

Industrial Photonics

Design of Beam Expanders

Ariel Priarone

s274149

(a.y. 2022/2023)

Contents

1	Introduction	2
2	Write the function	2
3	Reproduce the paper result 3.1 Claim about the magnification	6 8 8 10
4	Practical implementation	11
5	Study of the assignment arrangement	11
6	Design the beam expander	12
L	Schematic of the considered beam expander Plot of the arrangements proposed in [1]	2 7 7 9 9 11 12 13
\mathbf{L}	2. Linear dependency on d_1 8 3.2.1 Using theoretical magnification 8 3.2.2 Using the output beam radius 10 Practical implementation 11 tudy of the assignment arrangement 11 Design the beam expander 12 t of Figures 2 Schematic of the considered beam expander 2 Plot of the arrangements proposed in [1] 7 Plot of the arrangements proposed in [1], detail of the hyperbole shape 7 Plot of the magnification dependency on d_1 9 Plot of the linear approximation 9 Plot of the behaviour of the arrangement with negative second lens 12 Plot of the behaviour of the designed system 13 t of Tables Comparison between my results and the paper [1] results (all distances in mm) 6	
	1 Comparison between my results and the paper [1] results (all distances in mm) 2 Commercial lenses that meet the design requirements	

1 Introduction

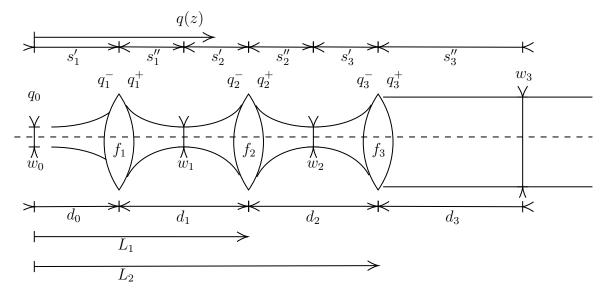


Figure 1: Schematic of the considered beam expander

This assignment asks to study the design of a beam expander provided in [1], in particular the behaviour of the magnification w.r.t. the position of the lenses. Then it's asked to study a practical implementation of the design given in the paper, and try to re-design another beam expander based on a given arrangement. To do that it's convenient to write a function that handle a general arrangement of three thin lenses, as depicted in **Figure 1**.

2 Write the function

The function is based on the propagation of the complex parameter $q(z) = z + j \cdot z_r$ on the z axis, thru air and lenses interfaces. The propagation thru the lenses is studied applying the matrix transfer function. As suggested in the paper the design should be optimized for a wavelength, in this case $\lambda_0 = 632.8$ nm.

From the theory we can write the Reileigh range of the starting beam:

$$z_r = \frac{\pi w_0^2}{\lambda_0} \tag{1}$$

also the magnification and waist position formulas are used:

$$M_i = \frac{w_{i+1}}{w_i} = \frac{\theta_i}{\theta_{i+1}} = \frac{f_i}{\sqrt{(d_i - f_i)^2 + z_{r,i}^2}}$$
(2)

$$s_i' = f_i + M_i^2 (s_i'' - f_i) (3)$$

as well as the propagation of the Reileigh range thru lenses:

$$z_r^{i+1} = M_i^2 \cdot z_r^i \tag{4}$$

the initial condition of the beam parameter (at origin, z=0):

$$q_0 = j \cdot z_{r,0} \tag{5}$$

and the propagation of q thru air and lenses:

$$L = \begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ -1/f & 1 \end{bmatrix}$$
 Lens matrix (6)

$$q_i^+ = \frac{A \cdot q_i^- + B}{C \cdot q_i^- + D} \qquad \text{propagation thru lens} \tag{7}$$

$$q_i(z+k) = q_i(z) + K$$
 propagation thru air (8)

$$q_{i+1}^- = q_i^+ + d_i$$
 propagation thru air length (9)

