

ALGEBRAIC GEOMETRY 2022–2023

| | DAY | TIME | WHERE | TYPE | TOPICS |
|------------------|------------------|---------------|------------------|-----------|--|
| LECTURE 1 | 11 October 2022 | 16:00 - 18:00 | Room 134 (SISSA) | Theory | Presheaves, sheaves, morphisms, constant presheaves, sheaf condition via equalisers. |
| LECTURE 2 | 13 October 2022 | 16:00 - 18:00 | Room 134 (SISSA) | Theory | Stalks, compatible germs. Surjectivity of maps of sheaves. Characterisation of isomorphisms via stalks (proof). Existence of sheafification (proof). |
| LECTURE 3 | 18 October 2022 | 9:00 - 11:00 | Room 136 (SISSA) | Theory | Skyscrapers. Exact sequences of sheaves. Defining sheaves on basic open sets. Direct image sheaf. Supports of sheaves and sections. |
| LECTURE 4 | 18 October 2022 | 16:00 - 18:00 | Room 128 (SISSA) | Theory | Inverse image sheaf and the adjunction with direct image. Locally ringed spaces, their morphisms. Closed immersions = ideal sheaves. |
| LECTURE 5 | 20 October 2022 | 16:00 - 18:00 | Room 137 (SISSA) | Theory | Spectrum of a ring, Zariski topology. Closed points. First examples of $\text{Spec}(A)$. |
| LECTURE 6 | 25 October 2022 | 9:00 - 11:00 | Room 136 (SISSA) | Theory | Localisation of a module. Structure sheaf of $\text{Spec}(A)$. Definition of affine schemes. Schemes. Quasicompact, connected, irreducible schemes. |
| LECTURE 7 | 25 October 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Exercises | Local ring of $\text{Spec}(A)$ at a prime ideal. Connectedness and idempotents. Localisation. Residue field of local ring at a maximal ideal of a ring. |
| LECTURE 8 | 27 October 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Theory | Definition of affine schemes and schemes. Morphisms of affine schemes. Spec is an equivalence $\text{Rings}^{\text{op}} \rightarrow \text{Aff}$. |
| LECTURE 9 | 8 November 2022 | 9:00 - 11:00 | Room 136 (SISSA) | Theory | |
| LECTURE 10 | 8 November 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Theory | |
| LECTURE 11 | 10 November 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Exercises | |
| LECTURE 12 | 15 November 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Theory | |
| LECTURE 13 | 22 November 2022 | 16:00 - 18:00 | Room 134 (SISSA) | Theory | |
| LECTURE 14 | 24 November 2022 | 16:00 - 18:00 | Room 134 (SISSA) | Theory | |
| LECTURE 15 | 29 November 2022 | 9:00 - 11:00 | Room 136 (SISSA) | Exercises | |
| LECTURE 16 | 29 November 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Theory | |
| LECTURE 17 | 1 December 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Theory | |
| LECTURE 18 | 6 December 2022 | 16:00 - 18:00 | Room 134 (SISSA) | Theory | |
| LECTURE 19 | 13 December 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Exercises | |
| LECTURE 20 | 15 December 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Theory | |
| LECTURE 21 | 20 December 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Theory | |
| LECTURE 22 | 22 December 2022 | 16:00 - 18:00 | Room 005 (SISSA) | Theory | |
| LECTURE 23 | 10 January 2023 | 16:00 - 18:00 | Room 005 (SISSA) | Exercises | |
| LECTURE 24 | 12 January 2023 | 16:00 - 18:00 | Room 005 (SISSA) | Exercises | |
| LECTURE 25 (PHD) | | | Room 005 (SISSA) | Theory | |
| LECTURE 26 (PHD) | | | Room 005 (SISSA) | Theory | |
| LECTURE 27 (PHD) | | | Room 005 (SISSA) | Theory | |
| LECTURE 28 (PHD) | | | Room 005 (SISSA) | Theory | |
| LECTURE 29 (PHD) | | | Room 005 (SISSA) | Theory | |
| LECTURE 30 (PHD) | | | Room 005 (SISSA) | Theory | |