

Mutable vrs. Immutable types

Not all python objects handle changes the same way.

- Some objects are mutable, meaning they **can be altered**.
- Others are immutable; they cannot be changed but **rather return new objects** when attempting to update.

Python closures

mutable datatypes?

(list, set, dictionary, user-defined classes)

Class	Description	Immutable?
bool	Boolean value	✓
int	integer (arbitrary magnitude)	✓
float	floating-point number	✓
list	mutable sequence of objects	
tuple	immutable sequence of objects	✓
str	character string	✓
set	unordered set of distinct objects	
frozenset	immutable form of set class	✓
dict	associative mapping (aka dictionary)	

- Primitive-like types are probably immutable.
- Container-like types are probably mutable.

When mutability matters!

(list, set, dictionary, user-defined classes)

```
container = {"hello", "world", "end"}
string_build = ""
for data in container:
    string_build += str(data)
print "id of string_build is ", id(string_build)
```

id of string_build is 140397490834864
id of string_build is 140397490835152
id of string_build is 140397490840552

```
container = {"hello", "world", "end"}
list_build = []
for data in container:
    list_build.append(str(data))
print "id of list_build is ", id(list_build)
```

id of list_build is 140633273771072
id of list_build is 140633273771072
id of list_build is 140633273771072

When mutability fails!

Python evaluates default arguments as part of the function definition only once for mutable type

```
def doSomething(param=[]):  
    param.append("thing")  
    return param
```

```
a1 = doSomething()  
print id(a1),"=",a1 #140114778712904 = ['thing']  
a2 = doSomething()  
print id(a2),"=",a2 #140114778712904 = ['thing', 'thing']  
a3 = doSomething()  
print id(a3),"=",a3 #140114778712904 = ['thing', 'thing', 'thing']  
a4 = doSomething(["passed_1"])  
print id(a4),"=",a4 #140114778713408 = ['passed_1', 'thing']  
a5 = doSomething(["passed_2"])  
print id(a5),"=",a5 #140114778713336 = ['passed_2', 'thing']
```

When mutability fails!

Use Immutable types for intended effect

```
def doSomething(param=None):
```

```
    if param == None:
```

```
        param = []
```

```
    param.append("thing")
```

```
    return param
```

```
a1 = doSomething()
```

```
print id(a1),"=",a1 #140114778713552 = ['thing']
```

```
a2 = doSomething()
```

```
print id(a2),"=",a2 #140114778713480 = ['thing']
```

```
a3 = doSomething()
```

```
print id(a3),"=",a3 #140114778656712 = ['thing']
```

```
a4 = doSomething(["passed_1"])
```

```
print id(a4),"=",a4 #140114778712904 = ['passed_1', 'thing']
```

```
a5 = doSomething(["passed_2"])
```

```
print id(a5),"=",a5 #140114778713408 = ['passed_2', 'thing']
```

TUPLES

- an ordered sequence of elements, can mix element types
- cannot change element values, **immutable**
- represented with parentheses

*remember
strings?*

`te = ()` *empty
tuple*

`t = (2, "mit", 3)`

`t[0]` → evaluates to 2

`(2, "mit", 3) + (5, 6)` → evaluates to `(2, "mit", 3, 5, 6)`

`t[1:2]` → slice tuple, evaluates to `("mit",)`

`t[1:3]` → slice tuple, evaluates to `("mit", 3)`

`len(t)` → evaluates to 3

`t[1] = 4` → gives error, can't modify object

*extra comma
means a tuple
with one element*

TUPLES

- conveniently used to **swap** variable values

```
x = y
```

```
y = x
```



```
temp = x
```

```
x = y
```

```
y = temp
```



```
(x, y) = (y, x)
```



- used to **return more than one value** from a function

```
def quotient_and_remainder(x, y):
```

```
    q = x // y
```







```
    r = x % y
```

```
    return (q, r)
```

