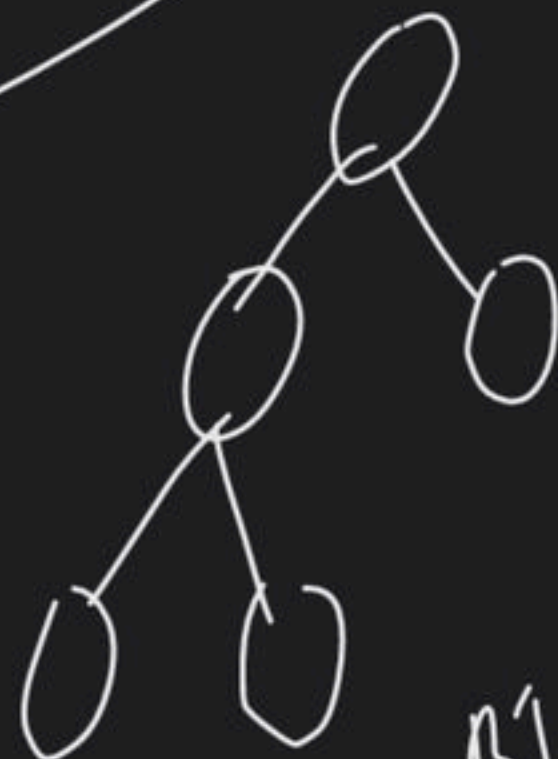


Bubble Sort

Complete Course on Algorithms - GATE

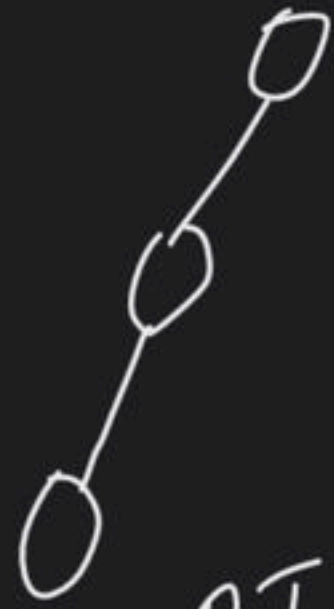
HeapSort

Binary Tree



BT ✓
ACBT ✓

