = \lambda$$

$$\lambda = 1$$

- (a) 0      (b)  $2\pi$

- (c) 1      (d)  $\frac{\pi}{2}$

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38.What is  $\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta}$  equal to ?

(GATE-ME-2011)

- (a)  $\theta$
- (b)  $\sin \theta$
- (c) 0

- (d) 1

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39. Consider the function  $f(x) = |x|$  in the interval  $-1 \leq x \leq 1$ . At the point  $x = 0$ ,  
 $f(x)$  is (GATE-ME,PI-2012)

- (a) continuous and differentiable
- (b) non-continuous and differentiable
- ~~(c) continuous and non-differentiable~~
- (d) neither continuous nor differentiable

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40.  $\lim_{x \rightarrow 0} \left( \frac{1 - \cos x}{x^2} \right)$  is

(GATE-ME,PI-2012)

(a) 1/4

(b) 1/2

(c) 1

(d) 2

$$\frac{0 + \sin x}{2x} = \frac{1}{2}.$$

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41. A function  $y = 5x^2 + 10x$  is defined over an open interval  $x = (1, 2)$ . At least at one point in this interval,  $\frac{dy}{dx}$  is exactly (GATE-EE-2013)

(a) 20

~~(b) 25~~

(c) 30

(d) 35

$$\frac{dy}{dx} = 10x + 10 \quad x = 1.5$$

$$\left. \frac{dy}{dx} \right|_{x=1.5} = 25$$

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42. Which one of the following functions is continuous at  $x = 3$ ?  
**(GATE-CS-2013)**

~~(a)  $f(x) = \begin{cases} 2, & \text{if } x = 3 \\ x - 1 & \text{if } x > 3 \\ \frac{x+3}{3}, & \text{if } x < 3 \end{cases}$~~

(c)  $f(x) = \begin{cases} x + 3, & \text{if } x \leq 3 \\ x - 4 & \text{if } x > 3 \end{cases}$

(b)  $f(x) = \begin{cases} 4, & \text{if } x = 3 \\ 8 - x & \text{if } x \neq 3 \end{cases}$

(d)  $f(x) = \frac{1}{x^3 - 27}$ , if  $x \neq 3$

LHL  
 $\lim_{x \rightarrow 3^-} f(x) = \lim_{x \rightarrow 3^-} x - 1 = 2$

RHL  
 $\lim_{x \rightarrow 3^+} f(x) = \lim_{x \rightarrow 3^+} \frac{x+3}{3} = \frac{2+3}{3} = 2$

Use the code: **BVREDDY**, to get maximum benefits

43. The value of  $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x$  is

(GATE-EC-SET-2-2014)

(a)  $\ln 2$

(b) 1.0

~~(c) e~~

(d)  $\infty$

$|^\infty$

$$e^{ab} = e^{|^\infty|}$$

Use the code: BVREDDY , to get maximum benefits

44.  $\lim_{x \rightarrow 0} \frac{x - \sin x}{1 - \cos x}$  is

(GATE-ME-SET-1-2014)

~~(a) 0~~

(b) 1

(c) 3

(d) not defined

$$\frac{1 - \cos x}{x + \sin x} = \frac{x - \sin x}{\cos x} = 0$$

Use the code: BVREDDY , to get maximum benefits

45.  $\lim_{x \rightarrow 0} \left( \frac{e^{2x} - 1}{\sin(4x)} \right)$  is equal to

(GATE-ME-SET-2-2014)

(a) 0

(b) 0.5

(c) 1

(d) 2

$$\begin{aligned} \frac{(e^{2x} - 1) \cdot \frac{1}{4x}}{\frac{\sin 4x}{4x}} &= \frac{e^{2x} - 1}{4x} \quad (1) \\ &= \frac{e^{2x}(2) - 0}{4} \\ &= \frac{1}{2} \end{aligned}$$

Use the code: BVREDDY , to get maximum benefits

46. If a function is continuous at a point,

(GATE-ME-SET-3-2014)

- (a) the limit of the function may not exist at the point
- (b) the function must be derivable at the point
- (c) the limit of the function at the point tends to infinity
- ~~(d) the limit must exist at the point and the value of limit should be same as the value of the function at the point.~~

L C D

Use the code: BVREDDY , to get maximum benefits

47.  $\lim_{x \rightarrow \infty} \left( \frac{x + \sin x}{x} \right)$  equal to

(GATE-CE-SET-1-2014)

- (a)  $-\infty$       (b) 0      (c) 1      (d)  $\infty$

$$1 + \frac{\sin x}{x} = 1 + 0 = 1$$

Use the code: BVREDDY , to get maximum benefits

48. The expression  $\lim_{a \rightarrow 0} \frac{x^a - 1}{a}$  is equal to

(GATE-CE-SET-2-2014)

(a)  $\log x$

(b) 0

(c)  $x \log x$

(d)  $\infty$

$$\boxed{\frac{dy}{da} = x^a \log x}$$

$$\frac{x^a \log x - 0}{1} = \log x$$

$$y = x^a.$$

$$\log y = a \log x.$$

$$\frac{1}{y} \frac{dy}{da} = \log x.$$

$$\frac{dy}{da} = y \log x.$$

Use the code: BVREDDY , to get maximum benefits

49. The function  $f(x) = x \sin x$  satisfies the following equation:

$f''(x) + f(x) + t \cos x = 0$ . The value of  $t$  is \_\_\_\_\_.

(GATE-CS-SET-1-2014)

$$f(x) = x \sin x$$

$$f'(x) = x \cos x + \sin x$$

$$f''(x) = -x \sin x + \cos x + \cos x$$

$$f''(x) + f(x) + t \cos x = 0$$

$$\cancel{-x \sin x} + 2 \cos x + x \sin x + t \cos x = 0$$

$$t = -2$$

Use the code: **BVREDDY**, to get maximum benefits

50. The value of  $\lim_{x \rightarrow \infty} \frac{\sqrt{9x^2 + 2020}}{x + 7}$  is

GATE-2021 (CE)

- (a) 1
- ~~(b) 3~~
- (c)  $\frac{7}{9}$
- (d) Indeterminable

$$\frac{x \sqrt{9 + \frac{2020}{x^2}}}{x(1 + 7/x)} = 3.$$

Use the code: BVREDDY , to get maximum benefits

51.  $\lim_{x \rightarrow \infty} x^{1/x}$  is

(GATE-CS-2015)

(a)  $\infty$

(b) 0

(c) 1

(d) Not defined

$$y = x^{1/x}$$

$$\log y = \frac{1}{x} \log x$$

$$\log y = \frac{1/x}{1}$$

$$\log y = 0$$

$$y = e^0 = 1$$

Use the code: BVREDDY , to get maximum benefits

52. The limit  $p = \lim_{x \rightarrow \pi} \left( \frac{x^2 + \alpha x + 2\pi^2}{x - \pi + 2\sin x} \right)$

has a finite value of real  $\alpha$ . The value of  $\alpha$  and the corresponding limit  $p$  are

- (a)  $\alpha = -3\pi$ , and  $p = \pi$
- (b)  $\alpha = -2\pi$ , and  $p = 2\pi$
- (c)  $\alpha = \pi$ , and  $p = \pi$
- (d)  $\alpha = 2\pi$ , and  $p = 3\pi$

(GATE-2022-ME)

$$\frac{x^2 - 3\pi x + 2\pi^2}{x - \pi + 2\sin x} =$$

$$\frac{2x - 3\pi}{1 + 2\cos x} = \frac{2\pi - 3\pi}{1 - 2} = +\pi.$$

Use the code: BVREDDY , to get maximum benefits

53. The value of  $\lim_{x \rightarrow \infty} (1+x^2)^{e^{-x}}$  is

(GATE-CS-2015)

(a) 0

(b)  $\frac{1}{2}$

(c) 1

(d)  $\infty$

$$y = (1+x^2)e^{-x}$$

$$\log y = e^{-x} \log(1+x^2)$$

$$\log y = \frac{\log(1+x^2)}{e^{-x}}$$

$$\log y = \frac{2x}{e^x(1+x^2)}$$

$$\log y = \frac{2x}{e^x(1+x^2)}$$

$$\log y = \frac{2}{e^x(1+x^2) + e^{-x}(2x)}$$

$$\log y = 0 \Rightarrow y = e^0 = 1.$$

Use the code: BVREDDY, to get maximum benefits

$$\log(1+x^2) \neq \log(1) + \log(x^2)$$

54.  $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^{2x}$  is equal to

(GATE-CE-2015)

(a)  $e^{-2}$

(b)  $e$

(c) 1

(d)  $e^2$

$e^2$

Use the code: BVREDDY , to get maximum benefits

55. The value of  $\lim_{x \rightarrow \infty} \frac{1 - \cos(x^2)}{2x^4}$  is

(GATE-ME-2015)

- (a) 0      (b)  $\frac{1}{2}$       (c)  $\frac{1}{4}$       (d) undefined

$$\frac{1}{2x^4} \left[ 1 - \frac{\cos(x^2)}{1} \right] = o \text{ (finite)}$$

$\xrightarrow{x \rightarrow \infty}$

finite.

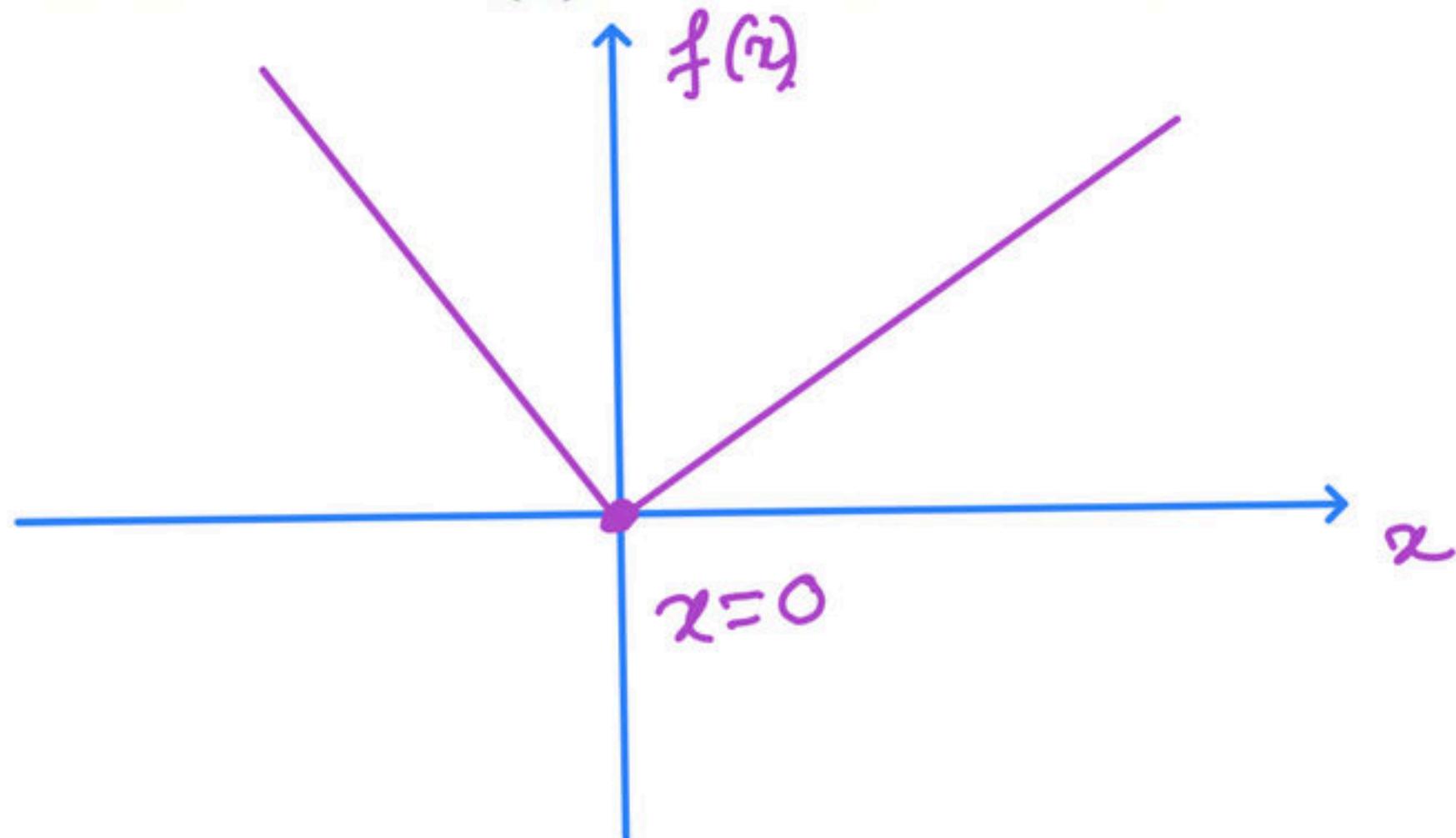
$$-1 \leq \cos(\theta) \leq 1$$

Use the code: BVREDDY , to get maximum benefits

56. At  $x = 0$ , the function  $f(x) = |x|$  has

(GATE-ME-2015)

- (a) A minimum
- (b) A maximum
- (c) A point of inflection
- (d) neither a maximum nor minimum



Use the code: BVREDDY , to get maximum benefits

57. The value of  $\lim_{x \rightarrow 0} \left( \frac{-\sin x}{2 \sin x - x \cos x} \right)$  is \_\_\_\_\_ (GATE-ME-2015)

$$\frac{-\cos x}{2\cos x + x \sin x - \cos x} = \frac{-1}{2+0-1} = -1$$

Use the code: BVREDDY , to get maximum benefits

58. The value of  $\lim_{x \rightarrow \infty} \frac{x^2 - 5x + 4}{4x^2 + 2x}$  is

GATE-2020 (CE)

(a) 0

(b) 1

(d)  $\frac{1}{2}$

(c)  $\frac{1}{4}$

$$\frac{x^2\left(1 - \frac{5}{x} + \frac{4}{x^2}\right)}{x^2\left(4 + \frac{2}{x}\right)} = \frac{1}{4}$$

Use the code: BVREDDY , to get maximum benefits

59. Consider the limit:

GATE-2021 (CE)

$$\lim_{x \rightarrow 1} \left( \frac{1}{\ln x} - \frac{1}{x-1} \right)$$

$\infty - \infty$

The limit (correct up to one decimal place) is \_\_\_\_\_

$\frac{0}{0}$

$$\begin{aligned}\frac{x-1-\ln x}{\ln x(x-1)} &= \frac{1-0-\frac{1}{2}}{\frac{1}{x}(x-1)+1\ln x} = \frac{x-1}{(x-1)+2\ln x} \\&= \frac{1-0}{1-0+\frac{x-1}{x}+1\ln x} = \frac{1}{1+1+0} \\&= \frac{1}{2}.\end{aligned}$$

Use the code: BVREDDY , to get maximum benefits

60. The value of  $\lim_{x \rightarrow \infty} \frac{x \ln(x)}{1 + x^2}$  is

GATE-20201(CE)

- (a) 1.0  
(c)  $\infty$

- (b) 0.5

~~(d) 0~~

$$\frac{x \cdot \frac{1}{x} + \ln(x)}{2x} = \frac{1 + \ln(x)}{2x} = \frac{0 + 1/x}{2}$$
$$= \frac{1}{2x} = 0.$$

Use the code: BVREDDY , to get maximum benefits

61. The function  $f(x,y) = x^2y - 3xy + 2y + x$  has  
**(GATE-ME-1994)**

- (a) No local extreme
- (b) One local maximum but no local minimum
- (c) One local minimum but no local maximum
- (d) One local minimum and one local maximum

62. The function  $y = x^2 + \frac{250}{x}$  at  $x = 5$  attains

(GATE-EC-1994)

- (a) Maximum
- (b) Minimum
- (c) Neither
- (d) 1

Use the code: BVREDDY , to get maximum benefits

63. The function  $f(x) = x^3 - 6x^2 + 9x + 25$  has

(GATE-EE-1995)

- (a) a maxima at  $x = 1$  and a minima at  $x = 3$
- (b) a maxima at  $x = 3$  and a minima at  $x = 1$
- (c) no maxima, but a minima at  $x = 3$
- (d) a maxima at  $x = 1$ , but no minima

Use the code: **BVREDDY** , to get maximum benefits

64. Find the points of local maxima and minima if any of the following function defined in  
 $0 \leq x \leq 6$ ,  $f(x) = x^3 - 6x^2 + 9x + 15.$   
(GATE-CS-1998)

**Use the code: BVREDDY , to get maximum benefits**

65. The continuous function  $f(x,y)$  is said to have saddle point at  $(a, b)$  if

- (a)  $f_x(a, b) = f_y(a, b) = 0, f_{xy}^2 - f_{xx}f_{yy} < 0$  at  $(a, b)$

**(GATE-EE-1998)**

- (b)  $f_x(a, b) = 0, f_y(a, b) = 0, f_{xy}^2 - f_{xx}f_{yy} > 0$  at  $(a, b)$

- (c)  $f_x(a, b) = 0, f_y(a, b) = 0, f_{xx}$  and  $f_{yy} < 0$  at  $(a, b)$

- (d)  $f_x(a, b) = 0, f_y(a, b) = 0, f_{xy}^2 - f_{xx}f_{yy} = 0$  at  $(a, b)$

**Use the code: BVREDDY , to get maximum benefits**

66. Number of inflection points for the curve  $y = x + 2x^4$  is \_\_\_\_\_

(GATE-CE-1999)

- (a) 3
- (b) 1
- (c) 0
- (d) 2

Use the code: BVREDDY , to get maximum benefits

67. If  $f(x, y, z) = (x^2 + y^2 + z^2)^{-1/2}$ ,  $\frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} + \frac{\partial^2 f}{\partial z^2}$  is equal to \_\_\_\_\_

(GATE-EC-2000)

- (a) 0
- (b) 1
- (c) 2
- (d)  $-3(x^2 + y^2 + z^2)^{-5/2}$

68. The following function has local minima at which value of x,

$$f(x) = x\sqrt{5-x^2}$$

- (a)  $\frac{-\sqrt{5}}{2}$       (b)  $\sqrt{5}$       (c)  $\sqrt{\frac{5}{2}}$       (d)  $-\sqrt{\frac{5}{2}}$

Use the code: **BVREDDY**, to get maximum benefits

69. The function  $f(x,y) = 2x^2 + 2xy - y^3$  has

(GATE-EC-2000)

- (a) Only one stationary point at (0, 0)
- (b) Two stationary points at (0, 0) and (1/6, -1/3)
- (c) Two stationary points at (0, 0) and (1, -1)
- (d) No stationary point

70. The function  $f(x) = 2x^3 - 3x^2 - 36x + 2$  has its maxima at

(GATE-CS-2004)

- (a)  $x = -2$  only
- (b)  $x = 0$  only
- (c)  $x = 3$  only
- (d) both  $x = -2$  and  $x = 3$

Use the code: **BVREDDY**, to get maximum benefits

71. For the function  $f(x) = x^2 e^{-x}$ , the maximum occurs when  $x$  is equal to

- (a) 2
- (b) 1
- (c) 0
- (d) -1

**Use the code: BVREDDY , to get maximum benefits**

72. For real  $x$ , the maximum value of  $\frac{e^{\sin x}}{e^{\cos x}}$  is

(GATE-IN-2007)

- (a) 1
- (b)  $e$
- (c)  $e^{\sqrt{2}}$
- (d)  $\infty$

Use the code: BVREDDY , to get maximum benefits

73. The minimum value of function  $y = x^2$  in the interval  $[1, 5]$  is

(GATE-ME-2007)

- (a) 0
- (b) 1
- (c) 25
- (d) undefined

a) 1

Use the code: BVREDDY , to get maximum benefits

74. For the function  $f(x,y) = x^2 - y^2$  defined on  $\mathbb{R}^2$ , the point  $(0, 0)$  is (GATE-PI-2007)

- (a) a local minimum
- (b) Neither a local minimum (nor) a local maximum
- (c) a local maximum
- (d) Both a local minimum and a local maximum

**Use the code: BVREDDY , to get maximum benefits**

75. Consider the function  $f(x) = x^2 - x - 2$ . The maximum value of  $f(x)$  in the closed interval  $[-4, 4]$  is

**(GATE-EC-2007)**

- (a) 18
- (b) 10
- (c) -2.25
- (d) indeterminate

**Use the code: BVREDDY , to get maximum benefits**

76. Consider the function  $f(x) = (x^2 - 4)^2$  where  $x$  is a real number. Then the function has  
**(GATE-EE-2007)**

- (a) Only one minimum
- (b) Only two minima
- (c) Three minima
- (d) Three maxima

**Use the code: BVREDDY , to get maximum benefits**

77. A point on the curve is said to be an extremum if it is a local minimum (or) a local maximum. The number of distinct extrema for the curve  $3x^4 - 16x^3 + 24x^2 + 37$  is \_\_\_\_\_

(GATE-CS-2008)

- (a) 0
- (b) 1
- (c) 2
- (d) 3

78. Consider the function  $y = x^2 - 6x + 9$ . The maximum value of  $y$  obtained when  $x$  varies over the interval 2 to 5 is **(GATE-IN-2008)**

- (a) 1
- (b) 3
- (c) 4
- (d) 9

79. For real values of  $x$ , the minimum value of function

$$f(x) = e^x + e^{-x}$$
 is

(GATE-EC-2008)

