RNA-seq differential analysis with CummeRbund

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Install the CummeRbund package

Analysis, exploration, manipulation, and visualization of Cufflinks high-throughput sequencing data

```
#if (!require("BiocManager", quietly = TRUE))
# install.packages("BiocManager")

#BiocManager::install("cummeRbund")
```

Load the CummeRbund package

```
library(cummeRbund)
```

Create a CummeRbund database from the Cuffdiff output

```
print(readCufflinks)
```

```
## function (dir = getwd(), dbFile = "cuffData.db", gtfFile = NULL,
##
       runInfoFile = "run.info", repTableFile = "read_groups.info",
##
       geneFPKM = "genes.fpkm_tracking", geneDiff = "gene_exp.diff",
       geneCount = "genes.count_tracking", geneRep = "genes.read_group_tracking",
##
       isoformFPKM = "isoforms.fpkm_tracking", isoformDiff = "isoform_exp.diff",
##
       isoformCount = "isoforms.count_tracking", isoformRep = "isoforms.read_group_tracking",
##
       TSSFPKM = "tss_groups.fpkm_tracking", TSSDiff = "tss_group_exp.diff",
##
       TSSCount = "tss_groups.count_tracking", TSSRep = "tss_groups.read_group_tracking",
##
       CDSFPKM = "cds.fpkm_tracking", CDSExpDiff = "cds_exp.diff",
##
##
       CDSCount = "cds.count_tracking", CDSRep = "cds.read_group_tracking",
       CDSDiff = "cds.diff", promoterFile = "promoters.diff", splicingFile = "splicing.diff",
##
       varModelFile = "var_model.info", driver = "SQLite", genome = NULL,
##
       rebuild = FALSE, verbose = FALSE, ...)
##
## {
##
       dbFile = file.path(dir, dbFile)
       runInfoFile = file.path(dir, runInfoFile)
##
##
       repTableFile = file.path(dir, repTableFile)
       geneFPKM = file.path(dir, geneFPKM)
##
##
       geneDiff = file.path(dir, geneDiff)
       geneCount = file.path(dir, geneCount)
##
##
       geneRep = file.path(dir, geneRep)
       isoformFPKM = file.path(dir, isoformFPKM)
##
```

```
isoformDiff = file.path(dir, isoformDiff)
##
##
       isoformCount = file.path(dir, isoformCount)
##
       isoformRep = file.path(dir, isoformRep)
       TSSFPKM = file.path(dir, TSSFPKM)
##
##
       TSSDiff = file.path(dir, TSSDiff)
##
       TSSCount = file.path(dir, TSSCount)
##
       TSSRep = file.path(dir, TSSRep)
       CDSFPKM = file.path(dir, CDSFPKM)
##
##
       CDSExpDiff = file.path(dir, CDSExpDiff)
##
       CDSCount = file.path(dir, CDSCount)
##
       CDSRep = file.path(dir, CDSRep)
       CDSDiff = file.path(dir, CDSDiff)
##
##
       promoterFile = file.path(dir, promoterFile)
##
       splicingFile = file.path(dir, splicingFile)
##
       varModelFile = file.path(dir, varModelFile)
##
       if (!file.exists(dbFile) || rebuild == TRUE) {
##
           write(paste("Creating database ", dbFile, sep = ""),
##
               stderr())
##
           dbConn <- createDB_noIndex(dbFile)</pre>
##
           if (file.exists(runInfoFile)) {
##
               loadRunInfo(runInfoFile, dbConn)
##
##
           if (file.exists(repTableFile)) {
               loadRepTable(repTableFile, dbConn)
##
           }
##
##
           if (file.exists(varModelFile)) {
##
               loadVarModelTable(varModelFile, dbConn)
##
##
           if (!is.null(gtfFile)) {
##
               if (!is.null(genome)) {
##
                    .loadGTF(gtfFile, genome, dbConn)
##
               }
##
##
                   stop("'genome' cannot be NULL if you are supplying a .gtf file!")
##
##
           }
##
           loadGenes(geneFPKM, geneDiff, promoterFile, countFile = geneCount,
##
               replicateFile = geneRep, dbConn)
##
           loadIsoforms(isoformFPKM, isoformDiff, isoformCount,
##
               isoformRep, dbConn)
##
           loadTSS(TSSFPKM, TSSDiff, splicingFile, TSSCount, TSSRep,
##
               dbConn)
           loadCDS(CDSFPKM, CDSExpDiff, CDSDiff, CDSCount, CDSRep,
##
##
               dbConn)
           write("Indexing Tables...", stderr())
##
##
           createIndices(dbFile, verbose = verbose)
##
##
       dbConn <- dbConnect(dbDriver(driver), dbFile)</pre>
##
       return(new("CuffSet", DB = dbConn, genes = new("CuffData",
           DB = dbConn, tables = list(mainTable = "genes", dataTable = "geneData",
##
##
               expDiffTable = "geneExpDiffData", featureTable = "geneFeatures",
               countTable = "geneCount", replicateTable = "geneReplicateData"),
