PROGRAM TITLE: Find the Minimum Path of all vertices from a given source in a Simple Graph using Dijkstra's Algorithm.

## PROGRAM ALGORITHM:

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Algo_Dijkstra's(G,S)
                //G is the Graph and S is the source vertex.
                               //Initially it is empty.
     Create a vertex set Q
     for each vertex v in G
                //Initialization.
     {
                                 //Unknown distance from source
           dist[v]=INFINITY
                                 //Previous Node is shortest path from source.
           prev[v]=UNDEFINED
                                 //All Nodes are in Q.
           add v to Q
     dist[S]=0
     remove S from Q
     while (Q is not empty)
           u=vertex in Q with minimum dist[u]
           remove u from Q
           for each neighbour v of u
                                 //Update all distances via u to all
                dist1=dist[u]+length(u,v) //unexplored vertices.
                if dist1<dist[v]</pre>
                      dist[v] = dist1
                      prev[v]=u
                 }
           }
     return (dist[],prev[])
}
PROGRAM CODE:
//C Program to find distance between two vertices using Dijkstra's
#include <stdio.h>
#include <stdlib.h>
#define datatype int
void create_graph(datatype **graph,int n)
{
     int i, j, x;
     datatype w;
     for(i=0;i<n;i++)
           for (j=0; j< n; j++)
                graph[i][j]=9999;
           }
     }
     printf("\tIdentify the adjoining vertices:");
     for(i=0;i<n;i++)
           printf("\n\tEnter the adjoining vertices of %d.Enter -99 to
stop::",i);
           for (j=0; j< n; j++)
                scanf("%d",&x);
```

if(x==-99)

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break;
                 else
                 {
                      if(graph[x][i]==9999)
                            printf("\tEnter corresponding weight::");
                            scanf("%d",&w);
                            graph[i][x]=w;
                      }
                      else
                            graph[i][x]=graph[x][i];
                      printf("\tEnter next adjoining vertex::");
                 }
           }
     }
}
void print_graph(datatype **graph,int n)
     int i,j;
     printf("\n\tThe Adjacency Matrix of the Graph is::");
     for(i=-1;i<n;i++)
           printf("\n");
           for (j=-1; j< n; j++)
                 if(i==-1)
                      printf("%d",j);
                 else if(j==-1)
                      printf("%d",i);
                 else
                      printf("%d",graph[i][j]);
                printf("\t");
           }
     printf("\n");
void print_path(int *prev,int n,int dest)
     int u=dest, i=n-1;
     int *s = (int*)malloc(n*sizeof(int));
     while (prev[u]!=-1)
      {
           s[i--]=u;
           u=prev[u];
      }
     s[i]=u;
     for(;i<n;i++)
           printf("%d-",s[i]);
      }
}
void dijkstra(datatype **graph,int n)
{
     int i,s,q=n,min,dest,u;
     datatype dist1;
     char ch='y';
     int *mark = (int*)malloc(n*sizeof(int));
```

```
datatype *dist = (datatype*)malloc(n*sizeof(datatype));
int *prev = (int*)malloc(n*sizeof(int));
for(i=0;i<n;i++)
     mark[i]=1;
     dist[i]=9999;
     prev[i]=-1;
}
printf("\n\tEnter the source vertex::");
scanf("%d",&s);
dist[s]=0;
while (q!=0)
     for (i=0, min=9999; i<n; i++)
           if((mark[i] == 1) && (dist[i] < min))</pre>
                 min=dist[i];
                 u=i;
           }
     mark[u]=0;
     q--;
     for(i=0;i<n;i++)
           if((graph[u][i]!=9999) && (mark[i]==1))
                 dist1=dist[u]+graph[u][i];
