

# Project1

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## Setup:

```
#clean workspace  
rm(list = ls())
```

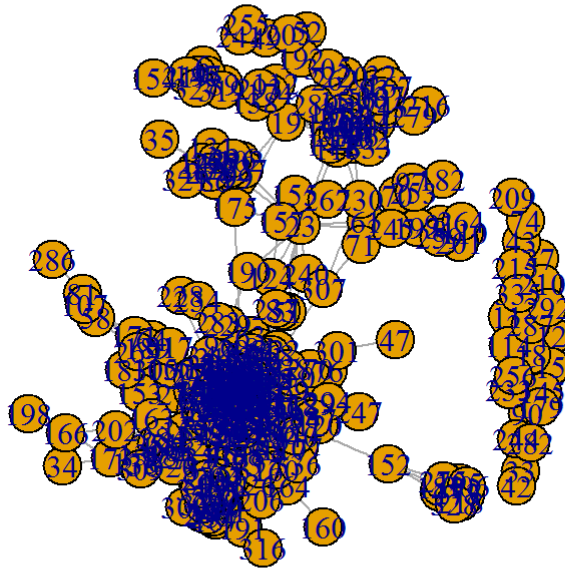
```
#require igraph  
library(igraph)
```

```
##  
## Attaching package: 'igraph'
```

```
## The following objects are masked from 'package:stats':  
##  
##      decompose, spectrum
```

```
## The following object is masked from 'package:base':  
##  
##      union
```

```
#read edges csv for nodeid 0  
graph.edges <- read.csv(file = 'facebook/0.edges', sep=" ", header=FALSE, col.names=c("source",  
"target"))  
  
#get edges  
graph.e <- graph.edges - min(graph.edges) + 1  
#get nodes  
graph.n <- data.frame(id=seq(max(graph.e) - min(graph.e) + 1))  
  
graph.n$group <- 1  
  
#import into igraph  
g = graph.data.frame(graph.e, directed=FALSE, vertices=graph.n)  
  
#simplify code  
g2 = simplify(g)  
  
#plot  
plot(g2)
```