##
##
           filters = list(), type = "genes", idField = "gene_id"),
           isoforms = new("CuffData", DB = dbConn, tables = list(mainTable = "isoforms",
##
```

```
##
               dataTable = "isoformData", expDiffTable = "isoformExpDiffData",
               featureTable = "isoformFeatures", countTable = "isoformCount",
##
               replicateTable = "isoformReplicateData"), filters = list(),
##
               type = "isoforms", idField = "isoform_id"), TSS = new("CuffData",
##
##
               DB = dbConn, tables = list(mainTable = "TSS", dataTable = "TSSData",
                   expDiffTable = "TSSExpDiffData", featureTable = "TSSFeatures",
##
                   countTable = "TSSCount", replicateTable = "TSSReplicateData"),
##
               filters = list(), type = "TSS", idField = "TSS_group_id"),
##
##
           CDS = new("CuffData", DB = dbConn, tables = list(mainTable = "CDS",
               dataTable = "CDSData", expDiffTable = "CDSExpDiffData",
##
##
               featureTable = "CDSFeatures", countTable = "CDSCount",
               replicateTable = "CDSReplicateData"), filters = list(),
##
##
               type = "CDS", idField = "CDS_id"), promoters = new("CuffDist",
               DB = dbConn, table = "promoterDiffData", type = "promoter",
##
               idField = "gene_id"), splicing = new("CuffDist",
##
##
               DB = dbConn, table = "splicingDiffData", type = "splicing",
               idField = "TSS_group_id"), relCDS = new("CuffDist",
##
##
               DB = dbConn, table = "CDSDiffData", type = "relCDS",
##
               idField = "gene_id")))
## }
## <bytecode: 0x00000004ee8a9e0>
## <environment: namespace:cummeRbund>
cuff_data <- readCufflinks(dir = '../cuffdiff/diff_out/')</pre>
cuff_data@genes # or genes(cuff_data)
## CuffData instance with:
     37178 features and 2 samples
getLevels(cuff_data)
## [1] "T" "U"
replicates(cuff_data)
##
                                                file sample_name replicate rep_name
## 1 ../tophat/T_SRR5272677_thout/accepted_hits.bam
                                                               Τ
                                                                          0
                                                                                 T_0
## 2 ../tophat/T_SRR5272678_thout/accepted_hits.bam
                                                               Τ
                                                                          1
                                                                                 T_1
                                                               Τ
                                                                          2
## 3 ../tophat/T_SRR5272679_thout/accepted_hits.bam
                                                                                 T_2
                                                               U
                                                                          0
## 4 ../tophat/U_SRR5272674_thout/accepted_hits.bam
                                                                                 U_0
## 5 ../tophat/U_SRR5272675_thout/accepted_hits.bam
                                                               U
                                                                          1
                                                                                 U_1
## 6 ../tophat/U_SRR5272676_thout/accepted_hits.bam
                                                                          2
                                                                                 U_2
     total_mass norm_mass internal_scale external_scale
## 1
       51717000 52101400
                                1.054330
                                                       1
       58200700 52101400
## 2
                                1.146160
                                                       1
## 3
       41277800 52101400
                                0.789822
                                                       1
## 4
       44710200 52101400
                                0.824518
                                                       1
## 5
       54362200 52101400
                                1.009880
                                                       1
## 6
       67322000 52101400
                                1.282890
```

