

Masters of Technology in Computer Science And Engineering

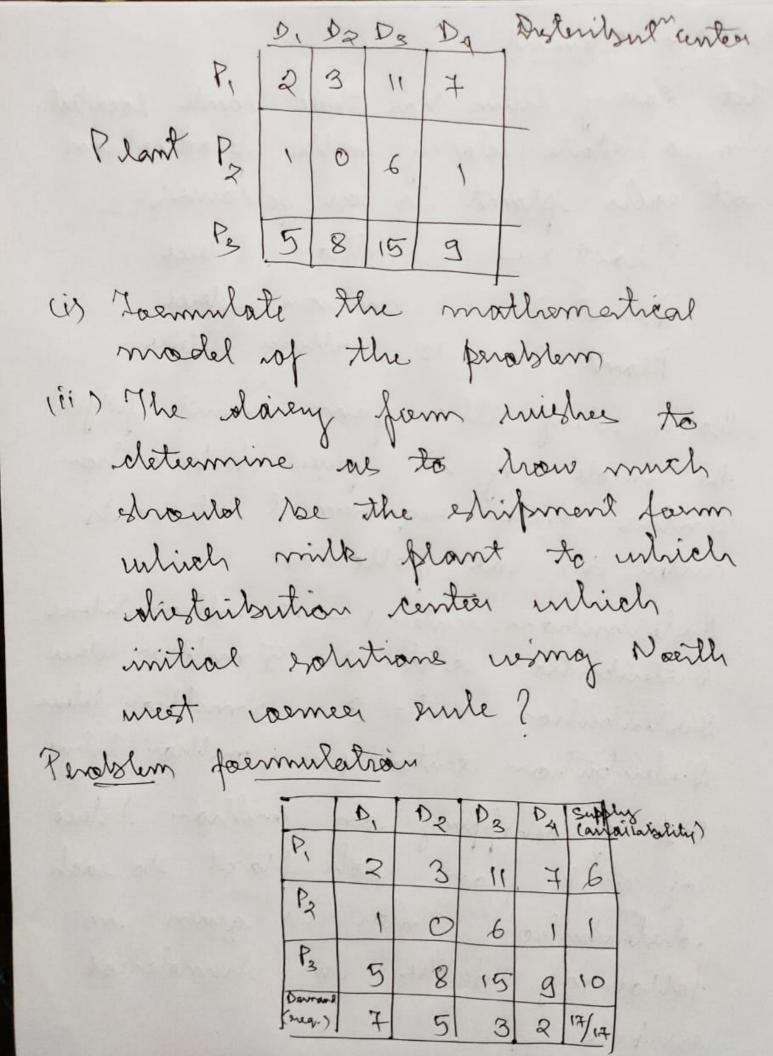
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submitted to
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Peroblem statement. Let clavery fier has three plants located in a state closery milk peraduction at each plant is as follows: Ylant 1 - 6 million literes Plant 2 - 1 million literes Plant 3 - 10 million literes Cook day the firm must fulfill the needs of its four distribution centers ville requirement at each center in as follows: distribution center (- 4 million litere Dietailantion center 2-5 million literes Distension center 3 - 3 million literes Disteribilition center 4 - 2 million litere last of shipping and million literes of milk ferom each front to each oristation conter is given in following fulles in hundered



het Mos & number of perceluite to be termesposeted from a percoluction facility i (9€1,2,3) to a abidentist center; (3E1, 2,3,4). The terontfort problem is italial or on It model is follows: Minimize (Notal steramespacitait cost) 2 Z = 29,1+3×1,2+11 ×13+7×19 + 1 M2, + 0 MQQ + 6 M 23+1 M24 + 5 Mg, + 8 Mg2 + 15 Mg3+ 9 Xg4 subject to the constraints-M,1+M,2+M,3+M,4=6 M21+M22+M23+M24=1 -carpphy M31 + M32 + M33 + M34210 M,, + Ma, + M3, 27 M12+ MR2+ 782= 5 713+ 723+ 733=3 M14 + 1/24 + 1/34 = 2

and 1/9 7,0 for 9 € 1,2,3 + 3 € 1,2,3,4 In the abone LP model, there are M=10 23 pg 212 décusion narrables, Mos and m + no 7 consteraint, where m are member of name of n are the member of column Criedonce of freedole solution; A vecessary and sufficient condition for a fearible solution to the teromefortation peroblem is, Testal empty 2 Total demand. 2 09 = 2 hg & 6+1+10 e 7+5+3+7 25 17 2.17

