

Masters of Technology in Computer Science And Engineering

submitted by Arghya Bandyopadhyay RollNo. 20CS4103

submitted to
Dr Nanda Dulal Jana
Assistant Professor
Dept. of CSE



National Institute of Technology, Durgapur

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Peroblem foermulation D, D2 D3 D4 Supply O, N. N. N. N. N. N. N.	. verng least root method.									
O. M. N. N. N. N. N. N.										
0, \\ \(\text{X}_{13} \) \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\	1	5,	2	D 3	D4	supply				
		di.	Xa 1	X13	X4 -					
02 X81 8 X82 X83 X84 1 15		6		()	5	14				
03 ×31 × × × × × × × × × × × × × × × × ×	02	X ₂₁ 8		X23 2	X50 T	12				
Derrand 6 10 10 4	02	X ₂₁ &		×23 2 ×133 6	x34 2 x34	12				
	02	X ₂₁ &			X29 7 X34 Q	12				

The teromospoertation puolstern is formula. ted ou an LP model ou follows: Minimize (Notal Aeromespoertan wist) 2 6M, + AM, 2+ M, 3+ 5 M 14 + 8 NR1 + 9 NRR+ 2 NRB+ 7 NRAF 4d31+3d32+6d33+2d34 Subject to the consternints M,1 + M12+ M18+ M14 219 721 + 722+ M23+ M24 = 12 M3, + M32+ M33+ M34 = 4 M, + MQ, + M3, E6 7,2+ M22+ M32=10 M13+ MR3+ M33=10 M14+ 124+ 13424 and Mig 20 for 1 1 1,2,3 f 321,2,3,4

In the above LP model, there are man = 3 rde 12 decision variables, of one one the montoers of many and mare the numbers of many wolumns.

Printence of fearible solver of Total solvers of Solver

The total empty is equal to total semand, hence the perabolism is a balanced tenantation perabolism.

Solution: -

Desert minimum rof coest materix i.e act (0, 303) and then compare

	D ,	Da	03	Da	Supply
0,	6	4 1	· (10)	5	14 4 2a,
02	8	9	2	7	12
	» (6)	3	6	2	80°a2
03	>	م	10	p (4)	0 2 0 3
Derron	nd to	100	100	40	
	20,	232	1 2 43	2 59	

a, and bz i.e 10 × 14, hence allaeate d, 2 × 10, bz gets enhanted and a, 24 delete column Dz

Design select the minimum east ferom the new court montains with De summered, i.e. 2 at (Oz, Pa) and then compane are by where Aze by where Aze 4, allocate Mzu 24, Ahis onhaute and by 20, whether Oz f

B We vesit min mum is & at (0,02) companing a & baie 4410, allocate Mia 24 & flis enhant 9,20 f leanes b2 = 6. delete now 0, (4) select 8 at (00, 0,). compane 927by i.e 622, allocate M2,26 of enhancet b, of leave b2 26, then exelect 9 i.e at (02, D2) ? alloeate hemaning value i e M22 26. This enhances all the supply & domand. Sorphy 12 4 Demond 6 30 10 10 4

Matel cont = 4 × 4+1 × 10 + 8 × 6 + 9 × 6 + 2 × 9

> 16+10+48+54+8

= 136

The number of allocations 25, fm+n-126 es 5 b = 6 home the solution is obegeneerate

No solve obegeneerory perobstem me have to esteat a pointion in the materia which is unablacated to also have maximum roest to also have maximum roest to

So if me fut the nature special at (0, b.) on (02,03), it will recent book whether west of the pointion is violetendent of.

and me can fut special on the position with minimum

nout i.e 3 at (03,02)

