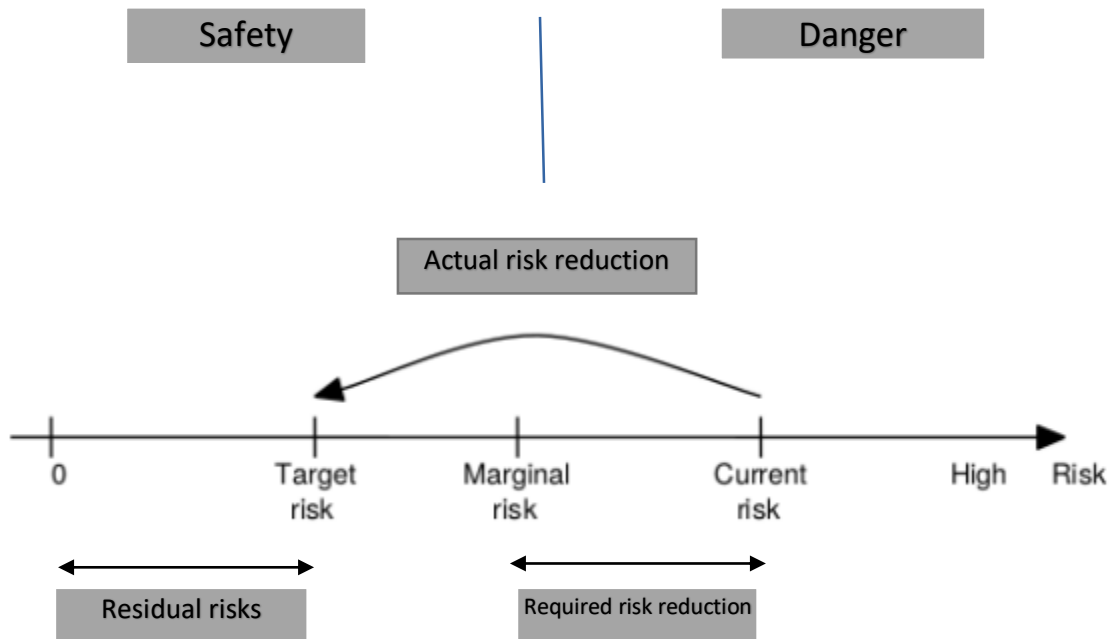


**Problem 1: Definition of "risk"**

1. Complete the graphic by filling in the gray boxes with the following concepts: Safety, Danger, Residual Risk, Required Risk Reduction and Actual Risk Reduction.

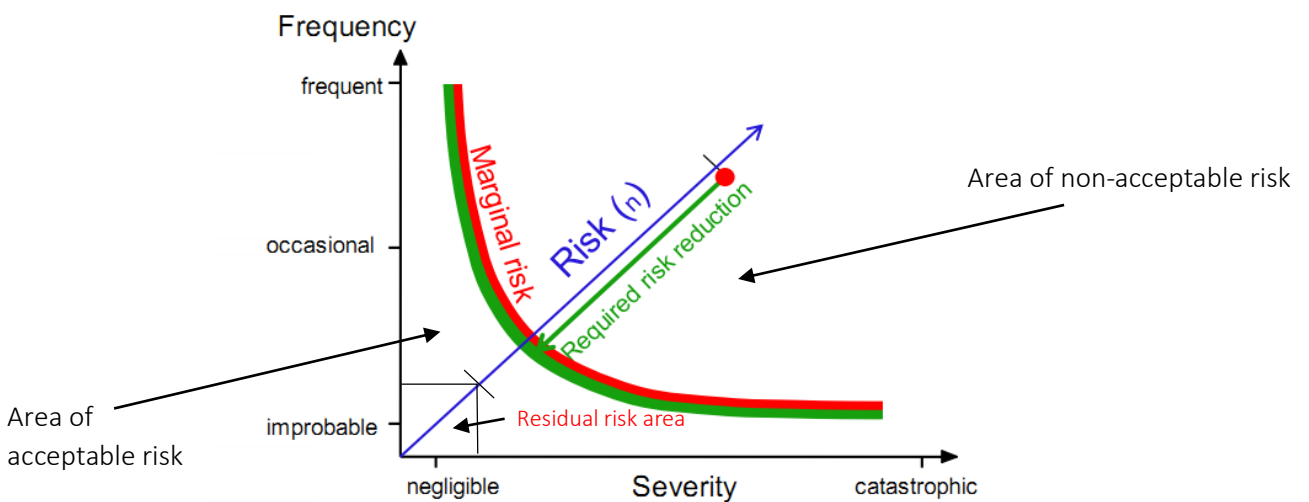


2. How is risk defined mathematically? Please depict your results from 1. by using a frequency vs. severity plot

Definition of risk:  $R = H * S$

H: Expected frequency of the occurrence of an event that leads to a particular harm.