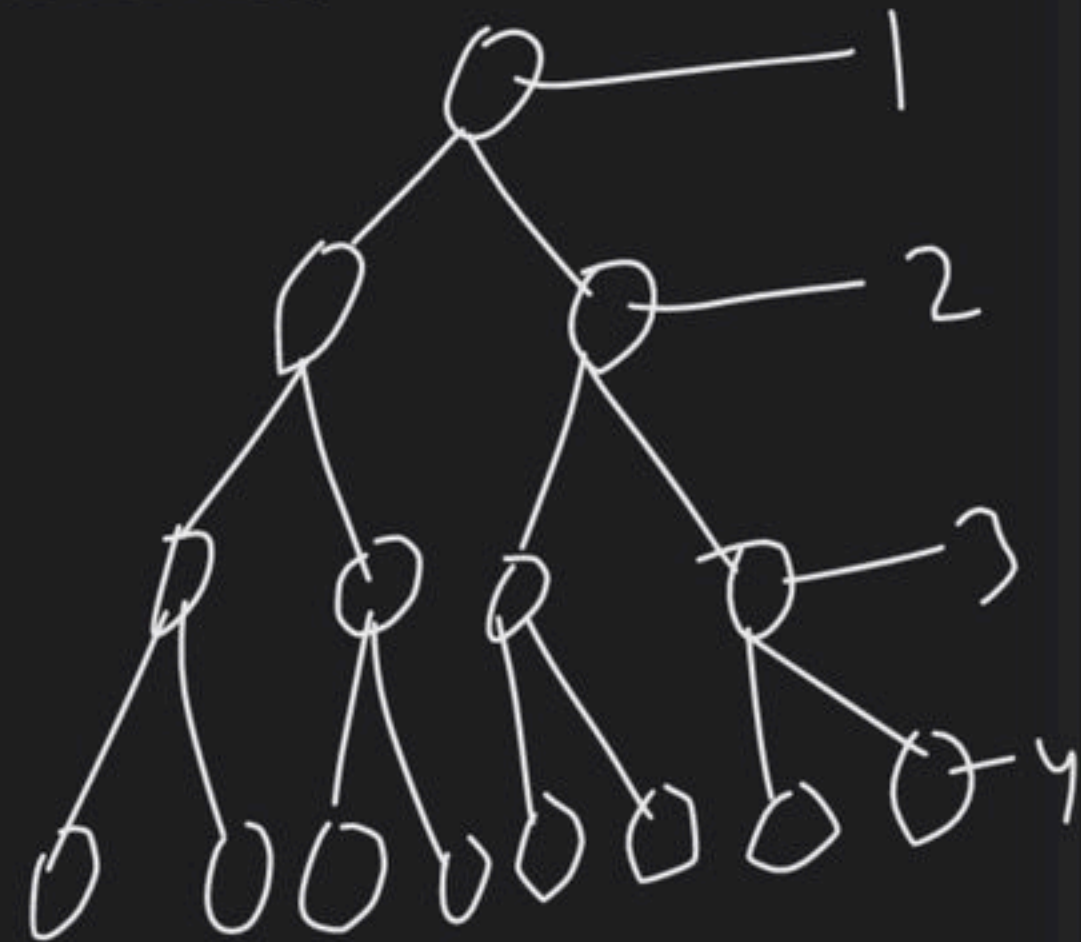
Almost complete Binary Tree



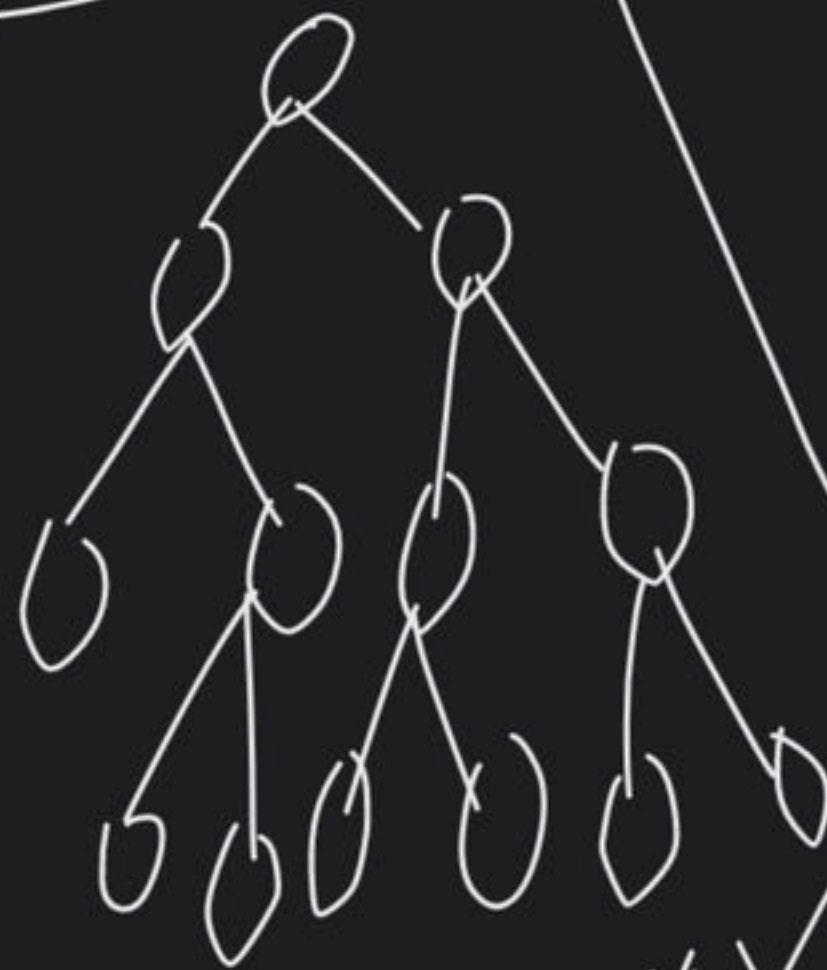
BT ✓
ACBT ✓



BT ✓
ACBT ✓

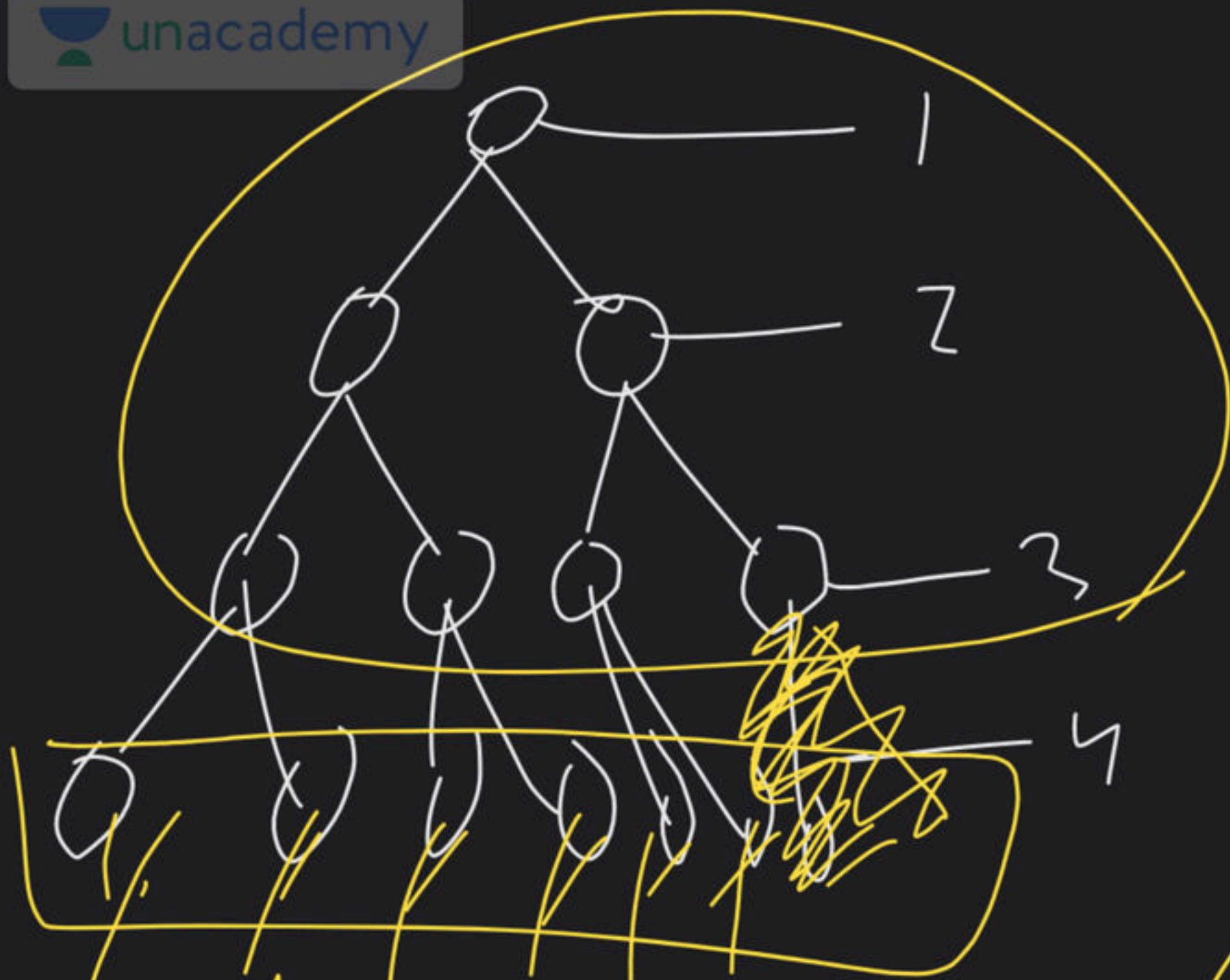


BT ✓
ACBT ✓
LCBT ✓ (F.L)



