



# Hashing Techniques

Course on C-Programming & Data Structures: GATE - 2024 & 2025



# Data Structure

# Hashing

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*Hello!*

**I am Vishvadeep Gothi**

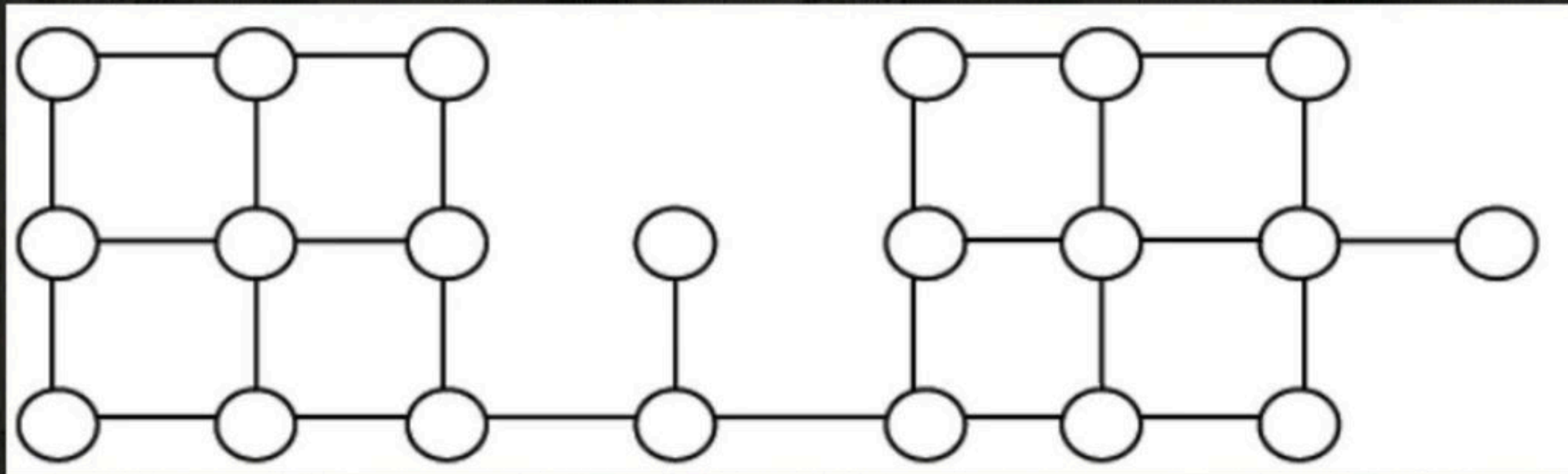
I am here because I love to teach

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## Question 4 GATE-2014

Suppose depth first search is executed on the graph below starting at some unknown vertex. Assume that a recursive call to visit a vertex is made only after first checking that the vertex has not been visited earlier. Then the maximum possible recursion depth (including the initial call) is \_\_\_\_\_.