S: Expected severity of the harm



## Problem 2: Railroad crossing

summary: MTTR = 12 hours

MTBF = 6 months

Every 100<sup>th</sup> crossing accident killing all passengers

Driver: 300 railroads crossings per year

5 seconds per crossing

1. calculate the individual risk of fatality for the driver of the car.

$$NP = \frac{300}{y} = \frac{300}{8760h} = \frac{5}{146h} = 3.42 \times 10^{-2} h^{-1}$$

$$HR = \frac{2}{y} = \frac{2}{8760h} = \frac{1}{4380h} = 2.28 \times 10^{-4} h^{-1}$$

$$D = 12h$$

$$E = 5 \text{ sec} = \frac{5}{3600h} = 0.001388 \ll D = 0$$

$$C = \frac{1}{100} = 0.01$$

$$IRF_i = \sum_{\text{hazard}_j} NP_i \cdot \left[ HR_j \cdot (D_j + E_{ij}) \cdot \sum_{\text{accidents}_k} A_{jk} \cdot F_{jk} \right]$$

$$F = 1_{\text{death}}$$

$$\begin{aligned} \text{So, Individual Risk of Fatality (IRF)} &= NP \cdot [HR(D+E) \cdot C \cdot F] \\ &= (3.42 \times 10^{-2} h^{-1}) \cdot (2.28 \times 10^{-4} h^{-1}) \cdot 12h \cdot 0.01 \text{ death} \\ &= 9.35 \cdot 10^{-7} \text{ deaths/h} \\ &= 8.2 \cdot 10^{-3} \text{ deaths/year} \end{aligned}$$

2. is the "Minimal Endogenous Mortality" criterion (MEM) satisfied?

"minimal endogenous mortality" MEM considers 10<sup>-5</sup> deaths per person and year to be the upper limit of the (additional) mortality caused by technical systems:

$$\left( 10^{-5} \frac{\text{deaths}}{\text{person.year}} \right) * 1 \text{ person} = \frac{10^{-5} \text{ deaths}}{8760h} = 1.142 * 10^{-9} \frac{\text{death}}{h}$$

$$IRF = 9.35 \cdot 10^{-7} \frac{\text{death}}{h} > 1.142 * 10^{-9} \frac{\text{death}}{h}$$

So, the MEM criterion is not fulfilled.

3. calculate also the availability  $a_c$  of the safe guarding controller.

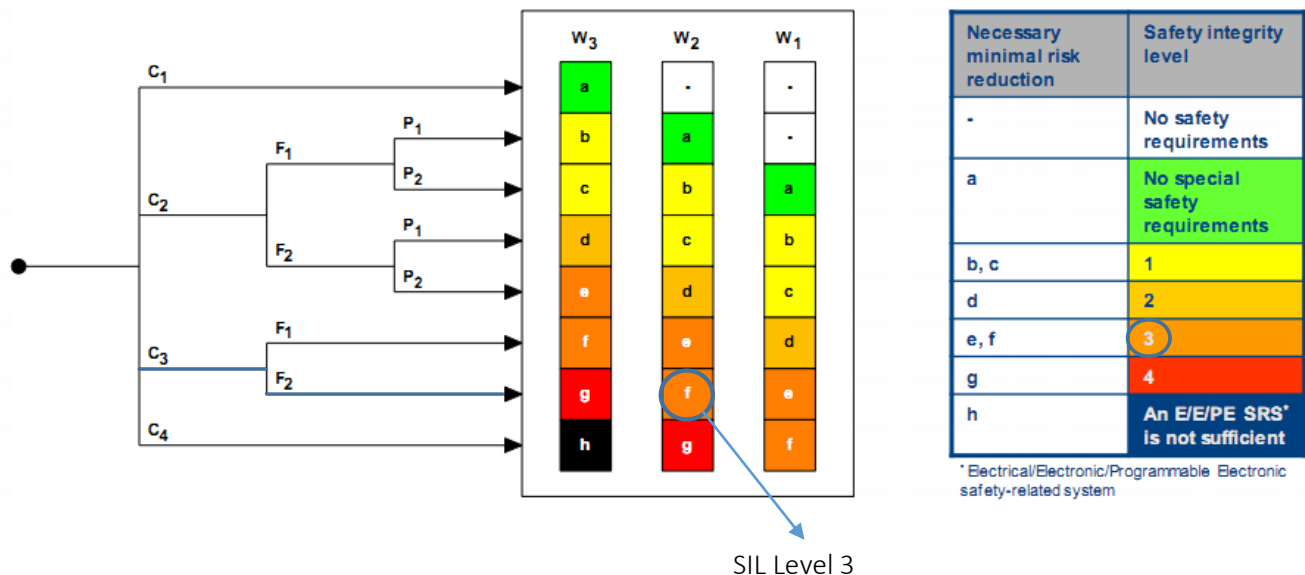
$$a_c = \frac{MTBF}{MTBF + MTTR} = \frac{4380}{4380 + 12} = 0.99727$$

### Problem 3: Adaptive Cruise Control System

- Please give a  $C$ ,  $F$ ,  $P$ ,  $W$  value for the hazards based on the values described in Chapter 3 and on the following assumptions (notice that they are not based on real data):
  - Acceleration is too high
  - Deceleration is too high

Consequence $C = C_3$	If an accident occurs due to these hazards, at least 2 people are killed and at most 10 people are killed. ( $C_3$ : Death of several people)
Frequency of and exposure time in the hazardous zone $F = F_2$	The ACC vehicle's passengers (including driver) sit inside the vehicle two hours per day in average. ( $F_2$ : Frequent to permanent)
Possibility of failing to avoid the hazardous event $P = P_1$	There is a high possibility to avoid these hazards by the deactivating the ACC system and giving the full control of the vehicle to the driver. ( $P_1$ : Possible under certain conditions)
Probability of the unwanted occurrence $W = W_2$	<ul style="list-style-type: none"> <li>It is known that each hazard might occur once in 10 years. (few unwanted occurrences <math>\rightarrow 1/87600 \approx 1.141 \times 10^{-5}</math>)</li> <li>According to a safety analysis, the likelihood that the ACC system is in a hazardous state is 0.02% (<b>Slight probability</b>)</li> </ul>

- Assign a SIL level for the ACC system by ranking the Hazards using the risk graph example provided in chapter



- What is the necessary risk reduction to be applied?

Minimum required risk reduction: f