BT ✓
ACBT ✓

$H-L-CBT = 2^h - 1$
 $K-L-CBT = 2^k - 1$
 $N-L-CBT = 2^N - 1$ nodes



$$\frac{14}{2} = 7$$

$$\frac{17}{2} = 8.5$$

$$\frac{15}{2} = 7.5$$

$$\lceil 7.5 \rceil = 8$$

$$\lceil \frac{15}{2} \rceil = 8$$

$$\lceil \frac{17}{2} \rceil = 9$$



- ① k-level CBT contain $= 2^k - 1$ nodes
- ② CBT — contain $\begin{cases} n \text{ nodes} \\ k \text{ levels} \end{cases}$

$$n = 2^k - 1$$

$$2^k = n + 1$$

$$\log_2 2^k = \log_2 (n + 1)$$

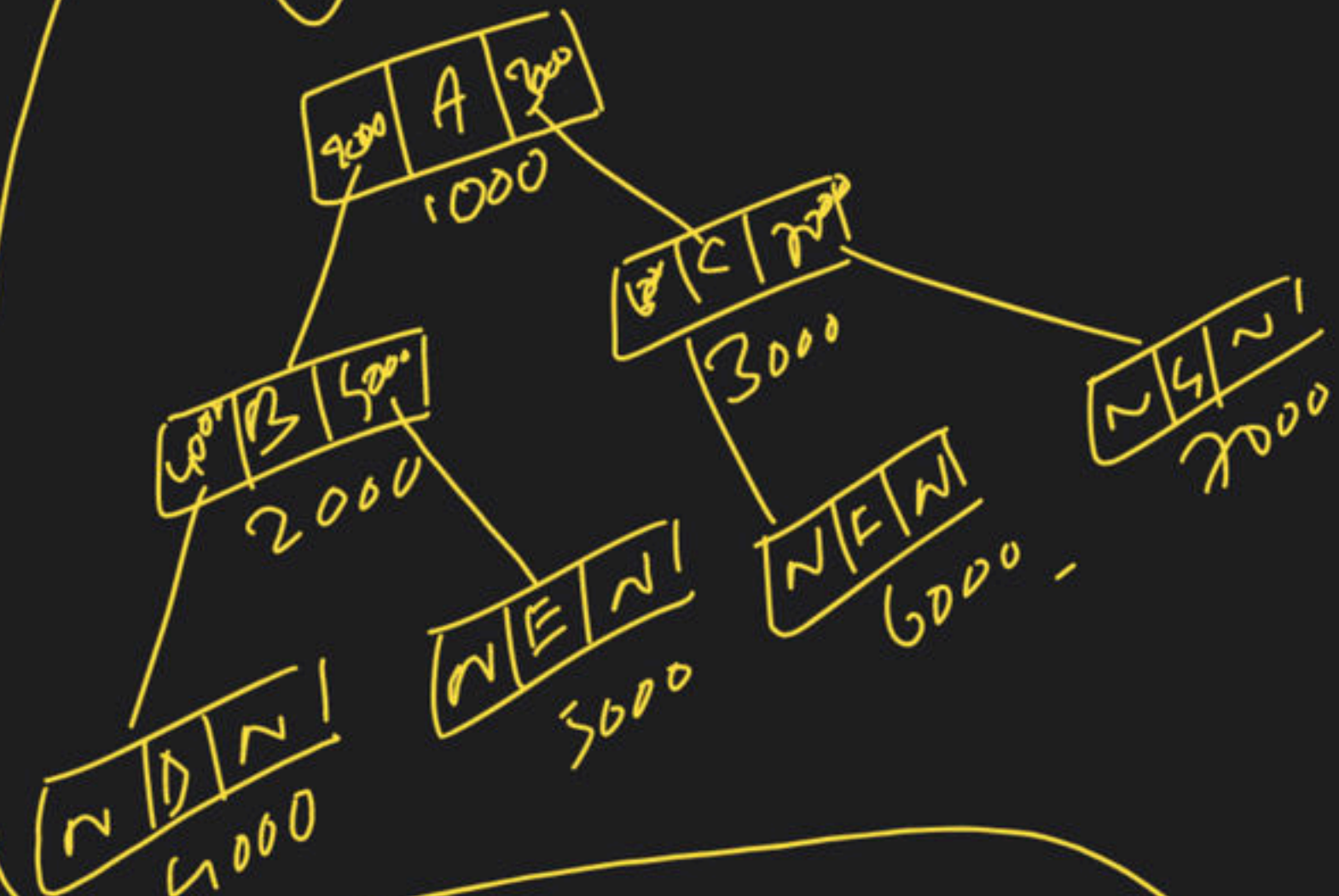
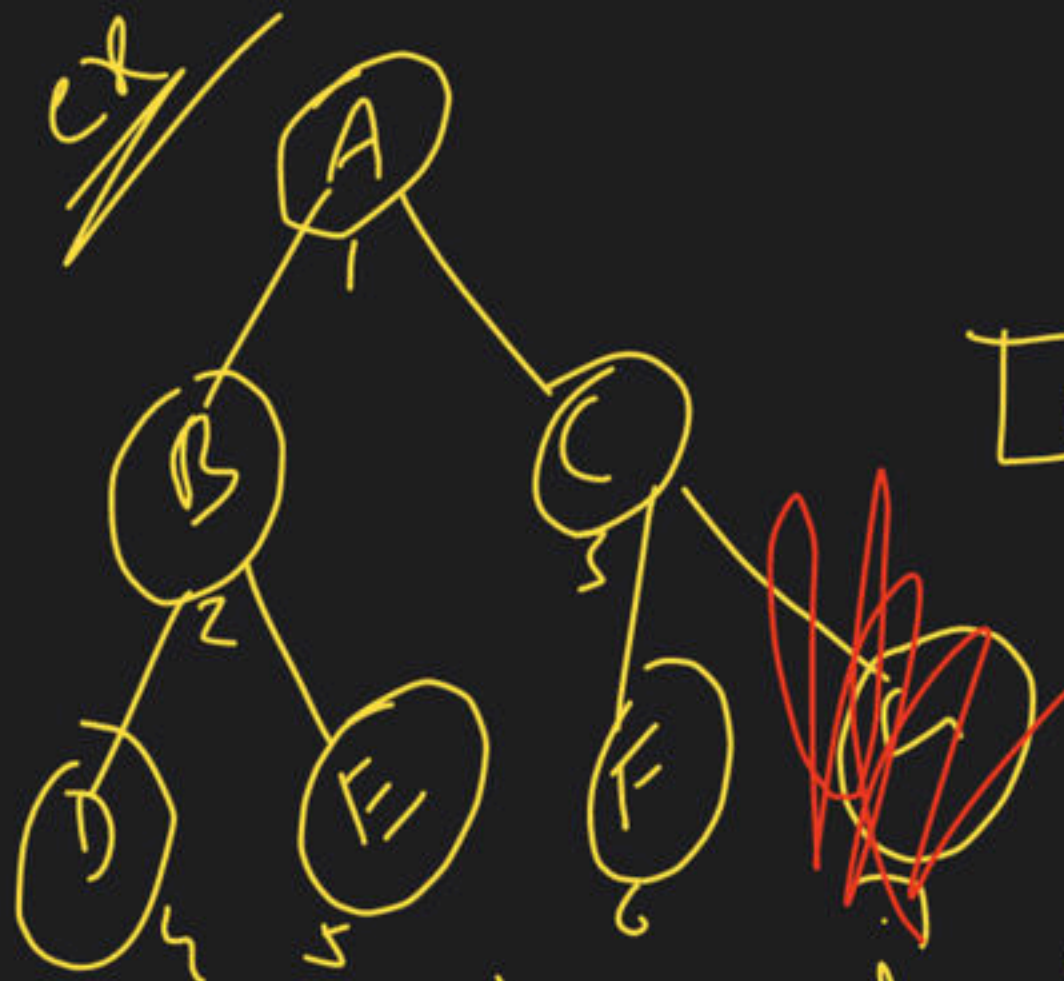
$$k = \log_2 (n + 1)$$