Always referring to **Figure 1**, it is possible to compute the radius thru all the length of the system:

$$w(z) = \begin{cases} \sqrt{-\frac{\lambda_0}{\pi \cdot \Im(\frac{1}{q_0 + z})}} & z \in [0, d_0) \\ \sqrt{-\frac{\lambda_0}{\pi \cdot \Im(\frac{1}{q_1^+ + z - d_0})}} & z \in [d_0, L_1) \\ \sqrt{-\frac{\lambda_0}{\pi \cdot \Im(\frac{1}{q_2^+ + z - L_1})}} & z \in [L_1, L_2) \\ \sqrt{-\frac{\lambda_0}{\pi \cdot \Im(\frac{1}{q_3^+ + z - L_2})}} & z \in [L_2, \infty) \end{cases}$$

$$(10)$$

The function to plot the beam radius thru the beam expander is implemented in python using the following code:

```
def BeamExpander(lam0,w0,d0,d1,d2,f1,f2,f3,npoint=1000,fig=None,axs=None,plot=True,MS=1,
        zmin=None,zmax=None):
         # this function aim to produce a plot of a gausiann beam that passes thru three thin lenses,
2
             the approach used is tho compute the complex beam parameter q and propagate that thru
             air and lenses, then compute the radius and show a plot
         # parameters:
3
             lam0
                         wavelength considered
                                                                             [mm]
                         initial beam waist
             wO
                                                                             [mm]
5
             d0
                         from initial waist to first thin lens
                                                                             [mm]
             d1
                         between first and second thin lenses
                                                                             [mm]
                         between second and third thin lenses
             d2
                                                                             Tmm7
8
         #
            f1
                         focal length first lens
                                                                             \Gamma mm7
9
                                                                             [mm]
                         focal length first lens
            f2
10
            f3
                         focal length first lens
                                                                             [mm]
11
                                                                             [--]
            npoint
                        number of points of the plot (resolution)
12
            fig=None
                        figure handle
13
                         axis handle
             axs=None
14
            plot=True
                       T=generate plot; F=generate only the data
15
                         quality factor of the beam (ref slide 05/177)
                                                                             [--]
            Ms
16
             zmin
                         z axis limit to consider
                                                                             [mm]
17
                         z axis limit to consider
             zmax
                                                                             \Gamma mm7
18
          returns:
19
                         figure handle of the plot
20
             fig
                         axis handle of the plot
21
```

```
overall magnification of the system
                                                                               \Gamma - - J
22
                          location of the output waist w.r.t. last lens
         #
             d3 (s3II)
                                                                               [mm]
23
             th3*10**5
                          angle of output beam *10^5
                                                                               [mrad*100]
         #
24
                          output waist (real beam)
                                                                               [mm]
25
                          beam radius at the end of the system (real beam) [mm]
             w_end
26
27
                      d0+d1
                                                         # second length position
         T.1
28
         L2
                      d0+d1+d2
                                                         # third length position
29
                      np.pi*w0**2/lam0
                                                         # Rayleigh range
         zr0
                                                         # complex beam parameter
31
         q0
                      1j*zr0
                                                         # divergence at the left of the first lens
         th0
                      lam0/np.pi/w0
32
                      MS**0.5
                                                         # sqrt of quality factor
33
34
         M1
                      f1/((d0-f1)**2+zr0**2)**0.5
                                                         # magnification first lens
35
         M1
                      abs(M1)
36
                      M1*w0
         ₩1
                                                         # weist of second beam
37
                      zr0*M1**2
                                                         # Rayleigh range right first lens
38
         zr1
                      th0/M1
                                                         # Divergence right first lens
         th1
39
                      q0+d0
                                                         # propagate left side first lens
         q1minus =
40
         A,B,C,D =
                      (1,0,-1/f1,1)
                                                         # matrix entries of first lens
41
         q1plus =
                      (A*q1minus+B)/(C*q1minus+D)
                                                         # propagate right side first lens
42
43
         s1I
                                                         # distance from first lens and waist (on the
44
         \hookrightarrow left)
                      f1+M1**2*(s1I-f1)
         s1II
                                                         # distance from first lens and waist (on the
45
         \hookrightarrow right)
         S2I
                      (d1-s1II)
                                                         # distance from second lens and waist (on the
             left)
         \hookrightarrow
         M2
                      f2/((S2I-f2)**2+zr1**2)**0.5
                                                         # magnification second lens
47
                      abs(M2)
         M2
48
                                                         # weist of third beam