## Question 3:

Explore with some functions from ppt

```
#get vertices
V(g2)
```

```
## + 347/347 vertices, named:
## [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17
## [18] 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34
## [35] 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51
## [52] 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68
## [69] 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85
## [86] 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102
## [103] 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119
## [120] 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136
## [137] 137 138 139 140 141 142 143 144 145 146 147 148 149 150 151 152 153
## [154] 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170
## + ... omitted several vertices
```

```
#get edges
edges(g2)
```

```
## [[1]]
## IGRAPH UN-- 347 2519 --
## + attr: name (v/c), group (v/n)
## + edges (vertex names):
## [1] 1--48 1--53 1--54 1--73 1--88 1--92 1--119 1--126 1--133 1--194
## [11] 1--236 1--280 1--299 1--315 1--322 1--346 2--20 2--115 2--116 2--149
## [21] 2--226 2--312 2--326 2--333 2--343 3--9 3--25 3--26 3--67 3--72
## [31] 3--85 3--122 3--142 3--170 3--188 3--200 3--228 3--274 3--280 3--283
## [41] 3--323 4--78 4--152 4--181 4--195 4--218 4--273 4--275 4--306 4--328
## [51] 5--87 5--122 5--156 5--158 5--169 5--180 5--187 5--204 5--213 5--235
## [61] 5--315 5--316 6--89 6--95 6--147 6--219 6--319 7--22 7--31 7--38
## [71] 7--65 7--87 7--103 7--129 7--136 7--168 7--213 7--246 7--291 7--304
## + ... omitted several edges
##
## attr("class")
## [1] "igraph.edge"
```

```
#find vertex attributes, did not load attributes so we should not expect much here
vertex_attr(g2)
```

```

## $name
## [1] "1" "2" "3" "4" "5" "6" "7" "8" "9" "10" "11"
## [12] "12" "13" "14" "15" "16" "17" "18" "19" "20" "21" "22"
## [23] "23" "24" "25" "26" "27" "28" "29" "30" "31" "32" "33"
## [34] "34" "35" "36" "37" "38" "39" "40" "41" "42" "43" "44"
## [45] "45" "46" "47" "48" "49" "50" "51" "52" "53" "54" "55"
## [56] "56" "57" "58" "59" "60" "61" "62" "63" "64" "65" "66"
## [67] "67" "68" "69" "70" "71" "72" "73" "74" "75" "76" "77"
## [78] "78" "79" "80" "81" "82" "83" "84" "85" "86" "87" "88"
## [89] "89" "90" "91" "92" "93" "94" "95" "96" "97" "98" "99"
## [100] "100" "101" "102" "103" "104" "105" "106" "107" "108" "109" "110"
## [111] "111" "112" "113" "114" "115" "116" "117" "118" "119" "120" "121"
## [122] "122" "123" "124" "125" "126" "127" "128" "129" "130" "131" "132"
## [133] "133" "134" "135" "136" "137" "138" "139" "140" "141" "142" "143"
## [144] "144" "145" "146" "147" "148" "149" "150" "151" "152" "153" "154"
## [155] "155" "156" "157" "158" "159" "160" "161" "162" "163" "164" "165"
## [166] "166" "167" "168" "169" "170" "171" "172" "173" "174" "175" "176"
## [177] "177" "178" "179" "180" "181" "182" "183" "184" "185" "186" "187"
## [188] "188" "189" "190" "191" "192" "193" "194" "195" "196" "197" "198"
## [199] "199" "200" "201" "202" "203" "204" "205" "206" "207" "208" "209"
## [210] "210" "211" "212" "213" "214" "215" "216" "217" "218" "219" "220"
## [221] "221" "222" "223" "224" "225" "226" "227" "228" "229" "230" "231"
## [232] "232" "233" "234" "235" "236" "237" "238" "239" "240" "241" "242"
## [243] "243" "244" "245" "246" "247" "248" "249" "250" "251" "252" "253"
## [254] "254" "255" "256" "257" "258" "259" "260" "261" "262" "263" "264"
## [265] "265" "266" "267" "268" "269" "270" "271" "272" "273" "274" "275"
## [276] "276" "277" "278" "279" "280" "281" "282" "283" "284" "285" "286"
## [287] "287" "288" "289" "290" "291" "292" "293" "294" "295" "296" "297"
## [298] "298" "299" "300" "301" "302" "303" "304" "305" "306" "307" "308"
## [309] "309" "310" "311" "312" "313" "314" "315" "316" "317" "318" "319"
## [320] "320" "321" "322" "323" "324" "325" "326" "327" "328" "329" "330"
## [331] "331" "332" "333" "334" "335" "336" "337" "338" "339" "340" "341"
## [342] "342" "343" "344" "345" "346" "347"
##
## $group
## [1] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [36] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [71] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [106] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [141] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [176] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [211] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [246] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [281] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## [316] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1

```

```

#check if the graph is simple (does not have loops or multiple edges between vertices)
is.simple(g2)

