Parsing with Context Free Grammars

CMSC 723 / LING 723 / INST 725

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Today's Agenda

- Grammar-based parsing with CFGs
 - CKY algorithm
- Dealing with ambiguity
 - Probabilistic CFGs
- Strategies for improvement
 - Rule rewriting / Lexicalization

Sample Grammar

Grammar	Lexicon
$S \rightarrow NP VP$	$Det \rightarrow that \mid this \mid a$
$S \rightarrow Aux NP VP$	$Noun \rightarrow book \mid flight \mid meal \mid money$
$S \rightarrow VP$	$Verb \rightarrow book \mid include \mid prefer$
$NP \rightarrow Pronoun$	$Pronoun \rightarrow I \mid she \mid me$
$NP \rightarrow Proper-Noun$	Proper-Noun → Houston NWA
$NP \rightarrow Det Nominal$	$Aux \rightarrow does$
<i>Nominal</i> → <i>Noun</i>	$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Nominal \rightarrow Nominal Noun$	
$Nominal \rightarrow Nominal PP$	
$VP \rightarrow Verb$	
$VP \rightarrow Verb NP$	
$VP \rightarrow Verb NP PP$	
$VP \rightarrow Verb PP$	
$VP \rightarrow VP PP$	
$PP \rightarrow Preposition NP$	

GRAMMAR-BASED PARSING: CKY

Grammar-based Parsing

- Problem setup
 - Input: string and a CFG
 - Output: parse tree assigning proper structure to input string
- "Proper structure"
 - Tree that covers all and only words in the input
 - Tree is rooted at an S
 - Derivations obey rules of the grammar
 - Usually, more than one parse tree...

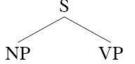
Parsing Algorithms

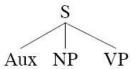
- Two basic (= bad) algorithms:
 - Top-down search
 - Bottom-up search
- A "real" algorithm:
 - CKY parsing

- Observation
 - trees must be rooted with an S node

- Parsing strategy
 - Start at top with an S node
 - Apply rules to build out trees
 - Work down toward leaves

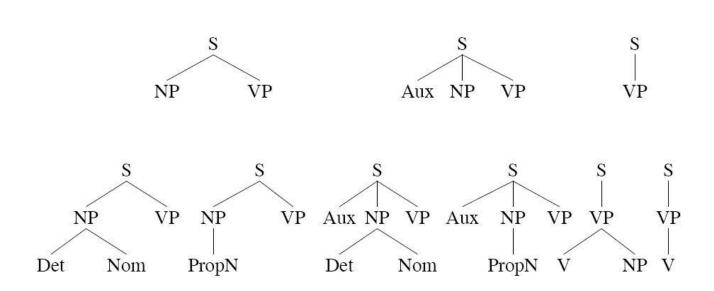
S





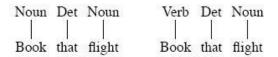


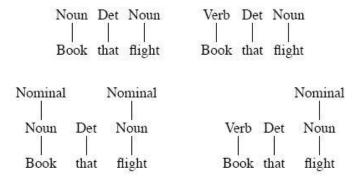
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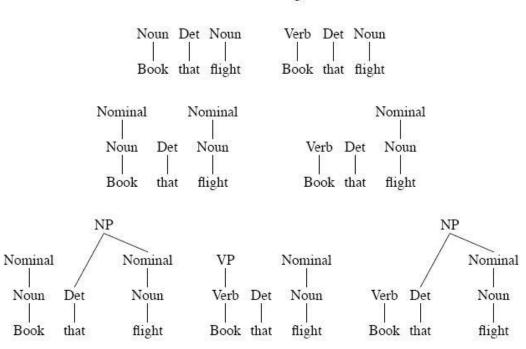


