

**PROGRAM STATEMENT:**For given set of values

$x$	0	1	3	3
$f(x)$	5	6	50	105

Compute the value of  $f(2)$  using Langrange's Interpolation Formula

**THEORY:** Let  $y=f(x)$  be a function defined in the interval  $[a,b]$  and is only known on a set of  $(n+1)$  distinct arguments,  $x_0, x_1, x_2, \dots, x_{r-1}, x_r, x_{r+1}, \dots, x_{n-1}, x_n$ , in general, are not equally spaced, in the interval of definition of  $f(x)$ . Lagrange's interpolation formula can be used to find a polynomial  $L(x)$  of degree not greater than  $n$ , such that  $L(x)$  replaces  $f(x)$  on the set of interpolation points  $x_j (j=0, 1, 2, \dots, n)$ .

$$L(x) = \sum_{r=0}^n w_r(x) / (x - x_r) * w'_r(x_r) * f(x_r)$$
 is called Lagrange's interpolation formula.

$w_r(x) = w(x) / (x - x_r) * w'_r(x_r)$ ,  $(r=0, 1, 2, \dots, n)$  is called the Lagrangian Function.

Where  $w(x)$  is a polynomial of degree  $n+1$  &

$w'_r(x_r) = (x_r - x_0)(x_r - x_1) \dots (x_r - x_n)$

**PROGRAM CODE:**

```
//C Program to implement Langrange's Interpolation Formula
#include <stdio.h>
int main()
{
    int n, i, j;
    printf("Enter number of arguments::");
    scanf("%d", &n);
    double f[n][n+4], x, d, w=1, s=0;
    printf("Enter values of x\n");
    for(i=0; i<n; i++)
    {
        scanf("%lf", &f[i][0]);
    }
    printf("Enter corresponding values of y\n");
    for(i=0; i<n; i++)
    {
        scanf("%lf", &f[i][n+2]);
    }
    printf("Enter the value of x for which you want to find the result::");
    scanf("%lf", &x);
    for(i=0; i<n; i++)
    {
        d=1;
        for(j=1; j<n+1; j++)
        {
            if(j==i+1)
            {
                f[i][j]=x-f[j-1][0];
                w=w*f[i][j];
            }
            else
            {
                f[i][j]=f[i][0]-f[j-1][0];
            }
        }
    }
}
```

```

        }
        d=d*f[i][j];
    }
    f[i][j]=d;
    f[i][j+2]=f[i][j+1]/d;
    s=s+f[i][j+2];
}
printf("The Computational Table is::\nx");
for(i=0;i<n-1;i++)
{
    printf("\t\t");
}
printf("Row Product=\t\tD\t\tty\t\tty/D\n");
for(i=0;i<n;i++)
{
    for(j=0;j<n+4;j++)
    {
        printf("%.2lf\t",f[i][j]);
    }
    printf("\n");
}
s=w*s;
printf("The value of y by langrange's formula is:%.2lf\n",s);
return 0;
}

```

### OUTPUT:

```

Enter number of arguments::4
Enter values of x
0 1 3 4
Enter corresponding values of y
5 6 50 105
Enter the value of x for which you want to find the result::2
The Computational Table is::
x          Row Product=          D          y          y/D
0.00  2.00  -1.00 -3.00 -4.00      -24.00      5.00      -0.21
1.00  1.00  1.00  -2.00 -3.00        6.00        6.00        1.00
3.00  3.00  2.00  -1.00 -1.00        6.00       50.00        8.33
4.00  4.00  3.00  1.00  -2.00      -24.00     105.00       -4.38
The value of y by langrange's formula is:19.00

```