

**PROGRAM STATEMENT:** Using Regular-Falsi Method, find a root of  $x^3+2x-2=0$  correct upto 3 significant figures.

**THEORY :** In this method we first find a sufficiently small interval  $[a_0, b_0]$ , such that  $f(a_0)f(b_0) < 0$ , by tabulation or graphical method, and which contains only one root  $x$  (say) of  $f(x) = 0$ , i.e.,  $f(x)$  maintains same sign in  $[a_0, b_0]$ .

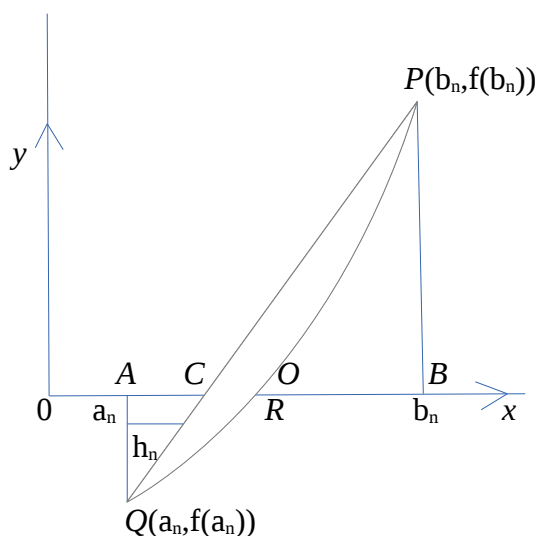
This method is method based on the assumption that the graph of  $y=f(x)$  in small interval  $[a_0, b_0]$  can be represented by the chord joining  $(a_0, f(a_0))$  and  $(b_0, f(b_0))$ . Therefore, the point  $x=a_1=a_0+h_0$  at which the chord meets the  $x$ -axis gives us an approximate value of the root  $x$  of the equation  $f(x)=0$ . Thus, we obtain two intervals  $[a_0, x_1]$  and  $[x_1, b_0]$ , one of which must contain the root  $x$ , depending upon the conditions  $f(a_0)f(x_1) < 0$  or  $f(x_1)f(b_0) < 0$ . If  $f(x_1)f(b_0) < 0$ , then  $x$  lies in the interval  $[x_1, b_0]$  which we rename as  $[a_1, b_1]$ . Again we consider that the graph of  $y=f(x)$  in  $[a_1, b_1]$  as the chord joining  $(a_1, f(a_1))$  and  $(b_1, f(b_1))$ , thus the point of intersection of the chord with the  $x$ -axis (say)  $x_2=a_1+h_1$  gives us an approximate value of the root  $x$  and  $x_2$  is called *second approximation* of the root  $x$ .

Proceeding in this way, we shall get a sequence  $\{x_1, x_2, x_3, \dots, x_n\}$ . Each member of which is the successive approximation of the exact root  $x$  of the equation  $f(x)=0$ .

Now we are going to establish an iteration formula which may generate a sequence of successive approximations of an exact root  $x$  of the equation  $f(x)=0$ , geometrically.

In the adjoining Fig. 6.8, we assume that one real root  $x$  of  $f(x)=0$  lies in the small interval  $[a_n, b_n]$  and  $f(a_n) < 0$  and  $f(b_n) > 0$ . Let  $PRQ$  be the graph of  $y=f(x)$  in  $[a_n, b_n]$  intersecting the  $x$ -axis at  $R$ .

Thus,  $x=0, R(=x)$  gives the exact value of the root  $x$ . If we consider curve  $PRQ$  as the chord  $PQ$ , in the small interval  $[a_n, b_n]$ , which intersects the  $x$ -axis at  $C$ , then  $OC=x_{n+1}=a_n+h_n$  approximates the root  $x$  of the equation  $f(x)=0$ .



Now from similar triangles  $AQC$  and  $CBP$ , we get ,

$$\frac{AC}{AQ} = \frac{CB}{BP} \quad \text{or} \quad AC = \frac{(AQ * CB)}{BP} = \frac{|f(a_n)|}{|f(b_n)|} (AB - AC)$$

$$\text{or} \quad AC [1 + \frac{|f(a_n)|}{|f(b_n)|}] = \frac{|f(a_n)|}{|f(b_n)|} \cdot AB = (b_n - a_n)$$

$$AC = h_n = \frac{\frac{|f(a_n)|}{|f(b_n)|} (b_n - a_n)}{1 + \frac{|f(a_n)|}{|f(b_n)|}}$$

$$x_{n+1} = a_n + h_n = a_n + \frac{|f(a_n)|(b-a)}{|f(a_n)| + |f(b_n)|}$$

### PROGRAM CODE:

```
//C Program to find the Soln of an Equation using Regular-Falsi Method
#include <stdio.h>
#include <math.h>
double eq(double x)
{
    return (pow(x,3)+2*x-2);
}
double mod(double x)
{
    if(x<0)
        return -x;
    else
        return x;
}
double error(int a)
{
    return 5*pow(10,-a-1);
}
int main()
{
    int i=0;
    double a,b,h=0.0,k,l,e;
    printf("The equation we are solving is-> x^3+2*x-2=0\n");
    printf("Enter value of a::");
    scanf("%lf",&a);
    printf("Enter value of b::");
    scanf("%lf",&b);
    printf("You need the answer correct upto how many decimal places? ::");
    scanf("%lf",&e);
    e=error(e);
    if((eq(a)>0&&eq(b)<0)|| (eq(b)>0&&eq(a)<0))//Condition that proves that
    the result lies between a and b
    {

printf("n\ta(n)\t\tb(n)\t\tf(a(n))\t\tf(b(n))\t\tf(h(n))\t\tf(x(n+1))\t\tf(x(n+1))\n");
        do
        {
            l=h;
            h=(mod(eq(a))*(b-a))/(mod(eq(a))+mod(eq(b)));
            k=a+h;
            printf("%d\t%lf\t%lf\t%lf\t%lf\t%lf\t%lf\n",i+
+ ,a,b,eq(a),eq(b),h,k,eq(k));
            if(eq(k)>0)
                b=k;
            else if(eq(k)<0)
                a=k;
            else
                break;
        }
    }
}
```

```

        }
        while(mod(1-h)>e);
        printf("The root is %.3lf\n",k);
    }
    else
    {
        printf("The result doesn't lie between a and b. Program
Terminated.\n");
    }
    return 0;
}

```

### OUTPUT:

The equation we are solving is- $x^3+2x-2=0$

Enter value of a::0

Enter value of b::1

You need the answer correct upto how many decimal places? ::3

n	a(n)	b(n)	f(a(n))	f(b(n))	h(n)	x(n+1)	f(x(n+1))
0	0.000000	1.000000	-2.000000	1.00	0.666667	0.666667	-0.370370
1	0.666667	1.000000	-0.370370	1.00	0.090090	0.756757	-0.053106
2	0.756757	1.000000	-0.053106	1.00	0.012266	0.769023	-0.007156
3	0.769023	1.000000	-0.007156	1.00	0.001641	0.770664	-0.000956
4	0.770664	1.000000	-0.000956	1.00	0.000219	0.770883	-0.000128
5	0.770883	1.000000	-0.000128	1.00	0.000029	0.770912	-0.000017

The root is 0.771