         w2
                      M2*w1
49
                      zr1*M2**2
                                                         # Rayleigh range right second lens
         zr2
50
                      th1/M2
                                                         # Divergence right second lens
         th2
51
                      q1plus+d1
                                                         # propagate left side second lens
         q2minus =
52
         A,B,C,D =
                      (1,0,-1/f2,1)
                                                         # matrix entries of second lens
                                                         # propagate right side second lens
                      (A*q2minus+B)/(C*q2minus+D)
         q2plus =
55
         s2II
                      f2+M2**2*(S2I-f2)
                                                         # distance from second lens and waist (on the
56
         \hookrightarrow right)
                                                         # distance from third lens and waist (on the
         S3I
                      (d2-s2II)
57
             left)
         МЗ
                      f3/((S3I-f3)**2+zr2**2)**0.5
                                                         # magnification third lens
58
         М3
                      abs(M3)
59
         w3
                      M3*w2
                                                         # weist of third beam
60
                      zr2*M3**2
                                                         # Rayleigh range right second lens
61
         zr3
                      th2/M3
         th3
                                                         # Divergence right second lens
62
         q3minus =
                      q2plus+d2
                                                         # propagate left side third lens
63
                      (1,0,-1/f3,1)
                                                         # matrix entries of third lens
         A,B,C,D =
64
                      (A*q3minus+B)/(C*q3minus+D)
                                                         # propagate right side third lens
         q3plus =
65
```

```
if zmin is None:
66
             zmin=
                                                        # min of z axis
67
         if zmax is None:
68
                     L2+2*f3
                                                        # max of z axis
             zmax=
69
                     np.linspace(zmin,zmax,npoint)
                                                       # points of z axis
         z_vect =
70
                                                        # initialize beam radius along z
                      Г٦
71
                      Г٦
                                                        # this will be the real beam (not gaussian)
72
         w_r
73
                 = f3+M3**2*(S3I-f3)
                                                        # location of output waist w.r.t. last lens (if
         S3II
         → negative, the beam is already diverging)
         for z in z_vect:
75
             if
                     0 \le z \le d0:
76
                 q = q0+(z-0)
                                                   # propagate q to z position
77
                 aux = 1/q
                                                   # auxilliary for radius calculation
78
                 w.append((-lam0/(np.pi*aux.imag))**0.5) # beam radius along z axis
79
                 w_r.append(M*w0*(1+((lam0*z)/(np.pi*w0**2))**2)**0.5)
                                                                                     # real beam radius
                  \hookrightarrow along z axis
                     d0<=z<L1:
             elif
                 q = q1plus+(z-d0)
                                                   # propagate q to z position
82
                 aux = 1/q
                                                   # auxilliary for radius calculation
83
                 w.append((-lam0/(np.pi*aux.imag))**0.5) # beam radius along z axis
84
                 w_r.append(M*w1*(1+((lam0*(z-d0-s1II))/(np.pi*w1**2))**2)**0.5) # real beam radius
85
                  \hookrightarrow along z axis
             elif L1 \le z \le L2:
86
                 q = q2plus+(z-L1)
                                                   # propagate q to z position
87
                 aux = 1/q
                                                   # auxilliary for radius calculation
                 w.append((-lam0/(np.pi*aux.imag))**0.5)  # beam radius along z axis
                 w_r.append(M*w2*(1+((lam0*(z-L1-s2II))/(np.pi*w2**2))**2)**0.5) # real beam radius
90
                  \hookrightarrow along z axis
             elif
                     L2 \le z:
91
                 q = q3plus+(z-L2)
                                                   # propagate q to z position
92
                                                   # auxilliary for radius calculation
                 aux = 1/q
93
                 w.append((-lam0/(np.pi*aux.imag))**0.5) # beam radius along z axis
94
                 w_r.append(M*w3*(1+((lam0*(z-L2-S3II))/(np.pi*w3**2))**2)**0.5) # real beam radius
95
                  \rightarrow along z axis
             ymax=max(w)*1.1;
                                  ymin=-0
         xmin=0; xmax=L2+2*f3
97
         if plot:
                                                        # plot if needed, skip if not
98
             if fig == None or axs == None:
99
                 fig, axs=plt.subplots()
100
             fig.tight_layout()
101
             axs.plot(z_vect, w, label=f'$d_1={d1}$; $d_2={d2}$')
102
             if (MS > 1):
103
                 axs.fill_between(z_vect, w_r, w, alpha=0.2) # if it's a gaussian beam, no need to
104
                  → plot the shade
             axs.set_xlabel('$z$ [mm]')
105
             axs.set_ylabel('beam radius [mm]')
106
             axs.set_ylim([ymin,ymax]); axs.set_xlim([xmin,xmax])
107
             axs.vlines([d0, L1, L2],ymin,ymax,linestyles="dashdot",color="magenta")
108
```

```
axs.grid(True, 'major')
axs.legend()
return fig, axs, M1*M2*M3, S3II, th3*10**5, w3*M, w_r[-1]
```

3 Reproduce the paper result

The second point of the assignment asks to reproduce the results of the paper [1]. To do that i used the already developed function to plot the beam radius along the z axis, with the following code, that produce the plot in **Figure 2**, that is also magnified, for a single configuration, in **Figure 3** to show the hyperbole shape of the beam radius w(z). The code spans the d_1 and d_2 used in the paper.