ACBT

- ③ If CBT — contain n nodes
 No. of leaf node $= \lceil n/2 \rceil$
 No. of Non-leaf $= \lfloor n/2 \rfloor$

Binary tree representation

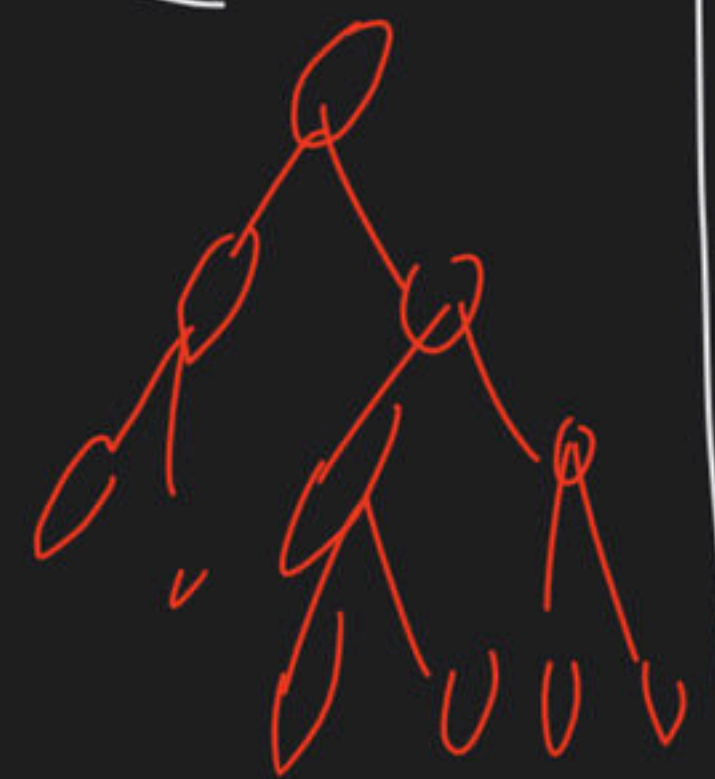