D, Da		Da	2 03		snopphy				
0,	0	4	10	0	14				
08	8	6	0.	0,	13				
08	03 0 6 0 4 4.								
Demand & 10 4 0									
Total rast = 4×4 + 10×1 + 6×8+6×9									
+ 3 > E + 4 + 2									
e 16+10+48+54+8+3E									
. 2136+3€									
~ 136 mhere 6 = 0									

```
Python Code:
        import numpy as np
def check_loop(p, row, column):
    p[row, column] = -1
    flag = 1
    while flag != 0:
        flag = 0
        if p.size != 0:
            row = np.count\_nonzero(p, axis=1)
            f = 0
            for index in range(len(row)):
                if row[index] < 2:
                     flag = 1
                    p = np. delete(p, (index - f), axis=0)
        if p.size != 0:
            e = 0
            col = np.count\_nonzero(p, axis=0)
            for index in range(len(col)):
                if col[index] < 2:
                     flag = 1
                    p = np. delete(p, (index - e), axis=1)
                     e += 1
    if p.size != 0:
        return 0
    else:
        return 1
if __name__ = '__main__ ':
   cm = np.array([[6.0, 4.0, 1.0, 5.0], [8.0, 9.0, 2.0, 7.0], [4.0, 3.0, 6.0, 2.0]])
    s = np. array([14.0, 12.0, 4.0])
    d = np. array([6.0, 10.0, 10.0, 4.0])
    c = cm.copy()
    print ("The Cost Matrix is: ")
    print(c)
    print ("The Supply is: ", s)
    print ("The Demand is: ", d)
   m, n = c.shape
    print("No of Rows & No of Columns: (", m, ", ", n, ")")
    total_cost = 0
    no\_alloc = 0
    total_demand = np.sum(d)
    total_supply = np.sum(s)
    alloc = []
    if total\_demand = total\_supply:
        print ("It is a Balanced Transportation Problem")
    else:
        print ("It is an UnBalanced Transportation Problem")
        if total_demand > total_supply:
```

```
new = np. array (np. zeros (n))
        c = np.row_stack((c, new))
        s = np.append(s, total_demand - total_supply)
        m = m + 1
    else:
        new = np. array (np. zeros (m))
        c = np.column_stack((c, new))
        d = np.append(d, total_supply - total_demand)
        n = n + 1
    print ("The New Balanced Cost Matrix is: ")
    print(c)
    print ("The Supply is: ", s)
    print ("The Demand is: ", d)
a = np.zeros(c.shape)
min_cost = np.amin(c)
while min_cost != np.inf:
    indexes = np.where(c = min_cost)
    i = indexes[0][0]
    j = indexes[1][0]
    x = \min(s[i], d[j])
    s[i] = x
    d[j] = x
    total_cost += (x * c[i, j])
    no\_alloc += 1
    a[i, j] = x
    alloc.append((i, j))
    if s[i] < d[j]:
        x = 0
        while x < n:
            c[i, x] = np.inf
            x += 1
    elif s[i] > d[j]:
        y = 0
        while y < m:
            c[y, j] = np.inf
            v += 1
    else:
        x = 0
        while x < n:
            c[i, x] = np.inf
            x += 1
        y = 0
        while y < m:
            c[y, j] = np.inf
            y += 1
    \min_{cost} = \operatorname{np.amin}(c)
print("Total Cost: ", total_cost)
unalloc = []
for i in range(m):
    for j in range(n):
        if not (i, j) in alloc:
             unalloc.append((i, j))
print("List of Allocated Positions: ", alloc)
print ("List of Unallocated Positions: ", unalloc)
```

```
print("Allocation Matrix: ")
print(a)
noloop = []
if no\_alloc = m + n - 1:
    print("Non Degeneracy")
else:
    print("Degeneracy")
    for i in unalloc:
         g = check_loop(a.copy(), i[0], i[1])
         if g == 1:
             no_loop.append(i)
    \min_{e} pi_{e} list = []
    for i in no_loop:
         \min_{e \in I} \operatorname{list.append} (\operatorname{cm}[i[0], i[1]])
    min_epi = min(min_epi_list)
    ind = min_epi_list.index(min_epi)
    loc = no\_loop[ind]
    a[loc[0], loc[1]] = -1
    print ("Allocation Matrix After Converting Degeneracy to Non-Degeneracy is : ")
    print(a)
```