The results comparison are summarized in **Table 1**.

```
# %% check result for all the row of the table
    table=[(10,120.006),
           (20,115.002),
3
           (30,113.334),
4
           (40,112.500),
5
           (50,112.000)]
    fig, ax = plt.subplots()
    for (d1,d2) in table:
        fig, ax, Mg, dout, thout, wout, w_end =
           BeamExpander(lam0=0.0006328,w0=0.5,d0=100,d1=d1,d2=d2,f1=-10,f2=10,f3=100
            ,npoint=1000,fig=fig,axs=ax)
        print(f'Mg={Mg}; dout={dout}; thout={thout}; wout={wout}')
10
11
    tikzplotlib_fix_ncols(fig)
12
    tikzplotlib.save('Assignment2/PLOT.tex',axis_width='0.9\\textwidth',axis_height ='7cm')
13
```

d_1	d_2	M		s_3''		$\theta_3 \cdot 10^5$		w_3	
$ a_1 $		paper	my script	paper	my script	paper	my script	paper	my script
10	120.006	10.032	10.0322	100.000	-601.821	4.017	4.015	5.016	5.016
20	115.002	20.071	20.069	100.000	7800.014	2.008	2.007	10.036	10.035
30	113.334	30.111	30.108	100.000	-12190.104	1.338	1.338	15.055	15.054
40	112.500	40.150	40.000	100.000	-171900.000	1.004	1.007	20.075	20.000
50	112.000	50.189	50.000	100.000	-269899.99	0.803	0.805	25.095	25.000
$f_1 = -10;$ $f_2 = 10;$ $f_3 = 100;$ $w_0 = 0.5;$ $d_0 = 100;$ $\lambda = 0.0006328$									

Table 1: Comparison between my results and the paper [1] results (all distances in mm)

3.1 Claim about the magnification

In the paper, the authors claim that "the expected magnification ratio always occurs at a distance equal to the focal length of the rightmost lens". Following the theory, the beam waist distances from the lenses, at which the expected magnification ratio happens, propagate thru the lenses as in **Equation 3**. So the distance s_3'' is not always 100 mm, as claimed in the paper, but vary with the configuration of the system. The results are reported in **Table 1**, in the column s_3'' . my results are

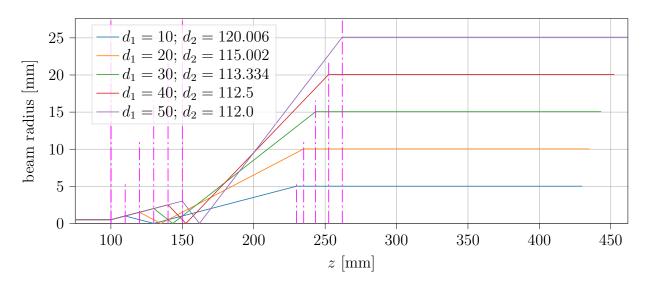


Figure 2: Plot of the arrangements proposed in [1]

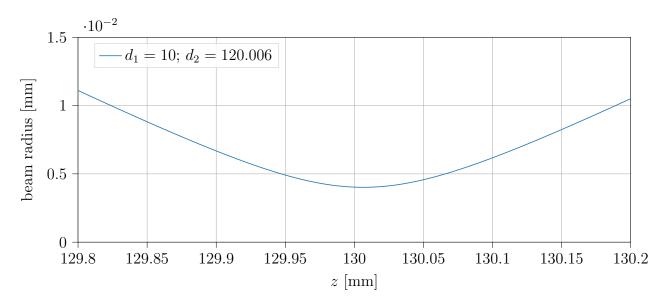


Figure 3: Plot of the arrangements proposed in [1], detail of the hyperbole shape

sometimes negative, that means that the beam is already diverging as soon as it exit the rightmost lens, and the distance indicate where the waist would have been (on the left on the lens) if such lens didn't exist in the path of the beam.

