

PROGRAM STATEMENT: Given $dy/dx=x^3+y$, $y(0)=1$, compute $y(.02)$, by Euler's Method taking step length $h=.01$

THEORY: Euler's method is simple and single-step but a crude numerical method for solving an ordinary initial value differential equation, where the solution will be obtained as a set of variables x and y .

Let us consider a first order and first degree differential eqn as:

$dy/dx=f(x,y)$, with $y(x_0)=y_0$.

Euler's general iteration formula is==>

$$y_n = y_{n-1} + hf(x_{n-1}, y_{n-1}) = y(x_n)$$

where h is the difference between two intervals & $f(x,y)$ is the function of x & y and x_r is the r 'th value of x and y_r is the r 'th value of y .

PROGRAM CODE:

```
//C Program to Find Solution of Ordinary Differential Equation of 1st Order
by Euler's Method
#include <stdio.h>
#include <math.h>
#define f(x,y) (pow(x,3)+y)
int main()
{
    int i;
    double x,y,h,s;
    printf("f(x,y)=x^3+y\nEnter Value of x::");
    scanf("%lf",&x);
    printf("Enter Value of y for x=%lf::",x);
    scanf("%lf",&y);
    printf("Enter Step length h::");
    scanf("%lf",&h);
    printf("Enter value of x for which y is to be computed::");
    scanf("%lf",&s);
    for(i=1;x<s;i++)
    {
        y=y+(h*f(x,y));
        x=x+h;
        printf("%d\ty(%.2lf)=%.8lf\n",i,x,y);
    }
    return 0;
}
```

OUTPUT:

```
f(x,y)=x^3+y
Enter Value of x::0
Enter Value of y for x=0.000000::1
Enter Step length h::.01
Enter value of x for which y is to be computed::.02
1    y(0.01)=1.01000000
2    y(0.02)=1.02010001
```