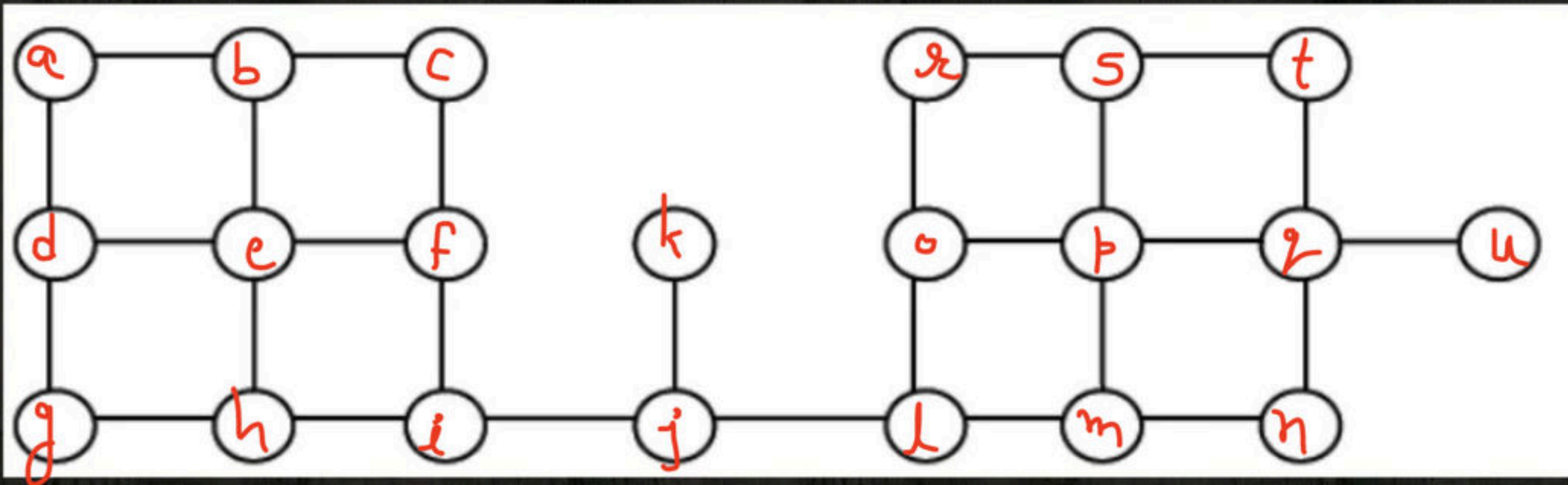




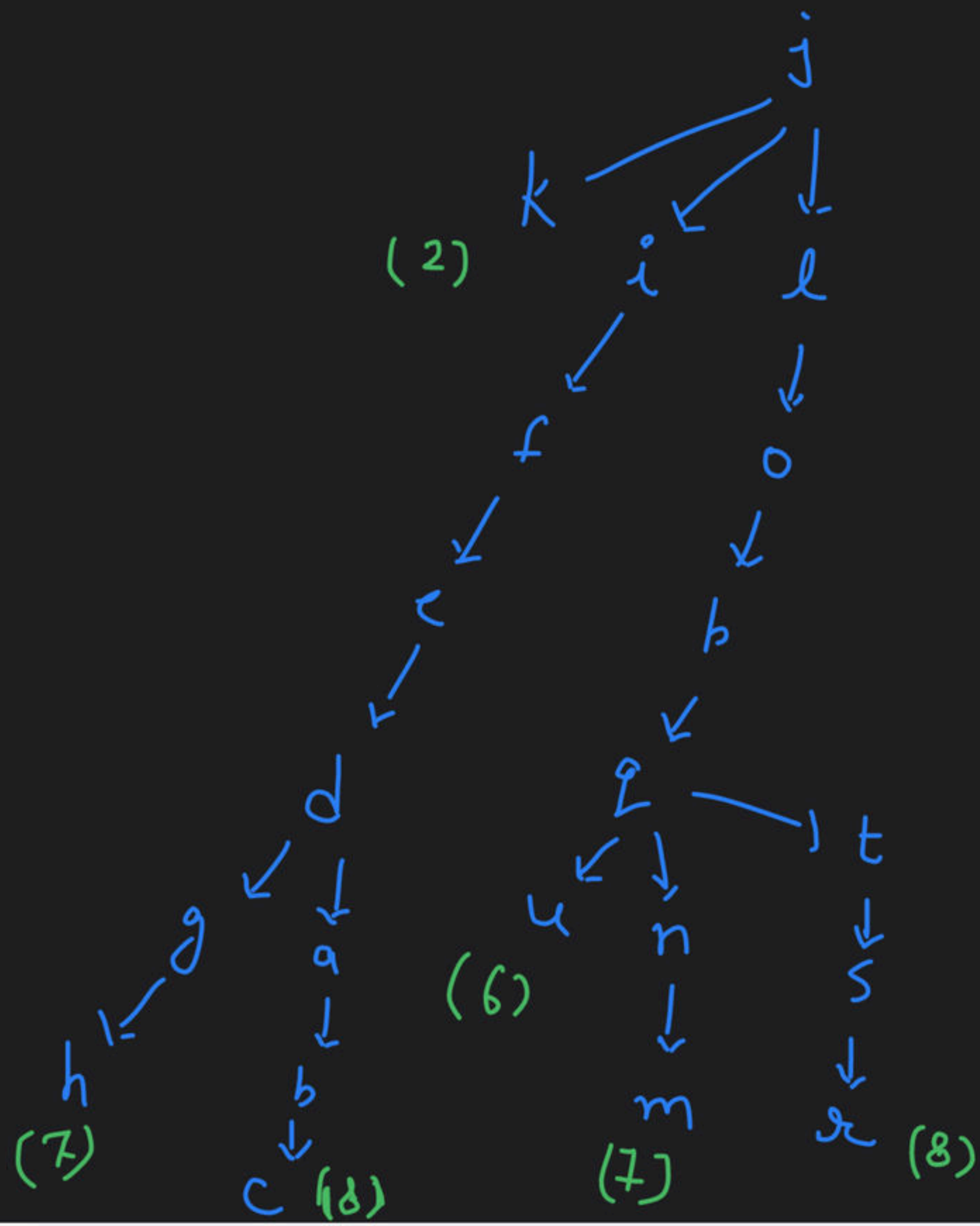
Ans = 8

## Question 5

Suppose depth first search is executed on the graph below starting at some unknown vertex. Assume that a recursive call to visit a vertex is made only after first checking that the vertex has not been visited earlier. Then the maximum possible recursion depth in best case (including the initial call) is 8.