3.2 Linear dependency on d_1

Another request of the assignment is to verify that "the magnification of such a system is approximately a linear function of the mutual distance d_1 between the first and the second element of the optical system". To do that I will first consider the theoretical definition of the magnification $M = w_3/w_0$, and then the "practical" magnification at double the focal length of the rightmost lens $M = w(z = L_2 + 2 \cdot f_3)/w_0$.

3.2.1 Using theoretical magnification

Using the theory definition, it is easy to show that the behaviour is not linear at all, as shown in **Figure 4**. Note that only half of this plot is referring to an actual beam waist at the right of the rightmost lens, because after the magnification reaches a maximum, the beam becomes diverging and the 'virtual" waist would be on the left of the last lens, where there is another beam.

I performed the calculation with the following script:

```
# %% check linearity
    fig, axs=plt.subplots()
2
    fig.tight_layout()
3
    Mg_vect=[]
                 112.5
                                               # note that this is optimized for 40x !!!
    d1\_vect = np.linspace(38,42,500)
                                               # try some d1
6
    for d1 in d1_vect:
        Mg =
         \rightarrow BeamExpander(lam0=0.0006328,w0=0.5,d0=100,d1=d1,d2=d2,f1=-10,f2=10,f3=100,plot=False)[2]
        Mg_vect.append(Mg)
9
    axs.plot(d1_vect, Mg_vect, label=f'$d_2={round(d2,3)}$')
10
    axs.set_xlabel('$d_1$ [mm]')
11
    axs.set_ylabel('Magnification [-]')
12
    axs.grid(True, 'Both')
13
    axs.legend()
14
15
    tikzplotlib_fix_ncols(fig)
16
    tikzplotlib.save('Assignment2/dvsm.tex',axis_width='0.9\\textwidth',axis_height ='7cm')
17
```

The question at this point could be: is it possible that the following statement is true?

$$\forall d_1 \exists d_2 | \max(M) = M(d_1, d_2)$$

i.e. for every d_1 , there is a d_2 that places the maximum in the position d_1 ? and then is it possible that the value of this maximum is linearly dependent on d_1 ?

In order to have an empirical proof of this statement i performed a gridding of both the parameters (d_1, d_2) , obtaining the **Figure 5**, where the linear dependency is quite evident.

The following script was used to produce the results:

