

~~P > 160-bits~~ prime number

$p \rightarrow n_b$ bits

$2^{(n_b/2)}$ operations

Miller-Rabin Primality Test Algorithm \rightarrow polynomial time (randomized algorithm)

$n^2, n^3 \dots$

$n = 13$

$n-1 = 12 = 2^2 \cdot 3, k = 2, q = 3$

select a and b from $Z_p = \{0, 1, 2, \dots, p-1\}$ such that $4a^3 + 27b^2 \not\equiv 0 \pmod{p}$

one-way function $h(\cdot) \rightarrow$

$G = (2, 7)$

$h(2 \parallel 7) = 20$

$\parallel \rightarrow$ concatenation operator

$h(1000 \parallel 1101) = h(10001101) = 30$

We call G is a base point in $E_p(a,b)$ of order n if $n \cdot G = G + G + \dots + G$ (n times) $= O$, point at infinity or zero point

Security Class (Sc_i) \rightarrow base point G_i , full (secret) key sk_i and partial (subsecret) key si

Security Class (Sc_j) \rightarrow base point G_j , full (secret) key sk_j and partial (subsecret) key sj

$Sc_k \geq Sc_j: (x - h(x_{k,j} \parallel y_{k,j}))$ where $sk \cdot G_j = (x_{k,j}, y_{k,j})$

Sc_j has a secret message: $MSG = \text{"Meet me after new year party at 10:30 AM at Stadium"}$

$Sc_j \rightarrow *: E_{Sk_j}[MSG]$

$Sc_i: D_{Sk_j}[E_{Sk_j}[MSG]] = MSG.$