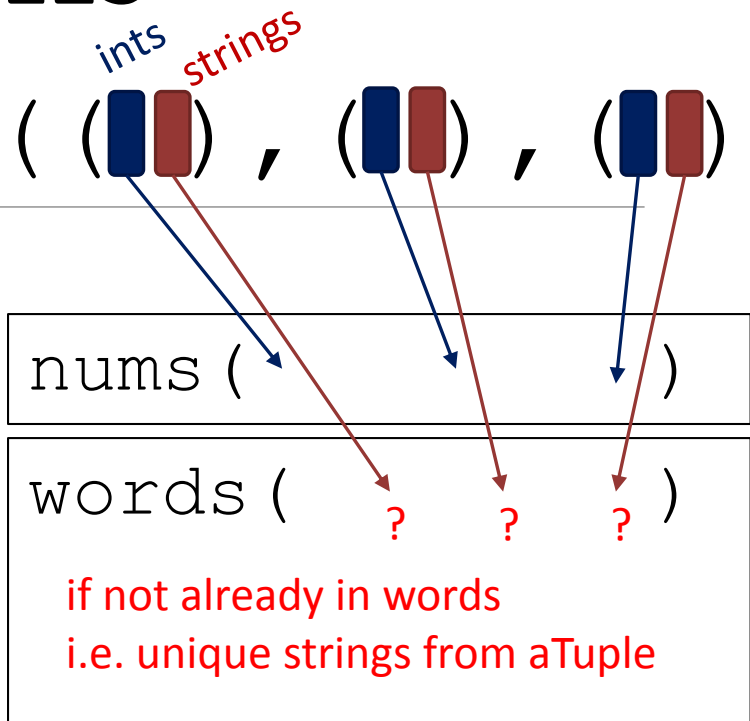
*integer
division*

```
(quot, rem) = quotient_and_remainder(4, 5)
```

MANIPULATING TUPLES

aTuple: (( ) , ( ) , ( ))

ints *strings*



- can **iterate** over tuples

```
def get_data(aTuple):  
    nums = ()  
    words = ()  
    for t in aTuple:  
        nums = nums + (t[0],)  
        if t[1] not in words:  
            words = words + (t[1],)  
    min_n = min(nums)  
    max_n = max(nums)  
    unique_words = len(words)  
    return (min_n, max_n, unique_words)
```

empty tuple

singleton tuple

nums (

)

words (? ? ?)

if not already in words
i.e. unique strings from aTuple

LISTS

- **ordered sequence** of information, accessible by index
- a list is denoted by **square brackets**, []
- a list contains **elements**
 - usually homogeneous (ie, all integers)
 - can contain mixed types (not common)
- list elements can be changed so a list is **mutable**

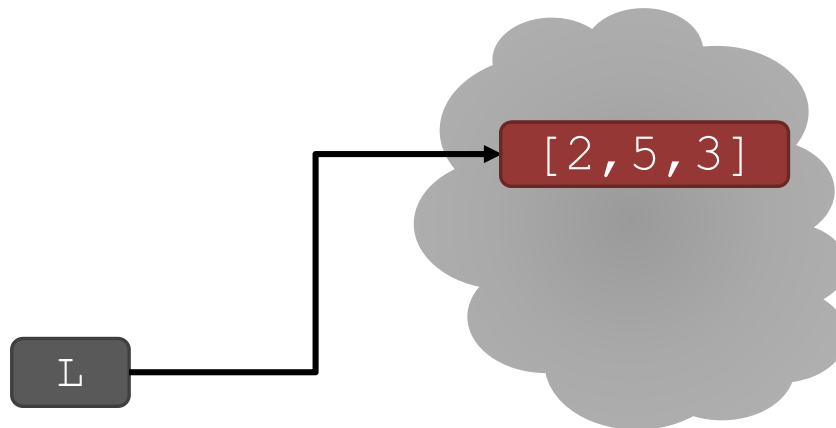
CHANGING ELEMENTS

- lists are **mutable**!
- assigning to an element at an index changes the value

`L = [2, 1, 3]`

`L[1] = 5`

- `L` is now `[2, 5, 3]`, note this is the **same object** `L`



ITERATING OVER A LIST

- compute the **sum of elements** of a list
- common pattern, iterate over list elements

```
total = 0
for i in range(len(L)):
    total += L[i]
print total
```

```
total = 0
for i in L:
    total += i
print total
```