The total empty is equal to total demand, so the ferolstern is balanced teranespositate perolstern.

Deamfreing a, & b, since a, x b, allocate of, 26. This entranstry the supply set D, & leaves I with as unsatisfied demand at D,

@ Mone to cell (P2, D,). compare 924 b, 92 eb, allocate M291

B) Move to cell (P3, D2). Since supply at P3 is equal to the elements at D2, D3 and Da, allowate 732 = 5,

M33 = 3 + M34 = 2

ft extrefies the fearible solution condition ; e \(\mathbb{Z} \) as = \(\mathbb{Z} \) bo.

earle some 5 which is host offer the certe some 5 which is host offer the engineered marked runnbases (mar) e (3+4-1) = 6. Thus only one combit is satisfied, so this solution is tegeneerate solution. The temperator technique coef associated with this solutionis

Notal coefe ((2*6) + (1*1) + (8*5) + (15*3) + (9*2)) * 100

2(12+1+40+45+18) *100

2 116 # 100

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the same of the sa

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Python Code:
import numpy as np
if __name__ == '__main__':
   total_cost = 0
   no\_alloc = 0
   cm = np.array([[7.0, 6, 4, 5, 9],
                        [8, 5, 6, 7, 8],
                        [6, 8, 9, 6, 5],
                        [5, 7, 7, 8, 6]])
   s_main = np.array([40.0, 30, 20, 10])
   d_main = np.array([30.0, 30, 15, 20, 5])
   print("Cost Matrix")
   print(cm)
   r, c = cm.shape
   print("Rows, Columns: (", r - 1, ",", c - 1, ")")
   total_demand = np.sum(cm[r - 1, :])
   total_supply = np.sum(cm[:, c - 1])
   if total_demand == total_supply:
       print("Balanced Transportation Problem.")
   else:
       print("Unbalanced Transportation Problem")
   i = 0
   j = 0
   while (i < r - 1) and (j < c - 1):
       x = \min(cm[r - 1, j], cm[i, c - 1])
        cm[r - 1, j] = cm[r - 1, j] - x
       cm[i, c - 1] = cm[i, c - 1] - x
       total_cost = total_cost + x * cm[i, j]
       no_alloc = no_alloc + 1
       if cm[r - 1, j] < cm[i, c - 1]:
            j = j + 1
        elif cm[r - 1, j] > cm[i, c - 1]:
            i = i + 1
        else:
            i = i + 1
            j = j + 1
   print("Total Cost: ", total_cost * 100)
   print("No of Allocation: ", no_alloc)
   if ((r - 1) + (c - 1) - 1) == no_alloc and 
            total_demand == total_supply:
       print("Non Degenerate & Feasible Solution")
   else:
       print("Degenerate Solution")
```

Output:

```
Cost Matrix
[[2 3 11 7 6]
 [1 0 6 1 1]
 [5 8 15 9 10]
 [7 5 3 2 0]]
Rows, Columns: (3,4)
Balanced Transportation Problem.
Total Cost: 1200
No of Allocation: 1
Degenerate Solution
Total Cost: 1300
No of Allocation: 2
Degenerate Solution
Total Cost: 5300
No of Allocation: 3
Degenerate Solution
Total Cost: 9800
No of Allocation: 4
Degenerate Solution
Total Cost: 11600
No of Allocation: 5
Degenerate Solution
```

terablem statement I company has foner marchouse f six stoeres. The marchouse raltogether have a energhie 22 units of a eginen commodity, prolinichal overflus at marchouse 1,2,3 and q are 5,6,2 and 9 write respectively. The sin etaces altogether need 22 unit of commodity, Individual requirement estoeres 1, 2,3, 4,5 and 6 are 4,4,6,2, & and 2 write expectively. lost of ediffing one unite of lammadity ferom a mahehouse i to estore 3 in surfece is given in the materia Belon:

		Stoerce					
		1 33	2	3	4	5	6
	(8	12	9	6	9	10
marchanse	2	7	3	7	7	5	5
	3	6	5	9	11	3	11
	4	6	8	11	2	2	10
			-		-	100	

(i) Faermulate the mathematical modes

four the perobstem.

(ii) Final the IBFS wring MWCR.

Peroblem faermulation

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W, 21 2 2 6 2 10 5

proble	m	Joseph	what	1001			
1	S,)52	53	Su	55	3,6	Surailable
. 2	X1,	712	2/13	X14	25	100	The state of the state of
w,	9	12	9	6	9	10	5
1.7	XX	MR	XR3	XRA	125	726	
Wa	7	3	7	= =	5	5	6
1.7	X31	7/32	733	×34	235	×36	
ws	Ь	5	9	(1	3	11	2
WA	da,	245	243	244	145	246	
٩	6	8	11	2	2	10	9
Regimes	2. 4	4	В	2	4	2	22

het Mege number of with of commodity ehilpped ferom morehouse ? (? E1, 2, 3, 4) to estate ? (361, 2, 3, 4, 5, 6)

The tenansfort fuolstom is stated as

Minimizing (Total ethipping cond) 2 Za 2 g M, +12 M, 2 + g M 13 + 6 M4 + g M 5 + 10 M 16 + 7 M2, + B M22 + 7 M23 + 7 M24 + 5 M25 + 5 M26 + 6 M31 + 5 M22 + 9 M33 + 11 M24 + 3 M35 + 11 M36 + 6 M4 + 8 MA2 + 11 M13 + 2 M44 2 M47 10 M46 subject to the consteraint

MI, # MIR # MIR # MIR # MIR # MIR = 5 M MRI # MRR # MRR # MRR # MRS # MRS = 6 MRI # MRR # MRS # MRR # MRS # MRS = 7 MAI # MAR # MAS # MRA # MRS # MAS = 9

M, + MR, + M3, + M4, = 4

M, 2+ M22+M32+M42=4

M, 3+ M23+ M33+ M43=6

Requirement

M, 4+ M24+ M34+ M44=2

M, 5+ M25+M35+M45=4

M, 6+ M26+M36+M46=2

f for M93>0 for 221,2,3,44 3=1,2,3,4,5,6 for the above LP model, there are mon = 400=29 decision variables, Mos and mon = 10 consteraints, where in are no. of nours and more the mo. of column.

Construct of feasible colution of Motol available a Motol enquinement of E a: 2 2 10 2 co

es 5+6+2+9=4+4+6+2+9+2 es 22=22

The total anomalousity is equal to total enequienements, so the problem is Isalamed teransportat peroblem.

Solution

Novith	teen	coeme	er mes	thod		arri.	
	5,	Sa	53	Sal	55	56	shoilark
w,	9 3	12	8	6	9	10	8 = a, x 0
We	7	3 3	7 3	7	5	5	\$2 a2 3 0
w ₃	6	5	9 8	11	3	11	2003
WA	6	8	0	2	3	0	8=24
1000	KEB,	42 b2 30	8 = b3	0	Az by	5 2≥4 ₈	

- Deamfraing a, & by, estrice a, >b,; allocate of, >b, i allocate of, 2a. This completes the enquinement at s, and leaves I wint as available at w.
 - De Mone to rell (10,52) compare a, 662 i.e 124. allocate 11,221. His enhant the availability at w, and leaves 3 wit enquirement at 52.
 - 3 Mone to cell (wa, Sa) compane a2+ ba i.e 6>3, allocate da2²3 this completed the a requirement cof Sa + leave 3 with available at wo
 - B) Mone to cell (wa 553). compane as 4 bs: e 3 Lb, allocate 1/2323, this exhausts the availability of wa 4 leave, 3 unit meatisfied enequierment at S3.
 - 6) Mone to cell (wasss). compane az and by i.e 366, allocate

of we areal leave tourit meatisfied enequiement at 52

(6) Mone to cell (wa, 53), since availability and way was Es equal to sequerement of S3, Sq, S5 and S6. Therefore Muse 2 , 14321, 14422, 149 = 4 and It satisfy the fearible solution condition conditions and It in about the hours of molinal is earnal to enequiened (m+n-1) i.e 4+6-leg Hurs, this satisfy both condition so et in mon-degenerate fearible sol. The Shiffing cost resocrated with this exhan in

Model 1002 = (3 m 4) + (12 m 1) + (3 m 3) + (7 m 3) + (9 m 2) + (10 m 2) + (10 m 2) + (11 m 1) + (2 m 2) + (4 m 2) + (10 m 2) + (10 m 2) + (20 m 2) + (20