                 if(dist1<dist[i])</pre>
                 {
                       dist[i]=dist1;
                       prev[i]=u;
                 }
           }
     }
printf("\n\tThe distances from %d are:",s);
for(i=0;i<n;i++)
     printf("\n\to %d = %d", i, dist[i]);
do
     printf("\ntDo you want to display a path(y/n)::");
     getchar();
     scanf("%c",&ch);
     if(ch=='n'||ch=='N')
           break;
     printf("\tEnter destination::");
     scanf("%d", &dest);
     if(dist[dest]!=9999)
     {
           printf("\tThe path from %d to %d is::",s,dest);
           print_path(prev,n,dest);
     }
     else
           printf("\n\tNo Path.");
while (ch=='y'||ch=='Y');
```

```
int main()
     int n,i;
     printf("\n\tEnter the number of vertices::");
     scanf("%d",&n);
     datatype **graph= (datatype**)malloc(n*sizeof(datatype*));
     for(i=0;i<n;i++)
           graph[i] = (datatype*) malloc (n*sizeof (datatype));
     }
     create_graph(graph, n);
     print_graph(graph,n);
     dijkstra(graph,n);
     return 0;
}
OUTPUT:
```

```
Enter the number of vertices::6
Identify the adjoining vertices:
Enter the adjoining vertices of 0.Enter -99 to stop::1
Enter corresponding weight::7
Enter next adjoining vertex::2
Enter corresponding weight::9
Enter next adjoining vertex::5
Enter corresponding weight::14
Enter next adjoining vertex::-99
Enter the adjoining vertices of 1.Enter -99 to stop::0
Enter next adjoining vertex::2
Enter corresponding weight::10
Enter next adjoining vertex::3
Enter corresponding weight::15
Enter next adjoining vertex::-99
Enter the adjoining vertices of 2.Enter -99 to stop::0
Enter next adjoining vertex::1
Enter next adjoining vertex::5
Enter corresponding weight::10
Enter next adjoining vertex::3
Enter corresponding weight::11
Enter next adjoining vertex::-99
Enter the adjoining vertices of 3.Enter -99 to stop::2
Enter next adjoining vertex::1
Enter next adjoining vertex::4
Enter corresponding weight::6
Enter next adjoining vertex::-99
Enter the adjoining vertices of 4.Enter -99 to stop::3
Enter next adjoining vertex::5
Enter corresponding weight::9
Enter next adjoining vertex::-99
Enter the adjoining vertices of 5.Enter -99 to stop::0
Enter next adjoining vertex::2
```

```
Enter next adjoining vertex::4
     Enter next adjoining vertex::-99
     The Adjacency Matrix of the Graph is::
         1 2 3 4
-1
                             5
     9999 7
              9
                    9999 9999 14
0
          9999 10 15 9999 9999
1
2
         10 9999 11 9999 10
3
     9999 15 11 9999 6 9999
     9999 9999 9999 6 9999 9
4
5
     14 9999 10 9999 9 9999
     Enter the source vertex::0
     The distances from 0 are:
     t \circ 0 = 0
     to 1 = 7
     to 2 = 9
     to 3 = 20
     to 4 = 23
     to 5 = 14
     Do you want to display a path (y/n)::y
     Enter destination::4
     The path from 0 to 4 is::0-5-4-
     Do you want to display a path (y/n)::y
     Enter destination::5
     The path from 0 to 5 is::0-5-
     Do you want to display a path (y/n)::y
     Enter destination::3
     The path from 0 to 3 is::0-2-3-
     Do you want to display a path (y/n)::y
     Enter destination::2
     The path from 0 to 2 is::0-2-
     Do you want to display a path (y/n)::y
     Enter destination::1
     The path from 0 to 1 is::0-1-
     Do you want to display a path (y/n)::y
     Enter destination::0
     The path from 0 to 0 is::0-
     Do you want to display a path (y/n)::n
```

## **DISCUSSION:**

- 1. We use Adjacency Matrix for storing the graph.
- 2. Complexity is  $O(|V|^2)$
- 3. The default weight is set arbitrarily high so that it is not considered in the computations.
  - 4. The program works for both directed and undirected graph.