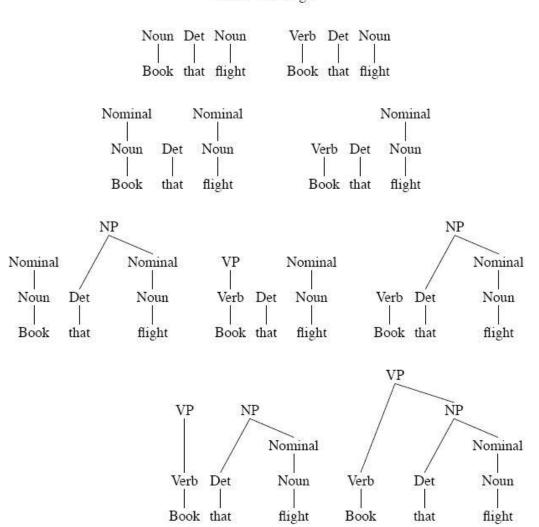
- Observation
 - trees must cover all input words

- Parsing strategy
 - Start at the bottom with input words
 - Build structure based on grammar
 - Work up towards the root S









Top-Down vs. Bottom-Up

- Top-down search
 - Only searches valid trees
 - But, considers trees that are not consistent with any of the words
- Bottom-up search
 - Only builds trees consistent with the input
 - But, considers trees that don't lead anywhere

Parsing as Search

- Search involves controlling choices in the search space
 - Which node to focus on in building structure
 - Which grammar rule to apply

- General strategy: backtracking
 - Make a choice, if it works out then fine
 - If not, back up and make a different choice

Shared Sub-Problems

- Observation
 - ambiguous parses still share sub-trees

- We don't want to redo work that's already been done
- Unfortunately, naïve backtracking leads to duplicate work

Efficient Parsing with the CKY Algorithm

- Solution: Dynamic programming
- Intuition: store partial results in tables
 - Thus avoid repeated work on shared subproblems
 - Thus efficiently store ambiguous structures with shared sub-parts
- We'll cover one example
 - CKY: roughly, bottom-up

CKY Parsing: CNF

- CKY parsing requires that the grammar consist of binary rules in Chomsky Normal Form
 - All rules of the form:

$$A \rightarrow B C$$

 $D \rightarrow w$

– What does the tree look like?

CKY Parsing with Arbitrary CFGs

- What if my grammar has rules like
 VP → NP PP PP
 - Problem: can't apply CKY!
 - Solution: rewrite grammar into CNF
 - Introduce new intermediate non-terminals into the grammar

$$A \rightarrow B C D$$
 $X \rightarrow B C$ (When does

(Where X is a symbol that doesn't occur anywhere else in the grammar)

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$Nominal \rightarrow Nominal PP$	
$VP \rightarrow Verb$	
$VP \rightarrow Verb NP$	
$VP \rightarrow Verb NP PP$	
$VP \rightarrow Verb PP$	
$VP \rightarrow VP PP$	
$PP \rightarrow Preposition NP$	

CNF Conversion

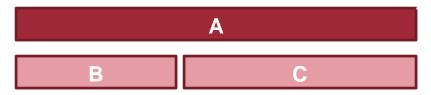
Original Grammar

CNF Version

CIVI VEISIOII
$S \rightarrow NP VP$
$S \rightarrow X1 VP$
$X1 \rightarrow Aux NP$
$S \rightarrow book \mid include \mid prefer$
$S \rightarrow Verb NP$
$S \rightarrow X2 PP$
$S \rightarrow Verb PP$
$S \rightarrow VPPP$
$NP \rightarrow I \mid she \mid me$
$NP \rightarrow TWA \mid Houston$
$NP \rightarrow Det Nominal$
$Nominal \rightarrow book \mid flight \mid meal \mid money$
$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$
$VP ightarrow book \mid include \mid prefer$
$VP \rightarrow Verb NP$
VP ightarrow X2 PP
$X2 \rightarrow Verb NP$
$VP \rightarrow Verb PP$
VP o VP PP
$PP \rightarrow Preposition NP$

