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1) $7n-2=O(n)$

$$f(n) \leq c \cdot g(n)$$

$$7n-2 \leq g(n)$$

$$7n-2 \leq c(n)$$

Let suppose $c=8$

$$7n-2 \leq 8 \cdot n$$

$$7n-2/n \leq 8$$

Here we take $n=2$

$$7(2)-2/2 \leq 8$$

$$14-2/2 \leq 8$$

$6 \leq 8$ hence, the equation is proved, firstly we have to choose the value of c and on that value suppose the n and then proof whether the equation is verified on that c value or not.

2) $7n-2=\theta(n)$

$$c_1 \cdot g(n) \leq f(n) \leq c_2 \cdot g(n) \rightarrow A$$

$$c_1 \cdot g(n) \leq 7n-2 \leq c_2 \cdot g(n)$$

first, we suppose $c=7, c=8$ and put in eq A

$$7(n) \leq 7n-2 \leq 8 \cdot g(n)$$

Then, $n=1$

$$7(1) \leq 7(1)-2 \leq 8(1)$$

$$7 \leq 7-2 \leq 8$$

$$7 \leq 5 \leq 8$$

$n=2,$

$$7(2) \leq 7(2)-2 \leq 8(2)$$

$$14 \leq 14-2 \leq 16$$

$$14 \leq 12 \leq 16$$

firstly, we have to choose the value of c_1 and c_2 and on that value suppose the n value and then proof whether the equation is verified on that c_1 and c_2 value or not Since, the equation is not proof for $n=1$ and $n=2$, $c_1=7$, $c_2=8$ but for $c_1=2$ and $c_2=6$ the equation is proved.

3) $7n-2 = \theta(n^2)$

$$c_1 \cdot g(n) \leq f(n) \leq c_2 \cdot g(n) \rightarrow B$$

$$c_1 \cdot g(n^2) \leq 7n-2 \leq c_2 \cdot g(n^2)$$

first, we suppose $c_1=1$, $c_2=5$ and put in eq B

$$1(n^2) \leq 7n-2 \leq 5 \cdot g(n^2)$$

Then, $n=2$ in eq B

$$1(2^2) \leq 7(2)-2 \leq 5 \cdot g(2^2)$$

$$4 \leq 14-2 \leq 20$$

$$4 \leq 12 \leq 20$$

$n=1$, in eq B

$$1(1^2) \leq 7(1)-2 \leq 5(1^2)$$

$$1 \leq 5 \leq 5 \text{ hence proved!}$$

firstly, we have to choose the value of c_1 and c_2 and on that value suppose the n value and then proof whether the equation is verified on that c_1 and c_2 value or not Since, the equation is proof for $n=1$ and $n=2$, $c_1=1$, $c_2=5$.

4) $3n^3+20n^2+5=O(n^6)$

$$f(n) \leq c \cdot g(n)$$

$$3n^3+20n^2+5 \leq c(n^6)$$

Let suppose $c=28$

$$3n^3+20n^2+5 \leq 28(n^6)$$

$$3n^3+20n^2+5 / n^6 \leq 28$$

Here we take $n=1$

$$3(1^3) + 20(1^2) + 5 / (1)^6 \leq 28$$

$$3+20+5 \leq 28$$

$$28 \leq 28 \text{ hence, proved!}$$

hence, the equation is proved, firstly we have to choose the value of c and on that value suppose the n and then proof whether the equation is verified on that c value or not.