

# The Second Law of Thermodynamics

First Law  $\rightarrow$  Conservation of energy

$$dU = dQ + dW$$

Places no limitation of the possibility of transforming  
one form of energy to another

1st. Law      heat  $\rightarrow$  work or work  $\rightarrow$  heat

OK  $\checkmark$  provided total amt of heat = total work

It turns out

work to heat     $\checkmark$  OK    heat by friction

heat to work  $\rightarrow$  severe limitations  
electric current - resistance

Kelvin- Planck Statement of Second Law:

A transformation whose **only** final result is to transform into work heat extracted from a source at a given temperature is **impossible**.

"only" is critical.  $\exists$  transformations that convert heat completely to work.  $\rightarrow$  e.g. Isothermal expansion of an ideal gas

$$dQ = d\overset{\rightarrow 0}{U} + dW \Rightarrow dQ = dW$$

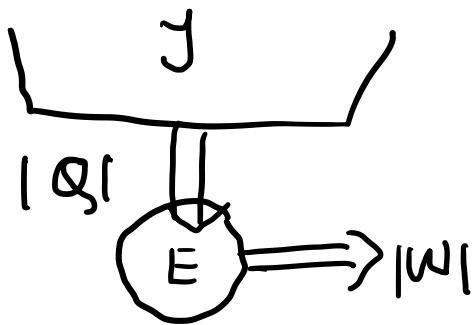
$U(T)$

not sole result  $\rightarrow$  volume is affected  
state changes

Kelvin statement  $\longrightarrow$  no "perfect" heat engine exists

perfect engine  $\longrightarrow$  operating in a cycle takes heat from a source  $\longrightarrow$  work  $\longrightarrow$  returns to original state ready to start again

$$\text{efficiency} = \eta = \frac{\text{output}}{\text{input}} = \frac{W}{Q} = 1 \quad \times \text{ not possible}$$



where  $|Q| = |W|$

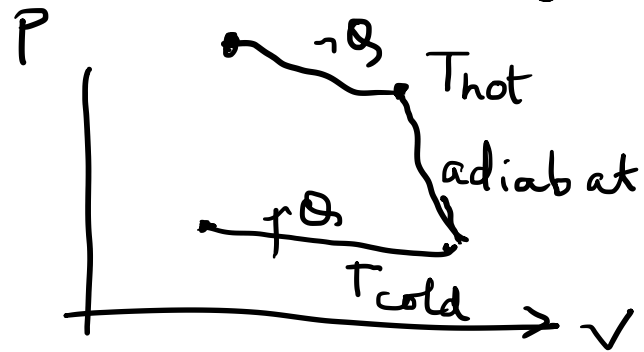
$\longrightarrow$  impossible!!

## Clausius Statement:

A transformation whose **only** result is to transfer heat from a cooler to a hotter body is **impossible**.

"only"

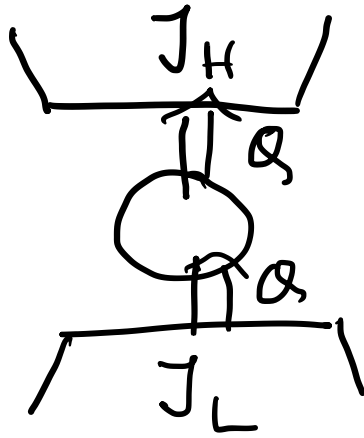
- gas expanded at const temp  $T_{\text{cold}}$ 
  - extracting heat  $Q$  from cold source.
- adiabatic compression to temp  $T_{\text{hot}}$