80. At  $t = 0$ , the function  $f(t) = \frac{\sin t}{t}$  has

(GATE-EE-2010)

- (a) a minimum
- (b) a discontinuity
- (c) a point of inflection
- (d) a maximum

Use the code: BVREDDY , to get maximum benefits

81. If  $e^y = x^{1/x}$  then y has a

(GATE-EC-2010)

- (a) maximum at  $x = e$
- (b) minimum at  $x = e$
- (c) maximum at  $x = e^{-1}$
- (d) minimum at  $x = e^{-1}$

**Use the code: BVREDDY , to get maximum benefits**

82. Given a function  $f(x,y) = 4x^2 + 6y^2 - 8x - 4y + 8$ , the optimal values of  $f(x, y)$  is  
**(GATE-CE-2010)**

- (a) a minimum equal to  $\frac{10}{3}$
- (b) a maximum equal to  $\frac{10}{3}$
- (c) a minimum equal to  $\frac{8}{3}$
- (d) a maximum equal to  $\frac{8}{3}$

**Use the code: BVREDDY , to get maximum benefits**

83. The function  $f(x) = 2x - x^2 + 3$  has

(GATE-EE-2011)

- (a) a maxima at  $x = 1$  and a minima at  $x = 5$
- (b) a maxima at  $x = 1$  and a minima at  $x = -5$
- (c) only a maxima at  $x = 1$
- (d) only a minima at  $x = 1$

Use the code: **BVREDDY**, to get maximum benefits

84. The maximum value of  $f(x) = x^3 - 9x^2 + 24x + 5$  in the interval  $[1, 6]$  is



GATE- 2012

**Use the code: BVREDDY , to get maximum benefits**

85. At  $x = 0$ , the function  $f(x) = x^3 + 1$  has

(GATE-ME,PI-2012)

- (a) a maximum value
- (b) a minimum value
- (c) a singularity
- (d) a point of inflection

Use the code: BVREDDY , to get maximum benefits

86. For  $0 \leq t < \infty$ , the maximum value of the function

$$f(t) = e^{-t} - 2e^{-2t}$$
 occurs at

- (a)  $t = \log_e 4$
- (b)  $t = \log_e 2$
- (c)  $t = 0$
- (d)  $t = \log_e 8$

87. The maximum value of the function  $f(x) = \ln(1+x) - x$  (where  $x > -1$ ) occurs at  $x = \underline{\hspace{2cm}}$ . **(GATE-EC-SET-3-2014)**

**Use the code: BVREDDY , to get maximum benefits**

88. The maximum value of  $f(x) = 2x^3 - 9x^2 + 12x - 3$  in the interval  $0 \leq x \leq 3$  is \_\_\_\_.

GATE-2014

2

Use the code: BVREDDY , to get maximum benefits

89. Let  $f(x) = xe^{-x}$ . The maximum value of the function in the interval  $(0, \infty)$  is
- (a)  $e^{-1}$       (b)  $e$       (c)  $1 - e^{-1}$       (d)  $1 + e^{-1}$

**GATE-2014**

**Use the code: BVREDDY , to get maximum benefits**

90. Minimum of the real valued function  $f(x) = (x-1)^{2/3}$  occurs at  $x$  equal to

(a)  $-\infty$

(b) 0

(c) 1

(d)  $\infty$

**GATE-2014**

**Use the code: BVREDDY , to get maximum benefits**

91. The minimum value of the function  $f(x) = x^3 - 3x^2 - 24x + 100$  in the interval  $[-3, 3]$  is (GATE-EC-SET-2-2014)

- (a) 20
- (b) 28
- (c) 16
- (d) 32

O

**Use the code: BVREDDY , to get maximum benefits**

92. While minimizing the function  $f(x)$ , necessary and sufficient conditions for a point,  $x_0$  to be a minima are : (GATE-CE-2015)

- (a)  $f'(x_0) > 0$  and  $f''(x_0) = 0$
- (b)  $f'(x_0) < 0$  and  $f''(x_0) = 0$
- (c)  $f'(x_0) = 0$  and  $f''(x_0) < 0$
- (d)  $f'(x_0) = 0$  and  $f''(x_0) > 0$

**Use the code: BVREDDY , to get maximum benefits**

93. The value of  $\varepsilon$  in the mean value theorem of  $f(b) - f(a) = (b-a) f'(\varepsilon)$  for  $f(x) = Ax^2 + Bx + C$  in  $(a, b)$  is **(GATE-EC-1994)**

- (a)  $b + a$
- (b)  $b - a$
- (c)  $\frac{b + a}{2}$
- (d)  $\frac{b - a}{2}$

**Use the code: BVREDDY , to get maximum benefits**

94. If  $f(0) = 2$  and  $f'(x) = \frac{1}{5-x^2}$ , then the lower and upper bounds of  $f(1)$  estimated by the mean value theorem are \_\_\_\_\_  $f(x)$  is defined in  $[0, 1]$  (GATE-EC-1995)

- (a) 1.9, 2.2 (b) 2.2, 2.25 (c) 2.25, 2.5 (d) None of the above

Use the code: BVREDDY , to get maximum benefits

95. A function  $f(x) = 1 - x^2 + x^3$  is defined in the closed interval  $[-1, 1]$ . The value of  $x$ , in the open interval  $(-1, 1)$  for which the mean value theorem is satisfied, is

**(GATE-EC-2015)**

- (a)  $-1/2$
- (b)  $-1/3$
- (c)  $1/3$
- (d)  $1/2$

**Use the code: BVREDDY , to get maximum benefits**

96. If a continuous function  $f(x)$  does not have a root in the interval  $[a, b]$ , then which one of the following statements is TRUE ? **(GATE-EE-2015)**

- (a)  $f(a).f(b) = 0$
- (b)  $f(a).f(b) < 0$
- (c)  $f(a).f(b) > 0$
- (d)  $f(a)/f(b) \leq 0$

**Use the code: BVREDDY , to get maximum benefits**

97. The third term in the taylor's series expansion of  $e^x$  about 'a' would be \_\_\_\_\_

- (a)  $e^a (x-a)$       (b)  $\frac{e^a}{2} (x-a)^2$       (c)  $\frac{e^a}{2}$       (d)  $\frac{e^a}{6} (x-a)^3$

GATE -1995

o

Use the code: BVREDDY , to get maximum benefits

98. The taylor's series expansion of sin x is \_\_\_\_\_ (GATE-EC-1998)

(a)  $1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots$

(b)  $1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots$

(c)  $x + \frac{x^3}{3!} + \frac{x^5}{5!} + \dots$

(d)  $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$

Use the code: BVREDDY , to get maximum benefits

99. A discontinuous real function can be expressed as

(GATE-CE-1998)

- (a) Taylor's series and Fourier's series
- (b) Taylor's series and not by Fourier's series
- (c) neither Taylor's series nor Fourier's series
- (d) not by Taylor's series, but by Fourier's series

**Use the code: BVREDDY , to get maximum benefits**

100. The Taylor series expansion of  $\sin x$  about  $x = \frac{\pi}{6}$  is given by (GATE-CE-2000)

(a)  $\frac{1}{2} + \frac{\sqrt{3}}{2} \left( x - \frac{\pi}{6} \right) - \frac{1}{4} \left( x - \frac{\pi}{6} \right)^2 - \frac{\sqrt{3}}{12} \left( x - \frac{\pi}{6} \right)^3 + \dots$

(b)  $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$

(c)  $\frac{x - \frac{\pi}{6}}{1!} - \frac{\left( x - \frac{\pi}{6} \right)^3}{3!} + \frac{\left( x - \frac{\pi}{6} \right)^5}{5!} - \frac{\left( x - \frac{\pi}{6} \right)^7}{7!} + \dots$

(d)  $\frac{1}{2}$

Use the code: BVREDDY , to get maximum benefits

101. Limit of the following series as x approaches

$$\frac{\pi}{2} \text{ is } f(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$$

- (a)  $\frac{2\pi}{3}$       (b)  $\frac{\pi}{2}$       (c)  $\frac{\pi}{3}$       (d) 1      (GATE-CE-2001)

Use the code: BVREDDY , to get maximum benefits

102. For the function  $e^{-x}$ , the linear approximation around  $x = 2$  is

(a)  $(3-x)e^{-2}$

(b)  $1 - x$

(c)  $\left[3 + 2\sqrt{2} - (1 + \sqrt{2})x\right]e^{-2}$

(d)  $e^{-2}$

GATE- 2007

Use the code: BVREDDY , to get maximum benefits

103. For  $|x| \ll 1$ ,  $\cot h(x)$  can be approximated as **(GATE-EC-2007)**

(a)  $x$

(b)  $x^2$

(c)  $\frac{1}{x}$

(d)  $\frac{1}{x^2}$

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104. The expression  $e^{\ln x}$  for  $x > 0$  is equal to

- (a)  $-x$
- (b)  $x$
- (c)  $x^{-1}$
- (d)  $-x^{-1}$

**(GATE-IN-2008)**

105. Which of the following function would have only odd powers of x in its Taylor series expansion about the point  $x = 0$ ? **(GATE-EC-2008)**

- (a)  $\sin(x^3)$
- (b)  $\sin(x^2)$
- (c)  $\cos(x^3)$
- (d)  $\cos(x^2)$

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106. In the Taylor series expansion of  $e^x + \sin x$  about the point  $x = \pi$ , the coefficient of  $(x - \pi)^2$  is **(GATE-EC-2008)**

- (a)  $e^\pi$
- (b)  $0.5 e^\pi$
- (c)  $e^\pi + 1$
- (d)  $e^\pi - 1$

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107. In the Taylor series expansion of  $e^x$  about  $x = 2$ , the coefficient of  $(x-2)^4$  is  
**(GATE-ME-2008)**

(a)  $\frac{1}{4!}$

(b)  $\frac{2^4}{4!}$

(c)  $\frac{e^2}{4!}$

(d)  $\frac{e^4}{4!}$

**Use the code: BVREDDY , to get maximum benefits**

108. The Taylor series expansion of  $\frac{\sin x}{x - \pi}$  at  $x = \pi$  is given by (GATE-EC-2010)

(a)  $1 + \frac{(x - \pi)^2}{3!} + \dots$

(c)  $1 - \frac{(x - \pi)^2}{3!} + \dots$

(b)  $-1 - \frac{(x - \pi)^2}{3!} + \dots$

(d)  $-1 + \frac{(x - \pi)^2}{3!} + \dots$

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109. The infinite series  $f(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$  Converges to (ME-2010)

- (a)  $\cos(x)$
- (b)  $\sin(x)$
- (c)  $\sin h(x)$
- (d)  $e^x$

Use the code: BVREDDY , to get maximum benefits

110. A series expansion for the function  $\sin\theta$  is \_\_\_\_\_

(GATE-ME-2011)

(a)  $1 - \frac{\theta^2}{2!} + \frac{\theta^4}{4!} - \dots$

(b)  $\theta - \frac{\theta^3}{3!} + \frac{\theta^5}{5!} - \dots$

(c)  $1 + \theta + \frac{\theta^2}{2!} + \frac{\theta^3}{3!} + \dots$

(d)  $\theta + \frac{\theta^3}{3!} + \frac{\theta^5}{5!} + \dots$

Use the code: BVREDDY , to get maximum benefits

**111.** Consider the following inequalities.

- (i)  $3p - q < 4$
- (ii)  $3q - p < 12$

Which one of the following expressions below satisfies the above two inequalities?

**(GATE-2022-PI)**

- (a)  $8 \leq p + q < 16$
- (b)  $p + q = 8$
- (c)  $p + q \geq 16$
- (d)  $p + q < 8$

**Use the code: BVREDDY , to get maximum benefits**

112. The infinite series  $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \dots$  corresponds to (GATE-CE-2012)
- (a)  $\sec x$       (b)  $e^x$       (c)  $\cos x$       (d)  $1 + \sin^2 x$

Use the code: BVREDDY , to get maximum benefits

113. The Taylor series expansion of  $3 \sin x + 2\cos x$  is

(GATE-EC-SET-1-2014)

(a)  $2 + 3x - x^2 - \frac{x^3}{2} + \dots$

(b)  $2 - 3x + x^2 - \frac{x^3}{2} + \dots$

(c)  $2 + 3x + x^2 + \frac{x^3}{2} + \dots$

(d)  $2 - 3x - x^2 + \frac{x^3}{2} + \dots$

Use the code: BVREDDY , to get maximum benefits

114. In which of the following functions Mean Value theorem is not applicable?

- (i)  $y = \frac{1}{x}$ ,  $x \in [-1, 1]$
  - (ii)  $y = |x|$ ,  $x \in [-1, 1]$
  - (iii)  $y = x \sin \frac{1}{x}$ ,  $x \in \left[ +\frac{\pi}{4}, \frac{\pi}{2} \right]$
  - (iv)  $y = \sin k \left[ 0, \frac{\pi}{2} \right]$
- (A) (i), (ii), (iii)      (B) (i), (ii)  
(C) (i), (iii)      (D) (i), (ii), (iii), (iv)

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**115.** Which one of the following not the correct statement?

- (a) The function  $\sqrt[x]{x}$ , ( $x > 0$ ), has the global minimum at  $x = e$
- (b) The function  $|x|$  has the global minima at  $x = 0$
- (c) The function  $x^3$  has neither global minima nor global maxima
- (d) The function  $\sqrt[x]{x}$ , ( $x > 0$ ), has the global maxima at  $x = e$

**(GATE-19-CE)**

**Use the code: BVREDDY , to get maximum benefits**

**116.** The following inequality is true for all x close to zero.  $\left(2 - \frac{x^2}{3}\right) < \frac{x\sin x}{1-\cos x} < 2$ , what is the value  $\lim_{x \rightarrow 0} \frac{x\sin x}{1-\cos x}$  ?

**(GATE-19-CE)**

(a) 2

(b) 1

(c) 0

(a)  $\frac{1}{2}$

**Use the code: BVREDDY , to get maximum benefits**

117. If  $f(x)$  satisfies Rolles theorem on  $[a,b]$ , then

the value of  $\int_a^b f'(x) dx$  is \_\_\_\_.

- (A)  $f(b)-f(a)$
- (B)  $f(a)$
- (C)  $f(b)$
- (D) 0

Use the code: **BVREDDY** , to get maximum benefits

**118.** Consider the polynomial  $f(x) = x^3 - 6x^2 + 11x - 6$  on the domain S given by  $1 \leq x \leq 3$ . the first and second derivatives are  $f'(x)$ and  $f''(x)$ .

Consider the following statements.

- I. The given polynomial is zero at the boundary points  $x = 1$  and  $x = 3$
- II. There exists one local maxima of  $f(x)$  within the domain S.
- III. The second derivative  $f''(x) > 0$  throughout the domain S.
- IV. There exists one local minima of  $f(x)$  within the domain S.

The correct option is.

**(GATE-2022-CE)**

- (a) Only statements I, II and III are correct
- (b) Only statements I, II and IV are correct
- (c) Only statements I and IV are correct
- (d) Only statements II and IV are correct

**Use the code: BVREDDY , to get maximum benefits**

119. The value of the following limit is \_\_\_\_\_

$$\lim_{x \rightarrow 0^+} \frac{\sqrt{x}}{1 - e^{2\sqrt{x}}}$$

(GATE-2022-CSE)

Use the code: BVREDDY , to get maximum benefits

**120.** A function  $y(x)$  is defined in the interval  $[0, 1]$  on the x-axis as

$$y(x) = \begin{cases} 2 & \text{if } 0 \leq x < \frac{1}{3} \\ 3 & \text{if } \frac{1}{3} \leq x \leq \frac{3}{4} \\ 1 & \text{if } \frac{3}{4} \leq x \leq 1 \end{cases}$$

Which one of the following is the area under the curve for the interval  $[0, 1]$  on the x-axis?

(GATE-2022-CSE)

- (a)  $\frac{5}{6}$
- (b)  $\frac{6}{5}$
- (c)  $\frac{13}{6}$
- (d)  $\frac{6}{13}$

**Use the code: BVREDDY , to get maximum benefits**

**121.** Let ‘r’ be a root of the equation  $x^2 + 2x + 6 = 0$ . Then the value of the expression  $(r + 2)(r + 3)(r + 4)(r + 5)$  is?

**(GATE-2022-CSE)**

- (a) 51
- (b) -51
- (c) 126
- (d) -126

122. Define  $[x]$  as the greatest integer less than or equal to  $x$ , for each  $x \in (-\infty, \infty)$ . If  $y = [x]$ , then area under  $y$  for  $x \in [1, 4]$  is \_\_\_\_\_.

- (a) 3
- (b) 1
- (c) 6
- (d) 4

**GATE- 2020 (ME)**

**Use the code: BVREDDY , to get maximum benefits**

123. The value of  $\lim_{x \rightarrow 1} \left( \frac{1 - e^{-c(1-x)}}{1 - xe^{-c(1-x)}} \right)$

GATE- 2020 (ME)

(a)  $c + 1$

(b)  $\frac{c+1}{c}$

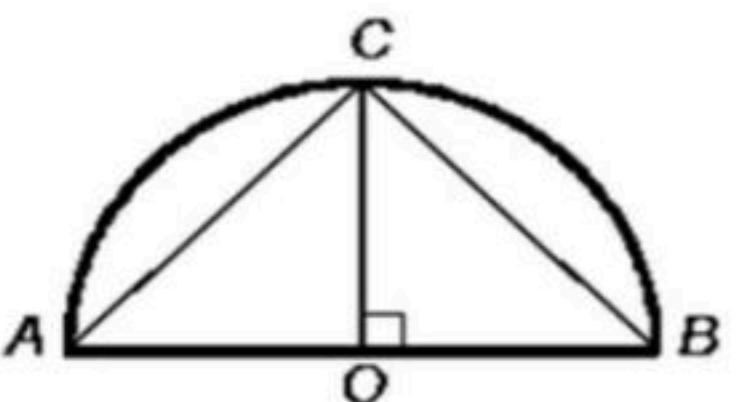
(c)  $c$

(d)  $\frac{c}{c+1}$

Use the code: BVREDDY , to get maximum benefits

124. Given a semicircle with  $O$  as the centre; as shown in the figure, the ratio  $\frac{\overline{AC} + \overline{CB}}{\overline{AB}}$  is \_\_\_\_\_ . Where  $\overline{AC}$ ,  $\overline{CB}$  and  $\overline{AB}$  are chords.

GATE- 2020 (EE)



- (a)  $\sqrt{2}$
- (b)  $\sqrt{3}$
- (c) 2
- (d) 3

Use the code: BVREDDY , to get maximum benefits

125. The real numbers,  $x$  and  $y$  with  $y = 3x^2 + 3x + 1$ , the maximum and minimum value of  $y$  for  $x \in [-2, 0]$  are respectively \_\_\_\_\_ .

GATE- 2020 (EE)

- (a) 7 and  $\frac{1}{4}$
- (b) 7 and 1
- (c) -2 and  $\frac{-1}{2}$
- (d) 1 and  $\frac{1}{4}$

Use the code: BVREDDY , to get maximum benefits

GATE- 2020 (CE)

**Use the code: BVREDDY , to get maximum benefits**

127. Consider the functions:

- I.  $e^{-x}$
- II.  $x^2 - \sin x$
- III.  $\sqrt{x^3 + 1}$

Which of the above functions is/are increasing everywhere in  $[0, 1]$ ?

- (a) I and III only
- (b) II and III only
- (c) III only
- (d) II only

GATE- 2020 (CS)

Use the code: BVREDDY , to get maximum benefits

128. Consider the function  $f(x, y) = x^2 + y^2$ . The minimum value of the function attains on the line  $x + y = 1$  (rounded off to two decimal places) is \_\_\_\_\_.

**GATE- 2020 (IN)**

**Use the code: BVREDDY , to get maximum benefits**

129. Let  $f(x)$  be a real-valued function such that  $f'(x_0)=0$  for some  $x_0 \in (0,1)$ , and  $f''(x) > 0$  for all  $x \in (0,1)$ . Then  $f(x)$  has

- (a) exactly one local minimum in  $(0,1)$
- (b) one local maximum in  $(0,1)$
- (c) no local minimum in  $(0,1)$
- (d) two distinct local minima in  $(0,1)$

**GATE- 2021 (EE)**

**Use the code: BVREDDY , to get maximum benefits**

130. A function,  $\lambda$ , is defined by

$$\lambda(p, q) = \begin{cases} (p - q)^2, & \text{if } p \geq q \\ p + q, & \text{if } p < q \end{cases}$$

**GATE- 2021 (CE)**

The value of the expression  $\frac{\lambda(-(-3+2), (-2+3))}{(-(2+1))}$  is

- (a)  $\frac{16}{3}$
- (b) -1
- (c) 0
- (d) 16

**Use the code: BVREDDY , to get maximum benefits**

131. If  $\left(x - \frac{1}{2}\right)^2 - \left(x - \frac{3}{2}\right)^2 = x + 2$ , then the value of  $x$  is :

**GATE- 2021 (CS)**

- (a) 2
- (b) 8
- (c) 4
- (d) 6

**Use the code: BVREDDY , to get maximum benefits**

132. Suppose that  $f: R \rightarrow R$  is a continuous function on the interval  $[-3, 3]$  and a differentiable function in the interval  $(-3, 3)$  such that for every  $x$  in the interval.  $f'(x) \leq 2$ . If  $f(-3) = 7$ , then  $f(3)$  is at most \_\_\_\_\_.