```
Python Code:
import numpy as np
if __name__ == '__main__':
   total_cost = 0
   no\_alloc = 0
   cm = np.array([[9, 12, 9, 6, 9, 10, 5], [7, 3, 7, 7, 5, 5, 6], [6, 5, 9, 11, 3, 11, 2], [6,
   8, 11, 2, 2, 10, 9],
              [4, 4, 6, 2, 4, 2, 0]]
   print("Cost Matrix")
   print(cm)
   # print()
   r, c = cm.shape
   print("Rows, Columns: (", r - 1, ",", c - 1, ")")
   # print()
   total_demand = np.sum(cm[r - 1, :])
   total_supply = np.sum(cm[:, c - 1])
   if total_demand == total_supply:
        print("Balanced Transportation Problem.")
        print("Unbalanced Transportation Problem")
   print()
   i = 0
   j = 0
   while (i < r - 1) and (j < c - 1):
        x = \min(cm[r - 1, j], cm[i, c - 1])
        cm[r - 1, j] = cm[r - 1, j] - x
        cm[i, c - 1] = cm[i, c - 1] - x
        total_cost = total_cost + x * cm[i, j]
        no_alloc = no_alloc + 1
        if cm[r - 1, j] < cm[i, c - 1]:
            j = j + 1
        elif cm[r - 1, j] > cm[i, c - 1]:
            i = i + 1
        else:
            i = i + 1
            j = j + 1
        print("Total Cost: ", total_cost)
        # print()
        print("No of Allocation: ", no_alloc)
        # print()
        if ((r - 1) + (c - 1) - 1) == no_alloc \setminus
                and total_demand == total_supply:
            print("Non Degenerate & Feasible Solution")
```

else:

print("Degenerate Solution")

Output:

```
Cost Matrix
[[912 9 6 9 10 5]
[7 3 7 7 5 5 6]
[6 5 9 11 3 11 2]
[6 8 11 2 2 10 9]
[4462420]]
Rows, Columns: (4,6)
Balanced Transportation Problem.
Total Cost: 36
No of Allocation: 1
Degenerate Solution
Total Cost: 48
No of Allocation: 2
Degenerate Solution
Total Cost: 57
No of Allocation: 3
Degenerate Solution
Total Cost: 78
No of Allocation: 4
Degenerate Solution
Total Cost: 96
No of Allocation: 5
Degenerate Solution
Total Cost: 107
No of Allocation: 6
Degenerate Solution
Total Cost: 111
No of Allocation: 7
Degenerate Solution
Total Cost: 119
No of Allocation: 8
Degenerate Solution
Total Cost: 139
No of Allocation: 9
```

Non Degenerate & Feasible Solution