*like strings,
can iterate
over list
elements
directly*

- notice
 - list elements are indexed 0 to $\text{len}(L) - 1$
 - `range(n)` goes from 0 to $n-1$

OPERATIONS ON LISTS - ADD

- **add** elements to end of list with `L.append(element)`

- **mutates** the list!

```
L = [2, 1, 3]
```

```
L.append(5)    → L is now [2, 1, 3, 5]
```



- what is the dot?
 - lists are Python objects, everything in Python is an object
 - objects have data
 - objects have methods and functions
 - access this information by `object_name.do_something()`
 - will learn more about these later

OPERATIONS ON LISTS - ADD

- to combine lists together use **concatenation**, + operator, to give you a new list
- **mutate** list with `L.extend(some_list)`

`L1 = [2, 1, 3]`

`L2 = [4, 5, 6]`

`L3 = L1 + L2`

→ `L3` is `[2, 1, 3, 4, 5, 6]`
`L1`, `L2` unchanged

`L1.extend([0, 6])`

→ mutated `L1` to `[2, 1, 3, 0, 6]`

OPERATIONS ON LISTS - REMOVE

- delete element at a **specific index** with `del (L[index])`
- remove element at **end of list** with `L.pop()`, returns the removed element
- remove a **specific element** with `L.remove(element)`
 - looks for the element and removes it
 - if element occurs multiple times, removes first occurrence
 - if element not in list, gives an error

all these
operations
mutate
the list

```
L = [2, 1, 3, 6, 3, 7, 0] # do below in order
L.remove(2) → mutates L = [1, 3, 6, 3, 7, 0]
L.remove(3) → mutates L = [1, 6, 3, 7, 0]
del(L[1])   → mutates L = [1, 3, 7, 0]
L.pop()     → returns 0 and mutates L = [1, 3, 7]
```

CONVERT LISTS TO STRINGS AND BACK

- convert **string to list** with `list(s)`, returns a list with every character from `s` as an element in `L`
- can use `s.split()`, to **split a string on a character** parameter, splits on spaces if called without a parameter
- use `' '.join(L)` to turn a **list of characters into a string**, can give a character in quotes to add char between every element

`s = "I<3 cs"`

→ `s` is a string

`list(s)`

→ returns `['I', '<', '3', ' ', 'c', 's']`

`s.split('<')`

→ returns `['I', '3 cs']`

`L = ['a', 'b', 'c']`

→ `L` is a list

`' '.join(L)`

→ returns `"abc"`

`'_'.join(L)`

→ returns `"a_b_c"`

OTHER LIST OPERATIONS

- `sort()` and `sorted()`

- `reverse()`

- and many more!

<https://docs.python.org/3/tutorial/datastructures.html>

`L = [9, 6, 0, 3]`

`sorted(L)` → returns sorted list, does **not mutate** `L`

`L.sort()` → **mutates** `L = [0, 3, 6, 9]`

`L.reverse()` → **mutates** `L = [9, 6, 3, 0]`

LISTS IN MEMORY

- lists are **mutable**
- behave differently than immutable types
- is an object in memory
- variable name points to object
- any variable pointing to that object is affected
- key phrase to keep in mind when working with lists is **side effects**

AN ANALOGY

- attributes of a person
 - singer, rich
- he is known by many names
- all nicknames point to the **same person**
 - add new attribute to **one nickname** ...