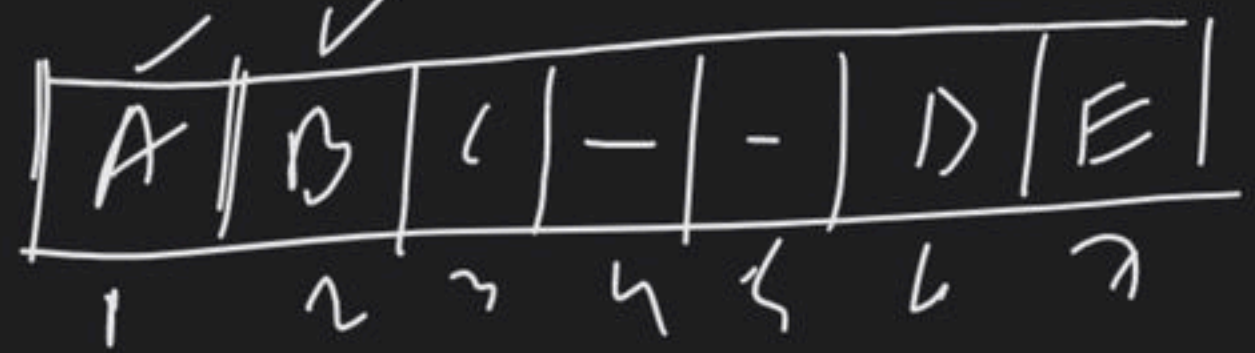
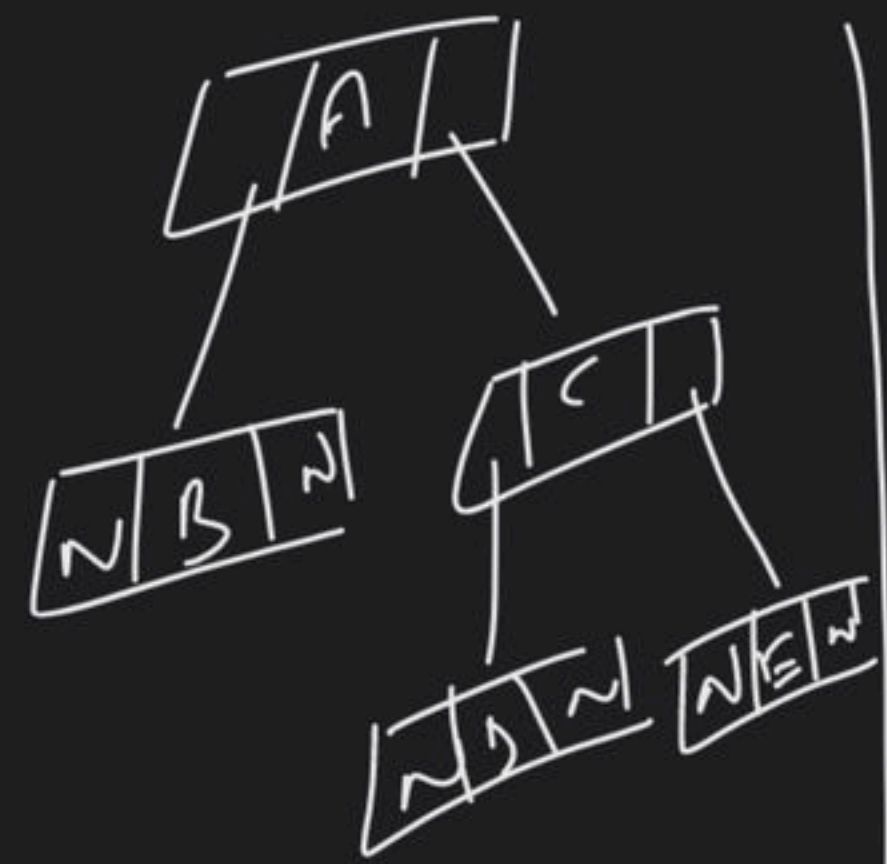
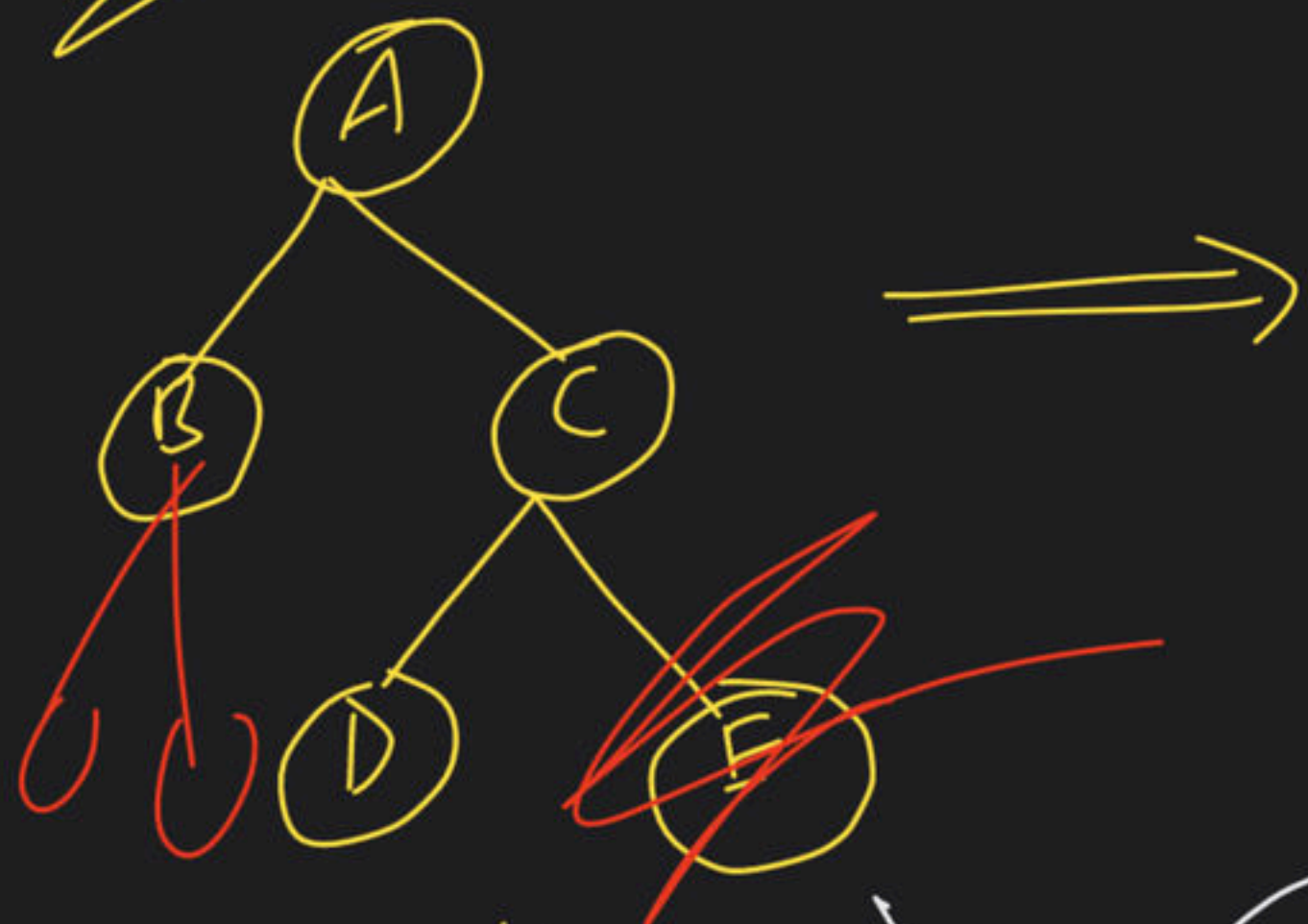
- ① Array Representation ② Linked List Rep