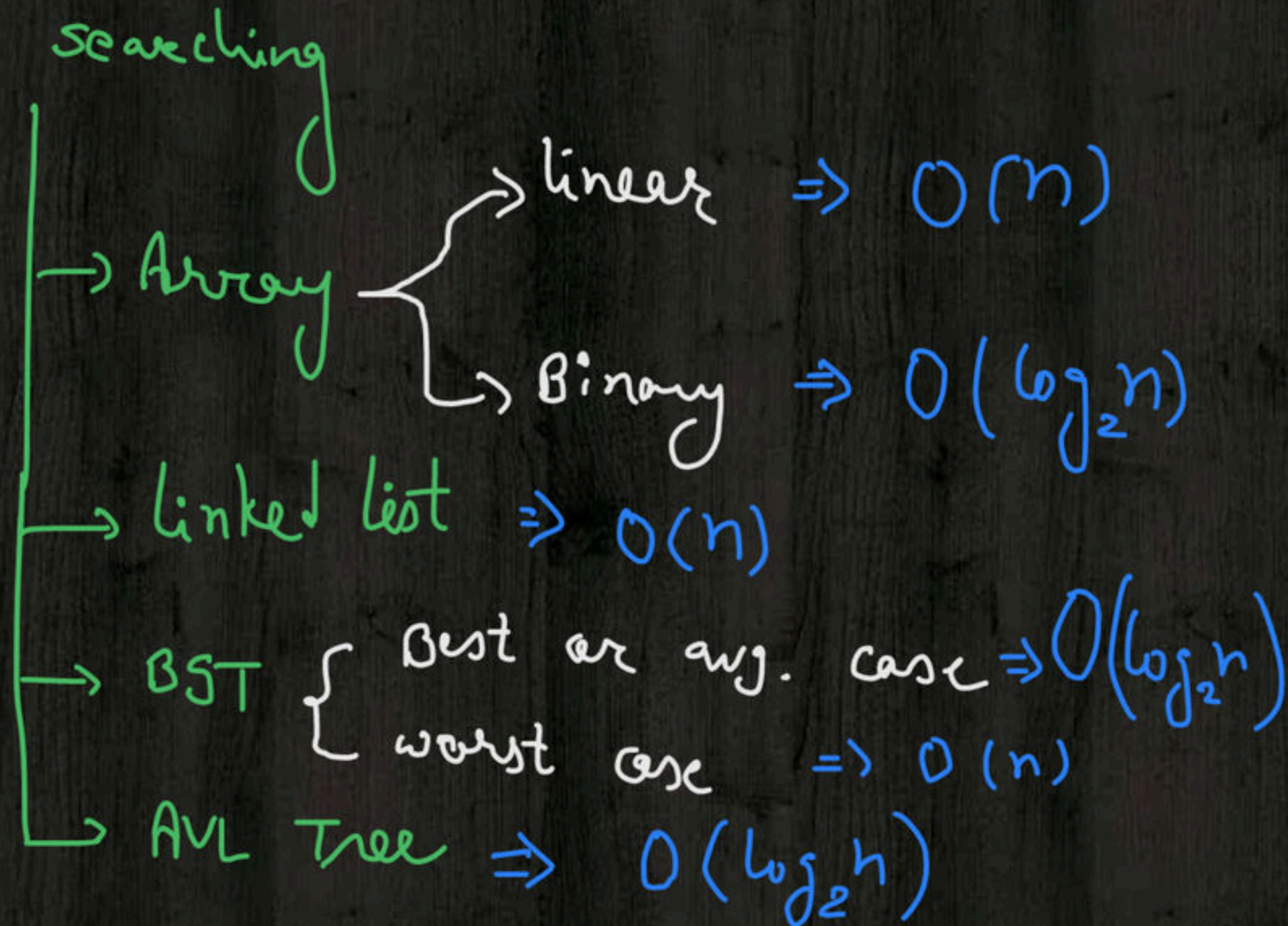






# Hashing

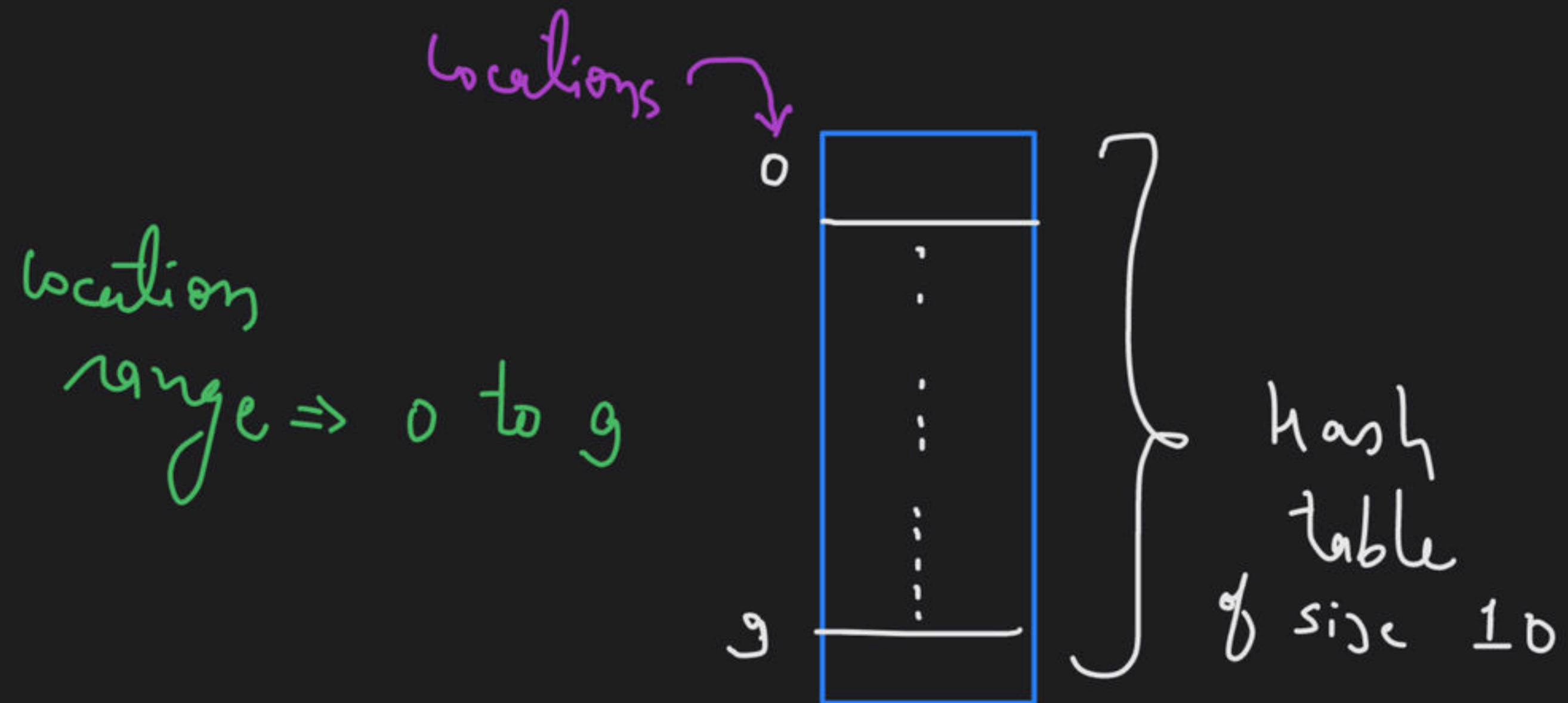
Searching technique which can provide result in constant time





Hash function  $H()$   $\Rightarrow$  applied on key  $\Rightarrow$  result = location

$$\text{Location} = H(\text{key})$$





# Hashing Techniques

1. Direct Hashing
2. Subtraction Method
- ~~3.~~ 3. Division Method ✓
4. Fold Shifting Method
5. Fold Boundary Method
6. Digit Extraction Method
7. Mid-square Method



