Assignment 4

EVR-5086 Fall 2025

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Assignment 4

To complete this assignment in R, I used the following packages:

- here: here() enables easy file referencing
- dplyr: functions for data manipulation
- tidyr: functions for reshaping data
- flextable: formatting tables
- ggplot2: for creating plots
- moments: functions for kurtosis and skewness
- fBasics: dagoTest() for the D'Agostino normality test

```
# Check if libraries are installed; install if not.
if (!require("pacman")) install.packages("pacman")
pacman::p_load(here, dplyr, flextable, ggplot2, tidyr, moments, fBasics)
```

To start, I read in MIA_J-D_T_Precip_inches.csv and assigned descriptive column names. Instead of computing the time series for one month at a time, I used dplyr::mutate() to divide each month's column by the total column. This results in a data frame of the fraction of the annual total by year and month. For the remainder of the assignment, I focus on the month of April. Figure 1 shows the fraction of annual rainfall in April in Miami, Florida, from 1906 to 2022. Table 1 reports the descriptive statistics, rounded to four significant digits, for the fraction of annual rainfall occurring in the month of April.

```
#Plot the time series for April's fraction of the annual total for each year
ggplot(mia_rain_fraction, aes(x = year, y = apr)) +
  geom_line() +
  labs(
    title = "Fraction of annual rainfall during April for Miami, Florida",
    subtitle = "Comparison between 1906 and 2022",
    x = "Year",
    y = "Fraction of annual rainfall during April"
)
```

Fraction of annual rainfall during April for Miami, Florida Comparison between 1906 and 2022

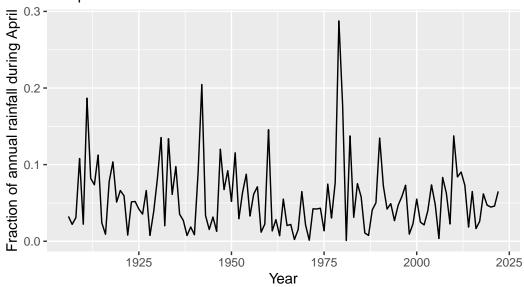


Figure 1: Fraction of annual rainfall during the month of April for the City of Miami, Florida, from 1906 to 2022.

Next, ahead of reshaping the data, I created factor levels to be able to rearrange the data by month of the year and computed the number of unique years in the data. In preparing the data for analysis, I reformatted the data, assigned factor levels, computed the log10-transformed data. In using pipes to reshape and add variables to the data, I reduced the number of intermediate objects created. Similarly with group_by() and summarize(), I was able to calculate various summary statistics at the same time for both the fraction and the log10 fraction of Miami rainfall by month.

The comparison of the histograms and Q-Q plots in Figure 2 show that the log10 transformed data appears more normal than the original data, but still show departures from the Q-Q line.

```
# Prep month levels for efficient ordering
month_levels <- c("jan", "feb", "mar", "apr", "may", "jun",</pre>
                  "jul", "aug", "sep", "oct", "nov", "dec")
# Calculate n
n_years <- n_distinct(mia_rain_fraction, "year")</pre>
# Prep data for upcoming analyses
mia_rain_fraction_tidy <- mia_rain_fraction |>
  # Remove total
  select(-total) |>
  # Reformat to tidy format (long)
  pivot_longer(
    cols = !year,
    names_to = "month",
    values to = "fraction"
  # Log transform monthly fractions and define month factor levels
  mutate(
    month = factor(month, levels = month_levels, ordered = TRUE),
    log10_fraction = log10(fraction)
  ) |>
  # Reformat to tidy format (long)
  pivot_longer(
    cols = !c(year, month),
    names_to = "stat",
    values_to = "values"
  ) |>
  # Sort by stat and year
```

```
arrange(stat, year, month)
# Compute descriptive statistics for mia rain fraction
mia_rain_fraction_summary <- mia_rain_fraction_tidy |>
  # Run calculation on unique combinations of year and stat
  group_by(month, stat) |>
  # Calculate summary stats
  summarise(min = round(min(values), 4),
            q1 = round(quantile(values, 0.25), 4),
            median = round(median(values), 4),
            mean = round(mean(values), 4),
            q3 = round(quantile(values, 0.75), 4),
            \max = \text{round}(\max(\text{values}), 4),
            variance = round(var(values), 4),
            sd = round(sd(values), 4),
            sk = round(skewness(values), 4),
            ku = round(kurtosis(values), 4),
            .groups = "drop") |>
  # Sort data by stat and month
  arrange(stat, month)
```

```
# Rearrange the summary statistics to print nicely for just April
apr_summary <- mia_rain_fraction_summary |>
 # Pivot the data so that the summary statistics have a long format
 pivot_longer(-c(month, stat), names_to = "metric", values_to = "value")|>
 # Pull out the stat into respective columns
 pivot_wider(names_from = stat, values_from = value) |>
 # Filter to just April
 filter(month == "apr") |>
 # Remove the month column
 select(-month) |>
 # Print reformatted and filtered data as a flextable
 flextable() |>
 # Include a blank first column header
 set_header_labels(metric = "") |>
 # Use simple format and autofit
 theme_booktabs() |>
 fontsize(size = 9, part = "all") |>
 autofit()
```

