## Assignment 4 Of Modelling & Simulation Lab (CS1052)

Masters of Technology in Computer Science And Engineering

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submitted to
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Perolsten statement 1 Tind the oftenal solut to the following tenome partour problem in which the cells contains the unit teromespoortal west in Inspece. wa ws anail w, wa WB F, 7 6 4 5 9 40 B 7 8 30 F2 8 5 9 6 5 20 F3 6 8 7 8 6 10 Fa 5 15 20 5 Reg. 30 30 and LCM for use NWCR fearable solut. initial basic Peroblem farmulat -

| w, I   | Wa       | wa   | wa in | 0 5 | mppy |
|--|----------|------|-------|-----|------|
| 1 2 x  | W 2 M2 6 | W3   | 7195  | 9   | 40   |
| 72 mai   | NRR 5    | 123  |       | 8   | 30   |
| 7 M31 6  | 8 8      | 3/30 | 6     |     | RO   |
| Doington 74'5  | Are      | da   |       |     | 10   |
| Dm. 30   | 30       | 1    | RO    | 1   |      |
| The teranspoortat percebben is foormul   |          |      |       |     |      |
| vited as on It model as foreins-   |          |      |       |     |      |
| Minimize (Total T.P west)-   |          |      |       |     |      |
| 17 M, + 8 M, R + A M, R + 5 M, 4 + 9 M, 5 ** WO  |          |      |       |     |      |
| 27 86022 7 7 88  |          |      |       |     |      |
| P 6 MB1 + 8 MB2 + 9 MB3 + 6 MBA + 5 MB5 @120   |          |      |       |     |      |
| + 504, + FRAR+ 7 Mys+ 8 140+ 0 75  |          |      |       |     |      |
| subject to consterant -  |          |      |       |     |      |
| HM + BM - + WM, R+ 5 914 + 7 1/5 = 20  |          |      |       |     |      |
| 8 Mai + 5 Maa + 6 Mas + 7 May + 8 May = 30<br>6 Mai + 8 Maz + 3 Maz + 6 May + 5 May = 20 |          |      |       |     |      |
| 5 Mg, + FMgg + FMgg + 8 Mgg + 6 Mg = 10  |          |      |       |     |      |

First me will exolve it using month met come sule. The allocat material is each that.

F, 40 00 No No No Sup F2 8 50 50 60//7//8/30 8 8 65//5/26 F3 /6 FA 5 7 7 16 108 15 20 50 50 180 Derrand 30 by estep deesenipst The step solut is eginen of this

as:

AM,1 +8 M21 + 6 M31 + 5 M41 2 30 6 MR +57RR +8 7874 +742 = 30 4 dz + 6 dz + 9 dz + 7 dz 2 1 5 5d4+ + They + 6d4+ 8Mg = 20 9 7/5 + 8725 + 5735+ 6 7252 5 and Mig > 0 fan de 1,2,3 ¢ Sel, 2,3,4 Motal no of supply count. 2 9 Motal no of demand canet = 5 Whey sym inal fact freder eso companed. Motal comply = 40+30+20+10 Notal domende 30 + 30 + 15 + 20 + 2100 Total employe = Total demonof >> Botomed Tenang. peroblem.

Nowth west rowner souler to The sum mil F, e 404 W, 230 min(f,, w,) = 30 is assigned to F, W, Wis meets the ternamel of my 4 lemmes 40-302 10 mith F, The sim name four \$230 \$ W2 = 20 are compared. The min(F2, W2) = 20. This meets the durionel of w2 & leaves 30-20010 mits with Fa The Irim natures for £ 2 210 and uzzit are compared. The emoller of the Amo i. e min. (10, 15) 210 is ourign. to Faws, this enhant

the capacity of Fa and leaves 15 -10 st write with ws. The sim value for  $f_3 = 20$  and W3 25 auc comfand. The min (20,5) 25 in averagned to F3 we Wis meets the complete demand of we and leaves 20-5215 mits mith F3 The sim values for F3215 and Wa 220 aue companed. The emaller of 15,20215 is assigned for F3 Wg, this exhaust the capacity of Fz and leaner 20-1925 mith wa. The even value for Faciois WH25 are campared. The

