

$f: X \rightarrow Y$ is one-one if x, y in X with $x \neq y$, then $f(x) \neq f(y)$.

OR

$f: X \rightarrow Y$ is one-one if x, y in X such that $f(x) = f(y) \Rightarrow x = y$.

$$|S_1| = n_1, |S_2| = n_2, \dots, |S_k| = n_k$$

$$|S_1 \cup S_2 \cup \dots \cup S_k| = (|S_1| + |S_2| + \dots + |S_k|) - (\dots) \dots$$

E = set of all even integers = subset of Z

O = set of all odd integers = subset of Z

$A = \{5x \mid x \text{ is a positive integer}\} = \text{subset of } Z$

$f: N \rightarrow A$

$f(n) = 5n, n \text{ in } N$

$$A_1 = A - \{a_1\}$$

$$A_2 = A_1 - \{a_2\} = A - \{a_1, a_2\}$$

.....

$$2 \rightarrow 1$$

$$4 \rightarrow 2$$

$$6 \rightarrow 3$$

.....

$$2n \rightarrow n$$

....

$$1 \rightarrow 0$$

$$3 \rightarrow -1$$

$$5 \rightarrow -2$$

$$7 \rightarrow -3$$

.....

$N \times N$ is countable

[0.0001, 0.5, 0.9998..., 0.25, 0.75,]
x1 x3 x5... x2 x4

$f: N \rightarrow N \times N$

$g: (a, b) \rightarrow (0, 1)$

$$g(a, b) = w = (x - a) / (b - a).$$

$$(0, 1) \rightarrow [0, 1) \rightarrow (0, 1] \rightarrow [0, 1]$$

(0.0001, 0.0002,)