Output:

```
The Cost Matrix is:
[[6. 4. 1. 5.]
[4. 3. 6. 2.]]
The Supply is: [14. 12. 4.]
The Demand is: [ 6. 10. 10. 4.]
No of Rows & No of Columns: (3, 4)
It is a Balanced Transportation Problem
Total Cost: 136.0
List of Allocated Positions: [(0, 2), (2, 3), (0, 1), (1, 0), (1, 1)]
List of Unallocated Positions: [(0, 0), (0, 3), (1, 2), (1, 3), (2, 0), (2, 1), (2, 2)]
Allocation Matrix:
[[ 0. 4. 10. 0.]
[6.6.0.0.]
[0. 0. 0. 4.]]
Degeneracy
Allocation Matrix After Converting Degeneracy to Non-Degeneracy is :
[[ 0. 4. 10. 0.]
[6.6.0.0.]
[ 0. -1. 0. 4.]]
```

Peroblem etatement							
Harmulate the following TP & find IBFS by LCM.							
IBFS by LCM. 1112 3 4 5 Anailable							
A	4	3	1	2	6	80.	
B	5	2	3	4	5	40	
C	3	5	1			40	
D	2	4	. 4	.5	3	20	
Requiered	60	60	30	1 40	10	200/180	
Peralsten foermulation							
The teromepoentat peroblem is formulated							
as ov	NIP	2 1	3	4	5	Anai Whole	
A	An 21	The 3 h	3 1	May 2	200 6	80	
3	75 J	2	3	M34 4	735	40	
0	3	5	6	3	Nas Q	40	
	7 2	4	4	5	3	20	
Required	60	60	30	40	10	200/180	

briestence of fearible solution of Zar 2 Z by e 60+60+30+40+10 2 80 + A0+ A0+ 20 180 \$ 200 Mence the Solution is unbalanced teransportar perobolem, so to some Alie guestion, me need to mesent ia dummy drow E, with coest (0) to all the cells and anailability 2 / Total Somando Total emphy/220 hence the new court material & 1 2 3 4 5 Ma 4 Muz 3 Mus 1 Mus 2 Mus 6 Ma 5 Max 2 Mas 3 Mas 5 Mas 3 Max 5 Mas 6 Mas 3 Mas 5 Mus 2 Max 4 Mas A Mas 5 Mus 3 Mus 2 Max 4 Mas A Mas 5 Mus 3 Mus 2 Max 4 Mas A Mas 5 Mus 3 Mus 2 Max 4 Mas A Mas 5 Mus 3 Mus 4 Mas A Mas 5 Mus 3 Mus 5 Mus 3 Mus 5 Mus 5 Mus 3 Mus 3 Mus 5 Mus 5 Mus 5 Mus 5 Mus 6 Mus 3 Mus 6 Mus 5 Mus 6 Mus 3 Mus 7 Mus 6 Mus 6 Mus 3 Mus 7 Mus 6 Mus 7 Mus 6 Mus 6 Mus 7 Mus Avail. 20 40 40 20 20

Thetal court = Adi, +8x,2+101,3+2x,4+6x,5+
5 M2, +2 M22+ BM23+4724+5729+
3 M3, +5 M32+6 M33+3034+3739+
2 M4, +4 M42+4 M43+5 M44+3 M49+
0 M3,+0 M32+0 M33+0 M44+0 M55

Subject to consteaml

M,, + M, 2+ M, 3+ M, 4+ M, 5 = 80 DR, + DRR + DRR + DRRA + MRG = 40 Mg1 + M32 + M33 + M34 M35 = 90 1 1/4 1 1/42 + 10/43 + 10/44 + MASERO Misi + Misz + Misz + Misq + Miss = 20 M1 & 18 21 & 1831 & 1841 & 251 260 1/12 + 1/22 + 1/32 + 1/42 + 1/42 = 60 71,34 733+ M33+ M32 = 30 That Ment Man + Man + Man = 40 MIS+ MRS+ MSS+ MAS+ MSS210 and Mpg 20 for 121,2,3,4,54 3 = 1, 2,3,4,5

of the above model, there are is 5 225 deivion movinables & m+ 25+5210 consterainte, where me evens for columns.