min (10,5)25 is ording to Fa Wa This meets the complete demand of wy and remes 10-525 inits with Fq The sim value for Fy 25 f wg . 5. are compared. The emaller of the Amo 1.2 main (B, B)=B) is oussian to Fawa The IBFS 2 wy Sample W, WR WB Na F, 78 6 5 3 40 65 95 5 t3 6, 8 E Fq 5 F 20 5 Demand 30 30 15

1,127-0,27 V2 & 620= N, 2 C1, - U, = 7-0 0 V, = 4 VQ20,2-4,26-02)VQ26 U2 2 C22 - V2 2 5 - 6 2 > U2= -1 V3 = C23 - U2 = 6+12) V3=7 Uz 2 C33 - V3 = 9 - 7 = > Uz= 2 U42 C44- J9=8-4=> U4=4 V52 C45 - U42 6-42 V52 ? W, W2 W3 W7 W5 S Ui

7 9 40 U,=0 8 50 50 7 8 20 4227 36 65 5 20 Uze 2 7 80 65 10 4204 15 RO 5 sprage. 1 V3=7 V4=4 4=2 VD= b V,e 7

The minimizent T. D. could 2 7 × 30+ 6 × 10+5 × 20+ 6 × 10+9× 5 + 6 × 15 + 8 × 5 + 6 × 5 = 635 allocated coll 2 & 2 m+n-1 2445-1 hence the sor is non degenerate Optimality test wind madi method. Allocato Halde is was was supp. F, 7 6 F2 8 5 0 0 5 9 40 7 8 30 6 5 20 95 F3 6 8 85 0 7 Fq 5 5 15 Dam. 30 floorate, of optimality test. O embs v, e 0, me get

mm(dig) 2 -6, Faw, closed pathe Fq w, -> Fawars Fswars FSWSSFZWZS F, Was F, W, allocated val among all-ne F2 8 50 40 F3 6 8 9 6 9 20 F4 5 7 7 8 6 10 D 30 30 15 The event is ragineerate since no of allow 2 A L 8 hence grandity & is oversign. to F, wa, which has min. t. p east ers

 $\frac{d24}{2} = \frac{7(-1+9)}{2} = \frac{3}{2}$   $\frac{d24}{2} = \frac{8-(-1+8)}{2} = \frac{1}{2}$   $\frac{d3}{2} = \frac{8-(1+6)}{2} = \frac{1}{2}$   $\frac{d3}{2} = \frac{9-(1+7)}{2} = \frac{1}{2}$   $\frac{d3}{2} = \frac{9-(1+7)}{2} = \frac{1}{2}$   $\frac{d4}{2} = \frac{7-(-2+7)}{2} = \frac{3}{2}$   $\frac{d4}{3} = \frac{7-(-2+7)}{2} = \frac{3}{2}$   $\frac{d4}{3} = \frac{8-(-2+7)}{2} = \frac{5}{2}$ 

min we value from all digeto and deraw fath from F3 W5 classed path is F3 W5 > F3 W4 > F, Wx > F, W, > F4 W, > F4 W5 min allow val armong all me point on eleved path 25 hence consistence from ~ 6 adding the.

d21=8-(-1+#)22

dx 2 7-(-1+9)23 CDU 5 8-(-144) 2 29126-(1+7)2-2 ds2 2 8-(1+6)21 2332 0 - (1+4)21 GAB 5 4- (-54P) = 3 993 5 ± - (-5+4)= 5 CAU 2 B- (-2+5) 25 dag 2 b-(-2+a)=q

3 d,3 = [-13] minimum

closed fort = F, west, was Fawas Fawa min alloe among all. (-ne) = 15

50 20 8 9 50 7 7 Demany 30 30 15

The sol is degenerate to 7 48 hence t is airight to F, Wa at mun coest of 6.

