

## The Second Law of Thermodynamics

First Law  $\rightarrow$  Conservation of energy

$$dU = dQ + dW$$

- Places no limitation of the possibility of transforming  
one form of energy to another
- 1st. Law      heat  $\rightarrow$  work or work  $\rightarrow$  heat  
ok ✓ provided total amt of heat = total work

It turns out

work to heat ✗ ok      heat by friction  
heat to work  $\rightarrow$  severe limitations  
electric current - resistance

Kelvin- Planck Statement of Second Law:

A transformation whose **only** final result is to transform into work heat extracted from a source at a given temperature is **impossible**.

"only" is critical.  $\exists$  transformations that convert heat completely to work.  $\rightarrow$  e.g. Isothermal expansion of an ideal gas

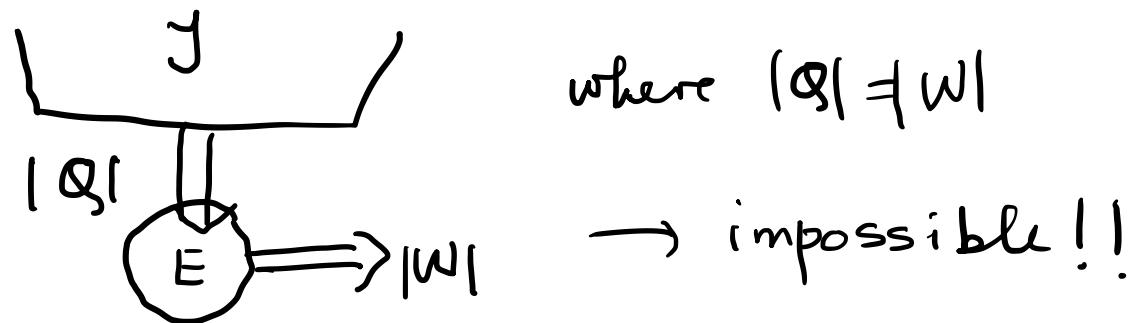
$$dQ = \cancel{dU}^0 + dW \Rightarrow dQ = dW$$

$$U(T)$$

not sole result  $\rightarrow$  volume is affected  
state changes

Kelvin statement  $\rightarrow$  no "perfect" heat engine exists  
perfect engine  $\rightarrow$  operating in a cycle takes heat  
from a source  $\rightarrow$  work  $\rightarrow$  returns to original state  
ready to start again

$$\text{efficiency} = \eta = \frac{\text{output}}{\text{input}} = \frac{W}{Q} = 1 \times \text{not possible}$$



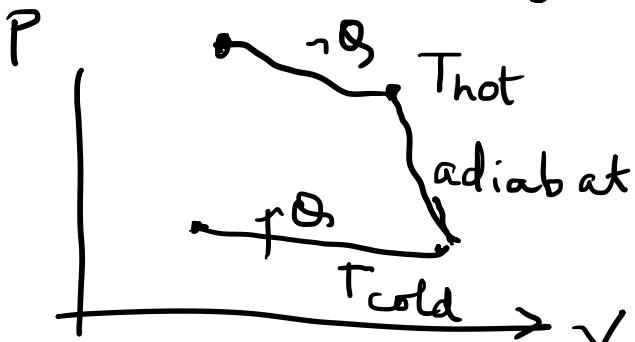
Clausius Statement:

A transformation whose **only** result is to transfer heat from a cooler to a hotter body is **impossible**.

