



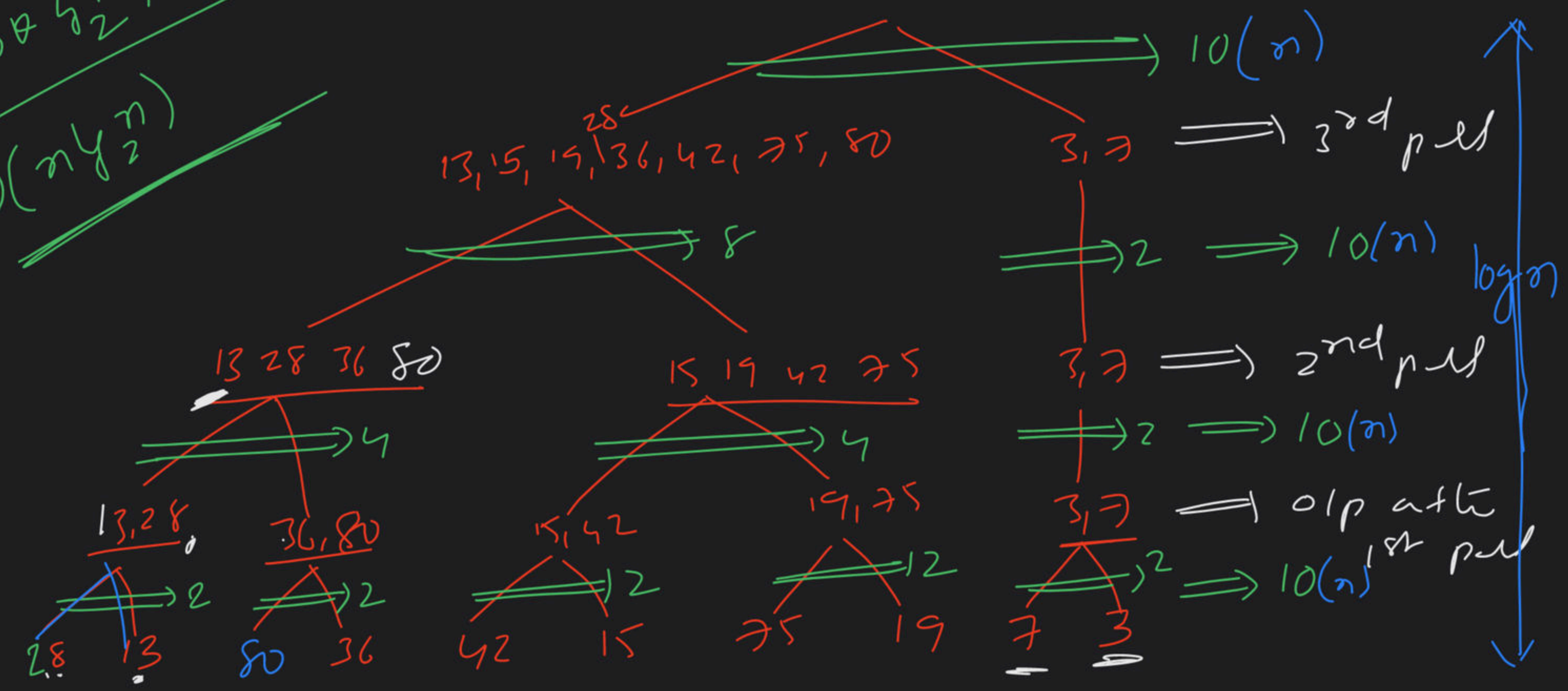
Doubt Clearing Session

Complete Course on Algorithm for GATE - CS & IT

Straight 2-way mergesort

~~$O(10 \times 4^{10})$~~
 ~~$O(n \log^2 n)$~~

7, 7, 13, 15, 15, 28, 36, 42, 75, 80 \Rightarrow 4th pass



n	0	1	2	3	4	5	6	7	8