greentran 4 substituting 4, 20, V, 27-0 E 7 UN 2 5-2 5-2 VR 26-0 26 U225-62-1 V324-0 -4 VW = 2 -0 5 2 M3=6-521 wy s lep Was 35 40 0 w, wa 5 (4) 7 (20) 6 8 30 -A3 8 2 5 5 20 1 B (-) 6 (+) 2' 6 10 -2 50 73 75 30 30 0 4 7 a) d, 5 2 9 - (0+4) 2 5 d2, 2 8-(-(+7)22 2282 6- (-1×4)23

Stevation 5 Simularization by putting 420 V, 27-0 c 7 U, 27-0 c 7 U, 25-72-7 V, 25-12 b V, 25-0 = 6 V, 25-0 = 6 V, 25-0 = 7 V, 25-0 = 7 V, 25-0 = 7

W CO 95 40 0 500 76 83 30 -1 50 82 6 5 20. -1 600 3 9 62 10 -2 50 73 75 95 30 30 4 E 9-(0+6) 23 d,52 8-(-1+7)=2 221 2 6- (-1+4)=3 2 23 Z

min Tat. TPC=7,5+4,015+5,20+5,30+6,015+5,05+

heart cost method -Dem. 30 30 35 36 37. The alloe to f, we a min (40319) This carlief. ordine dum. of my & learny 40-15-225. mith F, The ment TP voit is 5 intows

The alloe to Fower min (Bosse) W2 2 30 , F2 20.

- the next Th is is in f, wy

  the allow to f, wy 2 min (20, 20)

  Wy 20, F, 25
- > The next TP is 5 im Faw,
  allow of Faw, 2 min (10,30)=10

  Wye 20, Fa=0
- → The next This 5 in F3W5 allow of F3W5 = min(20,5) 25 W5 = 0, F3 = 15.
- ment min TP is b in F3W,

  The alloe to F3W, 2 min(19,20)

  This exhaust F3 20 & W, 25

  ment min TP is 7 in F, W,

  alloe to F, M 2 min (9,55)=5

F,20,W,20.

We b (E) 40 46 3 40 ( SO) A 8 30 8 F3 6(9) 8 56 20 8 as 500 B 10 8 7 20 30 30 15 min TPC2 705+4×15+920+9=30+ 6×19+ 5×19+ 9×10 here most alloer e \$

nost menrie dessrie 8 nerce it is degenerate. to mesome degeneracy, of me ablal & into F, W2 at court 6. Oftimal test embestituting 1,20, me get

V, e 7-0 e 7 4326-7= 7 V5=9+1 = 6 U429-7 = -2 Vo = 6-0 = 6 W2=9-6=1 Ng = 4-0 24 Va 2 9-0 25 dige 9-10+67=3 24526-(-2+6) da, 2 8-(-1+7)27 27 2 R3 2 6~ (~1+4)=3 d RA = 7- (-1+5)=3 dan = 8 + (-1+6)=3 032=8-(~+6)=3 83=3-(-1+4)e6 da = 6- (-1+5)= 7 CAR = 7- (-2+6)23 LAZ E 7 - (-2+A)25

ds 2 8 - (-2+9) 25

Since all des >0.