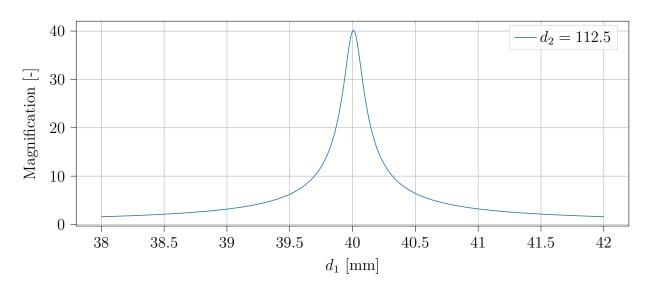


Figure 4: Plot of the magnification dependency on d_1

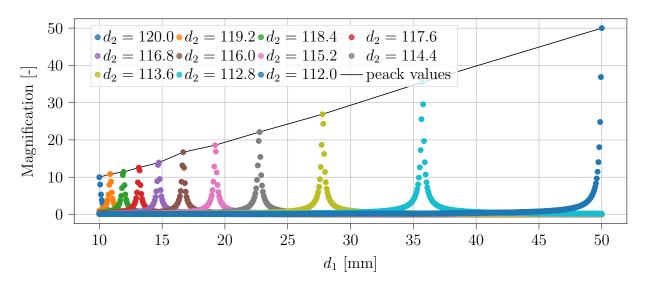


Figure 5: Plot of the linear approximation

```
# %% check linearity - envelope
    fig, axs=plt.subplots()
    fig.tight_layout()
    maximum=[]
    d max=[]
    for d2 in np.linspace(120,112,11):
        LinRel = [[],[]]
        for d1 in np.linspace(10,50,600):
             Mg = BeamExpander(lam0=0.0006328, w0=0.5, d0=100, d1=d1, d2=d2,
             \rightarrow f1=-10,f2=10,f3=100,plot=False)[2]
            LinRel[0].append(d1)
10
            LinRel[1].append(Mg)
11
        maximum.append(max(LinRel[1]))
12
        maxindex=LinRel[1].index(max(LinRel[1]))
13
        d_max.append(LinRel[0][maxindex])
14
        axs.scatter(LinRel[0],LinRel[1],marker='.',label=f'$d_2={round(d2,3)}$')
15
    axs.plot(d_max,maximum,'k',label=f'peack values')
16
    axs.set_xlabel('$d_1$ [mm]')
17
    axs.set_ylabel('Magnification [-]')
18
    axs.grid(True, 'Both')
19
    axs.legend(ncol=4)
20
21
    tikzplotlib_fix_ncols(fig)
22
    tikzplotlib.save('Assignment2/LinApprox.tex',axis_width='0.9\\textwidth',axis_height ='7cm')
23
```

3.2.2 Using the output beam radius

The previous **subsubsection 3.2.1** applied the definition using the waist radius, but a more practical approach would be to check the magnification in a predetermined point, independently from where the beam is focused. In this case it is the last point of the plot $(L_2 + 2 \cdot f_3)$. Again i used the script below to check the linearity for some configurations, and applying the new definition

$$M = \frac{w(z = L_2 + 2 \cdot f_3)}{w_0}$$

the linear behaviour is immediately evident (**Figure 6**), also because in all the configurations the divergence experienced in the near range of the device is really small.

```
# %% check linearity - definition with useful beam radius
                         fig, axs=plt.subplots()
                         fig.tight_layout()
                          d1_vect =
                                                                                                        np.linspace(10,50,10)
                                                                                                                                                                                                                                                                                               # try some d1
                          d2\_vect = np.linspace(120,112,5)
                                                                                                                                                                                                                                                                                       # try some d2
 5
  6
                         for d2 in d2_vect:
                                                    Mg_vect =
                                                                                                                                      []
                                                    for d1 in d1_vect:
                                                                                W_{out} = BeamExpander(lam0=0.0006328, w0=0.5, d0=100, d1=d1, d2=d2, f1=-10, f2=10, f3=100, d1=d1, d2=d2, f1=-10, f3=100, d1=d1, d2=d2, d1=d1, d1=d1, d2=d2, d1=d1, d1=d1, d2=d2, d1=d1, d1=d1, d1=d1, d1=d1
10
                                                                                                        plot=False)[6]
```

```
Mg_vect.append(W_out/0.5)
axs.plot(d1_vect,Mg_vect,label=f'$d_2={round(d2,3)}$')
axs.set_xlabel('$d_1$ [mm]')
axs.set_ylabel('$\\frac{w(z=L_2+2\\cdot f_3)}{w_0}$ [-]')
axs.grid(True, 'Both')
axs.legend()
tikzplotlib_fix_ncols(fig)
tikzplotlib.save('Assignment2/Woutvsm.tex',axis_width='0.9\\textwidth',axis_height ='7cm')
```

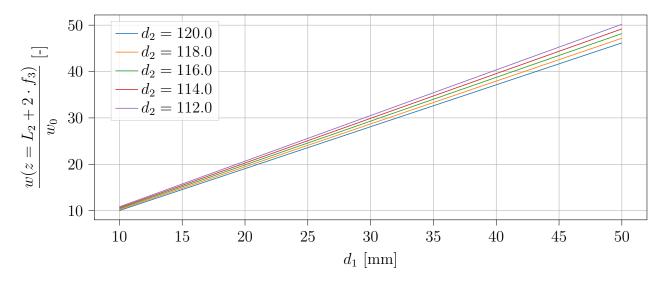


Figure 6: Plot of the linear behaviour

4 Practical implementation

The next step of the assignment is to find some commercially available devices that can be used to build the system. the requisites and products that i found are resumed in **Table 2**. These items are just lenses, without supports, so in a real application, also the structure for mounting and tune the positions of the lenses would have to be designed.

Long	Design			Commercial				
Lens	f [mm]	type	diameter [mm]	manufacturer	f [mm]	type	diameter [mm]	
1	-10	negative	>1	Techspec 62-437	-10	negative	6.25	
2	10	positive	>6	Techspec stock 63-535	10	positive	10.00	
3	100	positive	>50	Thorlabs LB1630-A	100	positive	50.8	

Table 2: Commercial lenses that meet the design requirements

5 Study of the assignment arrangement

The next request of the assignment is to study a different arrangement of three lens beam expander, in which the middle lens is the negative one. To do that I considered the distances of the arrangement of the paper, and changed the focal length of the lenses to simulate this different configuration. The script is the following and the results are shown in **Figure 7**.