```

```
## [1] TRUE
```

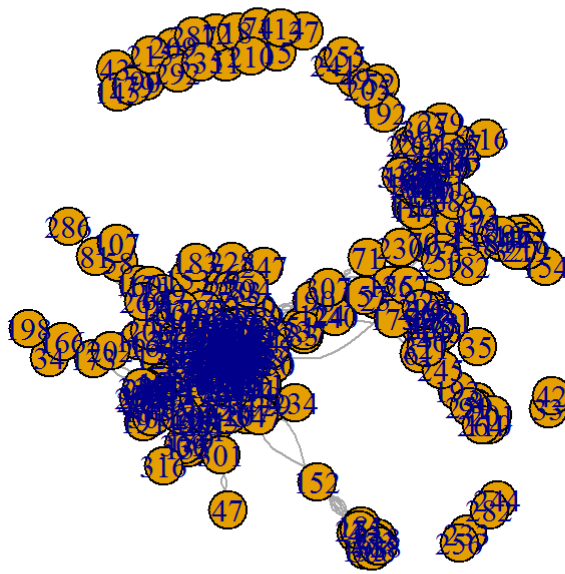
```
degree(g2, "198")
```

```
## 198
## 1
```

```
degree(g2)
```

```
## 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18
## 16 9 16 9 12 5 19 7 56 9 0 0 30 14 0 8 12 0
## 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36
## 15 14 64 10 16 15 68 67 4 12 12 16 22 5 1 1 1 10
## 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54
## 0 8 14 43 23 1 0 5 11 4 1 21 3 10 6 1 30 7
## 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72
## 16 77 14 3 18 7 2 25 5 6 11 14 75 8 9 1 2 23
## 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90
## 9 0 13 2 5 8 11 22 2 33 6 12 13 5 12 19 7 1
## 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108
## 7 20 7 21 5 8 2 48 12 8 18 5 15 31 13 7 2 12
## 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126
## 36 4 13 2 39 0 20 16 5 35 61 3 11 62 17 3 3 6
## 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144
## 15 27 6 15 6 15 17 18 9 21 15 1 8 10 27 42 11 14
## 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162
## 1 9 5 19 13 10 6 4 1 1 2 11 2 24 13 1 24 7
## 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178 179 180
## 5 2 10 3 6 10 37 45 7 40 5 3 16 13 10 12 2 19
## 181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 197 198
## 9 2 1 17 25 43 15 47 6 3 2 4 4 18 8 12 15 1
## 199 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216
## 46 56 3 3 56 21 1 3 2 6 0 0 29 17 38 16 0 1
## 217 218 219 220 221 222 223 224 225 226 227 228 229 230 231 232 233 234
## 7 8 5 3 7 10 26 27 9 13 14 2 5 8 20 24 1 1
## 235 236 237 238 239 240 241 242 243 244 245 246 247 248 249 250 251 252
## 4 36 6 22 58 2 1 23 7 1 4 13 2 20 23 4 13 64
## 253 254 255 256 257 258 259 260 261 262 263 264 265 266 267 268 269 270
## 2 16 1 1 17 14 7 7 37 3 6 4 26 17 1 10 5 3
## 271 272 273 274 275 276 277 278 279 280 281 282 283 284 285 286 287 288
## 72 44 8 13 9 17 64 9 1 42 15 1 4 15 46 1 0 3
## 289 290 291 292 293 294 295 296 297 298 299 300 301 302 303 304 305 306
## 3 13 35 0 2 2 9 6 24 10 19 6 2 19 20 54 1 8
## 307 308 309 310 311 312 313 314 315 316 317 318 319 320 321 322 323 324
## 3 23 9 12 6 25 36 12 55 1 6 10 7 20 2 71 38 25
## 325 326 327 328 329 330 331 332 333 334 335 336 337 338 339 340 341 342
## 38 18 3 8 29 15 19 42 7 27 0 2 8 6 26 5 11 33
## 343 344 345 346 347
## 17 8 15 26 6
```

```
astrocollab <- upgrade_graph(g)
plot(astrocollab)
```



## Question 4

### Explore 10 functions

The function `eccentricity()` calculates the shortest path distance from the farthest other node in the graph, for each node.

```
#find eccentricity of vertices, we are using head here so the markdown file does not get too long
head(eccentricity(g2))
```

```
## 1 2 3 4 5 6
## 8 9 8 9 8 9
```