So the sol is optimal & vinique

The min total townst. with

T+5+4 × 15 + 5 × 20 + 5 × 30 +

By 15 + 5 × 5 + 5 × 10

2510.

```
Python Code:
import numpy as np
from collections import Counter
import math
def check_loop(p, row, column):
        p[row, column] = -1
        flag = 1
        while flag != 0:
                 flag = 0
                 if p.size != 0:
                         row = np.count\_nonzero(p, axis=1)
                          for index in range(len(row)):
                                  if row[index] < 2:
                                           flag = 1
                                           p = np.delete(p, (index - f), axis=0)
                                           f += 1
                 if p.size != 0:
                          col = np.count\_nonzero(p, axis=0)
                          for index in range(len(col)):
                                  if col[index] < 2:
                                           flag = 1
                                           p = np.delete(p, (index - e), axis=1)
                                           e += 1
        if p.size != 0:
                 return 0
        else:
                 return 1
def max_allocation_row(non_zero_list):
        max_values = np.zeros(len(non_zero_list))
        for val in non_zero_list:
                 \max_{\text{values}} [\text{val}[0]] += 1.0
        return np.where (max_values = np.amax(max_values))
def modi(c_modi, a_modi, m_modi, n_modi):
        iteration\_count = 1
        while True:
        print()
        print("Iteration - ", iteration_count)
        print ("Start AL \n", a_modi)
        u = np. array([np.nan] * m_modi)
        v = np.array([np.nan] * n_modi)
        p = np.zeros((m_modi, n_modi))
        _{x}, _{y} = np.where(a_{modi} > 0)
        nonzero = list(zip(_x, _y))
        _{x1}, _{y1} = np. where (a_{modi} = -1)
        if -1 in a_modi:
                 nz_a = np. where (a_modi = -1)
```

```
nonzero.append((min(nz_a[0]), min(nz_a[1])))
f = max\_allocation\_row(nonzero)
u [f [0] [0]] = 0
for i, j in nonzero:
         if i = f[0][0]:
                  v[j] = c_modi[i, j] - u[i]
print("U = ", u)
print("V = ", v)
while any(np.isnan(u)) or any(np.isnan(v)):
         for i, j in nonzero:
                  for j2 in range (0, len(v)):
                            if j2 = j and not math. isnan(v[j])
                                     and math.isnan(u[i]):
                                     \mathbf{u}[\mathbf{i}] = \mathbf{c}_{-}\mathbf{modi}[\mathbf{i}, \mathbf{j}] - \mathbf{v}[\mathbf{j}]
         for i, j in nonzero:
                  for j2 in range (0, len(u)):
                            if j2 = i and not math. isnan(u[i])
                                     and math. isnan(v[j]):
                                     v[j] = c_modi[i, j] - u[i]
         print("U = ", u)
         print("V = ", v)
# Finding P-matrix
for i in range (m_modi):
         for j in range (n_modi):
                  if not nonzero.__contains__((i, j)):
                           p[i, j] = c_{-}modi[i, j] - u[i] - v[j]
print("P-matrix")
print(p)
# Stop condition
small_val = np.min(p)
if small_val >= 0:
         break
i, j = np.argwhere(p = small_val)[0]
start = (i, j)
print("Start : ", start)
# Finding cycle elements
t = np.copy(a_modi)
t[start] = 1
while True:
         _{xs}, _{ys} = _{np.nonzero(t)}
         xcount, ycount = Counter(_xs), Counter(_ys)
         for x, count in xcount.items():
                   if count \ll 1:
                           t[x, :] = 0
         for y, count in ycount.items():
                   if count \ll 1:
                           t[:, y] = 0
         if all(x > 1 \text{ for } x \text{ in } x \text{ count. } values()) and
                   all(y > 1 \text{ for y in ycount.values}()):
                  break
# Finding cycle chain order
```