**GATE- 2021 (CS)**

**Use the code: BVREDDY , to get maximum benefits**

133. Consider the following expression:

$$\lim_{x \rightarrow -3} \frac{\sqrt{2x+22}-4}{x+3}$$

**GATE- 2021 (CS)**

The value of the above expression (rounded to 2 decimal places) is \_\_\_\_\_.

**Use the code: BVREDDY , to get maximum benefits**

134.  $p$  and  $q$  are positive integers and  $\frac{p}{q} + \frac{q}{p} = 3$ ,

**GATE- 2021 (CS)**

then,  $\frac{p^2}{q^2} + \frac{q^2}{p^2} =$

- |        |       |
|--------|-------|
| (a) 3  | (b) 9 |
| (c) 11 | (d) 7 |

**Use the code: BVREDDY , to get maximum benefits**

135. A straight line of the form  $y = mx + c$  passes through the origin and the point  $(x, y) = (2, 6)$ . The value of  $m$  is \_\_\_\_\_.

(GATE-16-EC)

**Use the code: BVREDDY , to get maximum benefits**

136. Consider the function  $f(x) = -x^2 + 10x + 100$ . The minimum value of the function in the interval  $[5, 10]$  is \_\_\_\_\_. GATE- 2021 (CS)

**Use the code: BVREDDY , to get maximum benefits**

137. Let  $f: [-1,1] \rightarrow \mathbb{R}$ , where  $f(x) = 2x^3 - x^4 - 10$ . The minimum value of  $f(x)$  is \_\_\_\_\_.

(GATE-16-IN)

**Use the code: BVREDDY , to get maximum benefits**

138. Consider the function  $f(x) = 2x^3 - 3x^2$  in the domain  $[-1, 2]$ . The global minimum of  $f(x)$  is \_\_\_\_\_.

(GATE-16-ME)

**Use the code: BVREDDY , to get maximum benefits**

**139.** The values of  $x$  for which the function  $f(x) = \frac{x^2 - 3x - 4}{x^2 + 3x - 4}$  is NOT continuous are

**(GATE-16-ME)**

- (a) 4 and -1
- (b) 4 and 1
- (c) -4 and 1
- (d) -4 and -1

**Use the code: BVREDDY , to get maximum benefits**

140.  $\lim_{x \rightarrow 0} \frac{\log_e(1+4x)}{e^{3x}-1}$  is equal to

(GATE-16-ME)

(a) 0

(b)  $\frac{1}{12}$

(c)  $\frac{4}{3}$

(d) 1

Use the code: BVREDDY , to get maximum benefits

**141.**  $\lim_{x \rightarrow \infty} (\sqrt{x^2 + x - 1} - x)$  is

**(GATE-16-ME)**

- (a) 0
- (b)  $\infty$
- (c)  $\frac{1}{2}$
- (d)  $-\infty$

**Use the code: BVREDDY , to get maximum benefits**

**142.** At  $x = 0$ , the function is

$$f(x) = \left| \sin \frac{2\pi x}{L} \right| \quad (-\infty < x < \infty, L > 0)$$

**(GATE-16-PI)**

- (a) continuous and differentiable.
- (b) not continuous and not differentiable.
- (c) not continuous but differentiable.
- (d) continuous but not differentiable

**Use the code: BVREDDY , to get maximum benefits**

143. Absolute maxima or minima of a function  $f(x)$  occur

- (A) Only at the end point of the curve
- (B) Only at the critical points of the curve
- (C) Both at the end point and critical points of the curve
- (D) Either at the end point or at the critical point of the curve

**Use the code: BVREDDY , to get maximum benefits**

**144.** The range of values of k for which the function  $f(x) = (k^2 - 4)x^2 + 6x^3 + 8x^4$  has a local maxima at point  $x = 0$  is **(GATE-16-PI)**

- (a)  $k < -2$  or  $k > 2$
- (b)  $k \leq -2$  or  $k \geq 2$
- (c)  $-2 < k < 2$
- (d)  $-2 \leq k \leq 2$

**Use the code: BVREDDY , to get maximum benefits**

145.  $\lim_{x \rightarrow 0} \left( \frac{e^{5x}-1}{x} \right)^2$  is equal to \_\_\_\_\_.

(GATE-16-PI)

Use the code: BVREDDY , to get maximum benefits

$$146. \lim_{x \rightarrow 4} \frac{\sin(x-4)}{x-4} = \underline{\hspace{2cm}}$$

(GATE-16-CSE)

Use the code: BVREDDY , to get maximum benefits

**147.** The quadratic approximation of  $f(x) = x^3 - 3x^2 - 5$  at the point  $x = 0$  is

- (a)  $3x^2 - 6x + 5$       (b)  $-3x^2 - 5$       (c)  $-3x^2 + 6x - 5$       (d)  $3x^2 - 5$       **(GATE-16-PI)**

**Use the code: BVREDDY , to get maximum benefits**

**148.** The minimum value of the function  $f(x) = \frac{1}{3}x(x^2 - 3)$  in the interval  $-100 \leq x \leq 100$  occurs at  $x = \underline{\hspace{2cm}}$ .

(GATE-17-EC)

**Use the code: BVREDDY , to get maximum benefits**

**149.** Let  $f(x) = e^{x+x^2}$  for real  $x$ . From among the following. Choose the Taylor series approximation of  $f(x)$  around  $x = 0$ , which includes all powers of  $x$  less than or equal to 3.

**(GATE-17-EC)**

(a)  $1 + x + x^2 + x^3$

(b)  $1 + x + \frac{3}{2}x^2 + x^3$

(c)  $1 + x + \frac{3}{2}x^2 + \frac{7}{6}x^3$

(d)  $1 + x + 3x^2 + 7x^3$

**Use the code: BVREDDY , to get maximum benefits**

**150.** A function  $f(x)$  is defined as  $f(x) = \begin{cases} e^x, & x < 1 \\ \ln x + ax^2 + bx, & x \geq 1 \end{cases}$ , where  $x \in \mathbb{R}$ . Which one of the following statements is TRUE?

- (a)  $f(x)$  is NOT differentiable at  $x = 1$  for any values of  $a$  and  $b$ . **(GATE-17-EE)**
- (b)  $f(x)$  is differentiable at  $x = 1$  for the unique values of  $a$  and  $b$ .
- (c)  $f(x)$  is differentiable at  $x = 1$  for all values of  $a$  and  $b$  such that  $a + b = e$ .
- (d)  $f(x)$  is differentiable at  $x = 1$  for all values of  $a$  and  $b$ .

**Use the code: BVREDDY , to get maximum benefits**

**151.** Consider the following inequalities.

(i)  $2x - 1 > 7$

(ii)  $2x - 9 < 1$

Which one of the following expressions below satisfies the above two inequalities?

**(GATE-2022-ECE)**

(a)  $x \leq -4$

(b)  $-4 < x \leq 4$

(c)  $4 < x < 5$

(d)  $x \geq 5$

**Use the code: BVREDDY , to get maximum benefits**

**152.** The function  $f(x) = 8 \log_e x - x^2 + 3$  attains its minimum over the interval  $[1,e]$  at  $x = \underline{\hspace{2cm}}$  (Here  $\log_e x$  is the natural logarithm of  $x$ .) (GATE-2022-ECE)

- (a) 2
- (b) 1
- (c) e
- (d)  $\frac{1+e}{2}$

**Use the code: BVREDDY , to get maximum benefits**

153. In the open interval  $(0,1)$ , the polynomial  $p(x) = x^4 - 4x^3 + 2$  has
- (a) no real roots
  - (b) two real roots
  - (c) one real root
  - (d) three real roots

**Use the code: BVREDDY , to get maximum benefits**

**154.** Let  $y^2 - 2y + 1 = x$  and  $\sqrt{x} + y = 5$ . The value of  $x + \sqrt{y}$  equals \_\_\_\_\_. (Given the answer up to three decimal places)

**(GATE-17-EE)**

**Use the code: BVREDDY , to get maximum benefits**

155. Rolle's theorem cannot be applicable for

- (A)  $f(x) = \sqrt{4 - x^2}$  in  $[-2, 2]$
- (B)  $f(x) = [x]$  in  $[-1, 1]$
- (C)  $f(x) = x^2 + 3x - 4$  in  $[-4, 1]$
- (D)  $f(x) = \cos 2x$  in  $[0, \pi]$

Use the code: **BVREDDY**, to get maximum benefits

156. The number C that satisfy the conclusion of mean value theorem for  $f(x) = x + (4/x)$  in the interval  $[1, 8]$  is
- (a) 4.5
  - (b) 3.5
  - (c)  $2\sqrt{2}$
  - (d) 5

Use the code: **BVREDDY**, to get maximum benefits

157. If  $f'(x) = \frac{1}{1+x^2}$  for all  $x$  &  $f(0) = 0$  then an

interval in which  $f(2)$  lies, is

- (a)  $(2, 4)$
- (b)  $(0.4, 2)$
- (c)  $(0, 0.4)$
- (d)  $(0.1, 0.2)$

158. The value C of Cauchy's mean value theorem for  $f(x) = e^x$  and  $g(x) = e^{-x}$  in the interval  $(2, 3)$  is \_\_\_\_\_.

**159.** The Taylor's series expansion of  $f(x) = e^{\sin x}$  about  $x = 0$ , is

(a)  $f(x) = 1 + x + \frac{x^2}{2} + \dots$

(b)  $f(x) = x + \frac{x^2}{2} + \frac{x^3}{3} + \dots$

(c)  $f(x) = 1 - x + \frac{x^2}{2} - \dots$

(d)  $f(x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \dots$

**Use the code: BVREDDY , to get maximum benefits**

160. In the Taylor's series expansion of  $f(x) = \log \sec x$   
about  $x = 0$ , coefficient of  $x^4 = \underline{\hspace{2cm}}$ .

(a)  $\frac{1}{12}$

(b)  $\frac{1}{14}$

(c) 12

(d) 14

Use the code: BVREDDY , to get maximum benefits

161. The maximum value of the function

$$f(x) = \frac{x^3}{3} - x \text{ occurs at}$$

- (a) 1
- (b) -1
- (c)  $\frac{1}{\sqrt{3}}$
- (d) 0

Use the code: **BVREDDY**, to get maximum benefits

**162.** The maximum value of the function

$$f(x) = x^3 - 6x^2 + 9x + 1 \text{ in } [0, 2] \text{ is } \underline{\hspace{2cm}}.$$

**Use the code: BVREDDY , to get maximum benefits**

163. The maximum value of the function

$$x^3 + 3xy^2 - 15x^2 - 15y^2 + 72x \text{ is } \underline{\hspace{2cm}}.$$

Use the code: BVREDDY , to get maximum benefits

164. The maximum value of the determinant among all  $2 \times 2$  real symmetric matrices with trace 10 is \_\_\_\_\_.

**Use the code: BVREDDY , to get maximum benefits**

165. Find 'C' of Rolle's Theorem for

$$f(x) = e^x (\sin x - \cos x) \text{ in } [\pi/4, 5\pi/4]$$

(a)  $\pi / 2$

(b)  $3\pi / 4$

(c)  $\pi$

(d) does not exist

Use the code: BVREDDY , to get maximum benefits

166. The mean value C of Lagrange's Theorem

for the function  $f(x) = 3x^2 + 5x + 8$  in

$$\left[ \frac{11}{2}, \frac{13}{2} \right] \text{ is } \underline{\hspace{2cm}}$$

Use the code: BVREDDY , to get maximum benefits

**167.** If  $f(x) = \frac{1}{x}$ ,  $g(x) = \frac{1}{x^2}$  in  $[1, 2]$  then the

mean value  $C$  of Cauchy's mean value theorem is

- (a)  $\frac{4}{3}$
- (b)  $\frac{5}{4}$
- (c)  $\frac{5}{3}$
- (d) none of these

**168.** How many of the following functions satisfy Lagrange's mean value theorem in the given interval?

$$f(x) = |x + 2| \quad \text{in } [-2, 0]$$

$$g(x) = 2 + (4 - x)^{1/3} \quad \text{in } [1, 6]$$

$$h(x) = \log(1 + x^3) \quad \text{in } [0, 3]$$

$$p(x) = \begin{cases} 1+x^2, & 0 \leq x < 1 \\ 1, & x = 1 \end{cases}$$

169. Let  $f(x)$  and  $g(x)$  be differentiable for  $0 \leq x \leq 2$  such that  $f(0) = 4$ ,  $f(2) = 8$ ,  $g(0) = 0$  and  $f'(x) = g'(x)$  for all  $x$  in  $[0, 2]$  then the value of  $g(2)$  must be\_\_\_\_\_.

**Use the code: BVREDDY , to get maximum benefits**

170. The function  $f(x) = 3x^4 - 4x^3 + 10$  has a minimum value at  $x = \underline{\hspace{2cm}}$ .

**Use the code: BVREDDY , to get maximum benefits**

171. The maximum value of the function

$$f(x) = x^3 - 9x^2 + 24x + 5 \text{ in } [1,6] \text{ is}$$

**Use the code: BVREDDY , to get maximum benefits**

**172.** If  $f(x) = a \log x + bx^2 - x$  has its extreme values at  $x = -1$  and  $x = 2$  then

- (a)  $a = 2, b = -1$
- (b)  $a = 2, b = -1 / 2$
- (c)  $a = -2, b = 2$
- (d)  $a = -2, b = 1 / 2$

**Use the code: BVREDDY , to get maximum benefits**

173. The function  $f(x, y) = x^3 - 3x^2 + 4y^2 - 10$  at  $(2,0)$  has

- (a) a maximum
- (b) a minimum
- (c) a saddle point
- (d) both (a) & (b)

**Use the code: BVREDDY , to get maximum benefits**

**174.** The function

$$f(x, y) = x^2y - 3xy + 2y + x$$
 has

- (a) no local extremum
- (b) one local minimum but no local maximum
- (c) one local maximum but no local minimum
- (d) one local minimum and one local maximum

**Use the code: BVREDDY , to get maximum benefits**

175. If  $f(x,y) = xy + (x - y)$  then the saddle point  
of  $f(x, y)$  is

- (a)  $(1, -1)$
- (b)  $(-1, 1)$
- (c)  $(-1, -1)$
- (d)  $(1, 1)$

176. The distance between origin and a point nearest to it on the surface  $z^2 = 1 + xy$  is

- (a)  $\sqrt{3}$
- (b)  $\sqrt{2}$
- (c) 1
- (d) none of these

**177.** If  $f(x) = x^2 \sin\left(\frac{1}{x}\right)$  then which of the following is true?

- (a)  $f'(0)$  exists but  $f''(0)$  does not exist
- (b) both  $f'(0)$  and  $f''(0)$  exist
- (c) neither  $f'(0)$  nor  $f''(0)$  does not exist
- (d)  $f'(0)$  does not exist but  $f''(0)$  exists

**178.** If  $f(x) = x \left(1 + \left(\frac{1}{3}\right) \sin(\log x)\right)$  then  $f(x)$  is

- (a) continuous at  $x = 0$  but not differentiable at  $x = 0$
- (b) differentiable at  $x=0$  but not continuous at  $x = 0$
- (c) continuous and differentiable at  $x = 0$
- (d) neither continuous nor differentiable at  $x = 0$

**Use the code: BVREDDY , to get maximum benefits**

**179.** The function  $f(x) = |x| + |x + 1| + |x - 2|$  is differentiable at  $x =$

- (a) 1      (b) - 1  
(c) 0      (d) 2

**180.** Find C of the Rolle's theorem for

$$f(x) = x(x - 1)(x - 2) \text{ in } [1, 2]$$

(a) 1.5

(b)  $1 - (1/\sqrt{3})$

(c)  $1 + (1/\sqrt{3})$

(d) 1.25

**Use the code: BVREDDY , to get maximum benefits**

181. Find C of Rolle's theorem for

$$f(x) = (x + 2)^3 (x - 3)^4 \text{ in } [-2, 3]$$

- (a) 1/7
- (b) 2/7
- (c) 1/2
- (d) 3/2

Use the code: **BVREDDY** , to get maximum benefits

**182.** Find C of the Rolle's theorem for

$$f(x) = e^x \sin x \text{ in } [0, \pi]$$

- (a)  $\pi/4$
- (b)  $\pi/2$
- (c)  $3\pi/4$
- (d) does not exist

**Use the code: BVREDDY , to get maximum benefits**

$$183. \lim_{x \rightarrow 0} [(e^{2x} - 1) \cot 3x] =$$

- (a) 0
- (b)  $\frac{3}{2}$
- (c) 1
- (d)  $\frac{2}{3}$

Use the code: **BVREDDY**, to get maximum benefits

184. Find C of Rolle's theorem for

$$f(x) = \log[(x^2 + ab) / (a+b)x] \text{ in } [a,b]$$

- (a)  $(a+b)/2$
- . (b)  $\sqrt{ab}$
- (c)  $2ab / (a + b)$
- (d)  $(b - a)/2$

Use the code: **BVREDDY**, to get maximum benefits

- 185.** Rolle's theorem cannot be applied for the function  $f(x) = |x|$  in  $[-2, 2]$  because
- (a)  $f(x)$  is not continuous in  $[-2, 2]$
  - (b)  $f(x)$  is not differentiable in  $(-2, 2)$
  - (c)  $f(-2) \neq f(2)$
  - (d) none of the above

**Use the code: BVREDDY , to get maximum benefits**

**186.** Find C of Lagrange's mean value theorem

for  $f(x) = \log x$  in  $[1, e]$

(a)  $e - 2$

(b)  $e - 1$

(c)  $(e + 1) / 2$

(d)  $(e - 1) / 2$

**Use the code: BVREDDY , to get maximum benefits**

**187.** Find C of Lagrange's mean value theorem

for  $f(x) = lx^2 + mx + n$  in  $[a, b]$

- |                     |                 |
|---------------------|-----------------|
| (a) $(a + b) / 2$   | (b) $\sqrt{ab}$ |
| (c) $2ab / (a + b)$ | (d) $(b - a)/2$ |

**Use the code: BVREDDY , to get maximum benefits**

**188.** Find C of Lagrange's theorem mean value

theorem for  $f(x) = 7x^2 - 13x - 19$  in

$[-11/7, 13/7]$

- (a)  $1/7$
- (b)  $2/7$
- (c)  $3/7$
- (d)  $4/7$

**Use the code: BVREDDY , to get maximum benefits**

**189.** Find C of Lagrange's mean value theorem

for  $f(x) = e^x$  in  $[0, 1]$

- (a) 0.5
- (b)  $\log(e - 1)$
- (c)  $\log(e + 1)$
- (d)  $\log[(e + 1)/ (e - 1)]$

**Use the code: BVREDDY , to get maximum benefits**

**190.** Find C of Cauchy's mean value theorem for

the functions  $1/x$  and  $1/x^2$  in  $[a, b]$

(a)  $(a + b)/2$

(b)  $\sqrt{ab}$

(c)  $2ab / (a + b)$

(d)  $(b - a)/2$

**Use the code: BVREDDY , to get maximum benefits**

**191.** The function  $f(x) = 2x^3 - 3x^2 - 36x + 10$  has  
a maximum at  $x =$

- (a) 3
- (b) 2
- (c) -3
- (d) -2

192. The minimum value of

$$f(x) = 2x^3 - 3x^2 - 36x + 10$$

- (a) 0
  - (b) - 13
  - (c) - 17
  - (d) - 71

**Use the code: BVREDDY , to get maximum benefits**

193. A maximum value of  $f(x) = (\log x / x)$  is

- (a)  $e$
- (b)  $e^{-1}$
- (c)  $e - 1$
- (d)  $e + 1$

**Use the code: BVREDDY , to get maximum benefits**

194. The function  $f(x) = x^x$  has a minimum at  $x$

- (a)  $e$
- (b)  $e^{-1}$
- (c) 0
- (d)  $e + 1$

**Use the code: BVREDDY , to get maximum benefits**

195. The maximum value of  $x \cdot e^{-x}$  is

- (a)  $e$
- (b)  $e^{-1}$
- (c) 1
- (d)  $-e$

**Use the code: BVREDDY , to get maximum benefits**

**196.** At  $(a, a)$ ,  $f(x, y) = xy + a^3/x + a^3/y$  has

- (a) a maximum
- (b) a minimum
- (c) a maximum if  $a > 0$
- (d) neither maximum nor minimum

**Use the code: BVREDDY , to get maximum benefits**

197. If  $f'(x) = (x + 2)(x - 1)^2(2x - 1)(x - 3)$  then  
at  $x = \frac{1}{2}$ ,  $f(x)$  has
- (a) a maximum
  - (b) a minimum
  - (c) neither maximum nor minimum
  - (d) no stationary point

**Use the code: BVREDDY , to get maximum benefits**

198. Find the maximum value of  $x^2 + y^2 + z^2$

so that  $x + y + z = 1$

(a) 1

(b) 1/2

(c) 1/3

(d) 1/4

Use the code: BVREDDY , to get maximum benefits

199. If  $f(x) = \begin{cases} 4(3^x), & \text{if } x < 0 \\ 2a + x, & \text{if } x \geq 0 \end{cases}$   
is continuous at  $x = 0$ , then  $a = \underline{\hspace{2cm}}$ .