cuff_data

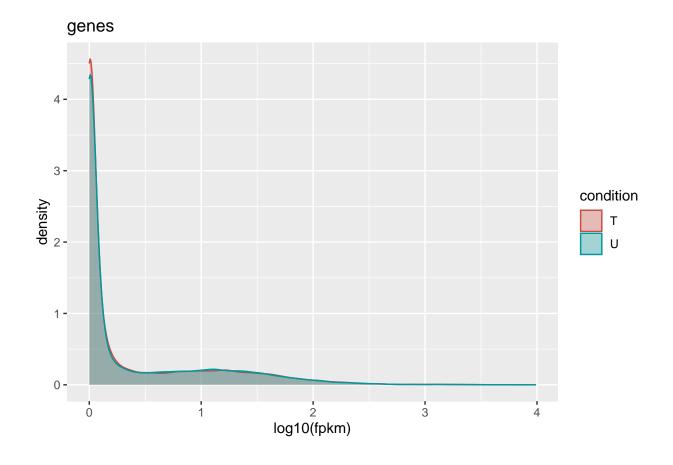
```
## CuffSet instance with:
##
     2 samples
##
     37178 genes
##
     0 isoforms
     0 TSS
##
##
     0 CDS
##
     0 promoters
##
     0 splicing
     0 relCDS
##
```

Plot the distribution of expression levels for all genes for each sample/condition

T - treated U - untreated

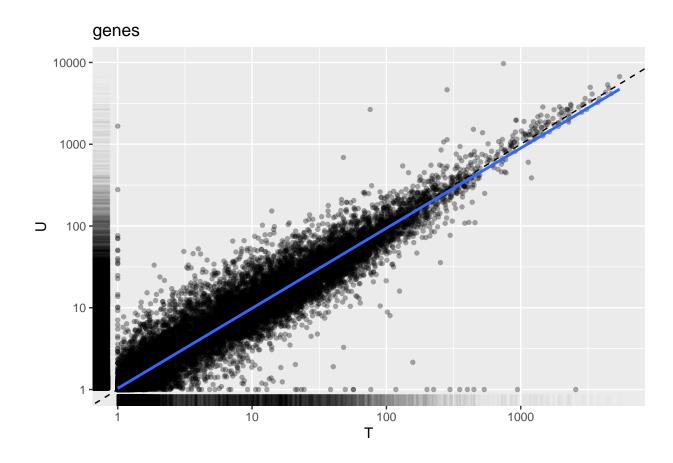
 ${\tt csDensity} \ {\tt method} \ {\tt creates} \ {\tt a} \ {\tt smoothed} \ {\tt density} \ {\tt plot}, \ {\tt by} \ {\tt sample}, \ {\tt for} \ {\tt log10} \ {\tt FPKM} \ {\tt values} \ {\tt from} \ {\tt a} \ {\tt cuffdiff} \ {\tt run} \ {\tt FPKM} \ {\tt -} \ {\tt fragments} \ {\tt per} \ {\tt kilobase} \ {\tt of} \ {\tt transcript} \ {\tt per} \ {\tt million} \ {\tt fragments} \ {\tt mapped}$

csDensity(cuff_data@genes, pseudocount=1.0)



Compare the expression of each gene in the two conditions

csScatter method creates a scatter plot comparing the FPKM values from the two samples in a cuffdiff run



Inspect differentially expressed genes

 ${\tt csVolcano}\ {\rm method}\ {\rm creates}\ {\rm a}\ {\rm volcano}\ {\rm plot}\ {\rm of}\ {\rm log}\ {\rm fold}\ {\rm change}\ {\rm in}\ {\rm expression}\ {\rm vs}\ {\rm significance}\ ({\tt -log(pval)})\ {\rm for}\ {\rm the}\ {\rm two}\ {\rm samples}\ {\rm in}\ {\rm a}\ {\rm cuffdiff}\ {\rm run}$