$f(n)$	0	1	1	2	3	5	8	13	21

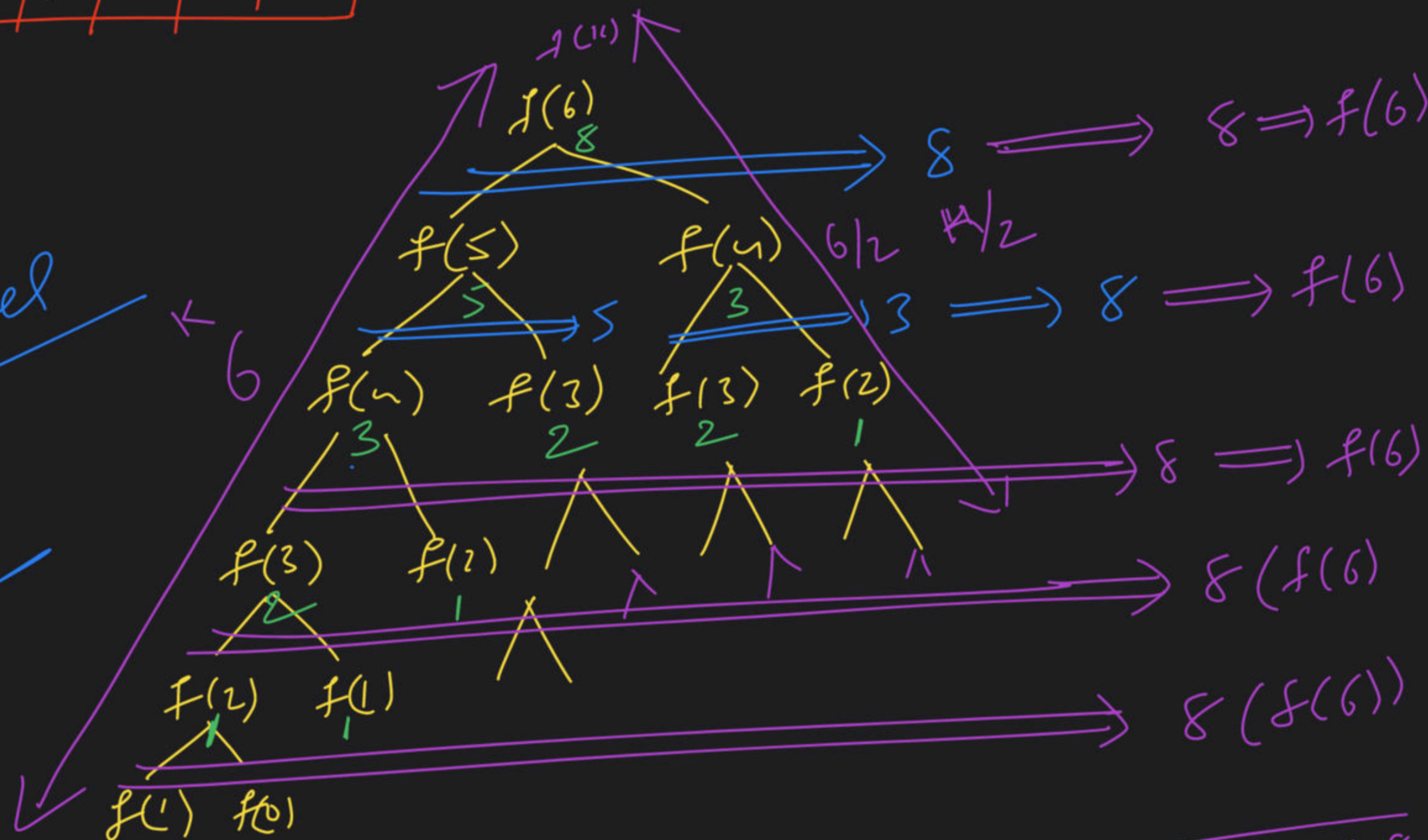
Fibonacci merge sort

Divide
in the form 15
Fibonacci series

combine
no-change

$\Theta(k \cdot f(k))$

$$\Theta(k \cdot f(k)) \leq T(k) \leq O[k \cdot f(k)] \leq 6 \cdot f(6) = 6 \cdot 8$$