The function `dfs()`, performs a depth-first search from the root node, in this case 1. This is an algorithm to traverse the graph. `bfs()` is another function that employs an algorithm, breadth-first search, this algorithm attempts to go to each edge.

```
#dfs with node 1 as root
dfs(g2, 1)
```

```
## $root
## [1] 0
##
## $neimode
## [1] "out"
##
## $order
## + 347/347 vertices, named:
##   [1] 1  48 30 9  3 25 21 13 26 40 29 16 82 56 55 67 10
##  [18] 142 31 7  22 87 5 122 45 104 98 59 118 65 203 50 109 119
##  [35] 27 54 53 24 57 80 88 73 126 260 160 170 62 96 133 141 38
##  [52] 117 77 231 106 169 103 136 120 247 277 39 69 105 148 113 66 134
##  [69] 132 72 165 121 206 178 186 123 200 75 85 156 188 79 185 271 63
##  [86] 261 172 128 150 64 100 163 173 34 166 198 202 329 130 191 204 92
## [103] 94 101 180 187 194 196 249 213 161 199 211 222 238 239 60 158 168
## [120] 129 291 208 285 146 313 84 51 23 61 193 8 91 110 259 201 245
## [137] 264 83 237 99 68 143 35 46 175 19 17 41 14 20 2 115 28
## [154] 116 140 137 32 93 111 44 312 144 149 162 326 214 230 70 71 307
## + ... omitted several vertices
##
## $order.out
## NULL
##
## $father
## NULL
##
## $dist
## NULL
```

```
#bfs with node 1 as root
bfs(g2, 1)
```

```
## $root
## [1] 1
##
## $neimode
## [1] "out"
##
## $order
## + 347/347 vertices, named:
## [1] 1 48 53 54 73 88 92 119 126 133 194 236 280 299 315 322 346
## [18] 30 57 80 130 180 199 203 271 302 320 330 332 24 94 101 146 191
## [35] 196 204 213 242 248 249 254 260 266 317 27 313 329 25 331 21 56
## [52] 106 164 178 186 303 336 187 9 13 26 39 50 64 67 79 82 98
## [69] 100 105 109 113 122 125 128 132 148 150 163 170 171 176 185 188 189
## [86] 200 208 217 229 239 252 261 269 277 285 297 318 323 324 325 339 342
## [103] 40 62 96 141 183 224 232 276 69 84 121 142 169 257 272 304 314
## [120] 3 31 117 153 231 290 291 300 5 7 87 136 158 211 223 246 288
## [137] 345 38 45 60 75 85 104 118 161 207 221 250 308 341 127 184 108
## [154] 173 72 134 172 212 222 238 265 298 29 55 59 65 268 270 334 338
## + ... omitted several vertices
##
## $rank
## NULL
##
## $father
## NULL
##
## $pred
## NULL
##
## $succ
## NULL
##
## $dist
## NULL
```

`count_triangles()` attempts to count how many triangles a node is a part of. A triangle, is a part of a graph that has a cycle with 3 nodes and 3 edges.

```
#count triangles a vertex is a part of
count_triangles(g2)
```



```
## [1] 41 31 70 30 14 9 63 12 578 28 0 0 273 64 0 16 45
## [18] 0 19 58 662 16 7 93 609 870 5 48 24 52 88 10 0 0
## [35] 0 43 0 5 38 340 106 0 0 10 37 6 0 55 0 21 12
## [52] 0 148 9 97 970 41 1 115 12 0 145 10 14 22 78 955 22
## [69] 20 0 1 144 15 0 56 1 4 28 51 110 0 201 12 21 46
## [86] 10 38 45 12 0 12 143 17 133 8 6 0 569 38 14 124 10
## [103] 51 271 48 5 1 50 317 6 38 1 380 0 92 74 2 303 482
## [120] 0 20 691 89 0 1 10 73 198 13 28 15 33 73 103 36 81
## [137] 49 0 27 39 183 437 29 60 0 12 9 61 58 21 13 3 0
## [154] 0 0 24 0 83 44 0 140 17 3 0 23 1 13 28 272 443
## [171] 11 337 1 2 42 53 32 24 0 125 30 0 0 80 150 428 88
## [188] 467 14 0 1 0 3 123 28 44 74 0 464 637 3 1 628 115
## [205] 0 0 1 12 0 0 232 90 187 61 0 0 16 28 6 3 17
## [222] 31 227 170 29 61 43 1 3 2 75 162 0 0 4 237 12 159
## [239] 658 0 0 142 11 0 3 41 0 86 150 4 58 775 0 107 0
## [256] 0 60 37 12 4 297 3 14 6 199 118 0 40 2 2 945 306
## [273] 28 38 30 98 657 27 0 380 74 0 2 69 422 0 0 2 2
## [290] 62 205 0 1 0 15 14 192 42 111 10 0 124 102 521 0 28
## [307] 1 108 36 30 5 114 298 21 432 0 5 19 12 81 1 675 321
## [324] 94 408 96 3 28 69 84 81 338 15 166 0 1 21 8 65 6
## [341] 40 291 80 10 63 160 11
```