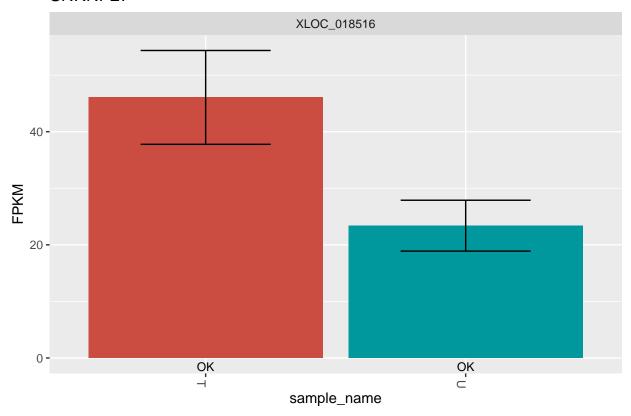
```
gene_diff_data <- diffData(cuff_data@genes, 'T', 'U')</pre>
gene_diff_data
## [1] gene_id
                          gene_id
                                             sample_1
                                                               sample_2
## [5] status
                          value_1
                                             value_2
                                                               log2_fold_change
## [9] test_stat
                          p_value
                                                               significant
                                             q_value
## <0 rows> (or 0-length row.names)
\#csVolcano\left(cuff\_data@genes, \ 'T', \ 'U', \ alpha=0.05, \ showSignificant=T\right)
# The call to csVolcano fails with
#Error in `$<-.data.frame`(`*tmp*`, "significant", value = "no") :</pre>
#replacement has 1 row, data has 0
```

OOPS! No significantly differential expressed genes found?! Figuring out the issue ...

Explore expression levels for some gene

```
mygene <- getGene(cuff_data, 'SNRNP27')
expressionBarplot(mygene)</pre>
```

SNRNP27



Look at the gene_exp.diff and iso_exp.diff files generated by cuffdiff
Issue found

```
gene_expr_diff <- read.delim2('../cuffdiff/diff_out/gene_exp.diff')
head(gene_expr_diff)</pre>
```