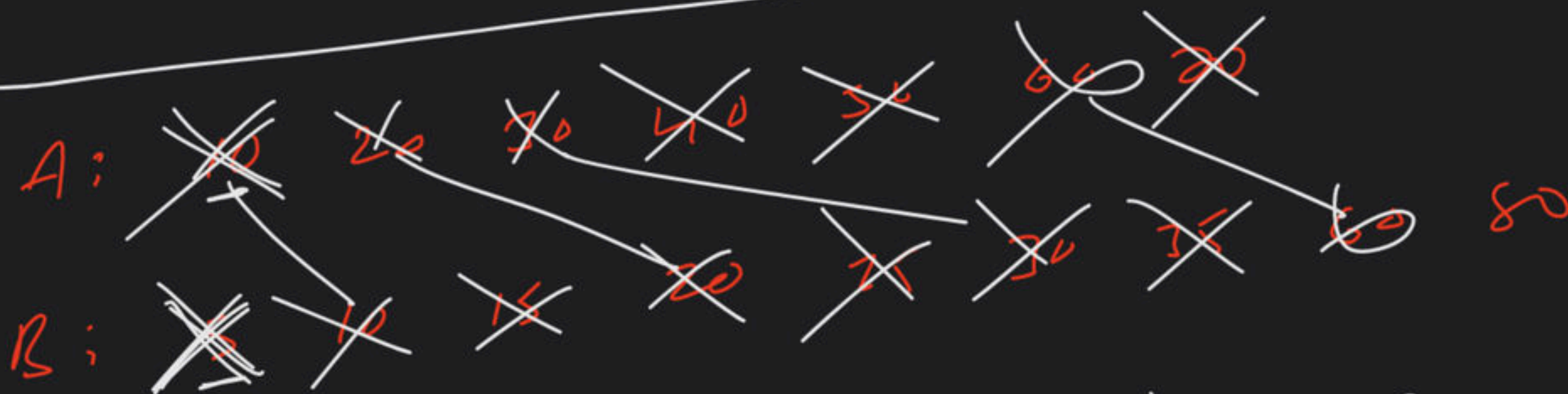
i/p: 2-~~sorted~~ arrays

A — m — distinct ele 5, 10
 B — n — distinct ele 5, 10, 20

o/p: Find $A \cap B$, $A \cup B$

Stable.

TC? [Best Algo]
 wc



$A \cap B$
 $m \& n$
 $m \& n$
 $O(n^2) [wc]$

$m \& 35(n)$
 $m \& \log n$
 $O(n \log n) [wc]$

$A \cap B$
 modified merge algo
 $\Rightarrow O(m+n)$
 (cr)
 $O(2n) \Rightarrow O(n)$

AUB

A: ~~10, 20, 30~~

B: ~~5, 8, 9, 10, 15, 20, 50~~

① LS

$O(n^2)$

③ modified merge

5 8 9 10 15 20 30 50

$\theta(n+n) \Rightarrow \theta(n)$

② BS

$O(n \log n)$

not sorted

$A \cap B, A \cup B$

1. sort \implies arr

2. Apply modified merge algo \implies

$\Theta(n \log n)$

i/p: 50, 10_a, 20, 10_b, 60

St ← 86

o/p: 10_a 10_b 50 60 20

o/p: 10_b 10_a

50 60 20

Not St ← 86

$$A = 10, 20, 30 \Rightarrow m$$

$$B = 10, 20, 40 \Rightarrow n$$

$$A = 10, 20, 30, 40, 110, 200$$

$$B = 10, 200$$

$$A \cup B = 10, 20, 30, 40 \left[\begin{array}{l} \max \Rightarrow m+n \\ \min \Rightarrow \max(m, n) \end{array} \right]$$

$$A \cap B = \{10, 10, 20, 20, 30, 40\} \text{ always } m+n$$

$A \cap B = \emptyset$	\min	\max	$\min(m, n)$	\max
			10	20
			20	30
			30	40
			40	
			10	40
			10, 40	