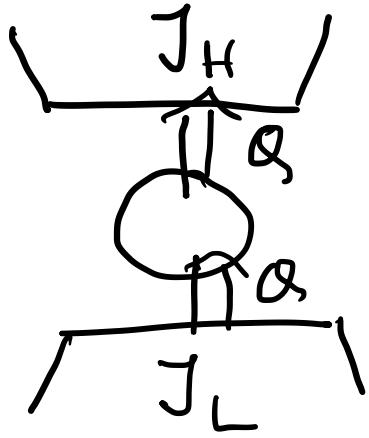
"only"

- gas expanded at const temp  $T_{cold}$ 
  - extracting heat  $Q$  from cold source.
- adiabatic compression to temp  $T_{hot}$

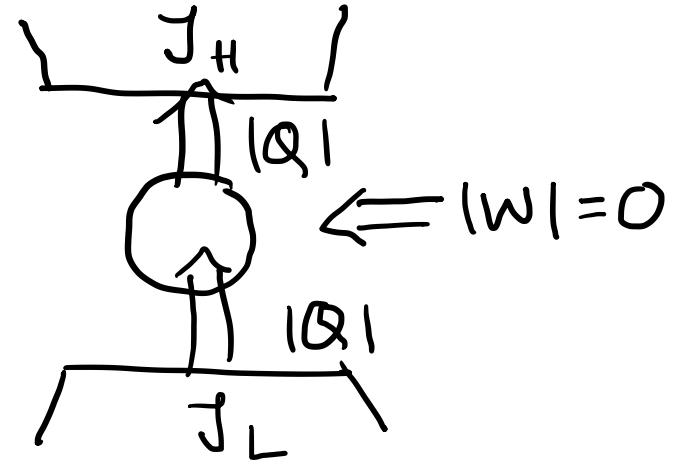
- isothermal compression delivering  $Q$  to the source  $\nexists$  at  $T_{hot}$



→ no violation of 2<sup>nd</sup> Law because  
System did not return to same state!!



impossible!



ideal/perfect refrigerator

coeff of performance  $K$

$$= \frac{\text{output}}{\text{input}} = \frac{Q}{W}, \quad \text{perfect } K \rightarrow \infty$$