def dist(x1, y1, x2, y2):

```
if x1 = x2 or y1 = y2:
                 return abs(x1 - x2) + abs(y1 - y2)
         else:
                 return np.inf
fringe = set(tuple(p) for p in np.argwhere(t != 0))
alloc_modi = fringe
size = len(fringe)
path = [start]
while len(path) < size:
         last = path[-1]
         if last in fringe:
                  fringe.remove(last)
         next_val = min(fringe, key=lambda xy: dist(last[0],
                  last[1], xy[0], xy[1])
         path.append(next_val)
# Improving solution on cycle elements
neg = path[1::2]
pos = path[::2]
print ("Negative Value:", neg)
print ("Positive Value:", pos)
ql = []
for row in neg:
         ql.append(a_modi[row[0], row[1]))
q = int(min(ql))
for row in neg:
         if a_{\text{modi}}[\text{row}[0], \text{row}[1]] = -1:
                 a_{\text{-}}modi [row [0], row [1]] = 0 - q
         else:
                 a_{-}modi [row [0], row [1]] -= q
for row in pos:
         if a_{-}modi[row[0], row[1]] == -1:
                 a \mod [row[0], row[1]] = 0 + q
         else:
                 a_{-}modi [row [0], row [1]] += q
x_al = np.nonzero(a_modi)[0]
y_al = np.nonzero(a_modi)[1]
for i in range (len (x_al)):
         alloc_modi.add((x_al[i], y_al[i]))
print ("Mid Allocation Table : \n", a_modi)
_{x2}, _{y2} = \text{np.where} (a_{modi} > 0)
\# alloc_modi = list(zip(_x2, _y2))
no_alloc_modi = np.count_nonzero(a_modi)
unalloc_modi = []
for i1 in range (m_modi):
         for j1 in range(n_modi):
                  if not (i1, j1) in alloc_modi:
                          unalloc_modi.append((i1, j1))
print (a_modi)
no\_loop\_modi = []
if no\_alloc\_modi = m\_modi + n\_modi - 1:
         print ("Non Degeneracy")
```

```
else:
                   print ("Degeneracy")
                   print ("Values of epsilon is -1")
                   for il in unalloc_modi:
                            if \operatorname{check\_loop}(a\_\operatorname{modi.copy}(), i1[0], i1[1]) == 1:
                                      no_loop_modi.append(i1)
                   \min_{\text{epi-list}} = []
                   for i1 in no_loop_modi:
                            \min_{e \in L} \operatorname{list} . \operatorname{append} (\operatorname{c-modi}[i1[0], i1[1]])
                   \min_{\text{epi}} = \min(\min_{\text{epi-list}})
                   ind = min_epi_list.index(min_epi)
                   loc = no_loop_modi[ind]
                   a_{\text{modi}} [loc [0], loc [1]] = -1
                   print ("END AL : \n", a_modi)
                   print()
         iteration\_count += 1
return a_modi
def nwcr(cm_nwcr, m_nwcr, n_nwcr, s_nwcr, d_nwcr):
         c_nwcr = cm_nwcr.copy()
         a = np.zeros(c_nwcr.shape)
         total_cost_nwcr = 0
         no\_alloc\_nwcr = 0
         alloc_nwcr = []
         i = 0
         j = 0
         while (i < m_main) and (j < n_main):
                  x = \min(s_n w cr[i], d_n w cr[j])
                   s_n w cr[i] = s_n w cr[i] - x
                   d_n w cr[j] = d_n w cr[j] - x
                   total_cost_nwcr = total_cost_nwcr + x * c_nwcr[i, j]
                   no\_alloc\_nwcr += 1
                   alloc_nwcr.append((i, j))
                   a[i, j] = x
                   if s_nwcr[i] < d_nwcr[j]:
                            i = i + 1
                   elif s_nwcr[i] > d_nwcr[j]:
                            i = i + 1
                   else:
                            i = i + 1
                            j = j + 1
         print("Total Cost: ", total_cost_nwcr)
         unalloc_nwcr = []
         for i1 in range (m_main):
                   for j1 in range (n_main):
                            if not (i1, j1) in alloc_nwcr:
                                      unalloc_nwcr.append((i1, j1))
         print \, ("\,Allocated \,\, Positions: \,\, "\,, \,\, alloc\_nwcr \,)
         print("Unallocated Positions: ", unalloc_nwcr)
         print (" Allocation Matrix: ")
         print(a)
         no\_loop\_nwcr = []
         if no\_alloc\_nwcr = m\_nwcr + n\_nwcr - 1:
```

```
print ("Non Degeneracy")
         else:
                  print ("Degeneracy")
                  print ("Values of epsilon is -1")
                  for i1 in unalloc_nwcr:
                           if \operatorname{check\_loop}(a.\operatorname{copy}(), i1[0], i1[1]) == 1:
                                    no_loop_nwcr.append(i1)
                  \min_{e} \operatorname{pi-list} = []
                  for i1 in no_loop_nwcr:
                           \min_{e \in I} = \min_{e \in I} (\operatorname{cm_nwcr}[i1[0], i1[1])
                  min_epi = min(min_epi_list)
                  ind = min_epi_list.index(min_epi)
                  loc = no\_loop\_nwcr[ind]
                  a[loc[0], loc[1]] = -1
                  print ("Allocation Matrix After Converting Degeneracy
                           to Non-Degeneracy is: ")
                  print(a)
         optl = modi(cm_nwcr.copy(), a.copy(), m_nwcr, n_nwcr,)
         print ('optimised Allocation Matrix: ')
         print (optl)