Use the code: BVREDDY , to get maximum benefits

**200.** A function  $f(x)$  differentiable in the interval  $0 \leq x \leq 5$ , is such that  $f(0) = 4$  and  $f(5) = -1$ .

If  $g(x) = \frac{f(x)}{x+1}$  then there exists a constant

$c \in (0, 5)$  such that  $g'(c) =$

(a)  $\frac{-2}{5}$

(b)  $\frac{2}{5}$

(c)  $\frac{-3}{5}$

(d)  $\frac{-5}{6}$

**Use the code: BVREDDY , to get maximum benefits**

**201.** If Rolle's Theorem hold for the function

$$f(x) = x^3 + ax^2 + bx \text{ in the interval}$$

$$1 \leq x \leq 2 \text{ at the point } x = \frac{4}{3}$$

then  $(a, b) = \underline{\hspace{2cm}}$ .

- (a)  $(-5, 8)$
- (b)  $(-8, -5)$
- (c)  $(5, 8)$
- (d) None of the above

**Use the code: BVREDDY , to get maximum benefits**

202. If  $f(x) = \frac{x^3 + 1}{x + 1}$  is continuous at  $x = -1$ , then

$$f(-1) = \underline{\hspace{2cm}}.$$

Use the code: BVREDDY , to get maximum benefits

203. If  $f(x) = \frac{ax + b}{cx + d}$  then  $f(x)$  has

- (a) a maximum
- (b) a minimum
- (c) no extremum
- (d) an extremum, if  $ad = bc$

**Use the code: BVREDDY , to get maximum benefits**

204. The function  $f(x) = x^{\frac{1}{x}}$  has \_\_\_\_\_.

- (a) a maximum at  $x = e^{-1}$
- (b) a minimum at  $x = e^{-1}$
- (c) a maximum at  $x = e$
- (d) a minimum at  $x = e$

**Use the code: BVREDDY , to get maximum benefits**

**205.**  $\lim_{x \rightarrow 0} \frac{|x|}{x} = \underline{\hspace{2cm}}$ , where  $|x|$  is a modulus function

- (a) 0
- (b) 1
- (c) -1
- (d) limit does not exist

**Use the code: BVREDDY , to get maximum benefits**

**206.**  $\lim_{x \rightarrow 6} [x] = \underline{\hspace{2cm}}$ , where  $[x]$  is a step

function

- (a) -6
- (b) 5
- (c) 0
- (d) limit does not exist

**Use the code: BVREDDY , to get maximum benefits**

207.  $\lim_{x \rightarrow 0} \frac{x - \sin x}{1 - \cos x} = \underline{\hspace{2cm}}$ .

- (a) 0
- (b) 4
- (c) -3
- (d) 1

Use the code: BVREDDY , to get maximum benefits

208.  $\lim_{x \rightarrow \frac{\pi}{2}} \left( \sec x - \frac{1}{1 - \sin x} \right) = \underline{\hspace{2cm}}$ .

- (a) 0      (b)  $\infty$       (c) -1      (d) 100

Use the code: BVREDDY , to get maximum benefits

**209.** If  $f(x) = \left(\frac{1-x}{x+1}\right)^{\frac{1}{x}}$  is continuous at  $x = 0$

then  $f(0) =$

- (a)  $e^{-2}$
- (b)  $e^2$
- (c)  $\sqrt{e}$
- (d)  $e^{-1/2}$

**Use the code: BVREDDY , to get maximum benefits**

210. If  $f(x) = \begin{cases} ax^2 + 1, & x \leq 1 \\ x^2 + ax + b, & x > 1 \end{cases}$  is differentiable

at  $x = 1$  then

- (a)  $a = 1, b = 1$
- (b)  $a = 1, b = 0$
- (c)  $a = 2, b = 0$
- (d)  $a = 2, b = 1$

Use the code: BVREDDY , to get maximum benefits

211. The function  $f(x) = |x - 4|$  on the interval  $[0, 5]$  is
- (a) continuous and differentiable
  - (b) neither continuous nor differentiable
  - (c) differentiable but not continuous
  - (d) continuous on the interval but not differentiable

**Use the code: BVREDDY , to get maximum benefits**

212. Lagrange's mean value theorem does not

hold for  $f(x) = x^{\frac{-2}{3}}$  in  $[-1, 1]$ , because

- (a) not continuous in  $(-1, 1)$
- (b) not differentiable in  $(-1, 1)$
- (c) continuous but not differentiable in  $(-1, 1)$
- (d) neither continuous nor differentiable in the given interval

**Use the code: BVREDDY , to get maximum benefits**

**213.** The value of 'c' of Cauchy's mean value

theorem for  $f(x) = \sqrt{x}$  and  $g(x) = \frac{1}{\sqrt{x}}$  in

[1, 3] is \_\_\_\_\_.

- (a) 1.732
- (b) 2.732
- (c) 3.732
- (d) -1.732

**214.** The coefficient of  $(x - 2)^3$  in the Taylor series expansion of the function  $f(x) = \log x$  about the point 2 is

- (a)  $\frac{1}{4}$
- (b)  $\frac{1}{12}$
- (c)  $\frac{1}{24}$
- (d)  $\frac{1}{36}$

**Use the code: BVREDDY , to get maximum benefits**

215.  $f(x) = \int_0^x (t-2)^2(t-1)dt$  has a

- (a) maximum at  $x = 1$
- (b) minimum at  $x = 1$
- (c) maximum at  $x = 2$
- (d) minimum at  $x = 2$

Use the code: **BVREDDY**, to get maximum benefits

**216.** Suppose that the function 'f' attains a maximum at  $x = x_1$  and a minimum at  $x = x_2$  such that  $x_2 = x_1^2$ .

If  $f(x) = 2x^3 - 9ax^2 + 12a^2 x + 1$ ,  $a > 0$  then the value of  $a = \underline{\hspace{2cm}}$ .

**217.** If  $\alpha, \beta$  are the roots of the equation  
 $x^2 - (a - 2)x - (a + 1) = 0$ , where 'a' is a  
variable then the minimum value of  
 $\alpha^2 + \beta^2 = \underline{\hspace{2cm}}$ .

**Use the code: BVREDDY , to get maximum benefits**

**218.** Let  $x$  and  $y$  be integers satisfying the following equations

$$2x^2 + y^2 = 34$$

$$x + 2y = 11$$

The value of  $(x + y)$  is \_\_\_\_\_.

**(GATE-17-EE)**

**Use the code: BVREDDY , to get maximum benefits**

**219.** Let  $g(x) = \begin{cases} -x, & x \leq 1 \\ x + 1, & x > 1 \end{cases}$  and

$$f(x) = \begin{cases} 1 - x, & x \leq 0 \\ x^2, & x > 0 \end{cases}$$

Consider the composition of f and g, i.e.,  $(fog)(x) = f(g(x))$ . The number of discontinuities in  $(fog)(x)$  present in the interval  $(-\infty, 0)$  is

- (a) 0
- (b) 1
- (c) 2
- (d) 4

**(GATE-17-EE)**

**220.** The value of  $\lim_{x \rightarrow 0} \left( \frac{x^3 - \sin(x)}{x} \right)$  is

- (a) 0
- (b) 0
- (c) 1
- (d) -1

**(GATE-17-ME)**

**Use the code: BVREDDY , to get maximum benefits**

**221.**  $\lim_{x \rightarrow 0} \left( \frac{\tan x}{x^2 - x} \right)$  is equal to \_\_\_\_\_

**(GATE-17-CE)**

**Use the code: BVREDDY , to get maximum benefits**

**222.** The value of  $\lim_{x \rightarrow 1} \frac{x^7 - 2x^5 + 1}{x^3 - 3x^2 + 2}$

**(GATE-17-CSIT)**

- (a) is 0
- (b) is -1
- (c) is 1
- (d) does not exists

**Use the code: BVREDDY , to get maximum benefits**

**223.** At the point  $x = 0$ , the function  $f(x) = x^3$  has

- (a) local maximum
- (b) local minimum
- (c) both local maximum and local minimum
- (d) Neither local maximum nor local minimum

**(GATE-18-CE)**

**Use the code: BVREDDY , to get maximum benefits**

**224.** Let  $f(x) = 3x^3 - 7x^2 + 5x + 6$ . The maximum value of  $f(x)$  over the interval  $[0, 2]$  is \_\_\_\_\_ (up to 2 decimal places)

**(GATE-18-EE)**

**Use the code: BVREDDY , to get maximum benefits**

**225.** Consider two functions  $f(x) = (x - 2)^2$  and  $g(x) = 2x - 1$ , where  $x$  is real. The smaller value of  $x$  for which  $f(x) = g(x)$  is \_\_\_\_\_

**(GATE-18-IN)**

**Use the code: BVREDDY , to get maximum benefits**

**226.** For  $0 \leq x \leq 2\pi$ ,  $\sin x$  and  $\cos x$  are both decreasing functions in the interval \_\_\_\_\_  
**(GATE-18-IN)**

(a)  $\left(0, \frac{\pi}{2}\right)$

(c)  $\left(\pi, \frac{3\pi}{2}\right)$

(a)  $\left(\frac{\pi}{2}, 0\right)$

(c)  $\left(\frac{\pi}{2}, \pi\right)$

**Use the code: BVREDDY , to get maximum benefits**

227. A political party orders an arch for the entrance to the ground in which the annual convention is being held. The profile of the arch follows the equation  $y = 2x - 0.1x^2$  where  $y$  is the height of the arch in meters. The maximum possible height of the arch is

(GATE-ME,PI-2012)

- (a) 8 meters
- (b) 10 meters
- (c) 12 meters
- (d) 14 meters

Use the code: BVREDDY , to get maximum benefits

**228.** A real-valued function  $y$  of real variable  $x$  is such that  $y = 5|x|$ . At  $x = 0$ , the function is **(GATE-18-PI)**

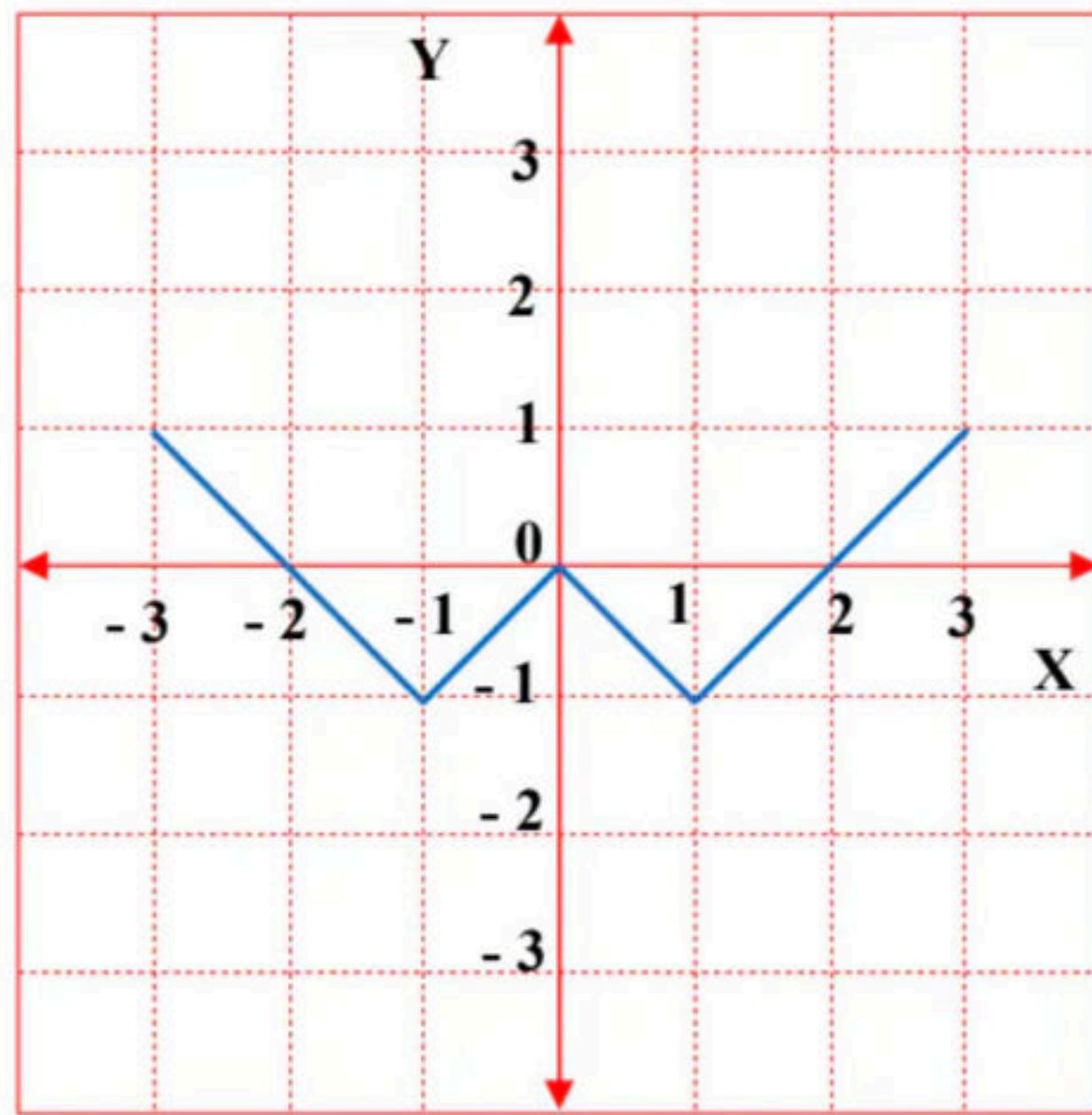
- (a) discontinuous but differentiable
- (b) both continuous and differentiable
- (c) discontinuous and not differentiable
- (d) continuous but not differentiable

**Use the code: BVREDDY , to get maximum benefits**

**229.** Which of the following functions describe the graph shown in the below figure?

**(GATE-18-PI)**

- (a)  $y = ||x| + 1| - 2$
- (b)  $y = ||x| - 1| - 1$
- (c)  $y = ||x| + 1| - 1$
- (d)  $y = |x - 1| - 1$



**Use the code: BVREDDY , to get maximum benefits**

**230.** Let  $f$  be the real-valued function of real variable defined as  $f(x) = x^2$  for  $x \geq 0$ , and  $f(x) = -x^2$  for  $x < 0$ . Which of the following statements is true?

**(GATE-18-EE)**

- a)  $f(x)$  is discontinuous at  $x = 0$
- (b)  $f(x)$  is continuous but not differentiable at  $x = 0$
- (c)  $f(x)$  is differentiable, but its first derivative is not continuous at  $x = 0$
- (d)  $f(x)$  is differentiable, but its first derivative is not differentiable at  $x = 0$

**Use the code: BVREDDY , to get maximum benefits**

231. Let  $f(x) = x^{-(1/3)}$  and  $A$  denote the area of the region bounded by  $f(x)$  and the X-axis, when  $x$  varies from  $-1$  to  $1$ . Which of the following statements is/are TRUE ?

(GATE-CS-2015)

- |                                    |                                      |
|------------------------------------|--------------------------------------|
| (I) $f$ is continuous in $[-1, 1]$ | (II) $f$ is not bounded in $[-1, 1]$ |
| (III) $A$ is nonzero and finite    | (a) II only      (b) III only        |
| (c) II and III only                | (d) I, II and III                    |

Use the code: **BVREDDY**, to get maximum benefits

**232.** Compute  $\lim_{x \rightarrow 3} \frac{x^4 - 81}{2x^2 - 5x - 3}$

**(GATE-19-CSIT)**

- (a) 1
- (b) Limit does not exist
- (c) 53/12
- (d) 108/7

**Use the code: BVREDDY , to get maximum benefits**

**233.Which of the following is correct?**

(a)  $\lim_{x \rightarrow 0} \left( \frac{\sin 4x}{\sin 2x} \right) = 2$  and  $\lim_{x \rightarrow 0} \left( \frac{\tan x}{x} \right) = 1$

**(GATE-19-CE)**

(b)  $\lim_{x \rightarrow 0} \left( \frac{\sin 4x}{\sin 2x} \right) = \infty$  and  $\lim_{x \rightarrow 0} \left( \frac{\tan x}{x} \right) = 1$

(c)  $\lim_{x \rightarrow 0} \left( \frac{\sin 4x}{\sin 2x} \right) = 1$  and  $\lim_{x \rightarrow 0} \left( \frac{\tan x}{x} \right) = 1$

(d)  $\lim_{x \rightarrow 0} \left( \frac{\sin 4x}{\sin 2x} \right) = 2$  and  $\lim_{x \rightarrow 0} \left( \frac{\tan x}{x} \right) = \infty$

**Use the code: BVREDDY , to get maximum benefits**

234. for a small value of h the Taylor series expansion for  $f(x + h)$  is

(GATE-19-CE)

(a)  $f(x) + hf'(x) + \frac{h^2}{2!} f''(x) + \frac{h^3}{3!} f'''(x) + \dots \dots \dots \infty$

(b)  $f(x) - hf'(x) + \frac{h^2}{2} f''(x) - \frac{h^3}{3} f'''(x) + \dots \dots \dots \infty$

(c)  $f(x) + hf'(x) + \frac{h^2}{2} f''(x) + \frac{h^3}{3} f'''(x) + \dots \dots \dots \infty$

(d)  $f(x) - hf'(x) + \frac{h^2}{2!} f''(x) - \frac{h^3}{3!} f'''(x) + \dots \dots \dots \infty$

Use the code: BVREDDY , to get maximum benefits

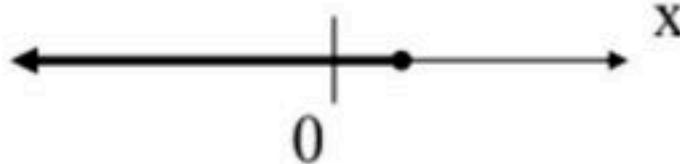
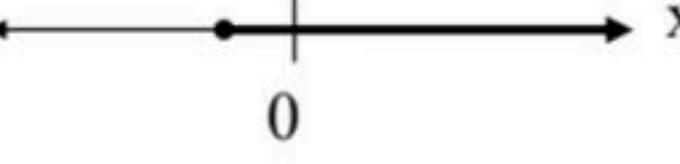
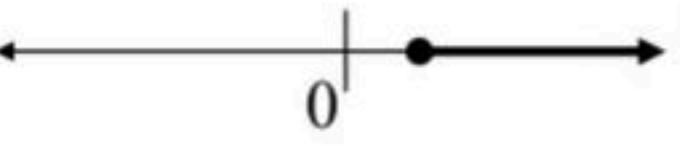
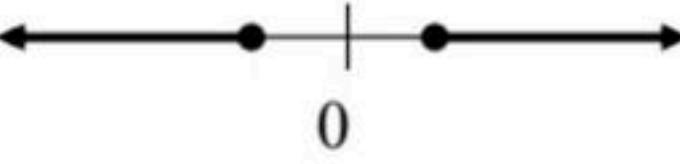
**235.** The global minimum of  $x^3 e^{-|x|}$  for  $x \in (-\infty, \infty)$  occurs at  $x = \underline{\hspace{2cm}}$  (round off to one decimal place)

**(GATE-2022-IN)**

**Use the code: BVREDDY , to get maximum benefits**

**236.** Which one of the following is a representation (not to scale and in bold) of all values of  $x$  satisfying the inequality  $2 - 5x \leq -\left(\frac{6x-5}{3}\right)$  on the real number line?