Print summary table
apr_summary

Table 1: Descriptive statistics for the fraction of annual rainfall during April for Miami, Florida between 1906 and 2022, and its log transformation.

	fraction	log10_fraction
min	0.0010	-3.0000
q1	0.0224	-1.6498
median	0.0470	-1.3279
mean	0.0560	-1.4140
q3	0.0735	-1.1337
max	0.2876	-0.5412
variance	0.0021	0.1850
sd	0.0463	0.4301
sk	1.8372	-1.0215
ku	5.0577	1.6156

```
# Create histogram
mia_rain_fraction_tidy |>
  filter(month == "apr", stat == "fraction") |>
  ggplot(aes(x = values)) +
  geom_histogram(bins = 30) +
  xlab("Fraction of annual rainfall in April") +
  ylab(paste0("Frequency (n = ", n_years, ")"))
# Create Q-Q plot
mia_rain_fraction_tidy |>
  filter(month == "apr", stat == "fraction") |>
  ggplot(aes(sample = values)) +
 stat_qq() +
 stat_qq_line() +
  xlab("Theoretical Quantiles") +
  ylab("Standardized residuals")
# Create histogram for log10 tranformed data
mia_rain_fraction_tidy |>
 filter(month == "apr", stat == "log10_fraction") |>
  ggplot(aes(x = values)) +
  geom_histogram(bins = 30) +
  xlab("Log10 transformed fraction of annual rainfall in April") +
  ylab(paste0("Frequency (n = ", n_years, ")"))
# Create Q-Q plot for log10 transformed data
mia_rain_fraction_tidy |>
  filter(month == "apr", stat == "log10_fraction") |>
  ggplot(aes(sample = values)) +
  stat_qq() +
  stat_qq_line() +
  xlab("Theoretical Quantiles") +
  ylab("Standardized residuals")
```

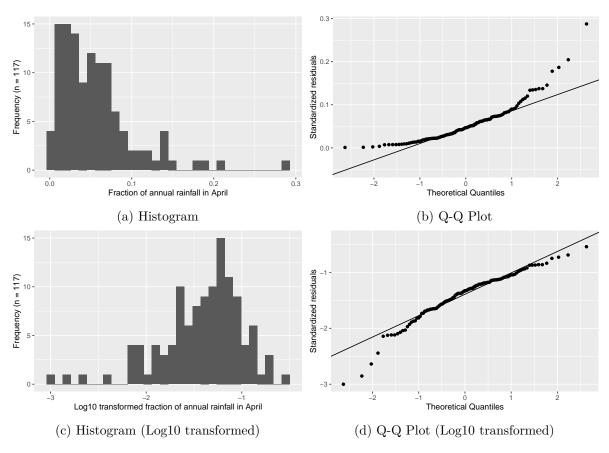


Figure 2: Histogram (a) and Q-Q plot (b) for the fraction of annual rainfall during April for Miami, Florida between 1906 and 2022, and histogram (c) and Q-Q plot (d) of the corresponding log transformed data.