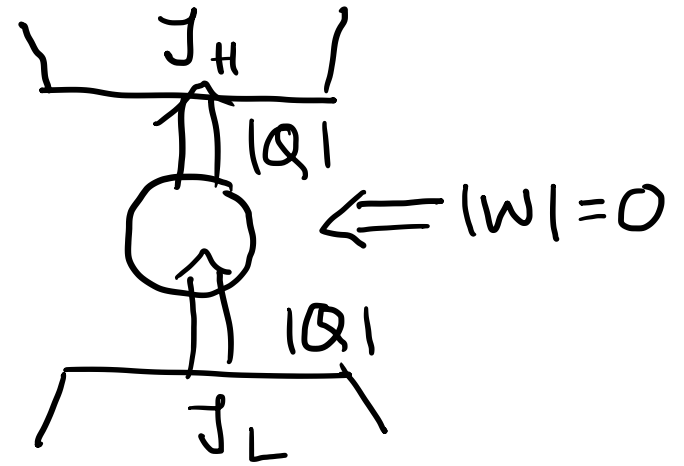
- isothermal compression delivering  $Q$  to the source ~~at~~ at  $T_{\text{hot}}$

→ no violation of 2<sup>nd</sup> Law because

System did not return to same state!!



impossible!



ideal/perfect refrigerator

coeff of performance  $\kappa$

$$= \frac{\text{output}}{\text{input}} = \frac{Q}{W}, \quad \text{perfect } \kappa \rightarrow \infty$$