Justin Bieber

singer

rich

troublemaker

- ... **all his nicknames** refer to old attributes AND all new ones

The Bieb

singer

rich

troublemaker

JBeebs

singer

rich

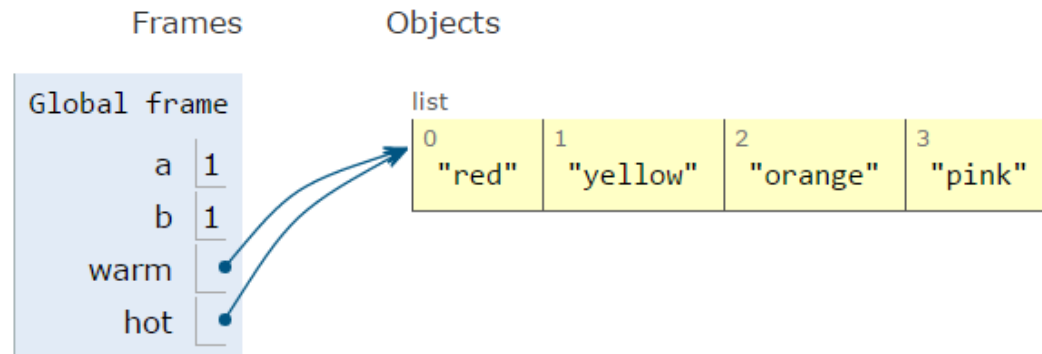
troublemaker

ALIASES

- `hot` is an **alias** for `warm` – changing one changes the other!
- `append()` has a side effect

```
1 a = 1
2 b = a
3 print(a)
4 print(b)
5
6 warm = ['red', 'yellow', 'orange']
7 hot = warm
8 hot.append('pink')
9 print(hot)
10 print(warm)
```

```
1
1
['red', 'yellow', 'orange', 'pink']
['red', 'yellow', 'orange', 'pink']
```

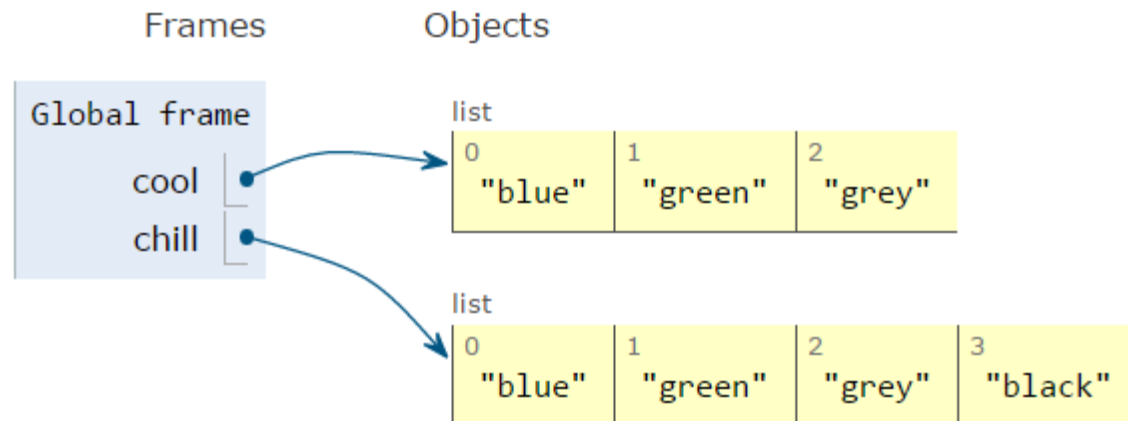


CLONING A LIST

- create a new list and **copy every element** using
`chill = cool[:]`

```
1 cool = ['blue', 'green', 'grey']
2 chill = cool[:]
3 chill.append('black')
4 print(chill)
5 print(cool)
```

```
['blue', 'green', 'grey', 'black']
['blue', 'green', 'grey']
```