CKY Parsing: Intuition

- Consider the rule D → w
 - Terminal (word) forms a constituent
 - Trivial to apply
- Consider the rule A → B C
 - "If there is an A somewhere in the input, then there must be a B followed by a C in the input"
 - First, precisely define span [i, j]
 - If A spans from i to j in the input then there must be some k such that i < k < j
 - Easy to apply: we just need to try different values for k



CKY Parsing: Table

- Any constituent can conceivably span [i, j] for all $0 \le i < j \le N$, where N = length of input string
 - We need an $N \times N$ table to keep track of all spans...
 - But we only need half of the table
- Semantics of table: cell [i, j] contains A iff A spans i to j
 in the input string
 - Of course, must be allowed by the grammar!

				TO:			
		1	2	3	4	5	6
	0	0-1	0–2	0–3	0–4	0–5	0–6
ED OM:	1		1-2	1–3	1–4	1–5	1–6
FROM:	2			2–3	2–4	2–5	2–6
	3				3–4	3–5	3–6
	4					4–5	4–6
	5	·		·	·		5–6

CKY Parsing: Table-Filling

- In order for A to span [i, j]
 - A → B C is a rule in the grammar, and
 - There must be a B in [i, k] and a C in [k, j] for some i < k < j
- Operationally
 - To apply rule A → B C, look for a B in [i, k] and a C in [k, j]
 - In the table: look left in the row and down in the column

				10.			
		1	2	3	4	5	6
	0	0-1	0–2	0–3	0-4	0–5	0–6
EDOM	1		1-2	1–3	1–4	1–5	1–6
FROM:	2			2–3	2–4	2–5	2–6
	3				3–4	3–5	3–6
	4					4–5	4–6
	5						5–6

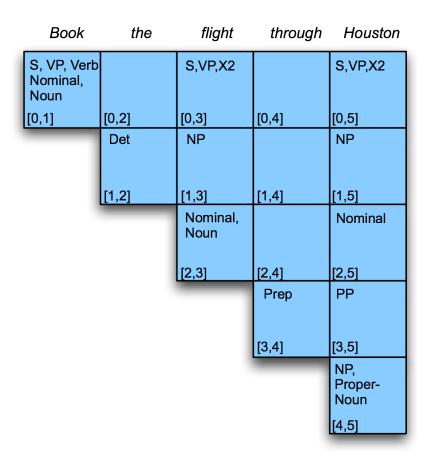
TO

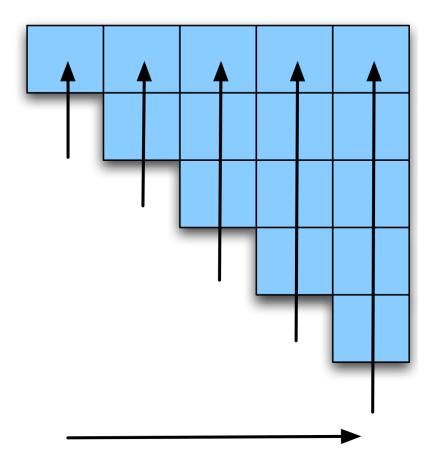
CKY Parsing: Canonical Ordering

- Standard CKY algorithm:
 - Fill the table a column at a time, from left to right, bottom to top
 - Whenever we're filling a cell, the parts needed are already in the table (to the left and below)