mergesort

⇓

space complexity

stack
space

⇓

$\log n$

merge-ops

⇓

n

$O(n)$

⇓

outplace

O.P.TC

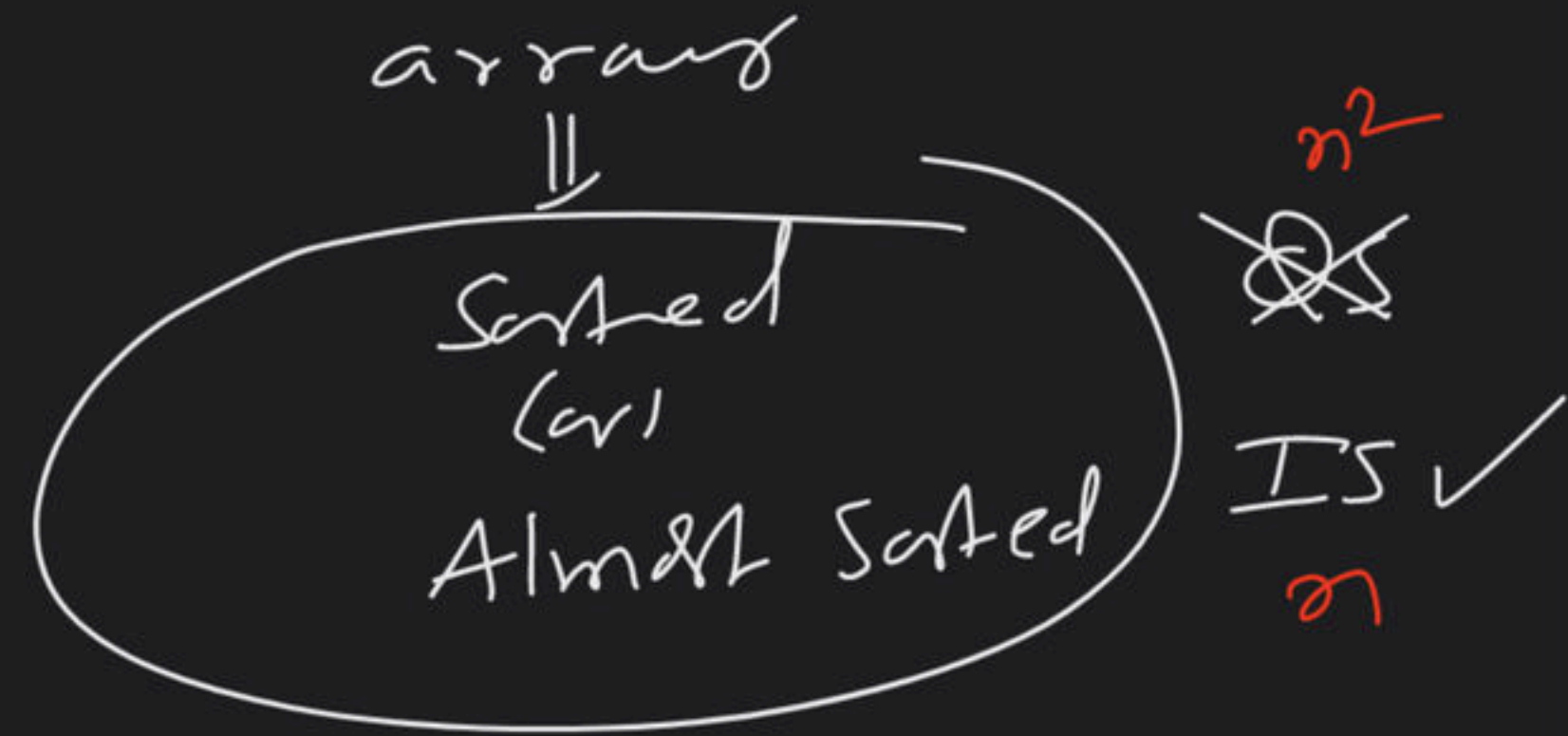
$$n \log n (2T(n/2) + \underline{n})$$

I.P.TC

$$n^2 (2T(n/2) + \underline{n^2})$$

Quicksort

1. Not stable
2. In-place sorting algo
3. practical sorting algo



Partition - Algo

