Exercises on

Quantum Field Theory

(Based on the lectures by $Dr.\ Mohammed\ Arshad\ Momen)$

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1 Exercise for Class-2 [Lecture (-1)]

Derive the Euler–Lagrange equations corresponding to this action:

$$S[x] = m \int \sqrt{\eta_{ab} \, dx^a dx^b} = m \int d\tau = m \int \sqrt{\eta_{ab} \, \frac{dx^a}{d\lambda} \, \frac{dx^b}{d\lambda}} \, d\lambda$$

2 Exercise for Class-4 [Lecture (1)]

2.1 Assignment-1

How does \hat{J}^{rs} transform under Poincaré transformation? (It's a semi direct product)

2.2 Assignment-2

Recover 3D rotation algebra from angular momentum.

3 Exercise for Class-5 [Lecture (2)]

3.1 Exercise-1

Show that we can recover the Lorentz force from the action:

$$S = \frac{1}{2} \int m \, \dot{\xi}^2 d\tau + q \int A_b(\xi) \dot{\xi}^b d\tau$$

[This latter interaction term is geometrical as well]

3.2 Exercise-2

Check the commutations:

$$[J, p] \sim p$$

 $[p, p] \sim 0$
 $[J, J] \sim J$
 $[J, p^2] \sim 0$
 $[J, p_a p^a] = [J, p_a] p^a + p_a [J, p^a] \sim 0$

4 Exercise for Class-6 [Lecture (3)]

4.1 Exercise-1

Show that the lie derivatives of vector field satisfies:

$$\mathfrak{L}_{\hat{V}}\mathfrak{L}_{\hat{W}} - \mathfrak{L}_{\hat{W}}\mathfrak{L}_{\hat{V}} = \mathfrak{L}_{[\hat{V},\hat{W}]}$$

4.2 Exercise-2

Derive the lie derivative for a tensor $\mathfrak{L}_{\hat{V}} \tilde{T}^a{}_b$.