 Nice property: processes input left to right, word at a time

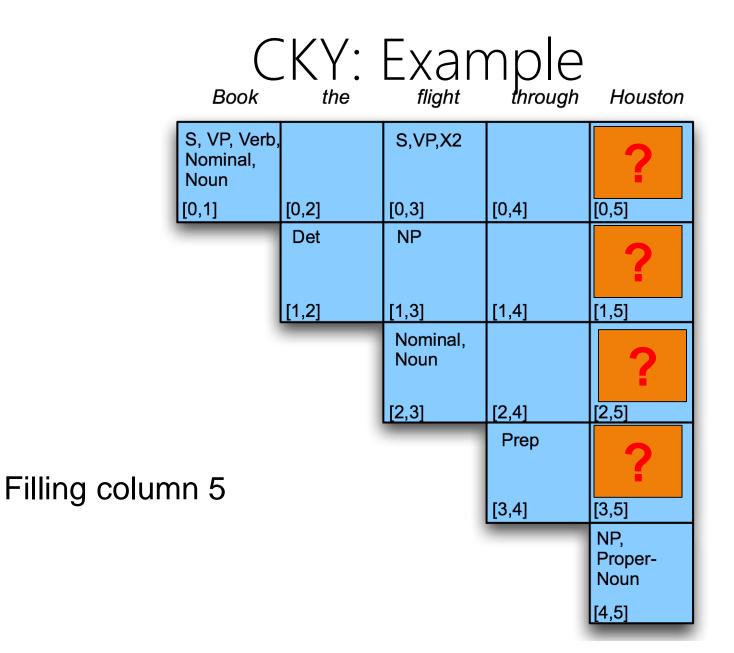
CKY Parsing: Ordering Illustrated





CKY Algorithm

function CKY-PARSE(words, grammar) **returns** table



Recall our CNF grammar:

•
$S \rightarrow NP VP$
$S \rightarrow X1 VP$
$X1 \rightarrow Aux NP$
$S \rightarrow book \mid include \mid prefer$
$S \rightarrow Verb NP$
$S \rightarrow X2 PP$
$S \rightarrow Verb PP$
$S \rightarrow VPPP$
$NP \rightarrow I \mid she \mid me$
$NP \rightarrow TWA \mid Houston$
$NP \rightarrow Det Nominal$
$Nominal \rightarrow book \mid flight \mid meal \mid money$
$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$
$VP \rightarrow book \mid include \mid prefer$
$VP \rightarrow Verb NP$
$VP \rightarrow X2 PP$
$X2 \rightarrow Verb NP$
$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$
$PP \rightarrow Preposition NP$

Book	the '	flight	through	Houston
S, VP, Verb, Nominal, Noun		S,VP,X2		?
[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
\neg	Det	NP		?
	[1,2]	[1,3]	[1,4]	[1,5]
		Nominal, Noun		?
		[2,3]	[2,4]	[2,5]
			Prep	?
			[3,4]	[3,5]
			\neg	NP, Proper- Noun
				[4,5]

Book	the	flight	through	Houston
S, VP, Verb, Nominal, Noun		S,VP,X2		?
[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
\neg	Det	NP		?
	[1,2]	[1,3]	[1,4]	[1,5]
		Nominal, Noun		?
		[2,3]	[2,4]	[2,5]
			Prep ← [3,4]	— PP [3,5] √
			[5,4]	
				NP, Proper- Noun
				[4,5]

Book	the	flight	through	Houston
S, VP, Verb, Nominal, Noun		S,VP,X2		?
[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	Det	NP		?
	[1,2]	[1,3]	[1,4]	[1,5]
	\neg	Nominal, ∢ Noun		–Nominal
		[2,3]	[2,4]	[2,5]
			Prep	PP
			[3,4]	[3,5]
			$\overline{}$	NP, Proper- Noun
				[4,5]

Recall our CNF grammar:

 $S \rightarrow NP VP$ $S \rightarrow X1 VP$ $X1 \rightarrow Aux NP$ $S \rightarrow book \mid include \mid prefer$ $S \rightarrow Verb NP$ $S \rightarrow X2 PP$ $S \rightarrow Verb PP$ $S \rightarrow VPPP$ $NP \rightarrow I \mid she \mid me$ $NP \rightarrow TWA \mid Houston$ $NP \rightarrow Det\ Nominal$ $Nominal \rightarrow book \mid flight \mid meal \mid money$ $Nominal \rightarrow Nominal Noun$ $Nominal \rightarrow Nominal PP$ $VP \rightarrow book \mid include \mid prefer$ $VP \rightarrow Verb NP$ $VP \rightarrow X2 PP$ $X2 \rightarrow Verb NP$ $VP \rightarrow Verb PP$ $VP \rightarrow VP PP$ $PP \rightarrow Preposition NP$