## Equivalence of K-P and Clausius

$K$  = truth of K-P

$\neg K$  = falsity of K-P

$C$  = truth of C

$\neg C$  = falsity of C

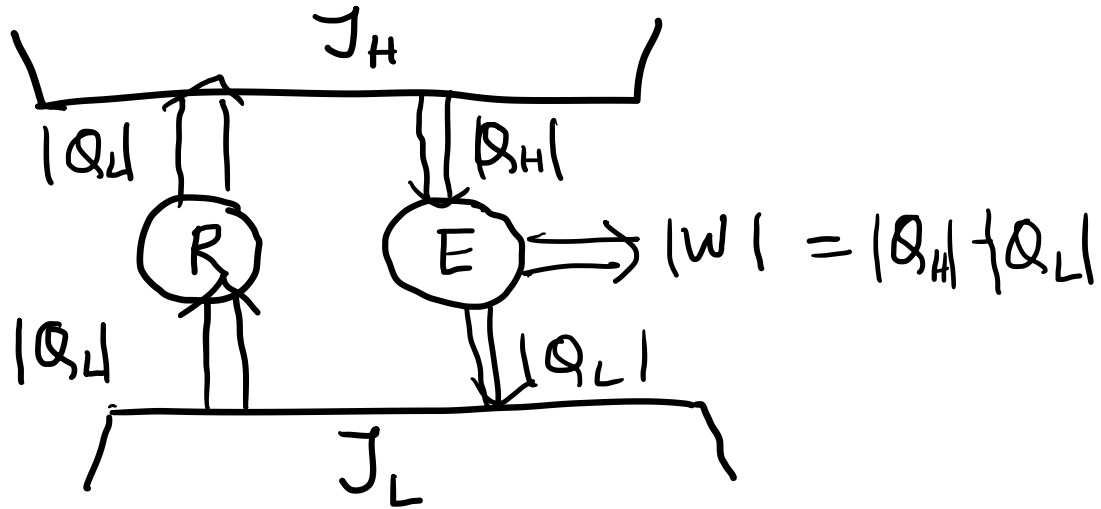
must show  $K \equiv C$

$K \Rightarrow C$        $C \Rightarrow K$

$\neg K \Rightarrow \neg C$        $\neg C \Rightarrow \neg K$

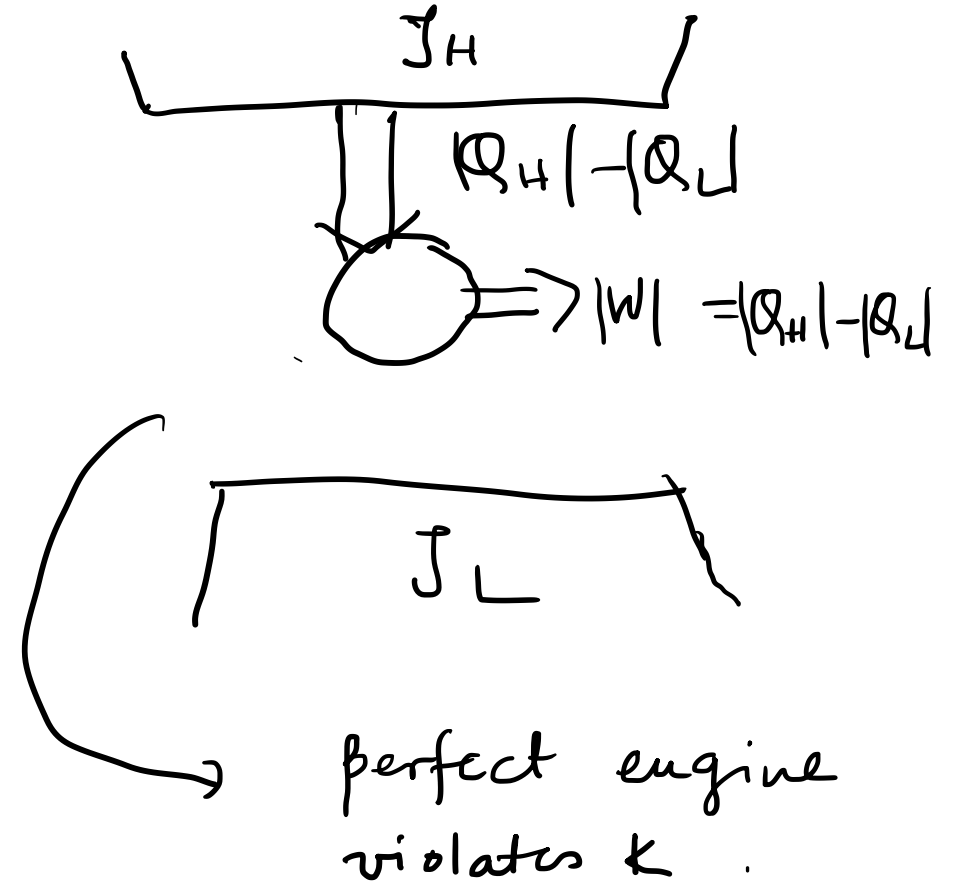
①

$$\sim C \Rightarrow \sim K$$



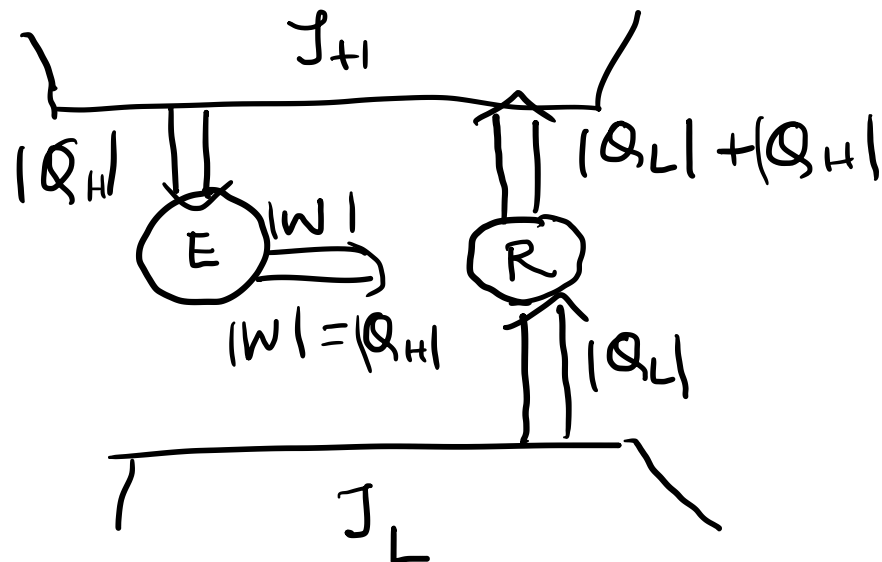