`is.directed()` checks to see if a graph is directed. `is.weighted()` checks to see if a graph has weights.  
`is.connected()` checks to see if a graph is connected (i.e. has a path between every pair of vertices).

```
#is the graph directed
is.directed(g2)
```

```
## [1] FALSE
```

```
#is the graph weighted
is.weighted(g2)
```

```
## [1] FALSE
```

```
#is the graph connected
is.connected(g2)
```

```
## [1] FALSE
```

`head()` retrieves the first few results of a function. `closeness()` computes the closeness centrality, how many steps to get to every other node from another node.

```
#get closeness centrality of vertices, we are using head here so the markdown file does not get too long
head(closeness(g2))
```

```
##           1           2           3           4           5
## 0.0001108402 0.0001047230 0.0001107052 0.0001050420 0.0001104362
##           6
## 0.0001028807
```

`count_multiple()` counts the multiple edges a node has, edges that have the same head and tail vertices.

```
#find loop edges, we are using head here so the markdown file does not get too Long
head(count_multiple(g2))
```

```
## [1] 1 1 1 1 1 1
```

`components()` finds connected components of a graph.

```
#fine components of graph
components(g2)
```

```

## $membership
## 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18
## 1 1 1 1 1 1 1 1 1 1 2 3 1 1 4 1 1 5
## 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36
## 1 1 1 1 1 1 1 1 1 1 1 1 1 1 6 1 1 1
## 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54
## 7 1 1 1 1 6 8 1 1 1 1 1 1 1 1 1 1 1
## 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72
## 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90
## 1 9 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 10
## 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108
## 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126
## 1 1 1 1 1 11 1 1 1 1 1 1 1 1 1 1 1 1
## 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144
## 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162
## 10 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178 179 180
## 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 10 1
## 181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 197 198
## 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## 199 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216
## 1 1 1 1 1 1 1 1 1 1 1 12 13 1 1 1 1 14 1
## 217 218 219 220 221 222 223 224 225 226 227 228 229 230 231 232 233 234
## 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 15 1
## 235 236 237 238 239 240 241 242 243 244 245 246 247 248 249 250 251 252
## 1 1 1 1 1 1 1 1 1 1 16 1 1 1 1 1 1 1
## 253 254 255 256 257 258 259 260 261 262 263 264 265 266 267 268 269 270
## 1 1 1 15 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## 271 272 273 274 275 276 277 278 279 280 281 282 283 284 285 286 287 288
## 1 1 1 1 1 1 1 1 1 1 1 16 1 1 1 1 17 1
## 289 290 291 292 293 294 295 296 297 298 299 300 301 302 303 304 305 306
## 1 1 1 18 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## 307 308 309 310 311 312 313 314 315 316 317 318 319 320 321 322 323 324
## 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
## 325 326 327 328 329 330 331 332 333 334 335 336 337 338 339 340 341 342
## 1 1 1 1 1 1 1 1 1 1 19 1 1 1 1 1 1 1
## 343 344 345 346 347
## 1 1 1 1 1
##
## $csize
## [1] 324 1 1 1 1 2 1 1 1 3 1 1 1 1 2 2 1
## [18] 1 1
##
## $no
## [1] 19