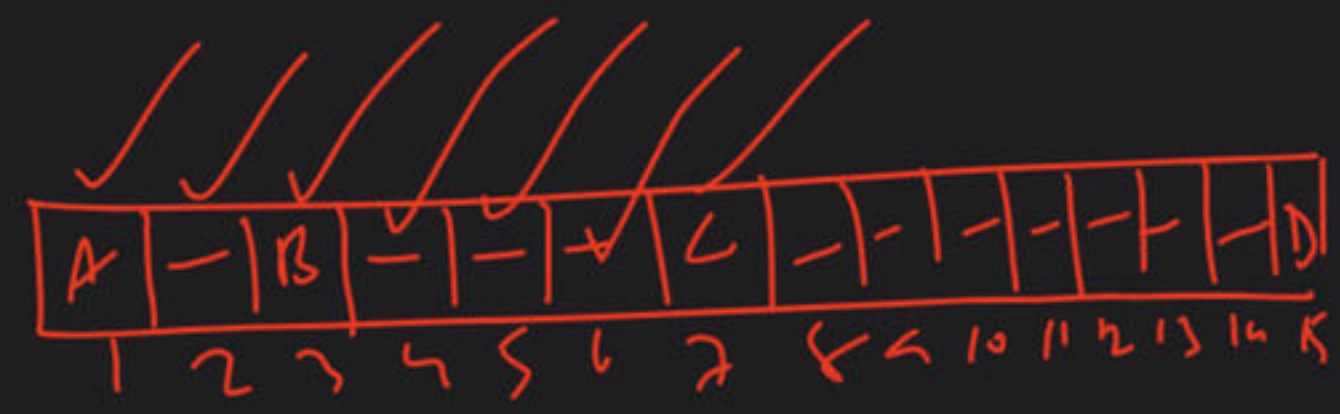
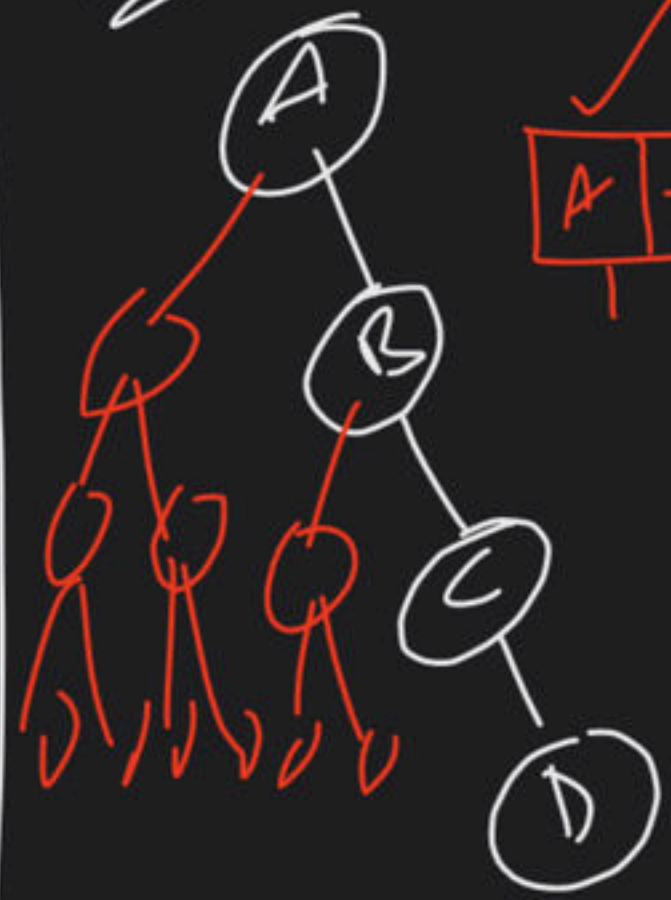
if a node is stored in its place of array in array rep

$$\textcircled{1} \text{ Parent}(i) = \lfloor i/2 \rfloor$$

$$\textcircled{2} \begin{aligned} \text{Left-child}(i) &= 2i \\ \text{Right " } &= (2i) + 1 \end{aligned}$$