         for row in range (0, m_nwcr):
                  for column in range (0, n_nwcr):
                           if optl[row][column] < 0:
                                    optl[row][column] = 0
         print("Total Optimal Cost = ", np.sum(optl * cm_nwcr))
def lcm(cm_lcm, m_lcm, n_lcm, s_lcm, d_lcm):
         c_{lcm} = cm_{lcm} \cdot copy()
         total\_cost\_lcm = 0
         no\_alloc\_lcm = 0
         alloc_lcm = []
        a = np. zeros(c_lcm.shape)
         \min_{cost} = \min_{cost} (c_{lcm})
         while min_cost != np.inf:
                  indexes = np.where(c_lcm = min_cost)
                  i = indexes[0][0]
                  j = indexes[1][0]
                  x = \min(s[i], d_lcm[j])
                  s_lcm[i] = x
                  d_{-lcm}[j] = x
                  total\_cost\_lcm += (x * c\_lcm[i, j])
                  no\_alloc\_lcm += 1
                  a[i, j] = x
                  alloc.append((i, j))
                  if s_{lcm}[i] < d_{lcm}[j]:
                           x = 0
                           while x < n_lcm:
                                    c_{lcm}[i, x] = np.inf
                                    x += 1
                  elif s_{lcm}[i] > d_{lcm}[j]:
                           y = 0
                           while y < m_{lcm}:
                                    c_{lcm}[y, j] = np.inf
```

```
y += 1
         else:
                  x = 0
                  while x < n_{lcm}:
                           c_{lcm}[i, x] = np.inf
                          x += 1
                  y = 0
                  while y < m_{lcm}:
                           c_{lcm}[y, j] = np.inf
                           v += 1
         min\_cost = np.amin(c\_lcm)
print("Total Cost: ", total_cost_lcm)
unalloc = []
for i in range (m_lcm):
         for j in range (n_lcm):
                  if not (i, j) in alloc:
                           unalloc.append((i, j))
print("List of Allocated Positions: ", alloc)
print ("List of Unallocated Positions: ", unalloc)
print ("Allocation Matrix: ")
print(a)
no\_loop\_lcm = []
if no\_alloc\_lcm = m\_lcm + n\_lcm - 1:
         print("Non Degeneracy")
else:
         print ("Degeneracy")
         for i in unalloc:
                  g = check_loop(a.copy(), i[0], i[1])
                  if g == 1:
                           no_loop_lcm.append(i)
                  min_epi_list = []
         for i in no_loop_lcm:
                  \min_{e \in I} \operatorname{list} . \operatorname{append} (\operatorname{cm}[i[0], i[1]])
         \min_{\text{epi}} = \min(\min_{\text{epi-list}})
         ind = min_epi_list.index(min_epi)
         loc = no\_loop\_lcm[ind]
         a[loc[0], loc[1]] = -1
         print ("Allocation Matrix After Converting
                  Degeneracy to Non-Degeneracy is: ")
         print(a)
optl = modi(cm_lcm.copy(), a.copy(), m_lcm, n_lcm,)
print('optimised Allocation Matrix: ')
print (optl)
for row in range (0, m_lcm):
         for column in range (0, n_lcm):
                  if optl[row][column] < 0:
                           optl[row][column] = 0
print("Total Optimal Cost = ", np.sum(optl * cm_lcm))
```

```
if __name__ = '__main__':
        cm_main = np.array([[7.0, 6, 4, 5, 9],
                [8, 5, 6, 7, 8],
                 [6, 8, 9, 6, 5],
                 [5, 7, 7, 8, 6]])
        s_main = np.array([40.0, 30, 20, 10])
        d_{\text{-}main} = \text{np.array}([30.0, 30, 15, 20, 5])
        c_{main} = cm_{main.copy}()
        print ("The Cost Matrix is: ")
        print (c_main)
        print ("The Supply is: ", s_main)
        print("The Demand is: ", d_main)
        m_{main}, n_{main} = c_{main}. shape
        print ("No of Rows & No of Columns: (", m_main, ", ", n_main, ")")
        total_demand = np.sum(d_main)
        total\_supply = np.sum(s\_main)
        if total_demand == total_supply:
                 print ("It is a Balanced Transportation Problem")
        else:
                 print ("It is an UnBalanced Transportation Problem")
                 if total_demand > total_supply:
                         new = np. array (np. zeros (n_main))
                         c_main = np.row_stack((c_main, new))
                         s_main = np.append(s, total_demand - total_supply)
                         m_main = m_main + 1
                 else:
                         new = np. array (np. zeros (m_main))
                         c_main = np.column_stack((c_main, new))
                         d = np.append(d, total\_supply - total\_demand)
                         n_{-}main = n_{-}main + 1
                 print ("The New Balanced Cost Matrix is: ")
                 print (c_main)
                 print ("The Supply is: ", s_main)
                 print ("The Demand is: ", d_main)
        print("Northwest corner method")
        nwcr(c_main.copy(), m_main, n_main, s_main.copy(), d_main.copy())
        print()
        print("Least Cost Method")
        lcm(c_main.copy(), m_main, n_main, s_main.copy(), d_main.copy())
        print()
```