## Equivalence of K-P and Clausius

$K$  = truth of  $K-P$

$\neg K$  = falsity of  $K-P$

$C$  = truth of  $C$

$\neg C$  = falsity of  $C$

must show  $K \equiv C$

$$K \Rightarrow C$$

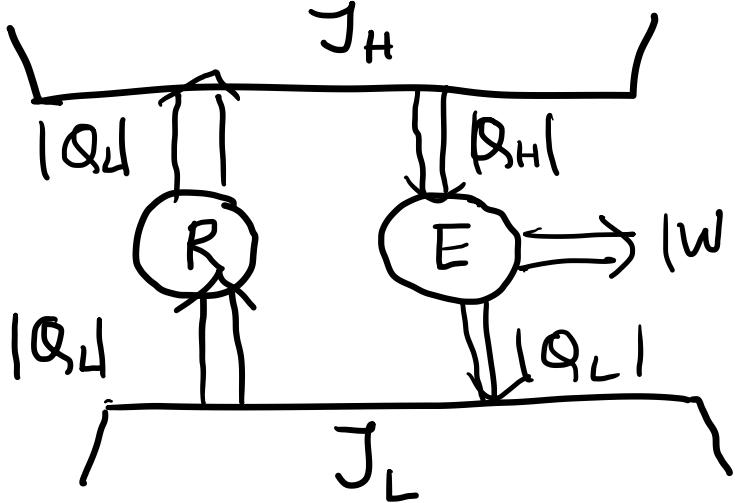
$$C \Rightarrow K$$

$$\neg K \Rightarrow \neg C$$

$$\neg C \Rightarrow \neg K$$

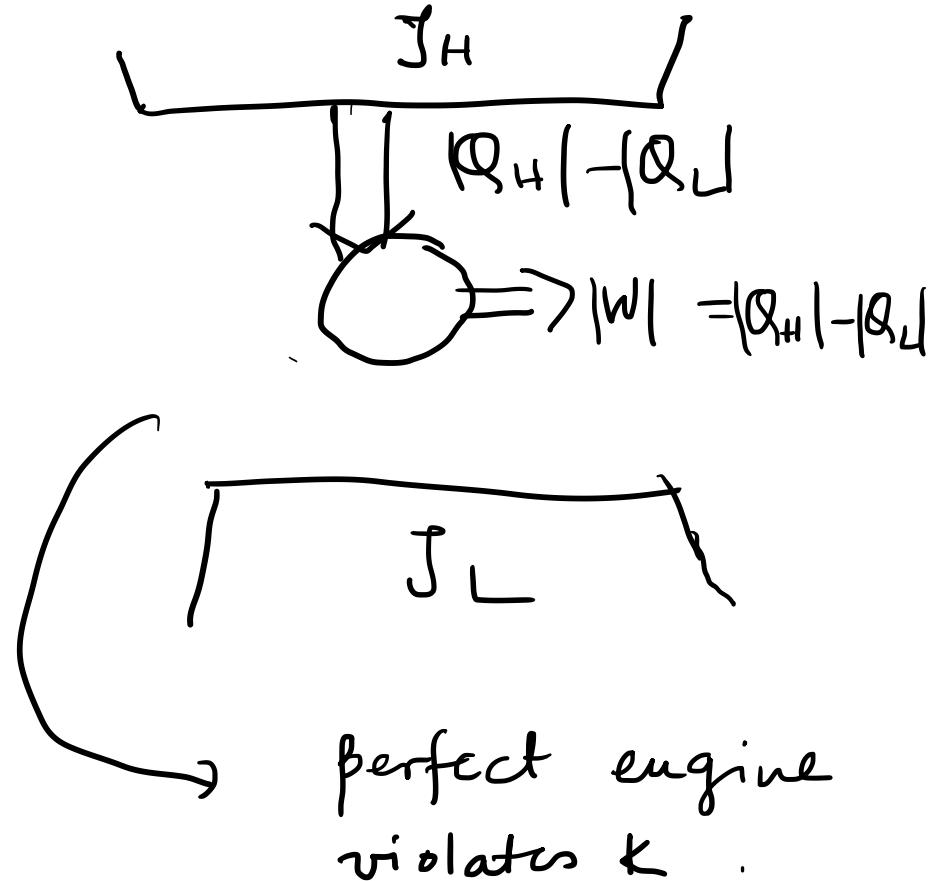
①

$$-C \Rightarrow -K$$



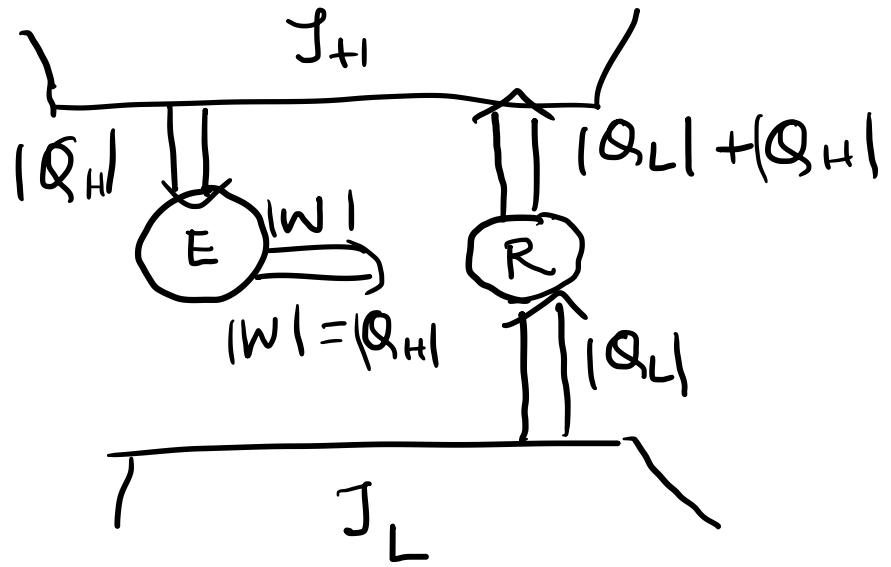