```

## Question 5

```
#determine central person
ac1 = alpha centrality(g)
tail(sort(ac1),5)
```

```
##      153      44      343      19      138
## 6.747615 6.901731 7.802863 9.675359 20.350718
```

```
#longest path, distances creates the distance table, which.max picks out highest non-inf value
which.max(distances(g2))
```

```
## [1] 11
```

```
#largest clique, we are using head here so the markdown file does not get too long
head(largest.cliques(g))
```

```
## [[1]]
## + 15/347 vertices, named:
## [1] 56 271 26 67 323 122 285 277 170 188 239 200 142 186 322
##
## [[2]]
## + 15/347 vertices, named:
## [1] 56 271 26 67 323 122 285 277 170 188 239 200 25 186 322
##
## [[3]]
## + 15/347 vertices, named:
## [1] 56 271 26 67 323 122 285 277 170 188 9 200 142 186 322
##
## [[4]]
## + 15/347 vertices, named:
## [1] 56 271 26 67 323 122 285 277 170 188 9 200 25 186 322
##
## [[5]]
## + 15/347 vertices, named:
## [1] 56 271 26 67 323 122 21 200 277 170 142 186 188 322 239
##
## [[6]]
## + 15/347 vertices, named:
## [1] 56 271 26 67 323 122 21 200 277 170 142 186 188 322 9
```

```
# Hence, the largest click is 15
```

```
#ego, we are using head here so the markdown file does not get too long
head(ego(g2, gorder(g2), V(g2)))
```

```

## [[1]]
## + 324/347 vertices, named:
## [1] 1 48 53 54 73 88 92 119 126 133 194 236 280 299 315 322 346
## [18] 30 57 80 130 180 199 203 271 302 320 330 332 24 94 101 146 191
## [35] 196 204 213 242 248 249 254 260 266 317 27 313 329 25 331 21 56
## [52] 106 164 178 186 303 336 187 9 13 26 39 50 64 67 79 82 98
## [69] 100 105 109 113 122 125 128 132 148 150 163 170 171 176 185 188 189
## [86] 200 208 217 229 239 252 261 269 277 285 297 318 323 324 325 339 342
## [103] 40 62 96 141 183 224 232 276 69 84 121 142 169 257 272 304 314
## [120] 3 31 117 153 231 290 291 300 5 7 87 136 158 211 223 246 288
## [137] 345 38 45 60 75 85 104 118 161 207 221 250 308 341 127 184 108
## [154] 173 72 134 172 212 222 238 265 298 29 55 59 65 268 270 334 338
## + ... omitted several vertices
##
## [[2]]
## + 324/347 vertices, named:
## [1] 2 20 115 116 149 226 312 326 333 343 14 41 44 111 162 214 17
## [18] 19 28 137 140 144 192 220 262 23 151 243 305 310 93 230 337 279
## [35] 289 89 112 138 174 175 227 293 319 32 167 49 52 205 51 61 83
## [52] 99 124 155 190 237 240 245 267 216 70 71 97 253 307 6 95 147
## [69] 219 327 46 68 86 102 143 177 225 263 277 278 296 321 131 241 255
## [86] 25 31 84 193 157 170 96 229 222 8 91 259 182 40 154 35 9
## [103] 10 13 21 22 26 39 50 55 56 57 67 98 104 105 109 113 118
## [120] 119 120 122 130 132 134 142 159 161 168 169 172 186 188 200 203 204
## [137] 208 213 239 248 252 271 272 280 285 290 291 294 304 308 311 315 322
## [154] 323 324 325 332 334 339 342 3 65 69 72 73 76 79 88 94 103
## + ... omitted several vertices
##
## [[3]]
## + 324/347 vertices, named:
## [1] 3 9 25 26 67 72 85 122 142 170 188 200 228 274 280 283 323
## [18] 21 30 56 66 69 75 79 105 113 119 128 133 134 141 148 156 161
## [35] 169 176 185 186 199 203 224 231 232 252 258 271 272 276 277 285 291
## [52] 295 297 304 315 322 329 334 341 342 31 39 40 51 65 73 76 83
## [69] 84 88 94 98 103 104 130 158 221 236 237 239 246 257 270 288 290
## [86] 325 331 332 336 13 55 62 109 118 123 172 212 223 248 265 298 308
## [103] 313 10 45 82 136 196 213 261 303 324 344 345 132 165 5 235 251
## [120] 281 284 124 211 250 260 268 208 96 1 117 121 153 100 108 127 159
## [137] 184 197 48 178 59 60 63 207 222 238 50 27 54 64 125 146 150
## [154] 163 171 189 217 229 269 318 339 183 38 87 314 106 22 29 338 77
## + ... omitted several vertices
##
## [[4]]
## + 324/347 vertices, named:
## [1] 4 78 152 181 195 218 273 275 306 328 339 7 22 31 38 65 87
## [18] 103 119 129 136 146 148 158 161 168 246 260 277 291 313 315 322 334
## [35] 340 347 213 304 308 185 324 21 25 51 67 83 84 109 122 142 200
## [52] 237 252 280 338 117 141 178 248 332 13 82 118 203 261 297 314 5
## [69] 56 98 169 172 211 271 285 323 1 9 26 27 39 48 50 54 64
## [86] 79 100 105 113 125 128 132 150 163 170 171 176 188 189 199 208 217
## [103] 229 239 269 318 325 329 331 342 120 156 53 317 224 272 40 60 232
## [120] 242 62 258 223 126 160 206 10 55 57 104 130 134 159 175 186 204
## [137] 290 294 311 72 231 63 222 238 265 80 94 121 133 236 249 257 288