Book	the	flight	through	Houston
S, VP, Verb, Nominal, Noun		S,VP,X2		?
[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	Det ←	NP		NP
	[1,2]	[1,3]	[1,4]	[15]
		Nominal, Noun		Nominal
		[2,3]	[2,4]	[2,5]
			Prep	PP
			[3,4]	[3,5]
				NP, Proper- Noun
				[4,5]

Book	the	flight	through	Houst	on
S, VP, Verb; Nominal, Noun		S, VP, ≪ X2 ≪		-S ₁ ,VP, 2	
[0,1]	[0,2]	X2 < [0,3]	[0,4]	V	\Box
	Det	NP		NP	
	[1,2]	[1,3]	[1,4]	[1,5]	
	\neg	Nominal, Noun		Nomina	
		[2,3]	[2,4]	[2,5]	
			Prep	PF	3
			[3,4]	[3,5]	
				NP, Proper- Noun	
				[4,5]	

CKY Parsing: Recognize or Parse

Recognizer

- Output is binary
- Can the complete span of the sentence be covered by an S symbol?

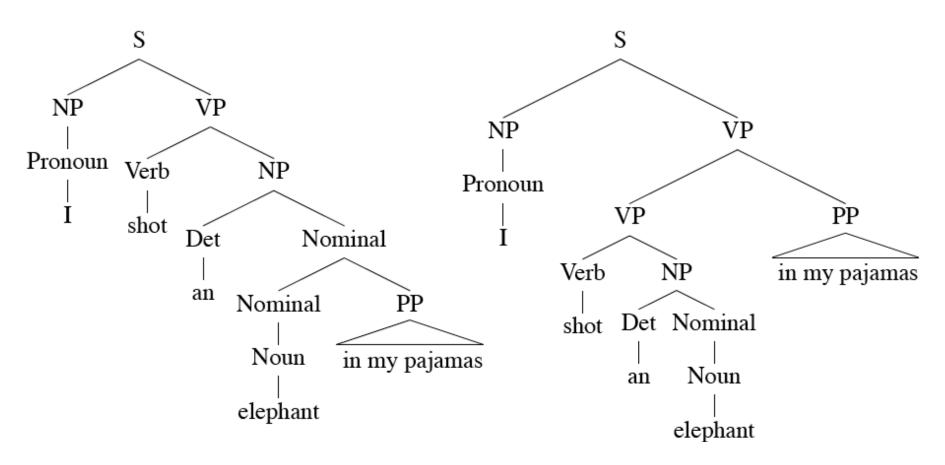
Parser

- Output is a parse tree
- From recognizer to parser: add backpointers!

Ambiguity

- CKY can return multiple parse trees
 - Plus: compact encoding with shared sub-trees
 - Plus: work deriving shared sub-trees is reused
 - Minus: algorithm doesn't tell us which parse is correct!

Ambiguity



PROBABILISTIC CONTEXT-FREE GRAMMARS

Simple Probability Model

- A derivation (tree) consists of the bag of grammar rules that are in the tree
 - The probability of a tree is the product of the probabilities of the rules in the derivation.

$$P(T,S) = \prod_{node \in T} P(rule(n))$$

Rule Probabilities

- What's the probability of a rule?
- Start at the top...
 - A tree should have an S at the top. So given that we know we need an S, we can ask about the probability of each particular S rule in the grammar: P(particular rule | S)
- In general we need $P(\alpha \rightarrow \beta \mid \alpha)$ for each rule in the grammar

Training the Model

We can get the estimates we need from a treebank

$$P(\alpha \to \beta | \alpha) = \frac{\text{Count}(\alpha \to \beta)}{\sum_{\gamma} \text{Count}(\alpha \to \gamma)} = \frac{\text{Count}(\alpha \to \beta)}{\text{Count}(\alpha)}$$

For example, to get the probability for a particular *VP* rule:

- count all the times the rule is used
- 2. divide by the number of *VP*s overall.