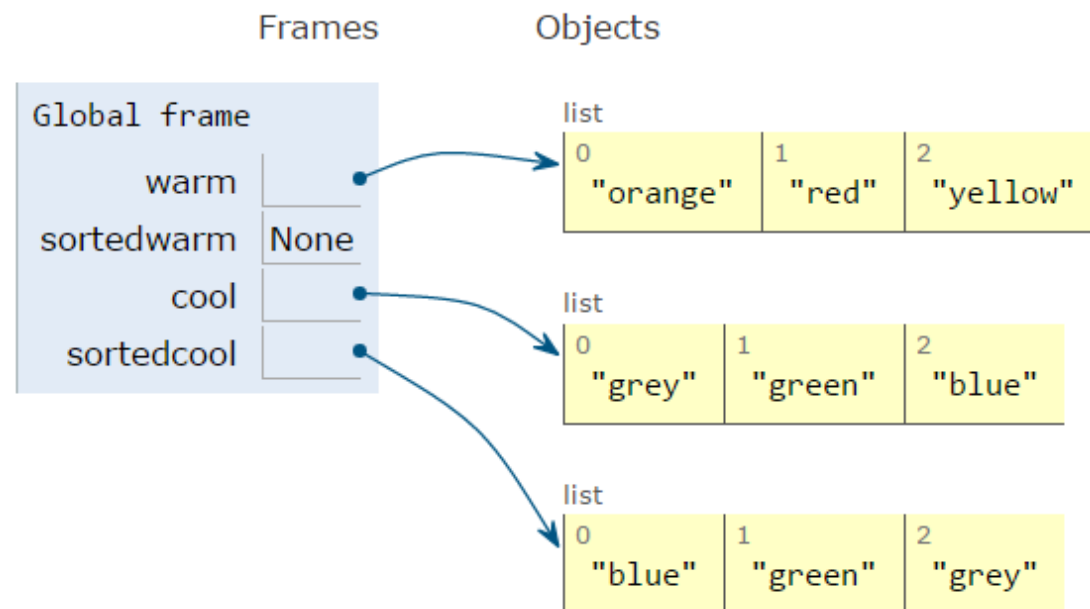


SORTING LISTS

- calling `sort()` **mutates** the list, returns nothing
- calling `sorted()` **does not mutate** list, must assign result to a variable

```
['orange', 'red', 'yellow']  
None  
['grey', 'green', 'blue']  
['blue', 'green', 'grey']
```

```
1 warm = ['red', 'yellow', 'orange']  
2 sortedwarm = warm.sort()  
3 print(warm)  
4 print(sortedwarm)  
5  
6 cool = ['grey', 'green', 'blue']  
7 sortedcool = sorted(cool)  
8 print(cool)  
9 print(sortedcool)
```

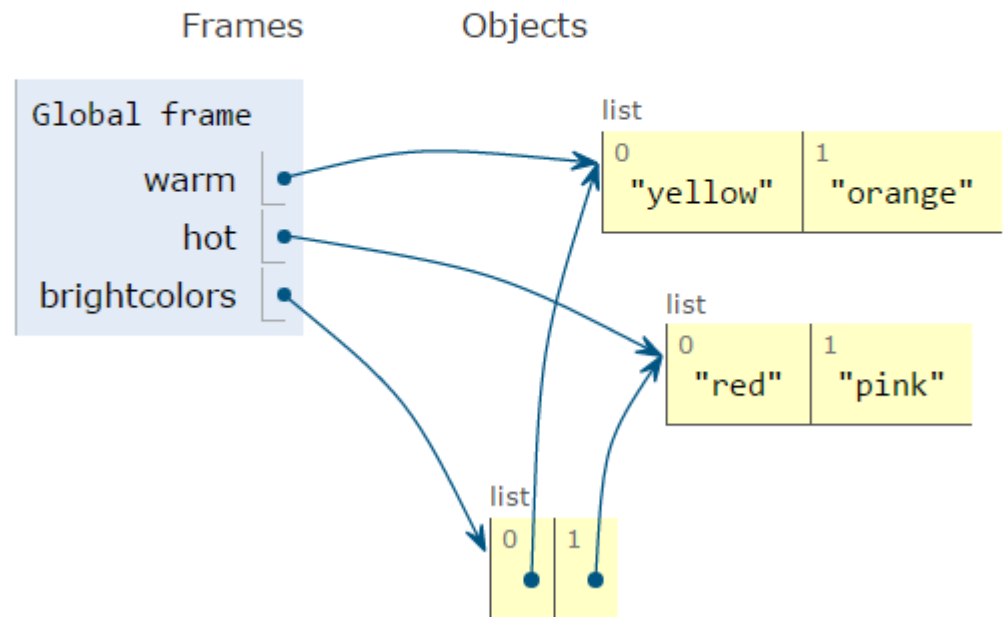


LISTS OF LISTS OF LISTS OF....

