

$1001 \Rightarrow$ complement of $1001 = 0110$ (unary operation) $\Rightarrow n=1$

$x + y \Rightarrow$ binary operation.... $\Rightarrow n=2$

For $n = 3 \Rightarrow$ ternary operation...

$x, y, z [x * y * z = ?]$

$f: X \times Y \times Z \rightarrow U$

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$F(x*y*z) = u$

Conditional operation (ternary operation):

$\text{isMember ? '$2.00' : '$10.00'}$

if (isMember it TRUE) then

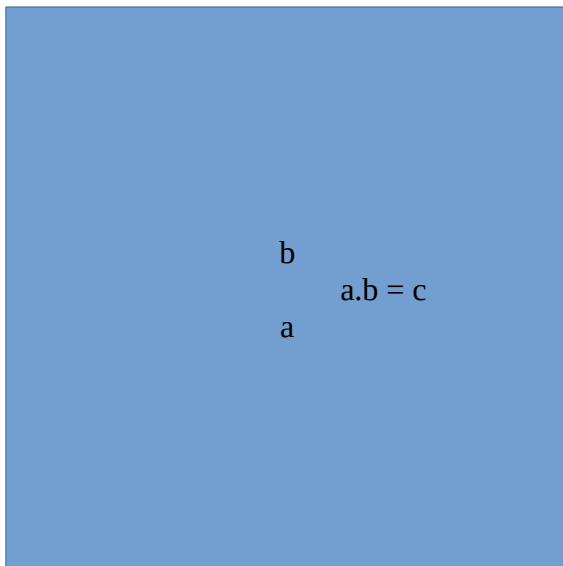
return \$2.00

else

return \$10.00

$x \text{ xor } y = ?$

$x \text{ xor } y \text{ xor } z = (x \text{ xor } y) \text{ xor } z = x \text{ xor } (y \text{ xor } z)$



$A = \{-1, 1, i, -i\}, i = \sqrt{-1}$

$g = i$

$i^1 = i$

$i^2 = -1$

$i^3 = -i$

$i^4 = 1$

$\{i^1, i^2, i^3, i^4\} = \{i, -1, -i, 1\} = A$

$g^1, g^2, \dots, g^n = e, \dots$ order of $g = n$
order of $i = 4$

$1 = 1 + i \cdot 0 = \cos 2n\pi + i \sin 2n\pi = e^{i 2n\pi}$

$$w^n = 1$$

Problem 1: Show that in any monoid, the mapping $g_a: x \mapsto x.a$ is one-one if a has a right inverse.

Problem 2: Let S be any monoid.

- (a) Show that an element a in S has a left inverse iff the transformation $f_a: x \mapsto a.x$ is one-one
- (b) Show that an element a has a left-inverse iff it has also a right inverse.