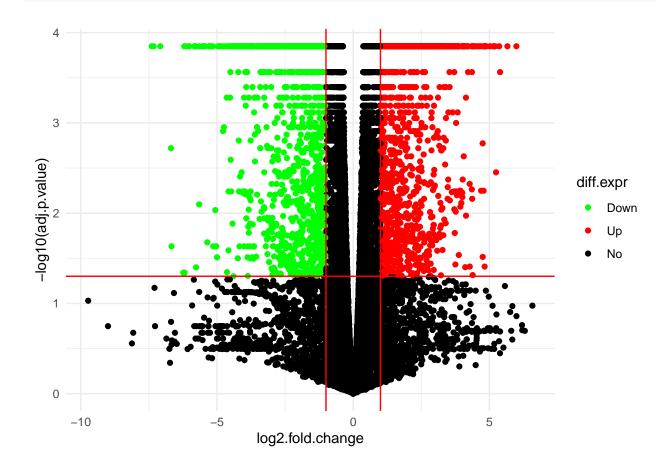
```
test_id
                     gene_id
                                     gene
                                                       locus sample_1 sample_2
## 1 XLOC_000001 XLOC_000001
                                                                 TRUE
                                  DDX11L1
                                            chr1:11873-29370
## 2 XLOC_000002 XLOC_000002
                                MIR1302-2
                                            chr1:30365-30503
                                                                 TRUE
                                                                             U
## 3 XLOC_000003 XLOC_000003
                                            chr1:69090-70008
                                                                 TRUE
                                                                             U
                                    OR4F5
## 4 XLOC_000004 XLOC_000004 LOC100287934 chr1:764864-810022
                                                                 TRUE
                                                                             U
## 5 XLOC_000005 XLOC_000005 LOC100287934 chr1:764864-810022
                                                                             U
                                                                 TRUE
## 6 XLOC_000006 XLOC_000006
                                  FAM87B chr1:817370-819834
                                                                 TRUE
                                                                             U
              value_1 value_2 log2.fold_change. test_stat p_value
##
     status
                                                                       q_value
```

```
## 1 NOTEST 0.186969 0.119911
                                        -0.640841
                                                                 1
                                                                            1
## 2 NOTEST
                   0
                                                         0
                             0
                                               0
                                                                 1
                                                                            1
## 3 NOTEST
                   0
                                               0
                                                         0
                                                                 1
                                        -2.67894 -1.96996 0.0027 0.00584503
## 4
             0.37868 0.059133
        OK
        OK 0.452312 0.572217
                                        0.339244 0.414573 0.4708
                                                                     0.545048
## 6 NOTEST 0.0173135 0.0384379
                                         1.15063
                                                         0
                                                                 1
    significant
## 1
## 2
             nο
## 3
             no
## 4
            yes
## 5
             no
## 6
             no
# Issue: the 'T' character label is the files is converted behind the scenes to logical TRUE
# in data.frame(s) OOPS!
# Lesson learned: Never use 'T' or 'F' to label conditions/samples
gene_expr_diff$sample_1 <- 'T' # replace logical TRUE interpretation for the original character label T
iso_expr_diff <- read.delim2('../cuffdiff/diff_out/isoform_exp.diff')</pre>
iso expr diff$sample 1 <- 'T'
dim(gene_expr_diff[gene_expr_diff$status == 'OK' & gene_expr_diff$significant == 'yes', ])
## [1] 10125
                14
head(gene_expr_diff[gene_expr_diff$status == 'OK' & gene_expr_diff$significant == 'yes', ])
                                                          locus sample_1 sample_2
          test_id
                     gene_id
                                     gene
## 4 XLOC_000004 XLOC_000004 LOC100287934
                                                                      Τ
                                                                                U
                                            chr1:764864-810022
## 11 XLOC_000011 XLOC_000011
                                  PLEKHN1
                                             chr1:966491-982093
                                                                      Т
                                                                                U
## 12 XLOC_000012 XLOC_000012
                                                                      Т
                                                                               U
                                    ISG15 chr1:1013466-1014540
## 13 XLOC_000013 XLOC_000013
                                     AGRN chr1:1020122-1056119
                                                                      Т
                                                                                U
## 14 XLOC 000014 XLOC 000014 LOC100288175 chr1:1059714-1067264
                                                                      Т
                                                                               IJ
## 16 XLOC 000016 XLOC 000016
                                        - chr1:1151935-1157301
                                                                      Τ
      status value_1 value_2 log2.fold_change. test_stat p_value
## 4
         OK 0.37868 0.059133
                                       -2.67894 -1.96996 0.0027 0.00584503
## 11
         OK 0.778295 1.58586
                                        1.02688
                                                  2.82337
                                                           5e-05 0.000141598
## 12
         OK 14.0938 24.7979
                                       0.815152 3.32746
                                                            5e-05 0.000141598
## 13
         OK 1.49063 5.56731
                                       1.90106 7.75049
                                                            5e-05 0.000141598
         OK 1.97514 3.18071
                                       0.687392
                                                  2.09137 0.00025 0.000645331
## 14
## 16
         OK 0.298565
                        1.018
                                        1.76962
                                                  5.66169
                                                            5e-05 0.000141598
     significant
##
## 4
             yes
## 11
              yes
## 12
             yes
## 13
             yes
## 14
             yes
## 16
             yes
dim(iso_expr_diff[iso_expr_diff$status == 'OK' & iso_expr_diff$significant == 'yes', ])
```

