

# DP - Part I

Complete Course on Algorithm for GATE - CS & IT



# Divide & conquer

Divide And Conquer ABW  $\rightarrow$

$DAC(a, i, j) \rightarrow T(n)$

$O(1)$   $\left\{ \begin{array}{l} \text{if (small}(a, i, j)) \\ \text{return (solution}(a, i, j)); \end{array} \right.$

else

$k = \text{Divide}(a, i, j);$

$f_1(n)$

$b = DAC(a, i, k);$

$c = DAC(a, k+1, j);$

$d = \text{combine}(b, c)$

$\text{return}(d);$

$O(1)$

Divide

$T(n/2)$   
conquer

$T(n/2)$

combine

$f_2(n)$

small()

small()

Divide()

combine()



# DAC algo Time complexity finding

$$T(n) = \begin{cases} O(1) & \text{if } n \text{ is small} \\ f_1(n) + \underbrace{T(n/2) + T(n/2)}_{\text{Time for subproblems}} + f_2(n) & \text{if } n \text{ is big} \end{cases}$$

$$T(n) = 2T(n/2) + f_1(n) + f_2(n)$$

$$= 2T(n/2) + f(n)$$

$$= 5T(n/5) + f(n)$$

$$= a \underbrace{T(n/b)}_{\text{Time of one subproblem}} + f(n)$$

No. of Subproblems

$$a \geq 1$$

Size of Subproblem

$$b > 1$$

Time for  
one subproblem

Time for  
all D & C



# applications of DAD

- ① Finding max & min
- ② Power of an element
- ③ Binary Search
- ④ Merge Sort
- ⑤ Quick Sort
- ⑥ Selection procedure
- ⑦ maximum contiguous Subarray Sum
- ⑧ Finding no. of inversions
- ⑨ Strassen's matrix multiplication.



# Finding max & min

I/p: An array of 7 distinct elements  
50 20 10 60 40 30 80 20 15

O/p: return maximum & minimum elements  
80 10

Straight maxmin algo

$\text{max} = \text{min} = a[1]$

for ( $i=2$ ;  $i \leq n$ ;  $i++$ )

if ( $\text{max} < a[i]$ )

$\text{max} = a[i]$

else

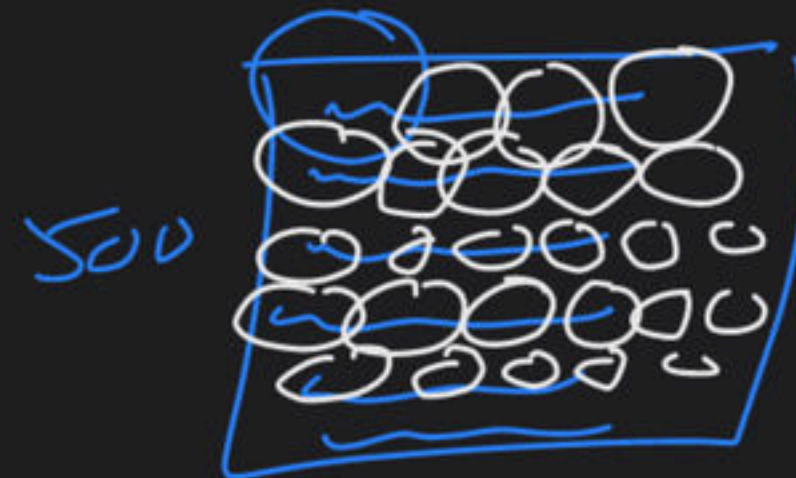
if ( $\text{min} > a[i]$ )

$\text{min} = a[i]$

$\Theta(n)$

EC

~~$\text{max} = 50$~~  80  
 ~~$\text{min} = 50$~~  10



Top row = 50

WIK-DAC

0 1 2 3 4 5

0 1 1 2 3 5

5

$$F(5) = \cancel{F(4)} + \cancel{F(3)}$$