Parsing (Decoding)

How can we get the best (most probable) parse for a given input?

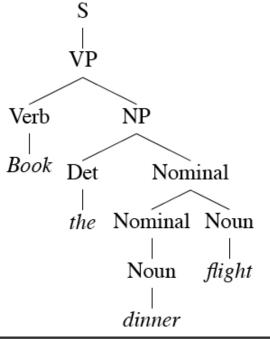
1. Enumerate all the trees for a sentence

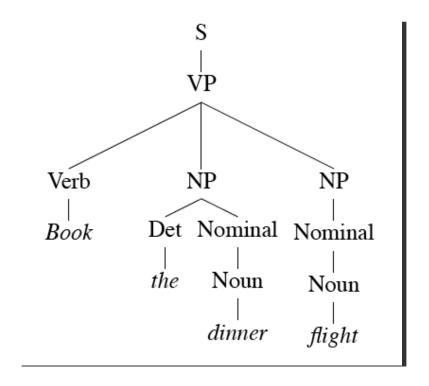
- 2. Assign a probability to each using the model
- 3. Return the argmax

Example

Consider...

Book the dinner flight





Examples

These trees consist of the following rules.

Rules			P		Rules		
S	\rightarrow	VP	.05	S	\rightarrow	VP	.05
VP	\rightarrow	Verb NP	.20	VP	\longrightarrow	Verb NP NP	.10
NP	\rightarrow	Det Nominal	.20	NP	\rightarrow	Det Nominal	.20
Nominal	\rightarrow	Nominal Noun	.20	NP	\rightarrow	Nominal	.15
Nominal	\longrightarrow	Noun	.75	Nominal	\longrightarrow	Noun	.75
				Nominal	\longrightarrow	Noun	.75
Verb	\rightarrow	book	.30	Verb	\rightarrow	book	.30
Det	\rightarrow	the	.60	Det	\rightarrow	the	.60
Noun	\longrightarrow	dinner	.10	Noun	\longrightarrow	dinner	.10
Noun	\rightarrow	flights	.40	Noun	\rightarrow	flights	.40

$$P(T_{left}) = .05 * .20 * .20 * .20 * .75 * .30 * .60 * .10 * .40 = 2.2 × 10-6$$

 $P(T_{right}) = .05 * .10 * .20 * .15 * .75 * .75 * .30 * .60 * .10 * .40 = 6.1 × 10-7$

Dynamic Programming

- Of course, as with normal parsing we don't really want to do it that way...
- Instead, we need to exploit dynamic programming
 - For the parsing (as with CKY)
 - And for computing the probabilities and returning the best parse (as with Viterbi and HMMs)

Probabilistic CKY

- Store probabilities of constituents in the table
 - table[i,j,A] = probability of constituent A that spans positions i through j in input
- If A is derived from the rule $A \rightarrow B C$:
 - table[i,j,A] = $P(A \rightarrow B C \mid A)$ * table[i,k,B] * table[k,j,C]
 - Where
 - $P(A \rightarrow B C \mid A)$ is the rule probability
 - table[i,k,B] and table[k,j,C] are already in the table given the way that CKY operates
- Only store the MAX probability over all the A rules.