# Direct Hashing

$$\text{location} = H(\text{key}) = \text{key}$$

range of keys limited  
by location range

key $\Rightarrow$ 15	21	1	90
loc $\Rightarrow$ 15	21	1	90

Assume there is a hash table with location  
range 00-99.  
key Range  $\Rightarrow$  0 to 99



## subtraction method

$$\text{location} = H(k) = k - m$$

$m$  is an integer

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example:-

$$H(k) = k - 4$$

keys range limited by  
location range

if location range 00 to 99

keys range  $\Rightarrow$  4 to 103



## Division / Modulo Division Method

$$\text{Location} = H(\text{key}) = \text{key} \bmod m$$

$m \Rightarrow$  is an integer

location range  $\Rightarrow 0$  to  $m-1$

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ex:-  $H(k) = k \bmod 5$

ex:- 152

$$152 \bmod 5 \Rightarrow 2$$

location range  $\Rightarrow 0$  to 4

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any key can be stored.



# Question 1

Which of the following is suitable hash function to have a range of locations from 1 to 1000?

- ☒ A.  $H(X) = X \% 1000$   $\rightarrow 0 \text{ to } 999$
- ☒ B.  $H(X) = X \% 999 + 1$   $\rightarrow (0 \text{ to } 998) + 1 \Rightarrow 1 \text{ to } 999$
- ☒ C.  $H(X) = (X+1) \% 1000$   $\rightarrow 0 \text{ to } 999$
- ☒ D.  $H(X) = (X \% 1000) + 1$   $\rightarrow (0 \text{ to } 999) + 1 \Rightarrow 1 \text{ to } 1000$
- ☒ E.  $H(X) = X \% (1000+1)$

$\downarrow$

$$x \% 1001 \Rightarrow 0 \text{ to } 1000$$



fold shifting

if location range  $\Rightarrow$  000 - 999

key:- 123112312

$$\begin{array}{r} 123 \\ + 112 \\ \hline 312 \end{array}$$

547  $\Leftarrow$  location

or

$$\begin{array}{r} 123 \\ + 312 \\ \hline 211 \end{array}$$

reverse of  
centre of fold

if sum > 999

sum % 1000  $\Rightarrow$  location



Fold boundary

key:- 321 // 2531

$$\begin{array}{r} 312 \\ + 531 \\ \hline 843 \end{array} \Rightarrow \text{location}$$

if sym > 999

$$(sum \% 1000) \Rightarrow \text{location}$$

key :- 1 2 3 4 5

12 345 or

12345

$$\begin{array}{r} 123 \\ 45 \\ \hline \end{array}$$

$$\begin{array}{r} 395 \\ + 12 \\ \hline \end{array}$$



## Digit Extraction

if location range  $\Rightarrow$  000 to 999

$$H(k) = (\text{key})_{1,4,5}$$

ex:-  $\text{key} = 492453$

$$H(k) = 923 \text{ or } 329$$

$$445$$



## Mid square:-

if location range  $\Rightarrow 000 - 999$

$$H(k) = (k^2)_{\text{middle 3 digits}}$$

ex:-  $k = 136$

$$\begin{aligned} H(k) &= (136^2)_{\text{middle}} = (18496)_{\text{middle}} \\ &= \underline{\underline{849}} \end{aligned}$$

if  $key = 58$

$$58^2 = 3364$$

$\downarrow$   
middle  $\Rightarrow 36$   
 $\Rightarrow 364$   
 $\Rightarrow 336$



# Collision



if  $H(k_1) \Rightarrow \text{location } L$

Collision at  $L$ , if location  $L$  is preoccupied.

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If for a key, hash function generates a preoccupied location, then there is a collision at that location.



ex:-  $H(k) = k \bmod 10$

$\Rightarrow$  location range  $\Rightarrow 0$  to  $9$

keys to store :-

32, 64, 55, 62

$$32 \% 10 \Rightarrow 2$$

$$64 \% 10 \Rightarrow 4$$

$$55 \% 10 \Rightarrow 5$$

$$62 \% 10 \Rightarrow 2 \Rightarrow \text{Collision}$$

0	
1	
2	32
3	
4	64
5	55
6	
7	
8	
9	



# Collision Resolution Techniques

open addressing  
or

closed Hashing

- Linear probing
- Quadratic Probing
- Random Probing
- Double Hashing

closed addressing  
or

open Hashing

- chaining or open chaining



# Linear Probing



# Quadratic Probing



# Random Probing



# Double Hashing



# Chaining



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# Happy Learning