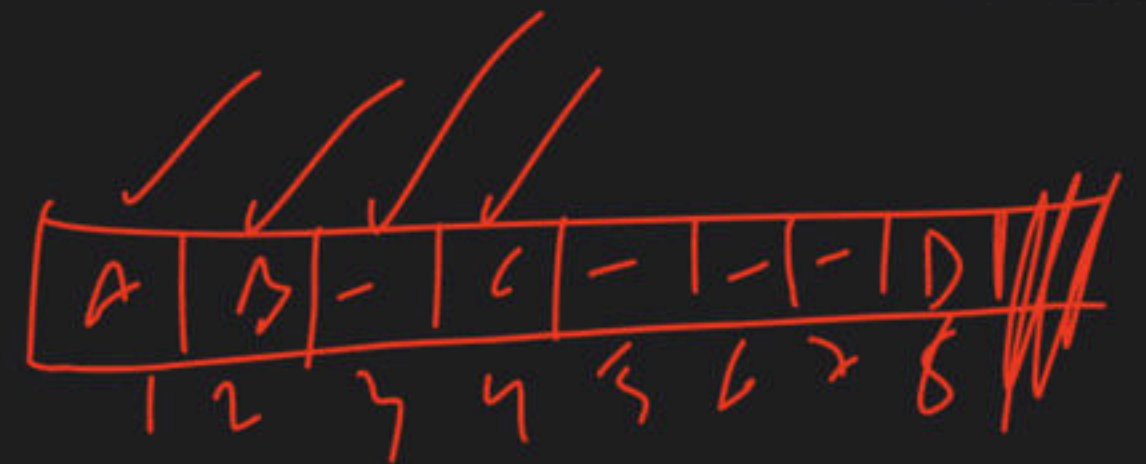
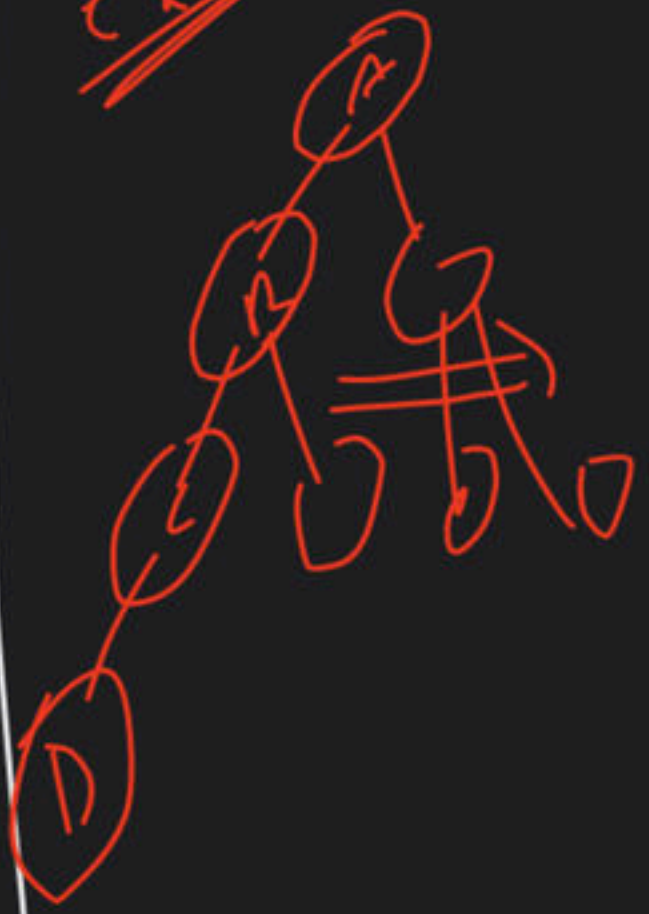