Probabilistic CKY

function PROBABILISTIC-CKY(words,grammar) **returns** most probable parse and its probability

```
for j \leftarrow from 1 to LENGTH(words) do

for all \{A \mid A \rightarrow words[j] \in grammar\}

table[j-1,j,A] \leftarrow P(A \rightarrow words[j])

for i \leftarrow from j-2 downto 0 do

for k \leftarrow i+1 to j-1 do

for all \{A \mid A \rightarrow BC \in grammar,

and table[i,k,B] > 0 and table[k,j,C] > 0 }

if (table[i,j,A] < P(A \rightarrow BC) \times table[i,k,B] \times table[k,j,C]) then

table[i,j,A] \leftarrow P(A \rightarrow BC) \times table[i,k,B] \times table[k,j,C]

back[i,j,A] \leftarrow \{k,B,C\}

return BUILD_TREE(back[1, LENGTH(words), S]), table[1, LENGTH(words), S]
```

Problems with PCFGs

- The probability model we're using is just based on the bag of rules in the derivation...
 - 1. Doesn't take the actual words into account in any useful way.
 - 2. Doesn't take into account *where* in the derivation a rule is used
 - 3. Doesn't work terribly well

IMPROVING OUR PARSER

Improved Approaches

There are two approaches to overcoming these shortcomings

Rewrite the grammar to better capture the dependencies among rules

Integrate lexical dependencies into the model

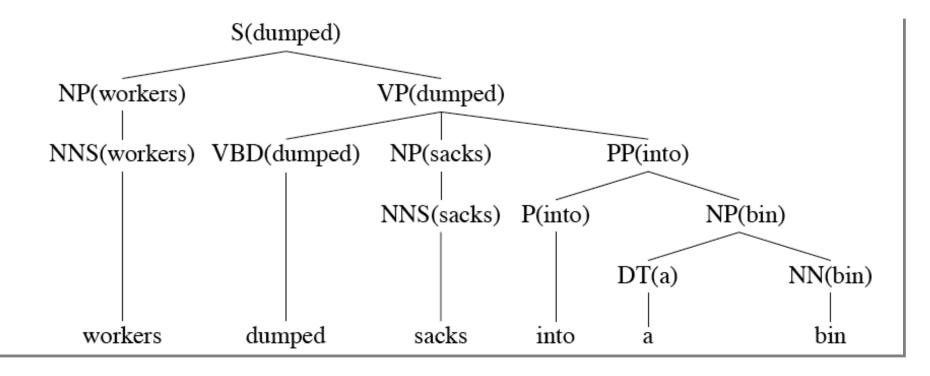
Solution 2: Lexicalized Grammars

Lexicalize the grammars with heads

Compute the rule probabilities on these lexicalized rules

Run Prob CKY as before

Lexicalized Grammars: Example



How can we learn probabilities for lexicalized rules?

- We used to have
 - $-VP \rightarrow VNPPP$
 - P(rule|VP) = count of this rule divided by the number of VPs in a treebank

- Now we have fully lexicalized rules...
 - VP(dumped)-> V(dumped) NP(sacks)PP(into)
 - P(r|VP ^ dumped is the verb ^ sacks is the head of the NP ^ into is the head of the PP)

We need to make independence assumptions

- Strategies: exploit independence and collect the statistics we can get
 - Many many ways to do this...
- Let's consider one generative story: given a rule we'll
 - 1. Generate the head
 - 2. Generate the stuff to the left of the head
 - 3. Generate the stuff to the right of the head

From the generative story to rule probabilities...

The rule probability for

```
P(VP(dumped, VBD) \rightarrow VBD(dumped, VBD) NP(sacks, NNS) PP(into, P)
```

Can be estimated as

```
P_H(VBD|VP, dumped) \times P_L(STOP|VP, VBD, dumped) \times P_R(NP(sacks, NNS)|VP, VBD, dumped) \times P_R(PP(into, P)|VP, VBD, dumped) \times P_R(STOP|VP, VBD, dumped)
```

Framework

- That's just one simple model
 - "Collins Model 1"

- Other assumptions that might lead to better models
 - make sure that you can get the counts you need
 - make sure they can get exploited efficiently during decoding

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 Tools for parsing English, Chinese, French, ... with PCFGs http://nlp.stanford.edu/software/lex-parser.shtml