## Output:

```
"/home/arghya/My Work/Python/pythonProject1/venv/bin/python" "/home/arghya/My Work/Python/pythonProject1/assignment4problem1.py
The Demand is: [30. 30. 15. 20. 5.]
Northwest corner method
Start AL
[ 0. 20. 10. 0. 0.]
U = [ 0. nan nan nan]
V = [7. 6. 7. nan nan]
U = [0. -1. 2. 4.]
P-matrix
Negative Value: [(0, 0), (1, 1), (2, 2), (3, 3)]
```

```
Mid Allocation Table :
[ 0. 15. 15. 0. 0.]
[ 0. 15. 15. 0. 0.]
Degeneracy
END AL :
Iteration - 2
Start AL
U = [ 0. nan nan nan]
Negative Value: [(3, 4), (0, 0), (2, 3)]
[ 0. 15. 15. 0. 0.]
[ 0. 15. 15. 0. 0.]
Iteration - 3
```

Start AL

```
Iteration - 3
P-matrix
Negative Value: [(0, 1), (1, 2)]
Mid Allocation Table :
[[20. 0. 15. 5. 0.]
Degeneracy
Values of epsilon is -1
END AL :
Iteration - 4
Start AL
```

P-matrix

```
P-matrix
Start : (2, 0)
Negative Value: [(0, 0), (2, 3)]
Mid Allocation Table :
[[ 5. -1. 15. 20. 0.]
Non Degeneracy
Iteration - 5
Start AL
[15. 0. 0. 0. 5.]
Iteration - 5
Start AL
P-matrix
optimised Allocation Matrix:
Total Optimal Cost = 510.0
Total Cost: 510.0
```

```
Degeneracy
Values of epsilon is -1
Iteration - 1
Start AL
P-matrix
optimised Allocation Matrix:
 [10. 0. 0. 0. 0.]]
Total Optimal Cost = 510.0
Process finished with exit code 0
```