Volcano Plot

```
ged <- gene_expr_diff[gene_expr_diff$status == 'OK' &</pre>
                        !is.infinite(as.numeric(gene_expr_diff$log2.fold_change.)), ]
ged$log2.fold.change <- as.numeric(ged$log2.fold_change.)</pre>
ged$adj.p.value <- as.numeric(ged$q_value)</pre>
head(ged)
##
          test id
                                                           locus sample_1 sample_2
                      gene id
                                       gene
## 4
      XLOC 000004 XLOC 000004 LOC100287934
                                                                         Τ
                                              chr1:764864-810022
                                                                                  U
     XLOC_000005 XLOC_000005 LOC100287934
                                                                         Τ
                                              chr1:764864-810022
     XLOC_000007 XLOC_000007
                                                                         Т
                                                                                  U
                                 LINC01128
                                              chr1:827590-859446
## 10 XLOC_000010 XLOC_000010
                                                                         Т
                                                                                  U
                                    KLHL17
                                              chr1:960586-965897
## 11 XLOC_000011 XLOC_000011
                                                                         Т
                                                                                  U
                                    PLEKHN1
                                              chr1:966491-982093
## 12 XLOC_000012 XLOC_000012
                                                                         Τ
                                                                                  IJ
                                      ISG15 chr1:1013466-1014540
      status value_1 value_2 log2.fold_change. test_stat p_value
##
                                                                         q_value
## 4
          OK 0.37868 0.059133
                                         -2.67894 -1.96996 0.0027
                                                                     0.00584503
## 5
          OK 0.452312 0.572217
                                        0.339244 0.414573 0.4708
                                                                        0.545048
## 7
          OK 3.91537 3.83394
                                       -0.0303199 -0.130856 0.8162
                                                                        0.855538
## 10
          OK 3.13695 3.44618
                                        0.424701
## 11
          OK 0.778295 1.58586
                                          1.02688
                                                    2.82337
                                                              5e-05 0.000141598
          OK 14.0938 24.7979
                                                              5e-05 0.000141598
## 12
                                        0.815152
                                                    3.32746
      significant log2.fold.change adj.p.value
##
## 4
                        -2.6789400 0.005845030
              yes
## 5
                         0.3392440 0.545048000
               no
## 7
                        -0.0303199 0.855538000
               no
## 10
               no
                         0.1356380 0.424701000
## 11
              yes
                         1.0268800 0.000141598
## 12
                         0.8151520 0.000141598
              yes
h.line \leftarrow -log10(0.05)
v.line \leftarrow log2(2)
ged$diff.expr <- "No"</pre>
ged$diff.expr[ged$log2.fold.change > v.line & -log10(ged$adj.p.value) > h.line ] <- "Up"</pre>
ged$diff.expr[ged$log2.fold.change < -v.line & -log10(ged$adj.p.value) > h.line ] <- "Down"</pre>
head(ged)
##
          test_id
                                                           locus sample_1 sample_2
                      gene_id
                                       gene
     XLOC_000004 XLOC_000004 LOC100287934
                                                                         Τ
## 4
                                              chr1:764864-810022
                                                                                  U
      XLOC_000005 XLOC_000005 LOC100287934
                                                                         Τ
                                                                                  U
                                              chr1:764864-810022
                                                                         Т
                                                                                  U
      XLOC_000007 XLOC_000007
                                 LINC01128
                                              chr1:827590-859446
## 10 XLOC_000010 XLOC_000010
                                                                         Т
                                                                                  U
                                    KLHL17
                                              chr1:960586-965897
  11 XLOC_000011 XLOC_000011
                                    PLEKHN1
                                              chr1:966491-982093
                                                                         Т
                                                                                  U
  12 XLOC_000012 XLOC_000012
                                                                                  U
##
                                      ISG15 chr1:1013466-1014540
                                                                         Τ
      status value_1 value_2 log2.fold_change. test_stat p_value
##
                                                                         q_value
          OK 0.37868 0.059133
## 4
                                         -2.67894 -1.96996 0.0027
                                                                     0.00584503
## 5
          OK 0.452312 0.572217
                                        0.339244 0.414573 0.4708
                                                                        0.545048
## 7
          OK 3.91537 3.83394
                                       -0.0303199 -0.130856 0.8162
                                                                        0.855538
## 10
          OK 3.13695 3.44618
                                        0.135638  0.534257  0.34895
                                                                        0.424701
## 11
          OK 0.778295 1.58586
                                          1.02688
                                                    2.82337
                                                              5e-05 0.000141598
```

```
## 12
          OK 14.0938 24.7979
                                         0.815152
                                                     3.32746
                                                                5e-05 0.000141598
##
      significant log2.fold.change adj.p.value diff.expr
## 4
                         -2.6789400 0.005845030
              yes
## 5
                          0.3392440 0.545048000
               no
                                                        No
## 7
               no
                         -0.0303199 0.855538000
                                                        No
## 10
                          0.1356380 0.424701000
                                                        No
               no
## 11
                          1.0268800 0.000141598
                                                        Uр
              yes
                          0.8151520 0.000141598
## 12
                                                        No
              yes
cols <- c("green", "red", "black")</pre>
names(cols) <- c("Down", "Up", "No")</pre>
vp <- ggplot(data=ged, aes(x=log2.fold.change, y=-log10(adj.p.value ), col=diff.expr)) +</pre>
  geom_point() + theme_minimal() +
  scale_color_manual(values=cols) +
  geom_vline(xintercept=c(-v.line, v.line), col="red") +
  geom_hline(yintercept=h.line, col="red")
vp
```