**(GATE-2022-ME)**

- (a) 
- (b) 
- (c) 
- (d) 

**Use the code: BVREDDY , to get maximum benefits**

237. The minimum value of  $2x+3y$ , when  $xy=6$  is  
(A) 12      (B) 9      (C) 8      (D) 6

**Use the code: BVREDDY , to get maximum benefits**

238.  $f(x) = \frac{1}{4x^2 + 2x + 1}$ , then its max value is

- (A)  $\frac{4}{3}$
- (B)  $\frac{2}{3}$
- (C) 1
- (D)  $\frac{3}{4}$

239. The series  $\sum_{m=0}^{\alpha} \frac{1}{4^m} (x-1)^{2m}$  converges for (GATE-IN-2011)
- (a)  $-2 < x < 2$       (b)  $-1 < x < 3$       (c)  $-3 < x < 1$       (d)  $x < 3$

Use the code: BVREDDY , to get maximum benefits

240. The series  $\sum_{n=0}^{\infty} \frac{1}{n!}$  converges to

(GATE-EC-SET-4-2014)

- (a)  $2 \ln 2$
- (b)  $\sqrt{2}$
- (c) 2
- (d) e

Use the code: BVREDDY , to get maximum benefits

241. The value of  $\sum_{n=0}^{\infty} n \left(\frac{1}{2}\right)^n$  is \_\_\_\_\_

(GATE-EC-2015)

Use the code: BVREDDY , to get maximum benefits

242. Consider the sequence,  $x_n = 0.5x_{n-1} + 1$ ,  $n = 1, 2, \dots$  with  $x_0 = 0$ . Then  $\lim_{n \rightarrow \infty} x_n$  is

- (a) 2
- (b) 1
- (c) 0
- (d)  $\infty$

**GATE- 2021 (CS)**

**Use the code: BVREDDY , to get maximum benefits**

**243.** Let  $S = \sum_{n=0}^{\infty} n\alpha^n$  where  $|\alpha| < 1$ . The value of  $\alpha$  in the range  $0 < \alpha < 1$ , such that  $S = 2\alpha$  is

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**(GATE-16-EE)**

**Use the code: BVREDDY , to get maximum benefits**

244.  $f(z) = (z - 1)^{-1} - 1 + (z - 1) - (z - 1)^2 + \dots$  is the series expansion of

(a)  $\frac{1}{(z - 1)^2}$  for  $|z - 1| < 1$

(b)  $\frac{1}{z(z - 1)}$  for  $|z - 1| < 1$

**GATE- 2021 (CS)**

(c)  $\frac{-1}{z(z - 1)}$  for  $|z - 1| < 1$

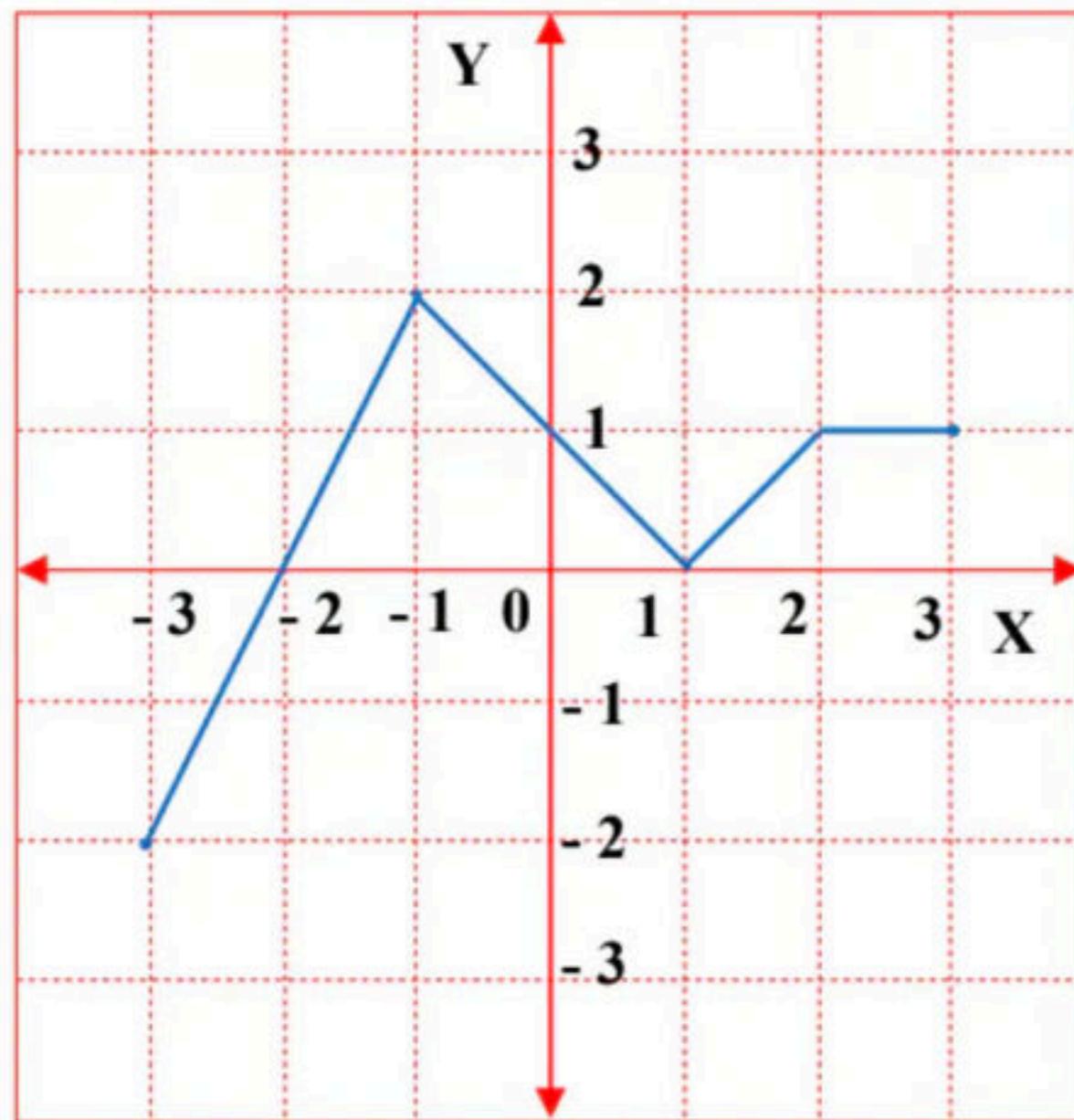
(d)  $\frac{-1}{(z - 1)}$  for  $|z - 1| < 1$

**Use the code: BVREDDY , to get maximum benefits**

245. Which of the following function(s) is an accurate description of the graph for the range(s) indicated?

- (i)  $y = 2x + 4$  for  $-3 \leq x \leq 1$
- (ii)  $y = |x - 1|$  for  $-1 \leq x \leq 2$
- (iii)  $y = ||x| - 1|$  for  $-1 \leq x \leq 2$
- (iv)  $y = 1$  for  $2 \leq x \leq 3$

- (a) (i), (ii) and (iii) only
- (b) (i), (ii) and (iv) only
- (c) (i) and (iv) only
- (d) (ii) and (iv) only



Use the code: **BVREDDY**, to get maximum benefits

**246.** Consider the following series:

$$\sum_{n=1}^{\infty} \frac{n^d}{c^n}$$

For which of the following combinations of c, d values does this series converge?

**(GATE-2022-ECE)**

- (a)  $c = 1, d = -1$
- (b)  $c = 2, d = 1$
- (c)  $c = 0.5, d = -10$
- (d)  $c = 1, d = -2$

**Use the code: BVREDDY , to get maximum benefits**

247. Let  $f$  be differentiable for all  $x$ , if  $f(1) = -2$ ,  
and  $f'(x) \geq 2$  for all  $x \in [1, 6]$  thus
- (A)  $f(6) < 8$       (B)  $f(6) \geq 8$   
(C)  $f(6) \geq 5$       (D)  $f(6) \leq 5$

**Use the code: BVREDDY , to get maximum benefits**

**Use the code: BVREDDY , to get maximum benefits**

$$249. \int_0^2 \int_0^3 xy \, dx \, dy$$

- (A) 0      (B) 9      (C) 8      (D) 1

Use the code: **BVREDDY**, to get maximum benefits

250.  $\int_0^{\frac{\pi}{2}} \int_{-1}^1 x^2 y^2 dx dy$

- (A)  $\frac{\pi^3}{36}$     (B)  $\frac{\pi}{0}$     (C) -1    (D) 0

Use the code: BVREDDY , to get maximum benefits

251. Evaluate  $\int_{-1}^2 (1 + |x|) dx$

- (A) 3.5
- (B) 5.5
- (C) 4
- (D) None of these

Use the code: BVREDDY , to get maximum benefits

252.  $\int_0^{\pi} \sin^5 x \cos^9 x dx =$  \_\_\_\_\_



**Use the code: BVREDDY , to get maximum benefits**

253. Let  $f(x)$  be any bounded real valued function in the interval  $[a, b]$ .

Consider the following statements:

A:  $\int_{-a}^a f(x) dx = \int_0^a \{f(x) + f(-x)\} dx$

B:  $\int_{-a}^a f(x) dx = 2 \int_0^a f(x) dx$

Then which of the following is appropriate?

- (A) A and B both are true and they are interdependent
- (B) A and B are true independently
- (C) A is true and B is false always
- (D) A is true and B is true in special case

**Use the code: BVREDDY , to get maximum benefits**

254. For which value of  $n$ ,

$\int_0^{\frac{\pi}{2}} \frac{dx}{16\cos^2 x + 25\sin^2 x}$  becomes equal to  $n\pi$ .

- (A)  $\frac{1}{40}$     (B)  $\frac{1}{50}$     (C)  $\frac{1}{20}$     (D)  $\frac{1}{30}$

255. Evaluate  $\int_0^1 \int_1^2 (x^2 + y^2) dx dy$

- (A)  $-\frac{8}{3}$     (B)  $\frac{8}{3}$     (C) 0    (D) 1

Use the code: BVREDDY , to get maximum benefits

256. The value of  $\int_{-4}^7 |x| dx$  is

- (a) 30.5
- (b) 30
- (c) 32.5
- (d) 32

Use the code: BVREDDY , to get maximum benefits

257. The value of  $\int_0^{1.5} x[x^2] dx$ , where  $[x]$  is a step function, is

(a)  $\frac{4}{3}$

(b)  $\frac{1}{2}$

(c)  $\frac{2}{3}$

(d)  $\frac{3}{4}$

Use the code: BVREDDY , to get maximum benefits

258. The value of  $\int_0^{\pi} x \sin^8(x) \cos^6(x) dx$  is

(a)  $\frac{\pi^2}{512}$

(b)  $\frac{105\pi^2}{512}$

(c)  $\frac{105\pi}{86016}$

(d)  $\frac{5\pi^2}{4096}$

Use the code: BVREDDY , to get maximum benefits

259. The value of  $\int_{x=1}^a \int_{y=1}^b \frac{1}{xy} dx dy$  is \_\_\_\_\_.

- (a)  $(\log a)(\log b)$
- (b)  $\log(ab)$
- (c)  $\log a - \log b$
- (d)  $\log(a + b)$

Use the code: BVREDDY , to get maximum benefits

260.  $\int_1^3 \int_1^2 xy^2 \, dx \, dy =$

- (a) 10
- (b) 11
- (c) 13
- (d) 12

Use the code: BVREDDY , to get maximum benefits

$$261. \int_0^1 \int_0^2 \int_0^2 x^2 yz \, dx \, dy \, dz =$$

(a)  $-\frac{7}{3}$

(b)  $\frac{7}{3}$

(c)  $\frac{7}{2}$

(d)  $-\frac{7}{2}$

Use the code: BVREDDY , to get maximum benefits

262. The value of  $\int_{x=0}^1 \int_{y=0}^2 xy \, dx \, dy$  is \_\_\_\_\_.

Use the code: BVREDDY , to get maximum benefits

263.  $\int_{-\frac{1}{2}}^{\frac{1}{2}} \cos x \log\left(\frac{1+x}{1-x}\right) dx = \underline{\hspace{2cm}}$



**Use the code: BVREDDY , to get maximum benefits**

264.  $\int_{-\pi}^{\pi} \sin^4 x \cdot dx =$

(a)  $\pi$

(b)  $\frac{\pi}{2}$

(c)  $\frac{3\pi}{4}$

(d) 0

Use the code: BVREDDY , to get maximum benefits

265.  $\int_{-1}^2 \frac{|x|}{x} dx = \dots$

Use the code: BVREDDY , to get maximum benefits

$$266. \int_0^{\pi} |\cos x| dx =$$

Use the code: BVREDDY , to get maximum benefits

267.  $\int_0^n [x] dx = \underline{\hspace{2cm}}$ , where  $[x]$  is a step function

and 'n' is an integer.

(a)  $\frac{n(n+1)}{2}$

(b)  $\frac{n(n-1)}{2}$

(c)  $\frac{n}{2}$

(d)  $\frac{n+1}{2}$

Use the code: BVREDDY , to get maximum benefits

268.  $\int_0^{\frac{\pi}{2}} \log(\tan x) dx =$

(a) 0

(b)  $\frac{\pi}{2}$

(c)  $\frac{\pi}{4}$

(d)  $\pi$

Use the code: BVREDDY , to get maximum benefits

269. Let  $\frac{d}{dx}[F(x)] = \frac{e^{\sin x}}{x}$ ,  $x > 0$ .

If  $\int_1^4 \left( \frac{2e^{\sin x^2}}{x} \right) dx = F(k) - F(1)$

then  $k = \underline{\hspace{2cm}}$ .

Use the code: BVREDDY , to get maximum benefits

270.  $\int_0^{\pi/4} \log(1 + \tan x) dx =$

- (a) 0
- (b)  $(\pi/2) \log 2$
- (c)  $(\pi/8) \log 2$
- (d)  $(-\pi/4) \log 2$

**Use the code: BVREDDY , to get maximum benefits**

$$271. \int_0^{\pi} \sin^4 x \cos^5 x \, dx =$$

(a) 0

(b)  $3\pi/256$

(c)  $3\pi/128$

(d)  $5\pi/128$

Use the code: **BVREDDY**, to get maximum benefits

272.  $\int_0^{2\pi} \sin^4 x \cos^6 x \, dx =$

- (a)  $3\pi/128$
- (b)  $3\pi/256$
- (c)  $3\pi/64$
- (d) 0

Use the code: **BVREDDY**, to get maximum benefits

273.  $\int_0^{2\pi} \sin^4 x \cos^5 x \, dx =$

- (a) 0
- (b)  $3\pi/128$
- (c)  $5\pi/128$
- (d)  $3\pi/256$

Use the code: BVREDDY , to get maximum benefits

$$274. \int_0^{\pi/2} \int_0^{\pi/2} s \sin(x+y) dx dy$$

(GATE-EC-2000)

(a) 0

(b)  $\pi$

(c)  $\pi/2$

(d) 2

Use the code: BVREDDY , to get maximum benefits

275. The value of the integral is  $I = \int_0^{\pi/4} \cos^2 x \, dx$  (GATE-CE-2001)

- (a)  $\frac{\pi}{8} + \frac{1}{4}$
- (b)  $\frac{\pi}{8} - \frac{1}{4}$
- (c)  $\frac{-\pi}{8} - \frac{1}{4}$
- (d)  $\frac{-\pi}{8} + \frac{1}{4}$

Use the code: BVREDDY , to get maximum benefits

276.

The value of the integral  $\int_{-\pi/2}^{\pi/2} (x \cos x) dx$  is

(GATE-PI-2008)

- (a) 0
- (b)  $\pi - 2$
- (c)  $\pi$
- (d)  $\pi + 2$

Use the code: BVREDDY , to get maximum benefits

277. The value of the following definite integral in  $\int_{-\pi/2}^{\pi/2} \frac{\sin 2x}{1 + \cos x} dx =$  (GATE-ME-2002)
- (a) -2log 2      (b) 2      (c) 0      (d) None

Use the code: BVREDDY , to get maximum benefits

278. The value of the following improper integral is  $\int_0^1 x \log x \, dx =$
- (GATE-ME-2002)
- (a) 1/4
  - (b) 0
  - (c) -1/4
  - (d) 1

Use the code: BVREDDY , to get maximum benefits

279.

$$\int_{-a}^a [\sin^6 x + \sin^7 x] dx$$

- (a)  $2 \int_0^a \sin^6 x dx$       (b)  $2 \int_0^a \sin^7 x dx$       (c)  $2 \int_0^a (\sin^6 x + \sin^7 x) dx$       (d) zero

(GATE-ME-2004)

Use the code: BVREDDY , to get maximum benefits

**280.** The value of  $\int_0^3 \int_0^x (6 - x - y) dx dy$  is \_\_\_\_\_ **(GATE-CS-2008)**

- (a) 13.5
- (b) 27.0
- (c) 40.5
- (d) 54.0

**Use the code: BVREDDY , to get maximum benefits**

281.

$$\int_0^a \int_0^x \int_0^{x+y} e^{x+y+z} dx dy dz$$

(A)  $\frac{e^{4a}}{8} - \frac{3e^{2a}}{4} + e^a - \frac{3}{8}$

(B)  $\frac{e^{4a}}{4} - \frac{3e^{2a}}{4}$

(C)  $\frac{e^{4a}}{8} - \frac{3e^{2a}}{4} - \frac{3}{8}$

(D) None

Use the code: BVREDDY , to get maximum benefits

282.  $\int_0^1 \int_x^{\sqrt{x}} (x^2 + y^2) dx dy =$

(a)  $\frac{2}{35}$

(b)  $-\frac{3}{35}$

(c)  $\frac{3}{35}$

(d)  $-\frac{2}{35}$

Use the code: BVREDDY , to get maximum benefits

283.

$$\int_0^1 \int_{4y}^4 e^{x^2} dx dy =$$

(a)  $\frac{(e^{16} - 1)}{8}$

(b)  $-\frac{(e^{16} + 1)}{8}$

(c) 0

(d)  $-\frac{(e^{16} - 1)}{8}$

Use the code: BVREDDY , to get maximum benefits

284.

$$\int_0^4 \int_0^{x^2} e^{y/x} dy dx =$$

(a)  $3e^4$

(b)  $3e^4 + 7$

(c)  $-3e^4$

(d)  $3e^4 - 7$

Use the code: BVREDDY , to get maximum benefits

285.

$$\int_0^{\infty} \int_x^{\infty} \left( \frac{e^{-y}}{y} \right) dy dx =$$

(a) 0

(b) 2

(c) 3

(d) 1

Use the code: BVREDDY , to get maximum benefits

$$286. \int_{-1}^1 \int_0^z \int_{x-z}^{x+z} (x + y + z) dx dy dz =$$

(a) 1

(b) 2

(c) 3

(d) 0

Use the code: BVREDDY , to get maximum benefits

287. The integral  $\int_0^1 \frac{dx}{\sqrt{(1-x)}}$  is equal to \_\_\_\_\_.

(GATE-16-EC)

Use the code: BVREDDY , to get maximum benefits

288.  $\int_{1/\pi}^{\pi} \frac{\cos(1/x)}{x^2} dx = \underline{\hspace{2cm}}$

(GATE-CS-2015)

Use the code: BVREDDY , to get maximum benefits

**289.** Given the following statements about a function  $f: \mathbb{R} \rightarrow \mathbb{R}$ , select the right option:

P: If  $f(x)$  is continuous at  $x = x_0$ , then it is also differentiable at  $x = x_0$

Q: If  $f(x)$  is continuous at  $x = x_0$ , then it may not be differentiable at  $x = x_0$

R: If  $f(x)$  is differentiable at  $x = x_0$ , then it is also continuous at  $x = x_0$

(a) P is true, Q is false, R is false

**(GATE-16-EC)**

(b) P is false, Q is true, R is true

(c) P is false, Q is true, R is false

(d) P is true, Q is false, R is true

**Use the code: BVREDDY , to get maximum benefits**

290. The value of  $\int_0^{\frac{\pi}{2}} \int_0^{2a\cos\theta} r \sin\theta dr d\theta$

is \_\_\_\_\_.

(a)  $\frac{a^2}{2}$

(b)  $2a^2$

(c)  $\frac{2a^2}{3}$

(d)  $4a^2$

Use the code: BVREDDY , to get maximum benefits

291.

$$\int_0^{\frac{\pi}{4}} \frac{\sin 2x}{\cos^4 x + \sin^4 x} dx = \underline{\hspace{2cm}}$$

Use the code: BVREDDY , to get maximum benefits

292.  $\int_0^1 \int_0^{\sqrt{1-x^2}} y^2 dx dy =$

(a)  $-\frac{\pi}{16}$

(b)  $\frac{\pi}{16}$

(c)  $\frac{\pi}{8}$

(d)  $-\frac{\pi}{8}$

Use the code: BVREDDY , to get maximum benefits

293. If  $[x]$  stands for greatest integer not exceeding 'x', then  $\int_4^{10} [x] dx = \underline{\hspace{2cm}}$ .

294. Change the order of integration in the

integral  $I = \int_{-a}^a \int_0^{\sqrt{a^2 - y^2}} f(x, y) dx dy$

(a)  $I = \int_0^a \int_{-\sqrt{a^2 - x^2}}^{\sqrt{a^2 - x^2}} f(x, y) dy dx$

(b)  $I = \int_{-a}^a \int_{-\sqrt{a^2 - x^2}}^{\sqrt{a^2 - x^2}} f(x, y) dy dx$

(c)  $I = \int_0^a \int_{-a}^a f(x, y) dy dx$

(d) None

**Use the code: BVREDDY , to get maximum benefits**

295. By reversing the order of integration, the

double integral  $\int_0^a \int_{\sqrt{ax}}^a \phi(x, y) dy dx$  is

represented as  $\int_p^q \int_r^s \phi(x, y) dx dy$  then the

product of q and s is \_\_\_\_\_.