As is, the device, produce a zoom effect, but the collimation of the output beam worsen with the increasing of the magnification.

```
# %% check result for all the row of the table
                     table=[(10,120.006),
  2
                                                        (20,115.002),
                                                        (30,113.334),
                                                        (40,112.500),
                                                        (50,112.000)]
  6
                    fig, ax = plt.subplots()
                    for (d1,d2) in table:
                                        fig, ax, Mg, dout, thout, wout, w_end =
                                          \hookrightarrow BeamExpander(lam0=0.0006328,w0=0.5,d0=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,f2=-10,f3=100,d1=d1,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=10,d2=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2,f1=d2
                                          → npoint=1000,fig=fig,axs=ax)
                                        print(f'Mg={Mg}; dout={dout}; thout={thout}; wout={wout}')
10
11
                     tikzplotlib_fix_ncols(fig)
12
                     tikzplotlib.save('Assignment2/AssArrangment.tex',axis_width='0.9\\textwidth',axis_height ='7cm')
13
```

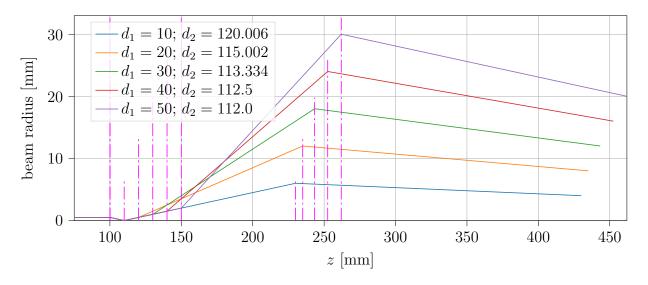


Figure 7: Plot of the behaviour of the arrangement with negative second lens

6 Design the beam expander

At this point the request is to find a strategy to improve the previous configuration to obtain a better beam expander. To optimize the device i used a manual bisection method on the parameter d_2 , trying to minimize the output divergence, for all the d_1 values.

With the following values i managed to obtain the results shown in **Figure 8** and resumed in **Table 3**.

```
# %% try to optimize oyher expander
table=[(10,119.98),
(20,115),
```

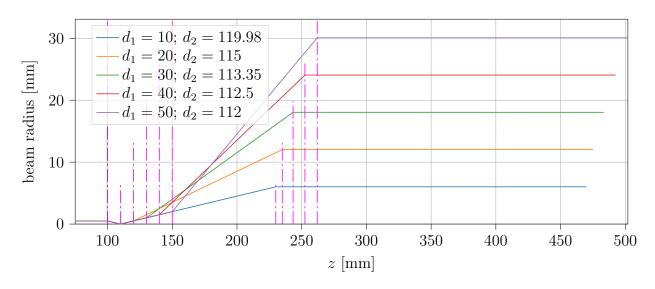


Figure 8: Plot of the behaviour of the designed system

d_1	d_2	M	θ_3	w_3			
10	119.98	11.47	3.51	5.7			
20	115.00	24.00	1.67	12.0			
30	113.35	17.51	2.29	8.7			
40	112.50	48.00	0.83	24.0			
50	112.00	60	0.67	30.0			
$f_1 = 10;$ $f_2 = -10;$ $f_3 = 120;$							
$w_0 = 0.5;$ $d_0 = 100;$ $\lambda = 0.0006328$							

Table 3: Performance at some configurations of my design

```
(30,113.35),
           (40,112.5),
           (50,112)]
   fig, ax = plt.subplots()
    for (d1,d2) in table:
       fig, ax, Mg, dout, thout, wout, w_end =
        \rightarrow BeamExpander(lam0=0.0006328, w0=0.5, d0=100, d1=d1, d2=d2, f1=10, f2=-10, f3=120,
        print(f'Mg={Mg}; dout={dout}; thout={thout}; wout={wout}')
10
11
    tikzplotlib_fix_ncols(fig)
12
    tikzplotlib.save('Assignment2/Mydesign.tex',axis_width='0.9\\textwidth',axis_height ='7cm')
13
   plt.show()
14
```

References

[1] Antonin Miks and Pavel Novak. Paraxial properties of three-element zoom systems for laser beam expanders. *Optics Express*, 22, 09 2014.