- can have **nested** lists
- side effects still possible after mutation

```
[['yellow', 'orange'], ['red']]  
['red', 'pink']  
[['yellow', 'orange'], ['red', 'pink']]
```


```
1 warm = ['yellow', 'orange']  
2 hot = ['red']  
3 brightcolors = [warm]  
4 brightcolors.append(hot)  
5 print(brightcolors)  
6 hot.append('pink')  
7 print(hot)  
8 print(brightcolors)
```



MUTATION AND ITERATION

Try this in Python Tutor!

- **avoid** mutating a list as you are iterating over it




```
def remove_dups(L1, L2):  
    for e in L1:  
        if e in L2:  
            L1.remove(e)
```

```
L1 = [1, 2, 3, 4]  
L2 = [1, 2, 5, 6]  
remove_dups(L1, L2)
```

- L1 is [2, 3, 4] not [3, 4] Why?

- Python uses an internal counter to keep track of index it is in the loop
- mutating changes the list length but Python doesn't update the counter
- loop never sees element 2



```
def remove_dups(L1, L2):  
    L1_copy = L1[:]  
    for e in L1_copy:  
        if e in L2:  
            L1.remove(e)
```

clone list first, note
that `L1_copy = L1`
does NOT clone

DICTIONARIES

HOW TO STORE STUDENT INFO

- so far, can store using separate lists for every info

```
names = ['Ana', 'John', 'Denise', 'Katy']
```

```
grade = ['B', 'A+', 'A', 'A']
```

```
course = [2.00, 6.0001, 20.002, 9.01]
```

- a **separate list** for each item
- each list must have the **same length**
- info stored across lists at **same index**, each index refers to info for a different person

HOW TO UPDATE/RETRIEVE STUDENT INFO

```
def get_grade(student, name_list, grade_list, course_list):  
    i = name_list.index(student)  
    grade = grade_list[i]  
    course = course_list[i]  
    return (course, grade)
```

- **messy** if have a lot of different info to keep track of
- must maintain **many lists** and pass them as arguments
- must **always index** using integers
- must remember to change multiple lists

A BETTER AND CLEANER WAY – A DICTIONARY

- nice to **index item of interest directly** (not always int)
- nice to use **one data structure**, no separate lists

A list

0	Elem 1
1	Elem 2
2	Elem 3
3	Elem 4
...	...

index

element

A dictionary

Key 1	Val 1
Key 2	Val 2
Key 3	Val 3
Key 4	Val 4
...	...

custom
index by
label

element

A PYTHON DICTIONARY

- store pairs of data
 - key
 - value

'Ana'	'B'
'Denise'	'A'
'John'	'A+'
'Katy'	'A'

custom
index by
label

element

my_dict = { } *empty dictionary*

grades = { 'Ana': 'B', 'John': 'A+', 'Denise': 'A', 'Katy': 'A' }

↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑
key1 val1 key2 val2 key3 val3 key4 val4

DICTIONARY LOOKUP

- similar to indexing into a list
- **looks up** the **key**
- **returns** the **value** associated with the key
- if key isn't found, get an error

'Ana'	'B'
'Denise'	'A'
'John'	'A+ '
'Katy'	'A'

```
grades = { 'Ana': 'B', 'John': 'A+', 'Denise': 'A', 'Katy': 'A' }
```

```
grades[ 'John' ]      → evaluates to 'A+ '
```

```
grades[ 'Sylvan' ]    → gives a KeyError
```

DICTIONARY OPERATIONS

'Ana'	'B'
'Denise'	'A'
'John'	'A+'
'Katy'	'A'
'Sylvan'	'A'

```
grades = { 'Ana': 'B', 'John': 'A+', 'Denise': 'A', 'Katy': 'A' }
```