- (a)  $y^2/a$
- (b)  $ay^2$
- (c)  $y^2$
- (d) 0

296. Changing the order of integration in double integral  $I = \int_0^8 \int_{x/4}^2 f(x, y) dy dx$  leads to

$$I = \int_p^q \int_r^s f(x, y) dy dx . \text{ What is } q? \quad (\text{GATE-EC-2005})$$

- (a)  $4y$
- (b)  $16y^2$
- (c)  $x$
- (d)  $8$

**297.** By reversing the order of integration  $\int_0^2 \int_{x^2}^{2x} f(x, y) dy dx$  may be represented as

(a)  $\int_0^2 \int_{x^2}^{2x} f(x, y) dy dx$

(b)  $\int_0^2 \int_y^{\sqrt{y}} f(x, y) dx dy$  **(GATE-EC-1995)**

(c)  $\int_0^4 \int_{y/2}^{\sqrt{y}} f(x, y) dx dy$

(d)  $\int_{x^2}^{2x^2} \int_0^2 f(x, y) dy dx$

**Use the code: BVREDDY , to get maximum benefits**

298. By a change of variables  $x = uv$ ,  $y = v/u$  in a double integral, the integral  $f(x,y)$  changes to  $f\left(\frac{uv}{v}, \frac{u}{v}\right) \phi(u,v)$ . Then  $\phi(u,v)$  is \_\_\_\_\_ (GATE-EE-2005)

- (a)  $\frac{2v}{u}$
- (b)  $2uv$
- (c)  $v^2$
- (d) 1

Use the code: BVREDDY , to get maximum benefits

**299.** To evaluate the double integral  $\int_0^8 \left( \int_{y/2}^{\left(\frac{y}{2}\right)+1} \left( \frac{2x-y}{2} \right) dx \right) dy$ , we make the substitution  $u = \left( \frac{2x-y}{2} \right)$  and  $v = \frac{y}{2}$ . The integral will reduce to

(A)  $\int_0^4 \left( \int_0^2 2udu \right) dv$

(C)  $\int_0^4 \left( \int_0^1 udu \right) dv$

(B)  $\int_0^4 \left( \int_0^1 2udu \right) dv$

(D)  $\int_0^4 \left( \int_0^{21} 2udu \right) dv$

**Use the code: BVREDDY , to get maximum benefits**

**300.** The values of the integrals  $\int_0^1 \left[ \int_0^1 \frac{x-y}{(x+y)^3} dy \right] dx$  and  $\int_0^1 \left[ \int_0^1 \frac{x-y}{(x+y)^3} dx \right] dy$  are

**(GATE-17-EC)**

- (a) same and equal to 0.5
- (b) same and equal to -0.5
- (c) 0.5 and -0.5, respectively
- (d) -0.5 and -0.5, respectively

**Use the code: BVREDDY , to get maximum benefits**

**301.** The value of  $\int_1^3 \int_{1/x}^1 \int_0^{\sqrt{xy}} xyz dz dy dx$  is \_\_\_\_\_

(A)  $\frac{13}{9} - \frac{\ln 3}{6}$

(B)  $\frac{7}{6} - \frac{\ln 3}{6}$

(C)  $\frac{1}{6} - \ln 3$

(D)  $\frac{3}{2} - \ln 3$

**Use the code: BVREDDY , to get maximum benefits**

**302.** The value of  $\int_0^1 \int_0^2 \int_1^2 x^2 y z dz dy dx$  is \_\_\_\_\_

- (A) 0
- (B) 1
- (C) 2
- (D) 3

**Use the code: BVREDDY , to get maximum benefits**

**303.** The Value of the integral  $\int_0^1 \int_y^1 y\sqrt{1+x^3} dx dy = \underline{\hspace{2cm}}$

(A)  $2\sqrt{2}$

(B)  $\frac{2\sqrt{2}-1}{2}$

(C)  $\frac{2\sqrt{2}-1}{8}$

(D)  $\frac{2\sqrt{2}-1}{9}$

**Use the code: BVREDDY , to get maximum benefits**

**304.** The value of  $\int_{-1}^2 \int_{x^2}^{x+2} dy dx = \underline{\hspace{2cm}}$

(A)  $\frac{7}{2}$

(B)  $\frac{9}{2}$

(C)  $\frac{11}{2}$

(D)  $\frac{5}{2}$

**Use the code: BVREDDY , to get maximum benefits**

**305.** The value of  $\int_0^1 \int_0^1 \frac{dydx}{\sqrt{1-x^2} \sqrt{1-y^2}} = \underline{\hspace{2cm}}$

(A)  $\frac{\pi^2}{4}$

(B)  $\frac{\pi^2}{2}$

(C)  $\frac{\pi^2}{8}$

(D)  $\frac{\pi^2}{16}$

**Use the code: BVREDDY , to get maximum benefits**

**306.** The value of  $\int_0^{100\pi} |\sin x| dx$  is \_\_\_\_\_

- (A) 100
- (B)  $100\pi$
- (C)  $200\pi$
- (D) 200

**Use the code: BVREDDY , to get maximum benefits**

**307.** The value of integral  $\int_{-1}^1 \ln \left( \frac{2-x\cos x}{2+x\cos x} \right) dx$  is \_\_\_\_\_

- (A)  $x \ln(2 + x \cos x)$
- (B)  $x \ln(2 - x \cos x)$
- (C)  $x \cos x$
- (D) 0

**Use the code: BVREDDY , to get maximum benefits**

**308.** If  $f(x) = \int_x^0 \sin t^2 dt$  then  $f'(x)$  is \_\_\_\_\_

- (A)  $2x \sin x^2$
- (B)  $-\sin x^2$
- (C)  $2x \cos x^2$
- (D)  $\cos x^2$

**Use the code: BVREDDY , to get maximum benefits**

309.  $\lim_{x \rightarrow 0} \frac{1}{x} \int_x^{2x} e^{-t^2} dt$  equals \_\_\_\_\_.

- (A) does not exists
- (B) infinite
- (C) exists and equals to 1
- (D) exists and equals to 0

Use the code: BVREDDY , to get maximum benefits

$$310. \int_0^{\frac{\pi}{4}} \frac{1}{a^2 \cos^2 x + b^2 \sin^2 x} dx = \text{_____} (a > 0)(b > 0)$$

(A)  $\frac{1}{ab}$

(B)  $\frac{1}{ab} \tan^{-1} \left( \frac{b}{a} \right)$

(B)  $\frac{1}{ab} \tan^{-1} \left( \frac{a}{b} \right)$

(D) 0

Use the code: BVREDDY , to get maximum benefits

**311.**  $\int_0^1 \frac{\ln(1+x)}{1+x^2} dx$  is

- (A)  $\frac{\pi}{4} \ln 2$
- (B)  $\frac{\pi}{2} \ln 2$
- (C)  $\frac{\pi}{8} \ln 2$
- (D) 0

**Use the code: BVREDDY , to get maximum benefits**

312. Let D be the determinant

$$\begin{bmatrix} \cos \theta & 1 & 0 \\ 0 & 2\cos \theta & 1 \\ 0 & 1 & 2\cos \theta \end{bmatrix}$$

Then  $\int_0^{\frac{\pi}{6}} D d\theta$

- |         |         |
|---------|---------|
| (A) 1   | (B) 1/3 |
| (C) 4/3 | (D) 3/2 |

313. The integral  $\int_0^{\frac{\pi}{2}} \min(\sin x, \cos x) dx$  equals

- (A)  $\sqrt{2} - 2$
- (B)  $2 - \sqrt{2}$
- (C)  $2\sqrt{2}$
- (D)  $2 + \sqrt{2}$

**Use the code: BVREDDY , to get maximum benefits**

314. The value of  $\int_0^1 \frac{dx}{\sqrt{x(1-x)}}$  is

- (A) 0
- (B)  $\frac{\pi}{2}$
- (C)  $\pi$
- (D)  $2\pi$

Use the code: BVREDDY , to get maximum benefits

**315.** The value of integral  $\int_0^9 \frac{dy}{\sqrt{y}\sqrt{1+\sqrt{y}}}$  is

- (A) 4
- (B)  $4(\sqrt{10} - 1)$
- (C) 8
- (D) 12

**316.** The value of  $\int_0^a \int_y^a \frac{xdx dy}{x^2+y^2}$  is \_\_\_\_\_

(A)  $\frac{\pi a}{4}$

(B)  $\frac{\pi a}{8}$

(C)  $\frac{\pi a}{2}$

(D)  $\pi a$

**Use the code: BVREDDY , to get maximum benefits**

$$317. \int_0^1 \int_0^{x^2} e^{\frac{y}{x}} dy dx = \underline{\hspace{2cm}}$$

- (A) 1
- (B) 1/2
- (C) 1/3
- (D) 1/4

Use the code: BVREDDY , to get maximum benefits

**318.** The value of  $\int_0^\infty \int_x^\infty \frac{1}{y} e^{-\frac{y}{2}} dy dx = \underline{\hspace{2cm}}$

- (A) 1
- (B) 2
- (C) 3
- (D) 4

319. The value of  $\int_0^a \int_0^x \int_0^y xyz dz dy dx$  is

(A)  $\frac{a^4}{16}$

(B)  $\frac{a^4}{12}$

(C)  $\frac{a^6}{48}$

(D)  $\frac{a^4}{4}$

**Use the code: BVREDDY , to get maximum benefits**

**320.** The value of  $\int_0^1 x^6 \sqrt{1 - x^2} dx$  is

(A)  $\frac{5\pi}{256}$

(C)  $\frac{5\pi}{512}$

(B)  $\frac{5\pi}{128}$

(D)  $\frac{3\pi}{512}$

**Use the code: BVREDDY , to get maximum benefits**

**321.** The value of  $\int_{x=0}^1 \int_{y=0}^{x^2} \int_{z=0}^y (y + 2z) dz dy dx$  is

- (A)  $\frac{1}{53}$
- (B)  $\frac{2}{21}$
- (C)  $\frac{1}{6}$
- (D)  $\frac{5}{3}$

**Use the code: BVREDDY , to get maximum benefits**

322. Let  $E = \{(x,y) \in R^2, 0 < x < y, 0 < y < \infty\}$  then  $\int \int_E ye^{-(x+y)} dx dy = \underline{\hspace{10cm}}$

**Use the code: BVREDDY , to get maximum benefits**

323. Let  $\int_0^1 \int_y^1 x y \sin(xy) dx dy = \int_0^1 \int_a^b x y \sin(xy) dy dx$  then

- (A)  $a = 0, b = x$
- (B)  $a = 1, b = x$
- (C)  $a = 0, b = 1$
- (D)  $a = -1, b = x$

**Use the code: BVREDDY , to get maximum benefits**

**324.** The integral  $\int_0^1 \int_{x^2}^x \left(\frac{x}{y}\right) e^{-\frac{x^2}{y}} dy dx$  equals

- (A)  $(e - 2)/e$
- (B)  $(e - 1)/2e$
- (C)  $(e - 1)/2$
- (D)  $(e - 2)/2e$

**Use the code: BVREDDY , to get maximum benefits**

**325.** Differentiate with respect to t.  $f(t) = \int_{-t^2}^{\alpha} e^{-x^2} dx$

(A)  $2te^{-t^4}$

(B)  $2te^{t^4}$

(C)  $-2te^{t^4}$

(D)  $-2te^{-t^4}$

**Use the code: BVREDDY , to get maximum benefits**

**326.** The area of the region enclosed by the curve  $y = x^2$  and the straight-line  $x + y = 2$  is

- (A) 3
- (B)  $27/2$
- (C)  $9/2$
- (D) 9

**Use the code: BVREDDY , to get maximum benefits**

**327.** The area of the region bounded by the curve  $x^2 = 2y$  and  $y^2 = 2x$  is

- |           |           |
|-----------|-----------|
| (A) $1/3$ | (B) $2/3$ |
| (C) $4/3$ | (D) $4$   |

**Use the code: BVREDDY , to get maximum benefits**

**328.** Area enclosed by the curves  $y^2 = x$  and  $y^2 = 2x - 1$  lying in the first quadrant is

- (A)  $1/6$
- (B)  $1/4$
- (C)  $1/2$
- (D)  $1/3$

**Use the code: BVREDDY , to get maximum benefits**

**329.** The value of  $\int \int xy(x + y)dx dy$  over the area between  $y = x^2$  and  $y = x$

- (A)  $1/90$
- (B)  $1/45$
- (C)  $3/56$
- (D)  $1/15$

**Use the code: BVREDDY , to get maximum benefits**

- 330.** The area bounded by the parabola  $2y = x^2$  and the lines  $x = y - 4$  is equal to  
(a) 6      (b) 18      (c)  $\infty$       (d) None      **(GATE-ME-1995)**

**Use the code: BVREDDY , to get maximum benefits**

331. Area bounded by the curve  $y = x^2$  and the lines  $x = 4$  and  $y = 0$  is given by

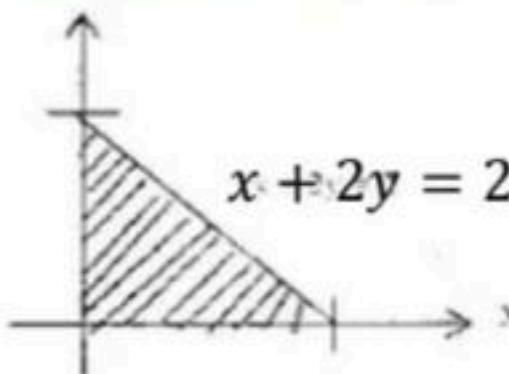
- (a) 64      (b)  $\frac{64}{3}$       (c)  $\frac{128}{3}$       (d)  $\frac{128}{4}$       (GATE-EE-1997)

Use the code: BVREDDY , to get maximum benefits

332. The area enclosed between the parabola  $y = x^2$  and the straight line  $y = x$  is
- (a)  $1/8$       (b)  $1/6$       (c)  $1/3$       (d)  $1/2$

**Use the code: BVREDDY , to get maximum benefits**

333. Consider the shaded triangular region P shown in the figure. What is  $\iint_P xy \, dx \, dy$ ?



(GATE-ME-2008)

- (a)  $\frac{1}{6}$
- (b)  $\frac{2}{9}$
- (c)  $\frac{7}{16}$
- (d) 1

Use the code: BVREDDY , to get maximum benefits

**334.** Consider the following definite integral

$$I = \int_0^1 \frac{(\sin^{-1}x)^2}{\sqrt{1-x^2}} dx$$

The value of the integral is

**(GATE-17-CE)**

(a)  $\frac{\pi^3}{24}$

(b)  $\frac{\pi^3}{12}$

(c)  $\frac{\pi^3}{48}$

(d)  $\frac{\pi^3}{64}$

**Use the code: BVREDDY , to get maximum benefits**

335. Let  $x$  be a continuous variable defined over the interval  $(-\infty, \infty)$  and  $f(x) = e^{-x-e^{-x}}$ . The integral  $g(x) = \int f(x)dx$  is equal to

(GATE-17-CE)

- (a)  $e^{e-x}$
- (b)  $e^{-e^{-x}}$
- (c)  $e^{-e^x}$
- (d)  $e^{-x}$

Use the code: BVREDDY , to get maximum benefits

336. The volume under the surface  $z(x, y) = x + y$  and above the triangle in the  $xy$  plane defined by  $\{0 \leq y \leq x \text{ and } 0 \leq x \leq 12\}$  is \_\_\_\_\_. (GATE-EC-SET-1-2014)

Use the code: **BVREDDY**, to get maximum benefits

337. The volume generated by revolving the area bounded by the parabola  $y^2 = 8x$  and the line  $x = 2$  about y-axis is **(GATE-EE-1994)**

- (a)  $\frac{128\pi}{5}$
- (b)  $\frac{5}{128\pi}$
- (c)  $\frac{127}{5\pi}$
- (d) None of the above

**Use the code: BVREDDY , to get maximum benefits**

338. The volume of an object expressed in spherical co-ordinates is given by

$$V = \int_0^{2\pi} \int_0^{\pi/3} \int_0^1 r^2 \sin\phi \, dr \, d\phi \, d\theta. \text{ The value of the integral } \quad (\text{GATE-EE-2004})$$

(a)  $\frac{\pi}{3}$

(b)  $\frac{\pi}{6}$

(c)  $\frac{2\pi}{3}$

(d)  $\frac{\pi}{4}$

Use the code: BVREDDY , to get maximum benefits

339. The volume enclosed by the surface  $f(x, y) = e^x$  over the triangle bounded by the line  $x = y$ ,  $x = 0$ ,  $y = 1$  in the  $xy$  plane is \_\_\_\_\_ (GATE-EE-2015)

Use the code: BVREDDY , to get maximum benefits

**340.** The region specified by

$$\left\{ (\rho, \varphi, z) : 3 \leq \rho \leq 5, \frac{\pi}{8} \leq \varphi \leq \frac{\pi}{4}, 3 \leq z \leq 4.5 \right\}$$

in cylindrical coordinates has volume of \_\_\_\_\_.

**(GATE-16-EC)**

**Use the code: BVREDDY , to get maximum benefits**

**341.** How many distinct values of  $x$  satisfy the equation  $\sin x = \frac{x}{2}$ , where  $x$  is in radians? **(GATE-16-EC)**

- (a) 1
- (b) 2
- (c) 3
- (d) 4 or more

**Use the code: BVREDDY , to get maximum benefits**

**342.** A triangle in the x-y plane is bounded by the straight lines  $2x = 3y$ ,  $y = 0$  and  $x = 3$ . The volume above the triangle and under the plane  $x + y + z = 6$  is \_\_\_\_\_.

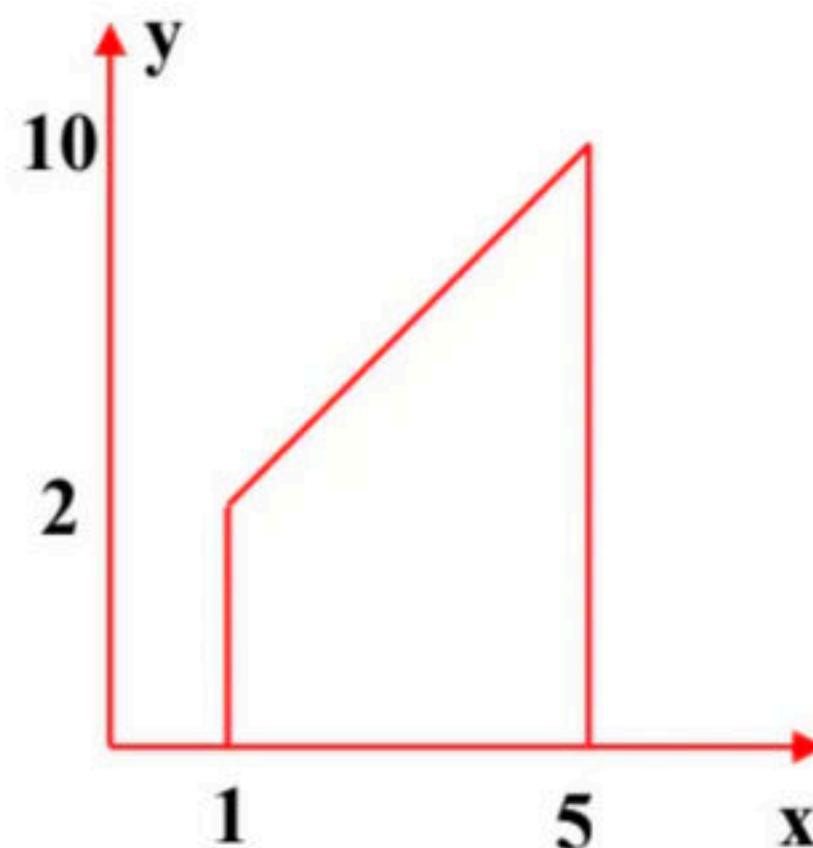
**(GATE-16-EC)**

**Use the code: BVREDDY , to get maximum benefits**

343. Let  $I = c \iint_R xy^2 dx dy$ , where  $R$  is the region shown in the figure and  $C = 6 \times 10^{-4}$ . The value of  $I$  equals \_\_\_\_\_.

(Give the answer up to two decimal places)

(GATE-17-EE)



Use the code: BVREDDY , to get maximum benefits

**344.** if  $f(x) = R \sin\left(\frac{\pi x}{2}\right) + S$ ,  $f'\left(\frac{1}{2}\right) = \sqrt{2}$  and  $\int_0^1 f(x) dx = \frac{2R}{\pi}$ , then constants R and S are respectively.