Solution 1 2 3 4 4 3 0 1 2 2 4 5 2 3 4 small. 0 % 3 5 6 3 4030 2 4 4 100 as 200 OM * 20 p 0 30 O any i.e o at (E,1) and then compane asf b, s) by > as hence allocate agie 20 which enhants as nonce delete enou E.

Desimilarly select 1 at (A,3) allocate M,3 = 30 % b3 La, this exhausts by hence delete Column 3. (3) select 2 at (A,4), allocate · MIA: 2 40. 00 ba La, , this exhausts by hence delete volum (1) select 2 at (B,2) allocate 1/2 2=40 do b2 > a2, this exhausts as hence delete non B. 3) select 2 at (cos), M35 210, selecte Rolumn 5th since 55 Laz and 55 gets enhanted (6) select Q at (D)1), Mu = 20, relete even s of by > 94 and as gets exhausted. (A) de select 3 at (A,2) Mario, obelete nous A Po b_>a, and a, gets enhanted.

E st-loved select min = 3 at (G1)

M31 = 20 , delete column (and)

Neft with min = 5 at (C, 2)

M3 2 10, t oblete 2nd column

f su the available & everiend

egets enhanted.

0								
Alacation materia								
	1 1	2	3	4	5	anailably		
A	0	10	30	20	0	80		
B	0		0		0			
C	20	10	0			40		
0	20	0				20		
E 20 0 0 0 20								
Reguired 60 60 30 Map 10 200								
No of allocative of & manne 5+5-1=0 honce								
the sol is non degenerate.								
Modal voit = (10 + 3) + (30 + (40 = 2) + (40 = 2)								
+ (20 *3) + (10 *5) + (10 *2) +								
(20+2)+(20-0)								
2 30+ 30+ 80+80+60+90+ 20+40+0								

```
Python Code:
```

```
import numpy as np
        def check_loop(p, row, column):
                p[row, column] = -1
                flag = 1
                while flag != 0:
        flag = 0
        if p.size != 0:
            row = np.count\_nonzero(p, axis=1)
            for index in range(len(row)):
                if row[index] < 2:
                     flag = 1
                    p = np.delete(p, (index - f), axis=0)
                     f += 1
        if p.size != 0:
            e = 0
            col = np.count\_nonzero(p, axis=0)
            for index in range(len(col)):
                if col[index] < 2:
                     flag = 1
                    p = np.delete(p, (index - e), axis=1)
    if p.size != 0:
        return 0
    else:
        return 1
if _{-name_{--}} = '_{-main_{--}}':
   cm = np.array([
        [4.0, 3.0, 1.0, 2.0, 6.0],
        [5.0, 2.0, 3.0, 4.0, 5.0],
        [3.0, 5.0, 6.0, 3.0, 2.0],
        [2.0, 4.0, 4.0, 5.0, 3.0]
   s = np. array([80.0, 40.0, 40.0, 20.0])
   d = np.array([60.0, 60.0, 30.0, 40.0, 10.0])
    c = cm.copy()
    print ("The Cost Matrix is: ")
    print(c)
    print ("The Supply is: ", s)
    print ("The Demand is: ", d)
   m, n = c.shape
   print("No of Rows & No of Columns: (", m, ", ", n, ")")
    total\_cost = 0
    no\_alloc = 0
    total_demand = np.sum(d)
    total_supply = np.sum(s)
    alloc = []
    if total_demand = total_supply:
        print ("It is a Balanced Transportation Problem")
```

```
else:
    print ("It is an UnBalanced Transportation Problem")
    if total_demand > total_supply:
        new = np. array (np. zeros (n))
        c = np.row_stack((c, new))
        s = np.append(s, total_demand - total_supply)
        m = m + 1
    else:
        new = np. array (np. zeros (m))
        c = np.column_stack((c, new))
        d = np.append(d, total\_supply - total\_demand)
        n = n + 1
    print ("The New Balanced Cost Matrix is: ")
    print(c)
    print("The Supply is: ", s)
    print ("The Demand is: ", d)
a = np. zeros(c.shape)
\min_{cost} = \operatorname{np.amin}(c)
while min_cost != np.inf:
    indexes = np.where(c = min_cost)
    i = indexes[0][0]
    j = indexes[1][0]
    x = \min(s[i], d[j])
    s[i] = x
    d[j] = x
    total_cost += (x * c[i, j])
    no_alloc += 1
    a[i, j] = x
    alloc.append((i, j))
    if \ s[i] < d[j]:
        x = 0
        while x < n:
            c[i, x] = np.inf
            x += 1
    elif s[i] > d[j]:
        y = 0
        while y < m:
            c[y, j] = np.inf
            y += 1
    else:
        x = 0
        while x < n:
            c[i, x] = np.inf
            x += 1
        y = 0
        while y < m:
            c[y, j] = np.inf
            y += 1
    min_cost = np.amin(c)
print("Total Cost: ", total_cost)
unalloc = []
for i in range(m):
    for j in range(n):
        if not (i, j) in alloc:
```

```
unalloc.append((i\ ,\ j\ ))
print("List of Allocated Positions: ", alloc)
print("List of Unallocated Positions: ", unalloc)
print("Allocation Matrix: ")
print(a)
no\_loop = []
if no\_alloc = m + n - 1:
    print("Non Degeneracy")
else:
    print("Degeneracy")
    for i in unalloc:
        g = check_loop(a.copy(), i[0], i[1])
        if g == 1:
             no_loop.append(i)
    min_epi_list = []
    for i in no_loop:
         \min_{e \in I} \operatorname{list.append} (\operatorname{cm}[i[0], i[1]])
    min_epi = min(min_epi_list)
    ind = min_epi_list.index(min_epi)
    loc = no\_loop[ind]
    a[loc[0], loc[1]] = -1
    print ("Allocation Matrix After Converting Degeneracy to Non-Degeneracy is: ")
    print(a)
    Output:
```

```
The Cost Matrix is:
[[4. 3. 1. 2. 6.]
 [5. 2. 3. 4. 5.]
 [3. 5. 6. 3. 2.]
 [2. 4. 4. 5. 3.]]
The Supply is: [80. 40. 40. 20.]
The Demand is: [60, 60, 30, 40, 10.]
No of Rows & No of Columns: (4, 5)
It is an UnBalanced Transportation Problem
The New Balanced Cost Matrix is:
[[4. 3. 1. 2. 6.]
 [5. 2. 3. 4. 5.]
 [3. 5. 6. 3. 2.]
 [2. 4. 4. 5. 3.]
 [0. 0. 0. 0. 0.]]
The Supply is: [80. 40. 40. 20. 20.]
The Demand is: [60. 60. 30. 40. 10.]
Total Cost: 390.0
List of Allocated Positions: [(4, 0), (0, 2), (0, 3), (1, 1), (2, 4), (3, 0), (0, 1), (2, 0), (2, 1)]
```

List of Unallocated Positions: [(0, 0), (0, 4), (1, 0), (1, 2), (1, 3), (1, 4), (2, 2), (2, 3), (3, 1), (3, 2), (3, 3), (3, 4), (4, 1), (4, 2), (4, 3), (4, 4)

```
Allocation Matrix:
[[ 0. 10. 30. 40. 0.]
  [ 0. 40. 0. 0. 0.]
  [20. 10. 0. 0. 10.]
  [20. 0. 0. 0. 0.]

[20. 0. 0. 0. 0.]

Non Degeneracy
```