- **add** an entry

```
grades[ 'Sylvan' ] = 'A'
```

- **test** if key in dictionary

```
'John' in grades      → returns True  
'Daniel' in grades   → returns False
```

- **delete** entry

```
del(grades[ 'Ana' ])
```

DICTIONARY OPERATIONS

'Ana'	'B'
'Denise'	'A'
'John'	'A+'
'Katy'	'A'

```
grades = { 'Ana': 'B', 'John': 'A+', 'Denise': 'A', 'Katy': 'A' }
```

- get an **iterable that acts like a tuple of all keys** *no guaranteed order*

```
grades.keys() → returns [ 'Denise', 'Katy', 'John', 'Ana' ]
```

- get an **iterable that acts like a tuple of all values**

```
grades.values() → returns [ 'A', 'A', 'A+', 'B' ]
```

no guaranteed order

DICTIONARY KEYS and VALUES

■ values

- any type (**immutable and mutable**)
- can be **duplicates**
- dictionary values can be lists, even other dictionaries!

■ keys

- must be **unique**
- **immutable** type (`int`, `float`, `string`, `tuple`, `bool`)
 - actually need an object that is **hashable**, but think of as immutable as all immutable types are hashable
- careful with `float` type as a key

■ **no order** to keys or values!

```
d = {4:{1:0}, (1,3):"twelve", 'const':[3.14,2.7,8.44]}
```


list vs dict

- **ordered** sequence of elements
- look up elements by an integer index
- indices have an **order**
- index is an **integer**

- **matches** “keys” to “values”
- look up one item by another item
- **no order** is guaranteed
- key can be any **immutable** type

EXAMPLE: 3 FUNCTIONS TO ANALYZE SONG LYRICS

- 1) create a **frequency dictionary** mapping `str: int`
- 2) find **word that occurs the most** and how many times
 - use a list, in case there is more than one word
 - return a tuple `(list, int)` for `(words_list, highest_freq)`
- 3) find the **words that occur at least X times**
 - let user choose “at least X times”, so allow as parameter
 - return a list of tuples, each tuple is a `(list, int)` containing the list of words ordered by their frequency
 - IDEA: From song dictionary, find most frequent word. Delete most common word. Repeat. It works because you are mutating the song dictionary.

CREATING A DICTIONARY

```
def lyrics_to_frequencies(lyrics):  
    myDict = {}  
    for word in lyrics:  
        if word in myDict:  
            myDict[word] += 1  
        else:  
            myDict[word] = 1  
    return myDict
```

can iterate over list
can iterate over keys
in dictionary
update value
associated with key

USING THE DICTIONARY

```
def most_common_words(freqs):  
    values = freqs.values()  
    best = max(values)  
    words = []  
    for k in freqs:  
        if freqs[k] == best:  
            words.append(k)  
    return (words, best)
```

*this is an iterable, so can
apply built-in function*

*can iterate over keys
in dictionary*

LEVERAGING DICTIONARY PROPERTIES

```
def words_often(freqs, minTimes):  
    result = []  
    done = False  
    while not done:  
        temp = most_common_words(freqs)  
        if temp[1] >= minTimes:  
            result.append(temp)  
            for w in temp[0]:  
                del(freqs[w])  
        else:  
            done = True  
    return result
```

*can directly mutate
dictionary; makes it
easier to iterate*

```
print(words_often(beatles, 5))
```