perfect refrigerator  
+ real engine

$$\sim C \Rightarrow \sim K$$



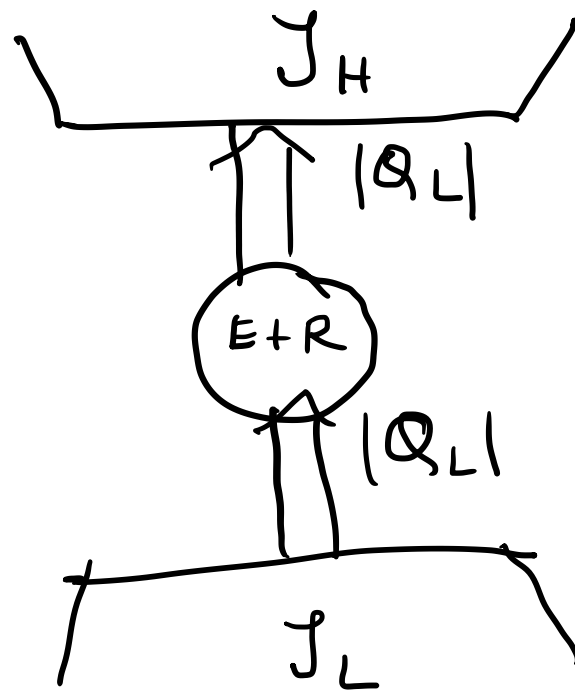
(2)

$$-K \Rightarrow -C$$



ideal engine + real refrigerator

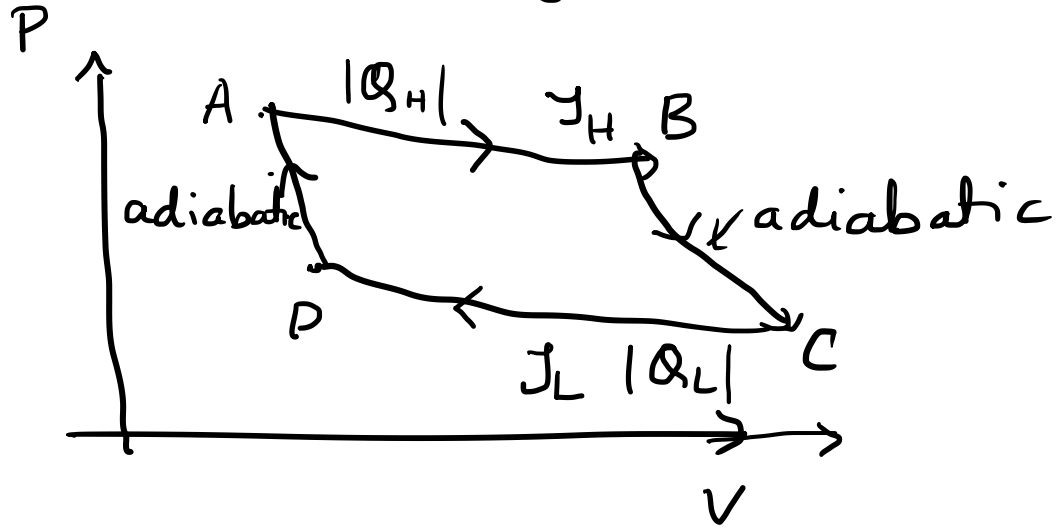
$$-K \Rightarrow -C$$



→ perfect refrigerator violates C



## Carnot Cycle/Engine



$$|W| = |Q_H| - |Q_L|$$

- Carnot cycle is reversible
- Heat is always transferred at const temp.
- Independent of working substance.