Circuit for batching Groth16 proofs

May 10, 2019

For reference, recall the Groth16 verification equation.

$$e(\pi_A, \pi_B) = \epsilon(\pi_C, [\delta]_2) \cdot \mathsf{PI}$$

Where PI is an element in \mathbb{G}_t derived by the verifier from the public input. Specificially,

$$\mathsf{PI} = \left[\alpha \beta + K_0 + \sum_{i=1}^{\ell} a_i \cdot K_i \right]_t$$

where (a_1, \ldots, a_n) is the public input, and $K_i = \beta u_i(x) + \alpha v_i(x) + w_i(x)$.

We move the second pairing to the LHS to receive

$$e(\pi_A, \pi_B) \cdot \epsilon(-\pi_C, [\delta]_2) = \mathsf{PI}$$

We use ML to denote a miller loop and FE to denote a multiexponetiation The private input for the circuit is a set of m Groth16 proofs $S := \{\pi_{A,i}, \pi_{B,i}, \pi_{C,i}\}_{i \in [m]}$

The public inputs of the circuit are

- 1. P the alleged pedersen hash of all proof elements.
- 2. F the alleged correct randomized combination of pairings of proof elements.
- 3. $r = \mathsf{Blake}(\mathsf{P})$, interperted as an element of \mathbb{F} .

The verifier computes r from P outside of the circuit, and checks outside of the circuit that

$$F = \prod_{i \in m} \mathsf{PI}_i^{r^i}$$

The circut computes

- 1. $M := \prod_{i \in [m]} \mathsf{ML}(\pi_{\mathsf{A},\mathsf{i}}, \pi_{\mathsf{B},\mathsf{i}}).$
- 2. $C' := -\sum_{i \in [m]} r^i \cdot \pi_{C,i}$
- 3. $C = ML(C', [\delta]_2)$

The circuit checks that

- 1. $F = \mathsf{FE}(M \cdot C)$.
- 2. P = ped(S).

References