

### Problem No: 03

Problem name : Suppose that the relation  $R_1$  and  $R_2$  on a set  $A$  are represented by the matrices

$$M_{R1} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} \text{ and } M_{R2} = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{bmatrix}. \text{ Write a program}$$

to find the  $M_{R1} \cup R_2$  and  $M_{R1} \oplus R_2$ .

Theory : The program shown above defines two functions, 'matrix\_union()' and 'matrix\_exclusive\_or()', to compute the union and symmetric union (exclusive or) of two matrices respectively.

The matrix\_union() function takes two matrices as input and returns a new matrix that represents the union of two input matrices. It uses list comprehension to perform element-wise logical OR operation between the elements of the two input matrices.

✓  
'The `matrix_exclusive_orz()`' function also takes two matrices as input and return a new matrices that represent the symmetric difference of the two input matrices. It uses list comprehension and the X-OR operators ( $\wedge$ ) to perform element-wise logical X-OR operation between the elements of the two input matrices.

After defining this functions, the program creates two matrices  $R_1$  and  $R_2$  which represent relations. These matrices are then passed to the `matrix_union()` and `matrix_exclusive_orz()` functions to compute the union and symmetric difference  $MR_1 \oplus R_2$ .

Here a python program is written below :

```
def matrix_union(matrix1, matrix2):  
    union_result = [[matrix1[i][j] or matrix2[i][j]  
                     for j in range(len(matrix1[0]))]  
                     for i in range(len(matrix1))]  
    return union_result
```

# Function to compute the matrix Union (element-wise OR) of the two matrices.

```
def matrix_exclusive_or (matrix1, matrix2):
```

```
    XOR_result = [[matrix1[i][j] ^ matrix2[i][j]
```

```
                    for j in range (len(matrix1[0])) for i in range (len(matrix1))]
```

```
    return XOR_result
```

# Function to compute the matrix exclusive OR (elementwise XOR) of the two matrix.

$R_1 = \begin{bmatrix} [1, 0, 1] \\ [1, 0, 0] \\ [0, 1, 1] \end{bmatrix}$ , # Give the matrix representing relation  $R_1$  and  $R_2$ .

$R_2 = \begin{bmatrix} [1, 0, 1] \\ [0, 1, 1] \\ [1, 0, 1] \end{bmatrix}$

~~MR1~~ ⊕

$MR1 \text{ XOR } R_2 = \text{matrix\_exclusive\_or}(R_1, R_2)$  # find  $MR1 \oplus R_2$

$MR1 \text{ union } R_2 = \text{matrix\_union}(R_1, R_2)$  and  $MR1 \cup R_2$ .

print("First Matrix = ",  $R_1$ )

print("Second Matrix = ",  $R_2$ )

print("Rows = ", len( $R_1$ ), "Cols = ", len( $R_1[0]$ ))

print("Matrix union  $MR1 \cup MR2$ ",  $MR1 \text{ union } R_2$ )

print("Matrix Exclusive OR  $MR1 \oplus R2$ ",  $MR1 \oplus R2$ )  
 # print the result,

Output:

First Matrix =  $\begin{bmatrix} [1, 0, 1] \\ [1, 0, 0] \\ [0, 1, 1] \end{bmatrix}$

Second Matrix =  $\begin{bmatrix} [1, 0, 1] \\ [0, 1, 1] \\ [1, 0, 1] \end{bmatrix}$

Rows = 3 Cols = 3

Matrix Union  $MR1 \cup R2$ :  $\begin{bmatrix} [1, 0, 1] \\ [1, 1, 1] \\ [1, 1, 1] \end{bmatrix}$

Matrix Exclusive OR  $MR1 \oplus R2$ :  $\begin{bmatrix} [0, 0, 0] \\ [1, 1, 1] \\ [1, 1, 0] \end{bmatrix}$

#### Problem no-4

Problem name: Write a program to find shortest path by Warshall's algorithm.

Theory : The program shown above applies the Floyd-Warshall algorithm to find the shortest paths in a graph.

The graph is represented by an adjacency matrix.

The function 'floydWarshall()' takes two arguments: the number of vertices in the graph and the adjacency matrix representing the graph. Within this function, the Floyd Warshall algorithm is implemented using nested for loops.

After applying the Floyd Warshall algorithm, the program prints the resulting adjacency matrix, showing the distance between each pair of vertices. The leftmost row represents the origin vertex, and the topmost column represents the destination vertex. The values in the matrix represent the shortest distance between the corresponding vertices.



In the `main()` function the number of vertices is set to 4. The adjacency matrix is defined based on the given graph.

Finally the `'main()'` function calls the `'floydwarshall()'` function with the number of vertices and the adjacency matrix as arguments to find the shortest paths in the graph.

Here a C++ program is written given below :

```
#include <iostream>
using namespace std; // Defining the infinity value.
const int INF = 1000000000;

// Function to apply Floyd-Warshall algorithm
void floydwarshall(int vertex, int adjacency_matrix[][4])
{
    // Iterate over all vertex as intermediate nodes
    for (int k = 0; k < vertex; k++)
    {
        // for each pair of vertex (i, j), check if going to vertex
        // k provides a short path
        for (int i = 0; i < vertex; i++)
            for (int j = 0; j < vertex; j++)
                if (adjacency_matrix[i][k] < INF && adjacency_matrix[k][j] < INF)
                    adjacency_matrix[i][j] = min(adjacency_matrix[i][j], adjacency_matrix[i][k] + adjacency_matrix[k][j]);
    }
}
```

P.T.O.

```
} for( int j=0; j< vertex; j++)
```

```
} // Relax the distance from i to j by allowing vertex k as an  
intermediate vertex
```

```
// considers which one is better, going through vertex k or  
the previous value
```

```
adjacency_matrix[i][j] = min( adjacency_matrix[i][j],  
adjacency_matrix[i][k] + adjacency_matrix[k][j] );
```

```
}
```

```
// Pretty print the graph
```

```
// o/d means the leftmost row is the origin vertex,
```

```
// and the topmost column as destination vertex
```

```
cout << "o/d" ;
```

```
for( int i=0; i< vertex; i++)
```

```
{ cout << '\t' << i+1;
```

```
}
```

```
cout << endl;
```

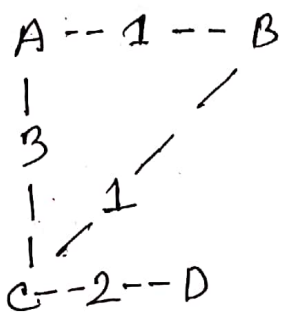
```
// printing the adjacency matrix
for (int i = 0; i < vertex; i++)
{
    cout << i+1;
    for (int j = 0; j < vertex; j++)
    {
        cout << 't' << adjacency_matrix[i][j];
    }
    cout << endl;
}
}
```

```
int main()
```

```
{
    // Number of vertex in the graph
    int vertex = 4;
```

```
/*
```

Input is given as adjacency matrix,  
input represent this undirected graph



should set infinite value for each pair of vertex  
that has no edge



// The adjacency matrix represented the graph

```
int adjacency_matrix[4][4] = {
    { 0, 5, INF, 10 },
    { INF, 0, 3, INF },
    { INF, INF, 0, 1 },
    { INF, INF, INF, 0 } } ;
```

// find the shortest path using Floyd-Warshall algorithm  
by call the function

```
floydwarshall(vertex, adjacency_matrix);
return 0;
}
```

Output:

O/d	1	2	3	4
1	0	5	8	9
2	10000000000	0	3	4
3	10000000000	10000000000	0	1
4	10000000000	10000000000	10000000000	0