Top 10 down- and up-regulated genes

```
ged.diff.expr <- ged[ged$diff.expr %in% c("Up", "Down"),]</pre>
dim(ged.diff.expr)
## [1] 4646
              17
dim(ged.diff.expr[ged.diff.expr$significant == "no",])
## [1] 0 17
ged.diff.expr.order <- ged.diff.expr[order(ged.diff.expr[, 15]),]</pre>
head(ged.diff.expr.order, n=5)
##
             test id
                         gene id
                                          gene
                                                                   locus sample 1
## 31661 XLOC 031661 XLOC 031661
                                         MGAM
                                                chr7:141911493-142106747
## 31969 XLOC 031969 XLOC 031969
                                                                                 Т
                                       NPC1L1
                                                  chr7:44512432-44543696
## 9661 XLOC_009661 XLOC_009661 LOC102723479 chr14:106399794-106496343
                                                                                 Т
                                                                                 Т
## 19407 XLOC_019407 XLOC_019407
                                                  chr2:38665909-38734767
                                          GALM
## 9955 XLOC_009955 XLOC_009955
                                     SYNDIG1L
                                                 chr14:74405892-74426102
                                                                                 Τ
##
         sample_2 status value_1
                                   value_2 log2.fold_change. test_stat p_value
## 31661
                U
                      OK
                         2.03008
                                    0.012047
                                                       -7.39671 -6.57524
                                                                            5e-05
## 31969
                                                                             5e-05
                U
                      OK 4.71272 0.0292933
                                                       -7.32985 -7.51378
## 9661
                U
                      OK
                                                         -7.083 -8.67029
                                                                            5e-05
                           156.26
                                     1.15253
## 19407
                U
                      OK 0.908096 0.00878361
                                                       -6.69189 -0.786757
                                                                           0.0008
## 9955
                U
                      OK 0.722329 0.00708826
                                                                   -4.504 0.01235
                                                       -6.67108
             q value significant log2.fold.change adj.p.value diff.expr
## 31661 0.000141598
                             yes
                                         -7.39671 0.000141598
                                                                    Down
## 31969 0.000141598
                                          -7.32985 0.000141598
                                                                    Down
                             yes
## 9661 0.000141598
                                         -7.08300 0.000141598
                                                                    Down
                             yes
## 19407 0.00190649
                                         -6.69189 0.001906490
                             yes
                                                                    Down
## 9955
            0.023295
                                          -6.67108 0.023295000
                             yes
                                                                    Down
tail(ged.diff.expr.order, n=5)
             test_id
                         gene_id
                                   gene
                                                            locus sample_1 sample_2
## 14418 XLOC 014418 XLOC 014418 GNGT2 chr17:49204331-49223325
                                                                         Т
                                                                                   IJ
                                                                                   U
## 27334 XLOC 027334 XLOC 027334 GPRIN1 chr5:176595801-176617357
## 8089 XLOC_008089 XLOC_008089
                                                                         Т
                                                                                   IJ
                                            chr12:1527089-1529969
## 33426 XLOC 033426 XLOC 033426 NUDT18
                                           chr8:22104944-22109419
                                                                         Т
                                                                                   U
## 23788 XLOC_023788 XLOC_023788 PFKFB4
                                           chr3:48517659-48556835
                                                                                   IJ
##
                   value_1 value_2 log2.fold_change. test_stat p_value
## 14418
             OK 0.00910793 0.344963
                                               5.24318 0.715596 0.00155
## 27334
             OK 0.0646707 2.65464
                                               5.35926
                                                         11.1728
                                                                   5e-05
## 8089
             OK 0.0141094 0.592514
                                               5.39212
                                                         4.31488
                                                                  0.0001
## 33426
             OK 0.0942486
                             4.7686
                                               5.66095
                                                         6.04928
                                                                   5e-05
## 23788
                  0.106216 6.75489
                                               5.99085
                                                         13.8721
                                                                   5e-05
             OK
##
             q_value significant log2.fold.change adj.p.value diff.expr
## 14418
            0.003528
                             yes
                                           5.24318 0.003528000
                                                                      Uр
## 27334 0.000141598
                             yes
                                           5.35926 0.000141598
## 8089 0.000273729
                             yes
                                           5.39212 0.000273729
                                                                      Uр
## 33426 0.000141598
                                           5.66095 0.000141598
                                                                      Uр
                             yes
```

5.99085 0.000141598

yes

23788 0.000141598