perfect refrigerator  
+ real engine

$$-C \Rightarrow -K$$

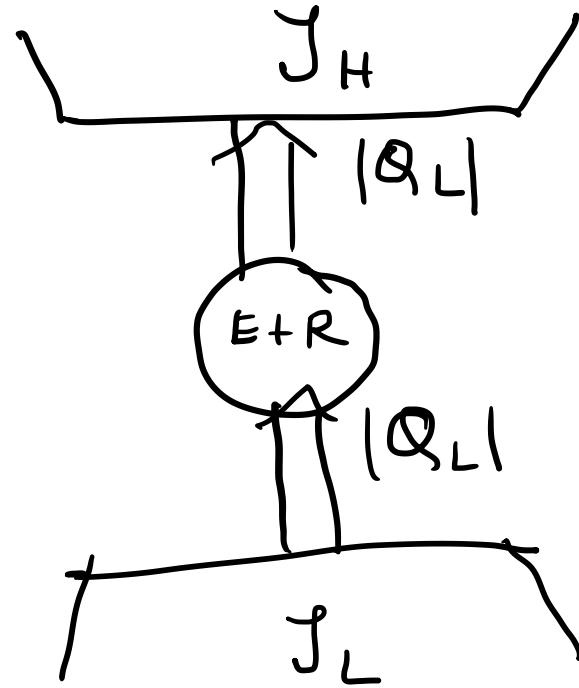


②

$$-K \Rightarrow -C$$



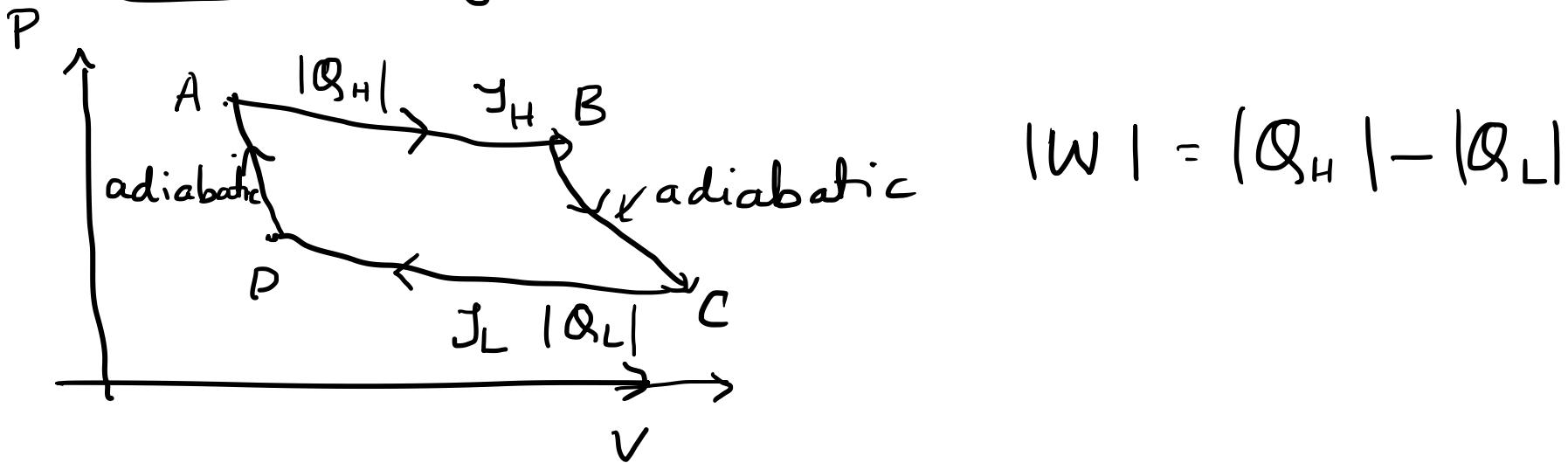
ideal engine + real refrigerator



→ perfect refrigerator  
violates C

$-K \Rightarrow -C$

## Carnot Cycle / Engine



$$|W| = |Q_H| - |Q_L|$$

- Carnot cycle is reversible
- Heat is always transferred at const temp .
- Independent of working substance .