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5
2-1

et

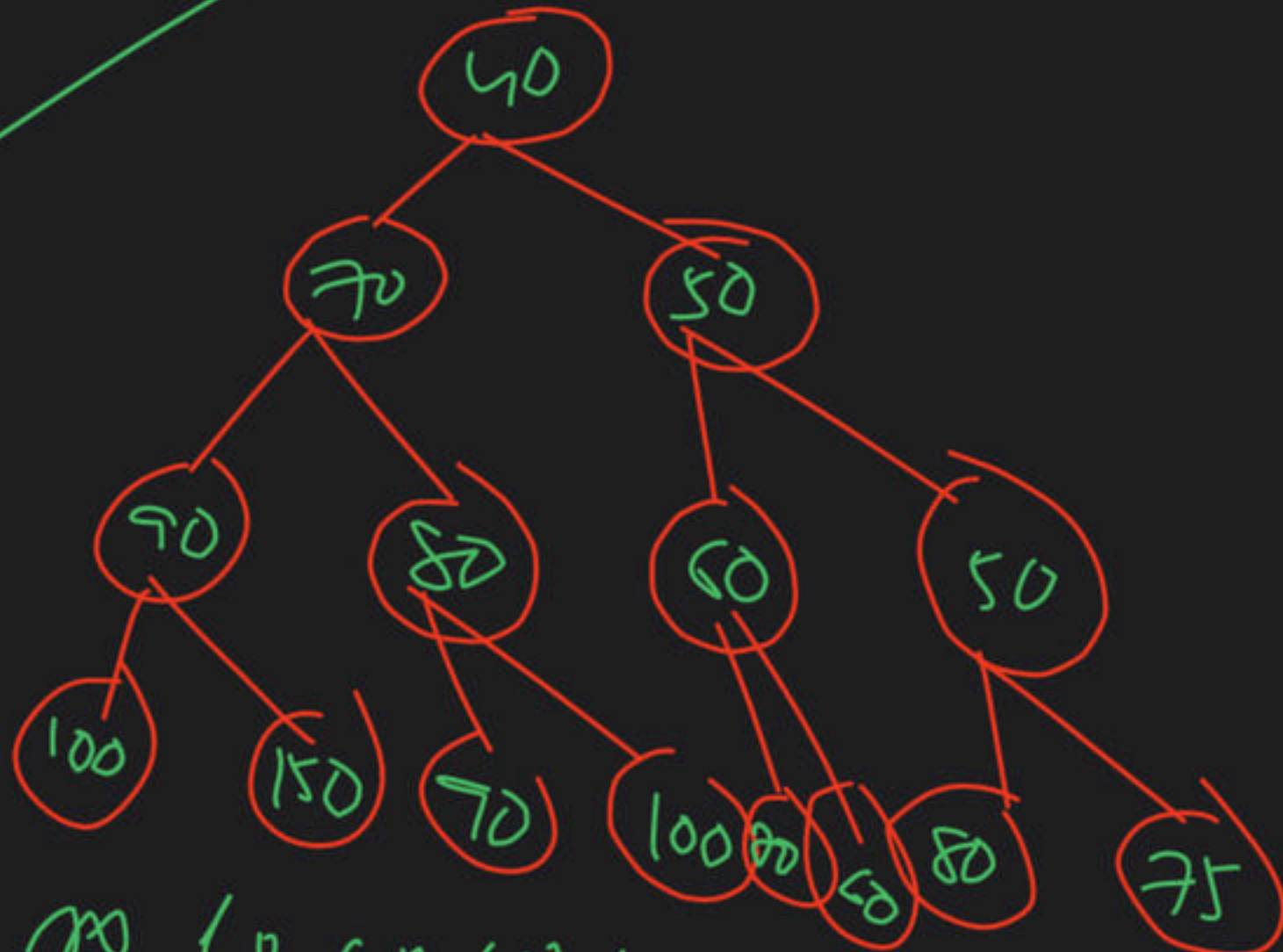


Heap Tree

Minheap Tree

1. ACBT

2.

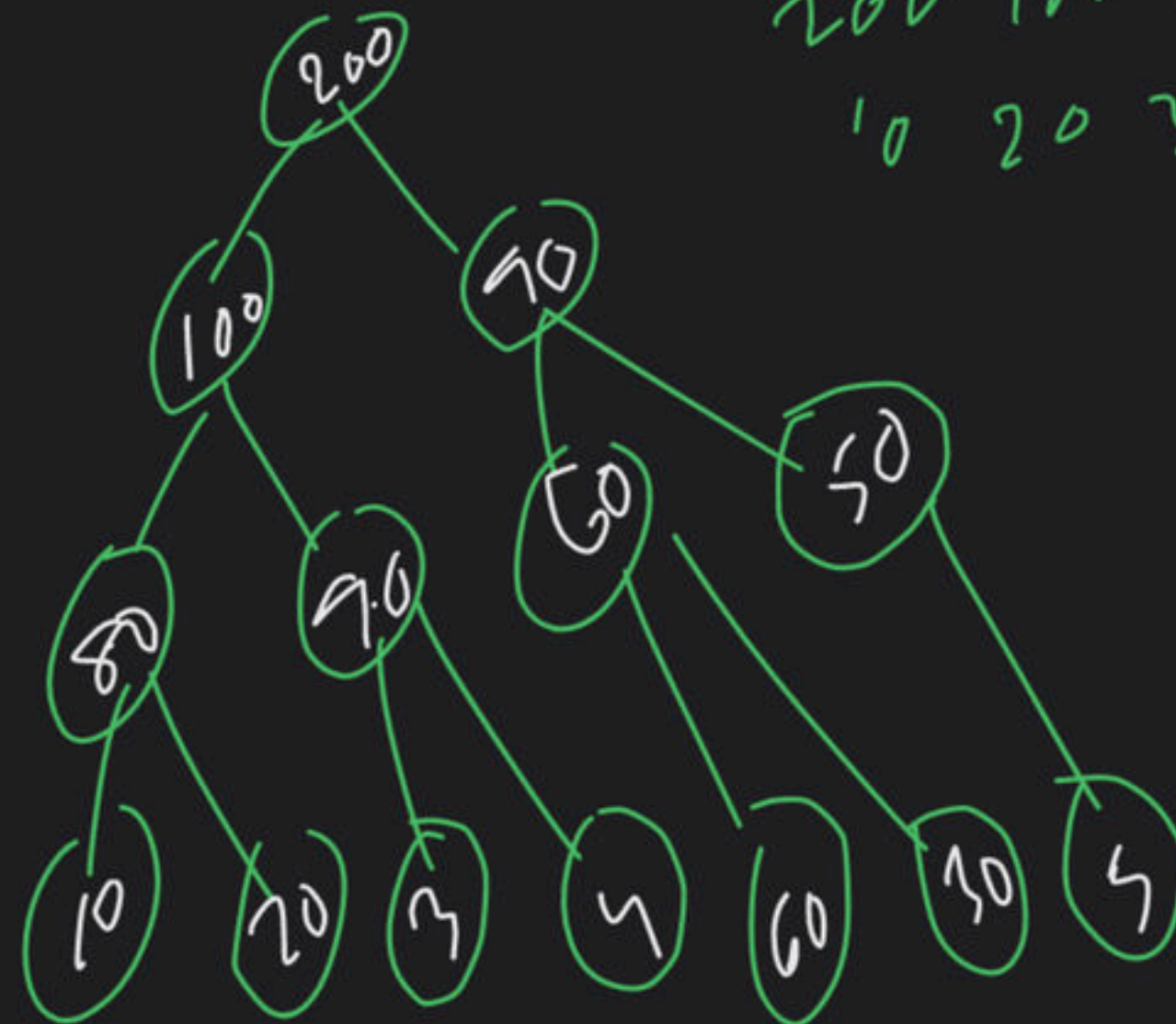


40 70 50 90 80 60 50 100 150 70 100 80 75 75

or maxheap

1. ACBT

2.



200 100 70 80 70 60 50
10 20 3 4 60 30 4