I used the descriptive statistics from the previous exercise to generate samples from a known normal distribution. I compared 1,000 versus 21 samples. Figure 3 shows how the Q-Q Q-Q plot improves with more samples. Meanwhile, in Figure 4 we can see how much worse the Q-Q plot looks with fewer samples!

```
# Generate realizations of 1000 samples from known normal distribution
apr_rain_fraction_sample_1000 <- round(
  rnorm(n = 1000,
        mean = mia_rain_fraction_summary |>
          filter(stat == "fraction",
                 month == "apr") |> pull(mean),
        sd = mia_rain_fraction_summary$sd[1]), 4
# Generate realization of 21 samples from known normal distribution
apr_rain_fraction_sample_21 <- round(
  rnorm(n = 21,
        mean = mia_rain_fraction_summary |>
          filter(stat == "fraction",
                 month == "apr") |> pull(mean),
        sd = mia_rain_fraction_summary$sd[1]), 4
# Generate realization of 1000 samples from known normal log10 distribution
apr_rain_fraction_log10_sample_1000 <- round(</pre>
  rnorm(n = 1000,
        mean = mia_rain_fraction_summary |>
          filter(stat == "log10_fraction",
                 month == "apr") |> pull(mean),
        sd = mia_rain_fraction_summary$sd[1]), 4
)
# Generate realization of 21 samples from known normal log10 distribution
apr_rain_fraction_log10_sample_21 <- round(
  rnorm(n = 21,
        mean = mia_rain_fraction_summary |>
          filter(stat == "log10_fraction",
                 month == "apr") |> pull(mean),
        sd = mia_rain_fraction_summary$sd[1]), 4
```

```
# Create histogram with 1000 samples
ggplot() +
 aes(x = apr rain fraction sample 1000) +
 geom histogram(bins = 30) +
 xlab("Realized samples of the fraction of annual rainfall in April") +
 ylab("Frequency (n = 1,000)")
# Create Q-Q plot with 1000 samples
ggplot() +
 aes(sample = apr_rain_fraction_sample_1000) +
 stat_qq() +
 stat_qq_line() +
 xlab("Theoretical Quantiles") +
 ylab("Standardized residuals")
# Create histogram with 1000 log10 samples
ggplot() +
 aes(x = apr_rain_fraction_log10_sample_1000) +
 geom_histogram(bins = 30) +
 xlab("Realized samples of the log10 fraction of annual rainfall in April") +
 ylab("Frequency (n = 1000)")
# Create Q-Q plot with 1000 log10 samples
ggplot() +
 aes(sample = apr_rain_fraction_log10_sample_1000) +
 stat_qq() +
 stat_qq_line() +
 xlab("Theoretical Quantiles") +
 ylab("Standardized residuals")
```

Here we plot samples from the known normal distribution with only 21 samples.

```
# Create histogram with 21 samples
ggplot() +
   aes(x = apr_rain_fraction_sample_21) +
   geom_histogram(bins = 30) +
   xlab("Realized samples of the fraction of annual rainfall in April") +
   ylab("Frequency (n = 21)")

# Create Q-Q plot with 21 samples
ggplot() +
   aes(sample = apr_rain_fraction_sample_21) +
```