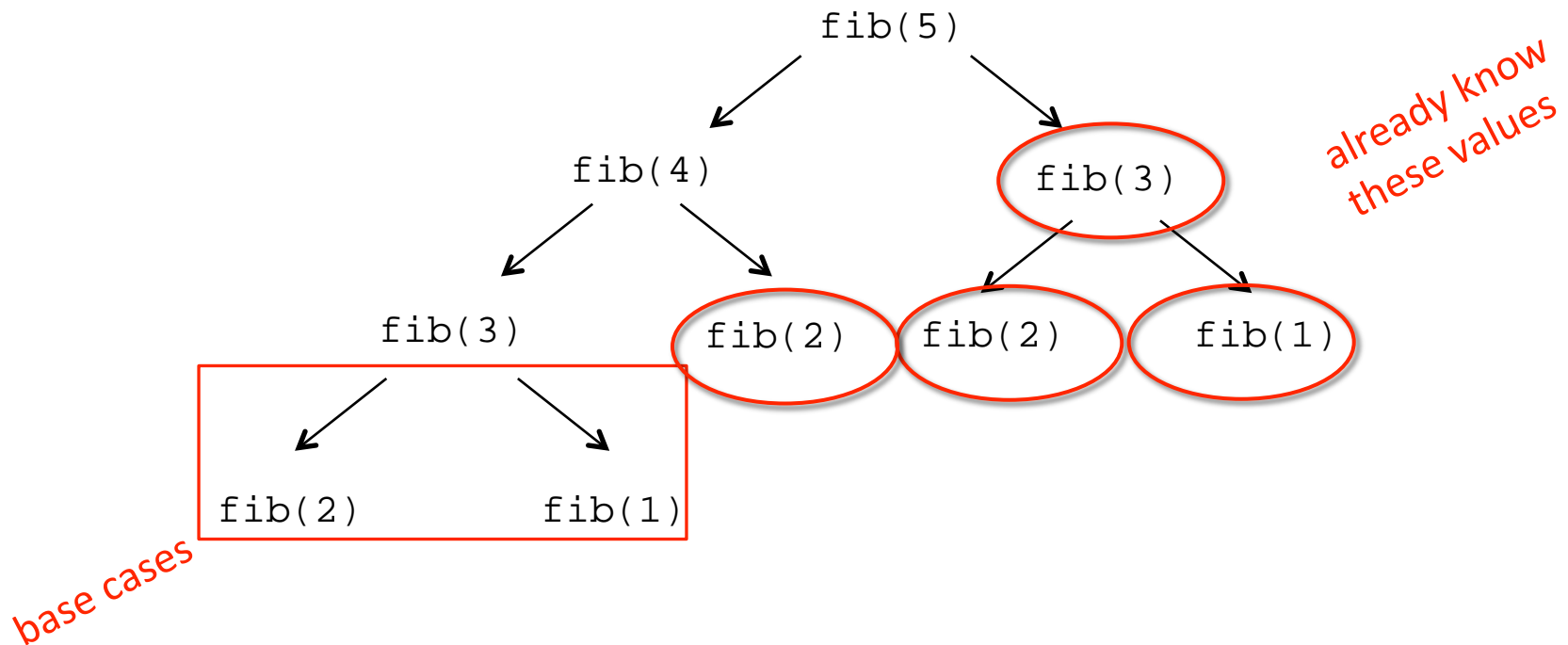
FIBONACCI RECURSIVE CODE

```
def fib(n):  
    if n == 1:  
        return 1  
    elif n == 2:  
        return 2  
    else:  
        return fib(n-1) + fib(n-2)
```

- two base cases
- calls itself twice
- this code is inefficient

INEFFICIENT FIBONACCI

$$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$$



- **recalculating** the same values many times!
- could keep **track** of already calculated values

FIBONACCI WITH A DICTIONARY

```
def fib_efficient(n, d):  
    if n in d:  
        return d[n]  
    else:  
        ans = fib_efficient(n-1, d) + fib_efficient(n-2, d)  
        d[n] = ans  
        return ans  
  
d = {1:1, 2:2}  
print(fib_efficient(6, d))
```

Method sometimes
called "memoization"

Initialize dictionary
with base cases

- do a **lookup first** in case already calculated the value
- **modify dictionary** as progress through function calls

EFFICIENCY GAINS

- Calling `fib(34)` results in 11,405,773 recursive calls to the procedure
- Calling `fib_efficient(34)` results in 65 recursive calls to the procedure
- Using dictionaries to capture intermediate results can be very efficient
- But note that this only works for procedures without side effects (i.e., the procedure will always produce the same result for a specific argument independent of any other computations between calls)