**(GATE-17-CSIT)**

(a)  $\frac{2}{\pi}$  and  $\frac{16}{\pi}$

(b)  $\frac{2}{\pi}$  and 0

(c)  $\frac{4}{\pi}$  and 0

(b)  $\frac{4}{\pi}$  and  $\frac{16}{\pi}$

**Use the code: BVREDDY , to get maximum benefits**

345. The value of the integral  $\int_0^{\pi} x \cos^2 x dx$  is

(GATE-18-CE)

(a)  $\frac{\pi^2}{8}$

(b)  $\frac{\pi^2}{4}$

(c)  $\frac{\pi^2}{2}$

(d)  $\pi^2$

Use the code: BVREDDY , to get maximum benefits

**346.** The value of  $\int_0^{\frac{\pi}{4}} x \cos(x^2) dx$  correct to 3 decimal places (assuming  $\pi = 3.14$  ) is \_\_\_\_\_

**(GATE-18-CSIT)**

**Use the code: BVREDDY , to get maximum benefits**

347. The value of the integral  $\int_0^{\pi} \int_y^{\pi} \frac{\sin x}{x} dx dy$  is equal

(GATE-19-CSIT)

Use the code: BVREDDY , to get maximum benefits

348. A parabola  $x = y^2$  with  $0 \leq x \leq 1$  is shown in the figure. The volume of the solid of rotation obtained by rotating the shaded area by  $360^\circ$  around the x-axis is

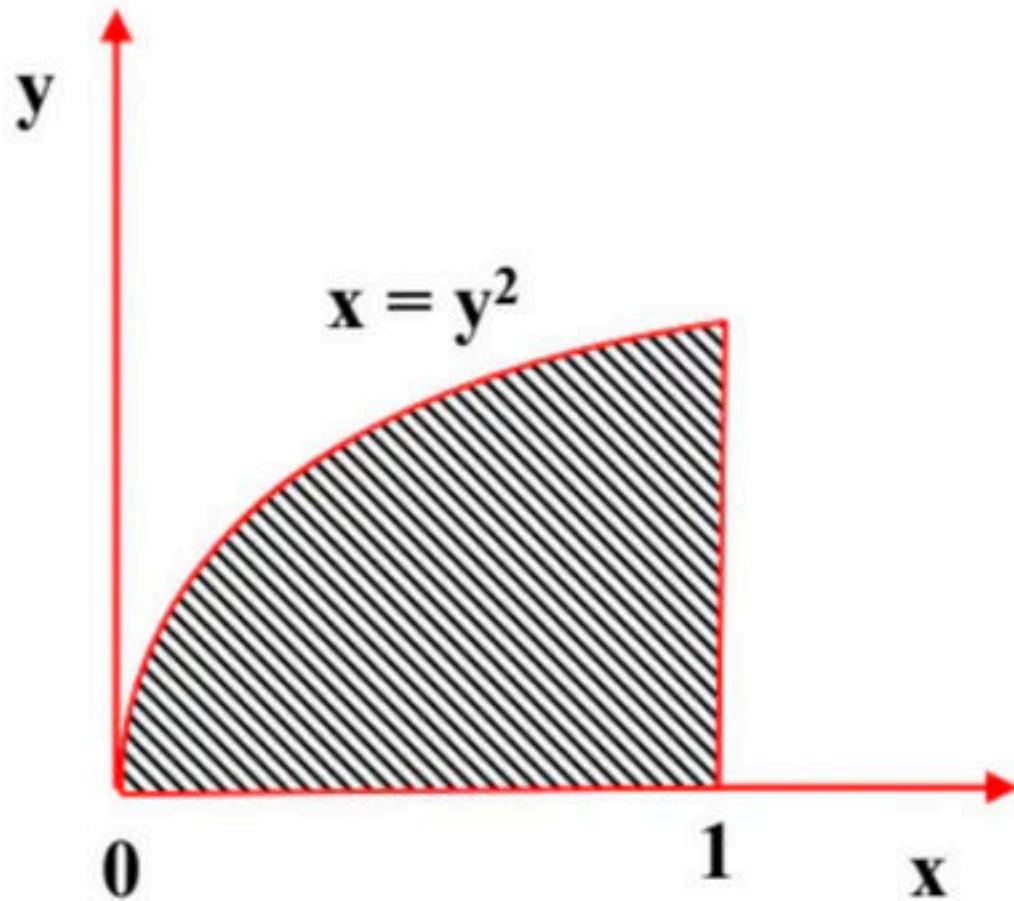
(GATE-19-ME)

(a)  $\pi$

(b)  $\frac{\pi}{4}$

(c)  $2\pi$

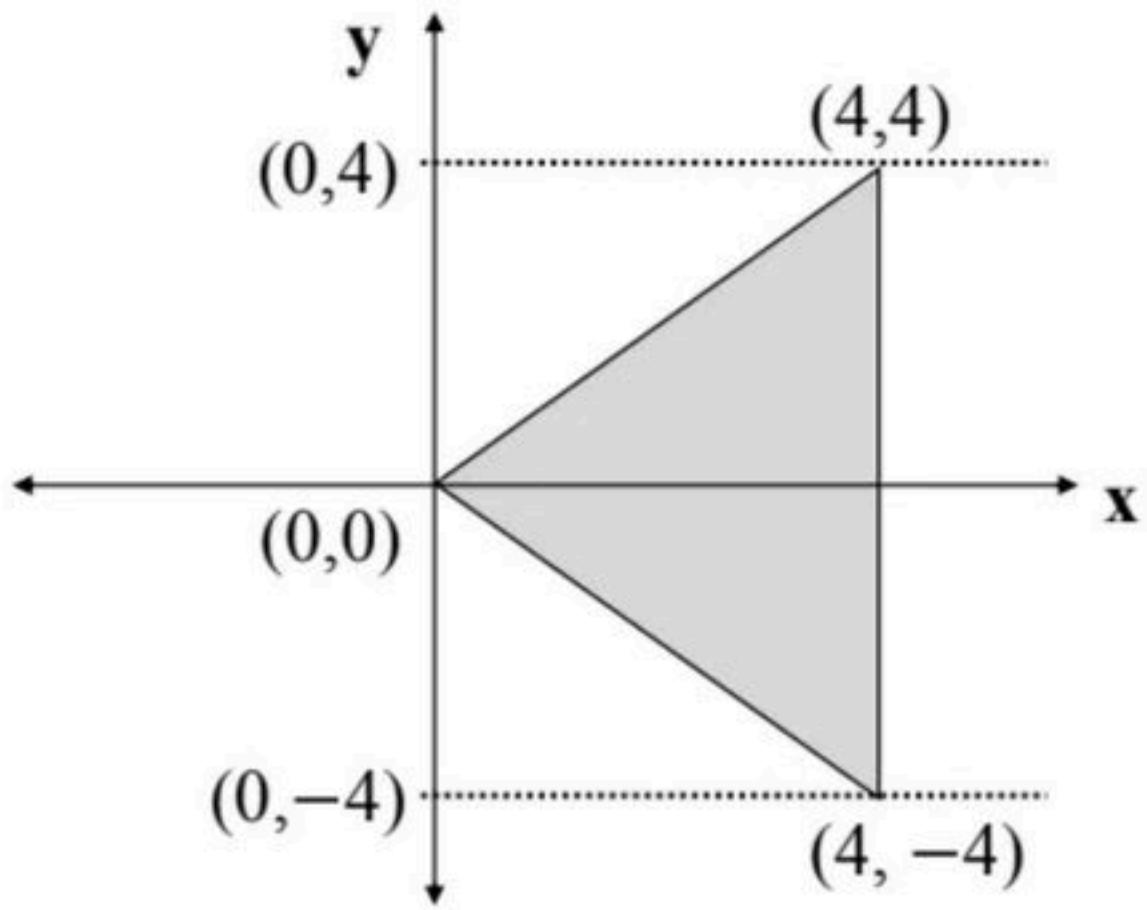
(d)  $\frac{\pi}{2}$



Use the code: BVREDDY , to get maximum benefits

349. The value of the integral  $\iint_D 3(x^2 + y^2) dx dy$   
where D is the shaded triangular region shown in the diagram is \_\_\_\_\_ (rounded off nearest integer).

(GATE-2022-ECE)



Use the code: BVREDDY , to get maximum benefits

**350.** If  $f(x) = 2\ln(\sqrt{e^x})$ , what is the area bounded by  $f(x)$  for the interval  $[0, 2]$  on the x-axis **(GATE-2022-ME)**

- (a)  $\frac{1}{2}$
- (b) 1
- (c) 2
- (d) 4

**Use the code: BVREDDY , to get maximum benefits**

**351.** The volume of the solid revolution generated by revolving the area bounded by the curve  $y = \sqrt{x}$  and the straight lines  $x=4$ ,  $y=0$  about the x-axis, is \_\_\_\_\_

- (A)  $2\pi$
- (B)  $4\pi$
- (C)  $8\pi$
- (D)  $12\pi$

**Use the code: BVREDDY , to get maximum benefits**

**352.** The volume of the revolution of  $y = \frac{a}{2} \left( e^{\frac{x}{a}} + e^{-\frac{x}{a}} \right)$  about x axis between  $x = 0$  and  $x = b$  is

(A)  $\frac{\pi a^3}{8} \left( e^{\frac{2b}{a}} - e^{-\frac{2b}{a}} \right) - \frac{\pi a^2 b}{2}$

(C)  $-\frac{\pi a^3}{8} \left( e^{\frac{2b}{a}} - e^{-\frac{2b}{a}} \right) - \frac{\pi a^2 b}{2}$

(B)  $-\frac{\pi a^3}{8} \left( e^{\frac{2b}{a}} - e^{-\frac{2b}{a}} \right) + \frac{\pi a^2 b}{2}$

(D)  $\frac{\pi a^3}{8} \left( e^{\frac{2b}{a}} - e^{-\frac{2b}{a}} \right) + \frac{\pi a^2 b}{2}$

**Use the code: BVREDDY , to get maximum benefits**

**353.** Let  $V$  be the region bounded by the planes  $x = 0$ ,  $x = 2$ ,  $y = 0$ ,  $z = 0$  and  $y + z = 1$ . Then the value of the integral  $\iiint_V y \, dx \, dy \, dz$  is

- (A)  $1/2$
- (B)  $4/3$
- (C)  $1$
- (D)  $1/3$

**Use the code: BVREDDY , to get maximum benefits**

**354.** Find the volume under the plane  $z = 8x + 6y$  over the region

$R = \{(x,y): 0 \leq x \leq 1, 0 \leq y \leq 2x^2\}$  is \_\_\_\_\_

(A)  $\frac{16}{5}$

(B)  $\frac{32}{5}$

(C) 16

(D) 32

**Use the code: BVREDDY , to get maximum benefits**

355. The value of  $\int_0^{\infty} e^{-y^3} \cdot y^{1/2} dy$  is \_\_\_\_\_

(GATE-ME-1994)

Use the code: BVREDDY , to get maximum benefits

**356.** For  $\lambda > 0$ , the value of integral  $\int_0^\infty e^{-\lambda x^2} dx$  equals

(A)  $\frac{1}{2} \sqrt{\frac{\pi}{\lambda}}$

(C)  $\sqrt{\frac{2\pi}{\lambda}}$

(B)  $\sqrt{\frac{\pi}{2\lambda}}$

(D)  $2 \sqrt{\frac{\pi}{\lambda}}$

**Use the code: BVREDDY , to get maximum benefits**

357. The value of the double integral  $\int_0^{1/x} \int_x^{1/x} \frac{x}{1+y^2} dx dy = \underline{\hspace{2cm}}$  (GATE-EC-1993)

Use the code: BVREDDY , to get maximum benefits

358. Given  $\int_{-\infty}^{\infty} e^{-x^2} dx = \sqrt{\pi}$ . If a and b are integers, the value of  $\int_{-\infty}^{\infty} e^{-a(x+b)^2} dx$  is \_\_\_\_\_ (GATE-2022-ME)

- (a)  $\sqrt{a\pi}$
- (b)  $\sqrt{\frac{\pi}{a}}$
- (c)  $b\sqrt{\pi a}$
- (d)  $b\sqrt{\frac{\pi}{a}}$

Use the code: BVREDDY , to get maximum benefits

359. The value of the integral  $\int_{-\infty}^0 e^{-\left(\frac{x^2}{20}\right)} dx$  is \_\_\_\_\_

- (A)  $1/2$
- (B)  $-\sqrt{5\pi}$
- (C)  $\sqrt{10}$
- (D)  $\pi$

Use the code: BVREDDY , to get maximum benefits

**360.** Evaluate:  $\lim_{x \rightarrow 0} \frac{1}{x^{191}}$

- (A)  $\infty$
- (B) 0
- (C)  $-\infty$
- (D) None of these

**Use the code: BVREDDY , to get maximum benefits**

**361.** Which of the following is true?

- (A) Every continuous function has derivative at every point
- (B) Every differentiable function may not be continuous everywhere
- (C) Every differentiable function is automatically continuous
- (D) A function is continuous iff it is differentiable

**Use the code: BVREDDY , to get maximum benefits**

**362.** Which of the following options are necessary so that a function is differentiable at a particular point  $x$ ?

- (i) The existence of function at  $x$
  - (ii) Existence of either right-handed or left-handed derivative or both
  - (iii) Continuity of the function at that particular point,  $x$
  - (iv) Existence of both right-handed and left-handed derivative at  $x$
  - (v) Existence and equality of both right-handed and left-handed derivative at  $x$
- |                |                 |
|----------------|-----------------|
| (A) (i), (v)   | (B) (iii), (iv) |
| (C) (i), (iii) | (D) (i), (ii)   |

**Use the code: BVRUEDDY , to get maximum benefits**

**363.** The function  $f(x) = |x - 4|$  on the interval  $[0, 5]$  is

- (a) continuous and differentiable
- (b) neither continuous nor differentiable
- (c) differentiable but not continuous
- (d) continuous on the interval but not differentiable

**Use the code: BVREDDY , to get maximum benefits**

**364.** Evaluate:  $\lim_{x \rightarrow 0} \frac{1 - \cos x}{x}$

(A) 0      (B) 1      (C) 2      (D)  $\infty$

**Use the code: BVREDDY , to get maximum benefits**

**365.** Consider the following statements:

S1:  $f(x) = \cos|x|$  is continuous at  $x = 0$

S2:  $f(x) = \cos|x|$  is differentiable at  $x = 0$

- (A) S1 and S2 both are true
- (B) S1 is true, S2 is false
- (C) S1 is false, S2 is true
- (D) Both are false

**366.** Consider the following function:

$$\begin{aligned}f(x) &= e^x \sin x \quad (x \neq 0) \\&= 0 \quad (x = 0)\end{aligned}$$

Which of the following is true?

- (A)  $f$  is differentiable and hence continuous at  $x = 0$
- (B)  $f$  is continuous but not differentiable at  $x = 0$
- (C)  $f$  is neither continuous nor differentiable at  $x = 0$
- (D)  $f$  is differentiable but not continuous at  $x = 0$

**367.** Consider the function:  $f(x) = [x] + 1$  over positive integer including 0.

Then the total number of point of discontinuities of  $f(x)$  are,

- (A) 1
- (B) Infinite
- (C) 0
- (D) None of these

**368.**

Consider the following function:

$$f(x) = x + |x| + 5$$

Which of the following is true?

- (A)  $f$  is continuous and differentiable at  
 $x = 0$
- (B)  $f$  is continuous but not differentiable at  
 $x = 0$
- (C)  $f$  is differentiable but not continuous at  
 $x = 0$
- (D)  $f$  is neither differentiable nor  
continuous at  $x = 0$

**Use the code: BVREDDY , to get maximum benefits**

**369.** The derivative of nth - root function

$$f(x) = \sqrt[n]{x}$$
 is,

(A)  $\frac{1}{n} x^{\frac{1}{n}-1}$

(B)  $nx^{n-1}$

(C)  $\frac{1}{n} x^{n-1}$

(D)  $\sqrt{n} x^{\sqrt{n}-1}$

**Use the code: BVREDDY , to get maximum benefits**

**370.** Which of the following points are least essential so that Mean Value theorem will be valid for the function  $f(x)$ ?

- (A) Continuity and differentiability of  $f(x)$  in the interval including end-points
- (B) Continuity and differentiability of  $f(x)$  in the interval excluding the end points
- (C) Continuity in closed interval and differentiability in the open interval
- (D) Only differentiability in closed interval

**Use the code: BVREDDY , to get maximum benefits**

**371.**  $\lim_{x \rightarrow 0} \frac{\sqrt[k]{1+x} - 1}{x}$  (k is a positive integer)

- (A) k      (B) -k      (C)  $\frac{1}{k}$       (D)  $-\frac{1}{k}$

Use the code: **BVREDDY**, to get maximum benefits

**372.**  $\lim_{x \rightarrow 1} \frac{x^2 - \sqrt{x}}{\sqrt{x} - 1}$

- (A) 1      (B) 2      (C) 3      (D) 4

Use the code: BVREDDY , to get maximum benefits

**373.**  $\lim_{x \rightarrow 0} \frac{\sqrt[3]{1+x} - \sqrt[3]{1-x}}{x} =$

- (A)  $\frac{1}{3}$       (B)  $\frac{2}{3}$       (C) 0      (D) 1

Use the code: BVREDDY , to get maximum benefits

**374.**

$$\lim_{x \rightarrow a} \frac{x^{\frac{5}{8}} - a^{\frac{5}{8}}}{x^{\frac{1}{3}} - a^{\frac{1}{3}}} =$$

(A)  $\frac{15}{8} a^{\frac{7}{24}}$

(C)  $\frac{-15}{8} a^{\frac{7}{24}}$

(B)  $\frac{15}{4} a^{\frac{7}{24}}$

(D)  $\frac{15}{4} a^{\frac{-7}{24}}$

**Use the code: BVREDDY , to get maximum benefits**

**375.**  $\lim_{x \rightarrow 0} \frac{\sin 3x \tan 4x}{x \sin 5x}$

- (A) 1      (B)  $\frac{5}{12}$       (C) 0      (D)  $\frac{12}{5}$

Use the code: **BVREDDY**, to get maximum benefits

**376.**  $\lim_{x \rightarrow 0} \frac{(1 - e^x) \sin x}{x^2 + x^3} =$

- (A) -1      (B) 0      (C) 1      (D) 2

**Use the code: BVREDDY , to get maximum benefits**

**377.**  $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\left(\frac{\pi}{2} - x\right) \sec x}{\cos \sec x} =$

- (A) 1      (B) 0      (C) -1      (D)  $\frac{1}{\pi}$

Use the code: BVREDDY , to get maximum benefits

**378.**  $\lim_{x \rightarrow 0} \frac{4^x - 9^x}{x(4^x + 9^x)} = \underline{\hspace{2cm}}$

(A)  $\ln\left(\frac{3}{2}\right)$

(B)  $\ln\left(\frac{2}{3}\right)$

(C)  $\ln\left(\frac{4}{3}\right)$

(D)  $\ln 2$

**Use the code: BVREDDY , to get maximum benefits**

**379.**

$$\lim_{x \rightarrow 0} \frac{a^{\tan x} - 1}{x} =$$

- (A) a      (B) 1      (C)  $2 \ln a$       (D)  $\ln a$

**Use the code: BVREDDY , to get maximum benefits**

380. The function  $f(x) = (1+x)^{\frac{5}{x}}$  for  $x \neq 0$   
 $= e^5$  for  $x = 0$

then

- (A)  $f(x)$  is continuous at  $x=0$
- (B) right continuous at  $x=0$
- (C) left continuous at  $x=0$
- (D) cannot be determined

381. Evaluate:  $\lim_{n \rightarrow \infty} \frac{n^2 + 1}{n^2 + n + 1}$

- (A) Undefined
- (B) 1
- (C) 0
- (D) None of these

Use the code: BVREDDY , to get maximum benefits

**382.** Evaluate:  $\lim_{x \rightarrow 7} \left[ \frac{x^6 - 7^6}{x - 7} + \frac{x^2 - 7^2}{x - 7} \right]$

- (A) 327040      (B) 100856  
(C)  $\infty$       (D) None of these

Use the code: **BVREDDY**, to get maximum benefits

**383.**

Evaluate:  $\lim_{x \rightarrow 0} \frac{\frac{2 \sin^4 x}{2}}{(x^4)^2}$

(A) 16

(B)  $\frac{1}{2}$

(C) not exist

(D)  $\frac{1}{4}$

**Use the code: BVREDDY , to get maximum benefits**

**384.** Consider the statements:

S1:  $f(x) = x + [x]$ ,  $x \in \mathbb{Z}$  is not continuous  
at  $x = 0$

S2:  $\lim_{x \rightarrow 0^+} f'(x) = \lim_{x \rightarrow 0^-} f'(x)$

- (A) S1 and S2 both are false
- (B) S1 is true, S2 is false
- (C) S1 is false, S2 is true
- (D) S1 and S2 both are true but S2 is not the correct explanation of S1

**Use the code: BVREDDY , to get maximum benefits**

**385.** Evaluate:  $\lim_{x \rightarrow 0} \frac{e^{2x} - 1}{\log(1 + x)}$

- (A) 0      (B) 2      (C) 4      (D)  $\frac{1}{2}$

Use the code: BVREDDY , to get maximum benefits

**386.** Evaluate:  $\lim_{x \rightarrow 0} \left( \frac{1}{\sin x} - \frac{1}{x} \right)$

- (A) 0      (B)  $\infty$       (C) 1      (D)  $\frac{\pi}{2}$

**Use the code: BVREDDY , to get maximum benefits**

**387.**  $f(x) = \frac{x^2 - 4}{x - 2}$ , ( $x \neq 2$ ) and  $f(x) = a$  at  $x = 2$

Then, which of the following is true?

- (A)  $f(x)$  is continuous at  $x = 2$  if  $a = 1$
- (B)  $f(x)$  is continuous at  $x = 2$  if  $a = 4$
- (C)  $f(x)$  is continuous at  $x = 2$  if  $a = 2$
- (D)  $f(x)$  is continuous at  $x = 2$  if  $a = 0$

**388.** Evaluate :  $\lim_{x \rightarrow 0} \frac{5e^{\frac{1}{x}}}{e^2 + e^x}$

- (A) Doesn't exist      (B) 0
- (C)  $\frac{5}{e}$       (D) None of these

**Use the code: BVREDDY , to get maximum benefits**

**389.** The value of  $\lim_{x \rightarrow 2a} \frac{\sqrt{x-2a} + \sqrt{x} - \sqrt{2a}}{\sqrt{x^2 - 4a^2}}$

- (A)  $\frac{1}{\sqrt{a}}$    (B)  $\frac{1}{2\sqrt{a}}$    (C)  $\frac{\sqrt{a}}{2}$    (D)  $2\sqrt{a}$

**Use the code: BVREDDY , to get maximum benefits**

**390.** The value  $\lim_{x \rightarrow a} \frac{x - a}{|x - a|}$

- (A) 0
- (B) 1
- (C) -1
- (D) does not exist

**Use the code: BVREDDY , to get maximum benefits**

**391.**  $\lim_{x \rightarrow 5} \frac{\sin^2(x-5) \tan(x-5)}{(x^2 - 25)(x-5)}$

- (A) 1      (B)  $\frac{1}{10}$       (C) 0      (D) -6

**Use the code: BVREDDY , to get maximum benefits**

**392.**  $\lim_{x \rightarrow 0} \frac{\tan x - \sin x}{x^3}$

- (A) 1      (B)  $\frac{1}{2}$       (C)  $\frac{1}{4}$       (D)  $\frac{-1}{3}$

**Use the code: BVREDDY , to get maximum benefits**

**393.** If  $\lim_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1$  then a and b  
are

- (A)  $\frac{1}{2}, \frac{-3}{2}$
- (B)  $\frac{5}{2}, \frac{3}{2}$
- (C)  $\frac{-5}{2}, \frac{-3}{2}$
- (D)  $\frac{5}{2}, \frac{-3}{2}$

**394.**

$$\lim_{x \rightarrow \infty} \left( \frac{x+a}{x+b} \right)^{x+b}$$

- (A) 1      (B)  $e^{b-a}$       (C)  $e^{a-b}$       (D)  $e^b$

**Use the code: BVREDDY , to get maximum benefits**

**395.** The function  $f(x) = \frac{x \tan 2x}{\sin 3x \sin 5x}$  for  $x \neq 0$   
 $= k$  for  $x=0$

is continuous at  $x=0$  then  $f(0)=\underline{\hspace{2cm}}$ .

