

Then,

$$S_p = \{ 6k + p : p = 0, 1, 2, 3, 4, 5 \text{ and } k = 0, \pm 1, \pm 2, \dots \}$$

$$S_0 = \{ \dots, -12, -6, 0, 6, 12, \dots \}$$

$$S_1 = \{ \dots, -11, -5, 1, 7, 13, \dots \}$$

$$S_2 = \{ \dots, -10, -4, 2, 8, 14, \dots \}$$

$$S_3 = \{ \dots, -9, -3, 3, 9, 15, \dots \}$$

$$S_4 = \{ \dots, -8, -2, 4, 10, 16, \dots \}$$

$$S_5 = \{ \dots, -7, -1, 5, 11, 17, \dots \}$$

$P = \{ S_0, S_1, S_2, S_3, S_4, S_5 \}$ is the partition of \mathbb{Z}

(i) $S_i \cap S_j = \emptyset, \forall \substack{i, j = 0, 1, \dots, 5, \\ i \neq j}$

(ii) $\bigcup_{i=0}^5 S_i = \mathbb{Z}.$