```

```
## [154] 302 303 345 30 45 75 85 88 207 221 250 276 341 66 123 165 96
## + ... omitted several vertices
##
## [[5]]
## + 324/347 vertices, named:
## [1] 5 87 122 156 158 169 180 187 204 213 235 315 316 7 22 136 161
## [18] 246 291 308 322 339 3 9 21 25 26 31 45 55 56 62 66 67
## [35] 98 104 109 113 119 123 128 141 142 170 176 186 188 200 203 224 232
## [52] 236 239 248 251 252 261 271 272 274 276 277 280 281 284 285 297 303
## [69] 304 323 325 332 342 344 345 85 258 295 40 60 82 132 168 242 317
## [86] 10 103 106 121 125 165 185 257 318 334 24 48 53 80 92 94 101
## [103] 194 196 249 254 266 299 302 346 57 130 329 330 30 96 178 231 324
## [120] 340 1 105 133 199 211 223 288 313 38 65 129 347 120 146 39 118
## [137] 314 72 208 172 338 75 88 126 207 221 250 260 290 341 148 152 228
## [154] 283 69 79 134 13 108 127 159 184 197 212 51 73 76 83 84 237
## + ... omitted several vertices
##
## [[6]]
## + 324/347 vertices, named:
## [1] 6 89 95 147 219 319 19 327 154 17 41 112 115 138 174 175 214
## [18] 227 289 293 312 343 111 116 137 140 144 310 326 14 20 28 44 93
## [35] 151 226 230 243 337 2 149 192 220 262 23 46 68 86 99 102 143
## [52] 177 225 263 277 278 296 321 333 131 162 305 279 32 167 70 71 97
## [69] 253 307 216 49 52 205 51 61 83 124 155 190 237 240 245 267 35
## [86] 9 10 13 21 22 25 26 31 39 40 50 55 56 57 67 98 104
## [103] 105 109 113 118 119 120 122 130 132 134 142 159 161 168 169 170 172
## [120] 186 188 200 203 204 208 213 239 248 252 271 272 280 285 290 291 294
## [137] 304 308 311 315 322 323 324 325 332 334 339 342 182 241 255 84 193
## [154] 157 96 229 222 8 91 259 3 30 66 69 72 75 79 85 128 133
## + ... omitted several vertices
```

```
# power centrality, we are using head here so the markdown file does not get too long
head(power_centrality(g, nodes = V(g)))
```

```
##           1           2           3           4           5           6
## -0.04147431  0.01926547 -0.68186769 -0.48702208 -0.53447243 -1.79416816
```