- (A)  $\frac{2}{13}$     (B)  $\frac{2}{17}$     (C)  $\frac{2}{11}$     (D)  $\frac{2}{15}$

**396.**  $\lim_{x \rightarrow \infty} \left( \frac{3x - 4}{3x + 2} \right)^{\frac{x+1}{3}} =$

- (A)  $e^{-\frac{2}{3}}$     (B)  $e^{\frac{3}{2}}$     (C)  $e^{\frac{2}{3}}$     (D)  $e$

**Use the code: BVREDDY , to get maximum benefits**

**397.** If the function  $f(x) = \frac{\sin^2 ax}{x^2}$  for  $x \neq 0$   
 $= 1$  for  $x = 0$

is continuous at  $x=0$  then  $a = \underline{\hspace{2cm}}$ .

- (A)  $\pm 1$     (B) 0    (C)  $\pm \frac{1}{2}$     (D)  $\pm \frac{1}{3}$

**398.** A function  $f(x)$  is defined as

$$f(x) = ax - b; \quad x \leq 1$$

$$3x; \quad 1 < x < 2$$

$$bx^2 - a; \quad x \geq 2$$

is continuous at  $x=1, 2$  then

(A)  $a=5, b=2$       (B)  $a=6, b=3$

(C)  $a=7, b=4$       (D)  $a=8, b=5$

**Use the code: BVREDDY , to get maximum benefits**

399.

Let  $f(x) = x$  for  $x < 1$

$= 2 - x$  for  $1 \leq x \leq 2$

$= -2 + 3x - x^2$  for  $x > 2$

then  $f(x)$  is

- (A) differentiable at  $x=1$ ,
- (B) differentiable at  $x=2$
- (C) differentiable at  $x=1$  and  $x=2$
- (D) differentiable at  $x=0$

**400.**  $L_{t_5}(x - [x]) = \underline{\hspace{2cm}}$ , where  $[x]$  is a step function

- (a)  $\frac{1}{4}$
- (b)  $-\frac{1}{4}$
- (c)  $\frac{1}{3}$
- (d) Doesn't exist

**Use the code: BVREDDY , to get maximum benefits**

**401.**  $\lim_{x \rightarrow 2} \frac{|x - 2|}{x - 2} = \underline{\hspace{2cm}}$ , where  $|x - 2|$  is a modulus function.

- (a) 1
- (b) 2
- (c) -1
- (d) Doesn't exist

**402.**  $\lim_{x \rightarrow 4} [x] = \underline{\hspace{2cm}}$ , where  $[x]$  is a step function

- (a) - 4
- (b) 4
- (c) 1
- (d) Doesn't exist

**Use the code: BVREDDY , to get maximum benefits**

**403.**  $\lim_{x \rightarrow 0} \frac{x \sin(x)}{1 - \cos(x)} = \underline{\hspace{2cm}}$ .

**Use the code: BVREDDY , to get maximum benefits**

**404.**  $\lim_{x \rightarrow \frac{\pi}{2}} (\tan x - \sec x) = \underline{\hspace{2cm}}$ .

**Use the code: BVREDDY , to get maximum benefits**

**405.**

$$\underset{x \rightarrow \infty}{\text{Lt}} (1+x^2)^{e^{-x}} = \underline{\hspace{2cm}}$$

- (a) 2      (b) 0      (c) 1      (d) -1

**Use the code: BVREDDY , to get maximum benefits**

**406.**

$$\lim_{x \rightarrow 0} x^x = \underline{\hspace{2cm}}$$

- (a) 0      (b) 1      (c) -1      (d) e

**Use the code: BVREDDY , to get maximum benefits**

407.  $\lim_{x \rightarrow 0} \frac{\sqrt{a+x} - \sqrt{a-x}}{x} =$

(a)  $\frac{1}{\sqrt{a}}$

(b)  $\sqrt{a}$

(c)  $\frac{1}{2\sqrt{a}}$

(d)  $2\sqrt{a}$

Use the code: BVREDDY , to get maximum benefits

**408.** Which of the following is continuous at  
 $x = 2$ ?

(a)  $f(x) = \begin{cases} 3 & , x = 2 \\ 2x - 1, & x > 2 \\ \frac{x+7}{3}, & x < 2 \end{cases}$

(b)  $f(x) = \begin{cases} 2 & , x = 2 \\ 8 - x, & x \neq 2 \end{cases}$

(c)  $f(x) = \begin{cases} x + 2, & x \leq 2 \\ x - 4, & x > 2 \end{cases}$

(d)  $f(x) = \frac{1}{x^3 - 8}, x \neq 2$

Use the code: DVRCVDV1, to get maximum benefits

**409.**

Let  $g(x) = \begin{cases} -x, & x \leq 1 \\ x+1, & x \geq 1 \end{cases}$  and

$$f(x) = \begin{cases} 1-x, & x \leq 0 \\ x^2, & x > 0 \end{cases}.$$

Consider the composition of f and g, i.e.

$$(f \circ g)(x) = f(g(x)).$$

The number of discontinuities in  $(f \circ g)(x)$

present in the interval  $(-\infty, 0)$  is

- |       |       |
|-------|-------|
| (a) 0 | (b) 1 |
| (c) 2 | (d) 4 |

**Use the code: BVREDDY , to get maximum benefits**

**410.**

$$\text{If } f(x) = \begin{cases} x & , \quad x \leq 1 \\ 2x - 1, & \text{when } x > 1 \end{cases}$$

then at  $x = 1$  which of the following is true?

- (a)  $f(x)$  is continuous but not differentiable
- (b)  $f(x)$  is continuous and differentiable
- (c)  $f(x)$  is neither continuous nor differentiable
- (d)  $f(x)$  is differentiable but not continuous

**Use the code: BVREDDY , to get maximum benefits**

**411.** Let  $f(x) = \begin{cases} x^2 & , \text{ if } x \leq 2 \\ mx + b, & \text{if } x > 2 \end{cases}$ .

If  $f(x)$  is differentiable every where then

- (a)  $m = 4$  and  $b = -4$
- (b)  $m = 4$  and  $b = 4$
- (c)  $m = -4$  and  $b = -4$
- (d)  $m = -4$  and  $b = 4$

**412.**

Which of the following functions is differentiable in the domain  $[-1, 1]$ ?

- (a)  $f(x) = |x|$
- (b)  $f(x) = \cot x$
- (c)  $f(x) = \sec x$
- (d)  $f(x) = \operatorname{cosec} x$

**Use the code: BVREDDY , to get maximum benefits**

**413.**  $\lim_{x \rightarrow 0} \frac{1 - \cos x}{x \sin x} =$

(a) 0

(b) 1

(c)  $\frac{1}{2}$

(d) does not exist

**Use the code: BVREDDY , to get maximum benefits**

**414.** If  $\lim_{x \rightarrow 0} \frac{\sin 2x + a \sin x}{x^3} = b$  where  $b$  is finite

value then find  $a$  and

- (a)  $a = -2, b = -1$
- (b)  $a = 2, b = -1$
- (c)  $a = 0, b = 3$
- (d)  $a = -2, b = 1$

**Use the code: BVREDDY , to get maximum benefits**

**415.**

$$\lim_{x \rightarrow 0} \frac{\log(\sin 2x)}{\log(\sin x)} = \underline{\hspace{2cm}}$$

**Use the code: BVREDDY , to get maximum benefits**

**416.**  $\lim_{x \rightarrow a} (a - x) \tan\left(\frac{\pi x}{2a}\right) = \underline{\hspace{2cm}}$ .

**Use the code: BVREDDY , to get maximum benefits**

417.  $\lim_{x \rightarrow 0} x^{\sin x} =$  \_\_\_\_\_.

Use the code: BVREDDY , to get maximum benefits

**418.**

$$\lim_{x \rightarrow 0} \left( \frac{1}{x} \right)^{\tan x} = \underline{\hspace{2cm}}$$

**Use the code: BVREDDY , to get maximum benefits**

**419.**  $\lim_{x \rightarrow \pi} \cot(x) =$

- (a) 0
- (b) 1
- (c) -1
- (d) does not exist

**Use the code: BVREDDY , to get maximum benefits**

**420.**

$\lim_{x \rightarrow a} [x] =$ , where  $[x]$  is step function and ‘a’

is an integer

- (a) a
- (b)  $a - 1$
- (c) 0
- (d) does not exist

**Use the code: BVREDDY , to get maximum benefits**

**421.**

$$\lim_{x \rightarrow \infty} x \tan\left(\frac{1}{x}\right) = \underline{\hspace{2cm}}.$$

**Use the code: BVREDDY , to get maximum benefits**

**422.**

If  $f(x) = (x + 1)^{\cot x}$  is continuous at  $x = 0$

then  $f(0) = \underline{\hspace{2cm}}$

(a) 0

(b) 1

(c) e

(d) none of these

**Use the code: BVREDDY , to get maximum benefits**

**423.**

Let  $f(x) = \begin{cases} 0 & \text{for } x = 0 \\ \frac{1}{2} - x & \text{for } 0 < x < \frac{1}{2} \\ \frac{1}{2} & \text{for } x = \frac{1}{2} \\ \frac{3}{2} - x & \text{for } \frac{1}{2} < x < 1 \\ 1 & \text{for } x \geq 1 \end{cases}$

then which of the following is true?

(a)  $f(x)$  is right continuous at  $x = 0$

(b)  $f(x)$  is discontinuous at  $x = \frac{1}{2}$

(c)  $f(x)$  is continuous at  $x = 1$

(d) All are true

', to get maximum benefits

**424.** If  $f(x) = 3 + x$  when  $x \geq 0$

$$= 3 - x \text{ when } x < 0$$

then  $f(x)$  at  $x = 0$  is

- (a) continuous but not differentiable
- (b) continuous and differentiable
- (c) neither continuous nor differentiable
- (d) differentiable but not continuous

**425.** If  $f(x) = x|x|$  then  $f(x)$  at  $x = 0$  is

- (a) continuous and differentiable
- (b) continuous but not differentiable
- (c) differentiable but not continuous
- (d) neither continuous nor differentiable

**Use the code: BVREDDY , to get maximum benefits**

**426.** The function  $f(x) = |x+1|$  on the interval  $[-2,0]$   
is

- (a) continuous and differentiable
- (b) continuous on the interval but not differentiable
- (c) neither continuous nor differentiable
- (d) differentiable but not continuous

**Use the code: BVREDDY , to get maximum benefits**

**427.** The function

$$f(x) = \begin{cases} \frac{x e^{1/x}}{1 + e^{1/x}}, & x \neq 0 \\ 0, & x = 0 \end{cases}$$

- (a) differentiable but not continuous at  $x = 0$
- (b) not differentiable at  $x = 0$
- (c) differentiable and continuous at  $x = 0$
- (d) not continuous at  $x = 0$

**Use the code: BVREDDY , to get maximum benefits**

**428.**  $\lim_{x \rightarrow 0} \sin\left(\frac{1}{x}\right) =$

- (a)  $\infty$
- (b) 0
- (c) 1
- (d) does not exist

**Use the code: BVREDDY , to get maximum benefits**

**429.**  $\lim_{x \rightarrow 0} x \cdot \sin\left(\frac{1}{x}\right) =$

- (a) 0
- (b) 1
- (c)  $\infty$
- (d) does not exist

**Use the code: BVREDDY , to get maximum benefits**

**430.**  $\lim_{x \rightarrow 2} \sqrt{4 - x^2} =$

- (a) 0
- (b) imaginary
- (c) does not exist
- (d) indeterminate

**Use the code: BVREDDY , to get maximum benefits**

**431.**  $\lim_{x \rightarrow 0^+} \log x =$

- (a)  $\infty$
- (b)  $-\infty$
- (c) 0
- (d) does not exist

**Use the code: BVREDDY , to get maximum benefits**

**432.** If  $\lim_{x \rightarrow 0} \left\{ \frac{x(1 + a \cos x) - b \sin x}{x^3} \right\} = 1$

then  $(a, b) =$

- |                 |                  |
|-----------------|------------------|
| (a) $-5/2, 3/2$ | (b) $5/2, -3/2$  |
| (c) $5/2, 3/2$  | (d) $-5/2, -3/2$ |

**433.**  $\lim_{x \rightarrow 0} \left( \frac{\log x}{\log \cosec x} \right) =$

- (a) 1
- (b) -1
- (c) 0
- (d) does not exist

**Use the code: BVREDDY , to get maximum benefits**

**434.**  $\lim_{x \rightarrow \infty} \left( \frac{x^n}{e^x} \right) =$

- (a) 0
- (b)  $n!$
- (c) 1
- (d)  $\infty$

**Use the code: BVREDDY , to get maximum benefits**

**435.**

$$\lim_{x \rightarrow \infty} \left( \frac{\log x}{x^n} \right) =$$

(a) 0

(b) 1/n

(c) 1

(d) -1/n

**Use the code: BVREDDY , to get maximum benefits**

**436.** If  $f(x) = \begin{cases} \sin^2(ax) / x^2, & x \neq 0 \\ 1, & x = 0 \end{cases}$

is continuous then  $a =$

- (a) 0, 1
- (b) -1, 1
- (c) 0, -1
- (d) none of these

**Use the code: BVREDDY , to get maximum benefits**

**437.** If  $f(x) = \begin{cases} 1 & \text{when } x < 0 \\ 1 + \sin x & \text{when } 0 \leq x \leq \pi/2 \\ 2 + (x - \pi/2)^2 & \text{when } x > \pi/2 \end{cases}$

then  $f(x)$  is

- (a) continuous at  $x = 0$  but discontinuous at  $x = \pi/2$
- (b) continuous at  $x = \pi/2$  but discontinuous at  $x = 0$
- (c) continuous for all values of  $x$
- (d) discontinuous at  $x = 0$  and at  $x = \pi/2$

**438.** If  $f(x) = x^2 \sin\left(\frac{1}{x}\right)$  then which of the following is true?

- (a)  $f'(0)$  exists but  $f''(0)$  does not exist
- (b) both  $f'(0)$  and  $f''(0)$  does not exist
- (c) neither  $f'(0)$  nor  $f''(0)$  does not exist
- (d)  $f'(0)$  does not exist but  $f''(0)$  exists

**Use the code: BVREDDY , to get maximum benefits**

- 439.** If  $f(x) = x \left(1 + \left(\frac{1}{3}\right) \sin(\log x)\right)$  then  $f(x)$  is
- (a) continuous at  $x = 0$  but not differentiable at  $x = 0$
  - (b) differentiable at  $x = 0$  but not continuous at  $x = 0$
  - (c) continuous and differentiable at  $x = 0$
  - (d) neither continuous nor differentiable at  $x = 0$

**Use the code: BVREDDY , to get maximum benefits**

**440.** The function  $f(x) = |x| + |x + 1| + |x - 2|$  is

differentiable at  $x =$

- (a) 1
- (b) -1
- (c) 0
- (d) 2

**Use the code: BVREDDY , to get maximum benefits**

**441.** If  $f(x) = 2 + x$  when  $x \geq 0$

$$= 2 - x \text{ when } x < 0$$

then  $f(x)$  at  $x = 0$  is

- (a) continuous but not differentiable
- (b) continuous and differentiable
- (c) neither continuous nor differentiable
- (d) differentiable at  $x = 0$  but not continuous

**442.**

$$\text{Let } f(x) = \begin{cases} x^2 \cdot \sin\left(\frac{1}{x}\right), & x \neq 0 \\ 0, & x = 0 \end{cases}$$

At  $x = 0$ , which of the following is *true* ?

- (a)  $f(x)$  is continuous but not differentiable
- (b)  $f(x)$  is differentiable and continuous
- (c)  $f(x)$  is neither continuous nor  
differentiable
- (d)  $f(x)$  is differentiable but not continuous

**Use the code: BVREDDY , to get maximum benefits**

- 443.** If  $f(x) = x \cdot |x|$  then at  $x = 0$  which of the following statements is *true*?
- (a)  $f(x)$  is continuous and differentiable
  - (b)  $f(x)$  is not continuous and not differentiable
  - (c)  $f(x)$  is continuous but not differentiable
  - (d)  $f(x)$  is differentiable but not continuous

**Use the code: BVREDDY , to get maximum benefits**

**444.**

Let  $f(x) = \begin{cases} x, & \text{if } x \text{ is rational} \\ -x, & \text{if } x \text{ is irrational} \end{cases}$

Which of the following is *true*?

- (a)  $f(x)$  is continuous every where
- (b)  $f(x)$  is discontinuous every where
- (c)  $f(x)$  is discontinuous only at  $x = 0$
- (d)  $f(x)$  is continuous only at  $x = 0$

**Use the code: BVREDDY , to get maximum benefits**

**445.**  $\lim_{x \rightarrow 0} \frac{|x|}{x} = \underline{\hspace{2cm}}$ , where  $|x|$  is a modulus

function

- (a) 0
- (b) 1
- (c) -1
- (d) limit does not exist

**Use the code: BVREDDY , to get maximum benefits**

**446.**  $\lim_{x \rightarrow 6} [x] = \underline{\hspace{2cm}}$ , where  $[x]$  is a step

function

- (a) -6
- (b) 5
- (c) 0
- (d) limit does not exist

**Use the code: BVREDDY , to get maximum benefits**

**447.**

$$\lim_{x \rightarrow 0} \frac{x - \sin x}{1 - \cos x} = \underline{\hspace{2cm}}$$

(a) 0

(b) 4

(c) -3

(d) 1

**Use the code: BVREDDY , to get maximum benefits**

**448.**

$$\lim_{x \rightarrow \frac{\pi}{2}} \left( \sec x - \frac{1}{1 - \sin x} \right) = \text{_____}.$$

- (a) 0      (b)  $\infty$       (c) -1      (d) 100

**Use the code: BVREDDY , to get maximum benefits**

**449.**

$$\underset{n \rightarrow \infty}{\text{Lt}} \left( 7^n + 5^n \right)^{\frac{1}{n}} = \underline{\hspace{2cm}}.$$

(a) 7

(b) -7

(c) 5

(d) 0

**Use the code: BVREDDY , to get maximum benefits**

**450.** If  $f(x) = \left(\frac{1-x}{x+1}\right)^{\frac{1}{x}}$  is continuous at  $x = 0$

then  $f(0) =$

- (a)  $e^{-2}$
- (b)  $e^2$
- (c)  $\sqrt{e}$
- (d)  $e^{-1/2}$

**Use the code: BVREDDY , to get maximum benefits**

**451.** Which one of the following functions is continuous at  $x = 3$ ?

(a)  $f(x) = \begin{cases} 5, & \text{if } x = 3 \\ 2x - 1, & \text{if } x > 3 \\ \frac{x+7}{2}, & \text{if } x < 3 \end{cases}$

(b)  $f(x) = \begin{cases} 4, & \text{if } x = 3 \\ 8 - x & \text{if } x \neq 3 \end{cases}$

(c)  $f(x) = \begin{cases} x + 3, & \text{if } x \leq 3 \\ x - 4 & \text{if } x > 3 \end{cases}$

(d)  $f(x) = \frac{1}{x^3 - 27}, \quad \text{if } x \neq 3$

**Use the code: BVREDDY , to get maximum benefits**

**452.** Let  $f$  be a real-valued function of a real variable defined as

$$f(x) = x^2 \text{ for } x \geq 0, \text{ and } f(x) = -x^2 \text{ for } x < 0.$$

Which one of the following statements is true?

- (a)  $f(x)$  is discontinuous at  $x = 0$
- (b)  $f(x)$  is continuous but not differentiable at  $x = 0$
- (c)  $f(x)$  is differentiable but its first derivative is not continuous at  $x = 0$
- (d)  $f(x)$  is differentiable but its first derivative is not differentiable at  $x = 0$

**Use the code: BVREDDY , to get maximum benefits**

**453.** If  $f(x) = \begin{cases} ax^2 + 1, & x \leq 1 \\ x^2 + ax + b, & x > 1 \end{cases}$  is differentiable

at  $x = 1$  then

- (a)  $a = 1, b = 1$
- (b)  $a = 1, b = 0$
- (c)  $a = 2, b = 0$
- (d)  $a = 2, b = 1$

**Use the code: BVREDDY , to get maximum benefits**