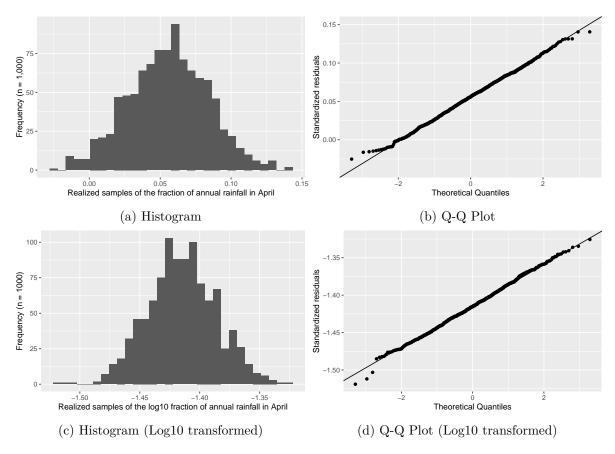


Figure 3: Histogram (a) and Q-Q plot (b) for 1000 samples realized from a normal distribution based on the fraction of annual rainfall during April for Miami, Florida between 1906 and 2022, and histogram (c) and Q-Q plot (d) of the corresponding log transformed data.

```
stat_qq() +
 stat_qq_line() +
 xlab("Theoretical Quantiles") +
 ylab("Standardized residuals")
# Create histogram with 21 log10 samples
ggplot() +
 aes(x = apr_rain_fraction_log10_sample_21) +
 geom_histogram(bins = 30) +
 xlab("Realized samples of the log10 fraction of annual rainfall in April") +
 ylab("Frequency (n = 21)")
# Create Q-Q plot with 21 log10 samples
ggplot() +
 aes(sample = apr_rain_fraction_log10_sample_21) +
 stat_qq() +
 stat_qq_line() +
 xlab("Theoretical Quantiles") +
 ylab("Standardized residuals")
```

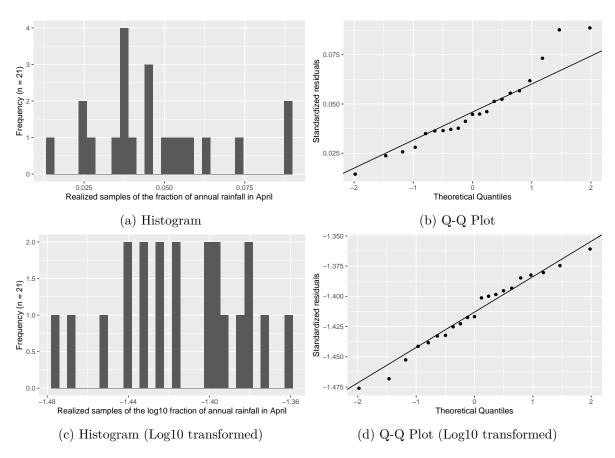


Figure 4: Histogram (a) and Q-Q plot (b) for 21 samples realized from a normal distribution based on the fraction of annual rainfall during April for Miami, Florida between 1906 and 2022, and histogram (c) and Q-Q plot (d) of the corresponding log transformed data.

I used dagoTest() to run the D'Agostino normality test on:

- 1. the fraction of annual rainfall for April
- 2. the log10 transformed fraction of annual rainfall for April
- 3. 1,000 realized samples from a normal distribution
- 4. 1,000 realized samples from a log10 transformed normal distribution
- 5. the waiting time between Old Faithful's eruptions
- 6. the log10 transformed waiting time between Old Faithful's eruptions

In Figure 5, I include histograms and Q-Q plots for the waiting time between Old Faithful's eruptions. Table 2 provides key values for the normality tests listed above. In reading more about the test, I was reminded that the null hypothesis of the data being drawn from a normally distributed population is rejected when the p-value is less than the significance level (0.05). Following this decision rule, all of the tests listed above were rejected, except the samples that were realized from a normal distribution (numbers 3 and 4 above). This result aligns with the Q-Q plots shown previously, where all of them show departures from the expected theoretical quantiles, except the 1,000 realized samples that generated using a normal distribution (Figure 3).

```
# Calculate sample size
n_eruptions <- length(faithful$waiting)</pre>
# Create histogram
faithful |>
  ggplot(aes(x = waiting)) +
  geom_histogram(bins = 30) +
  xlab("Waiting time between Old Faithful's eruptions") +
  ylab(paste0("Frequency (n = ", n_eruptions, ")"))
# Create Q-Q plot
faithful |>
  ggplot(aes(sample = waiting)) +
  stat_qq() +
  stat_qq_line() +
  xlab("Theoretical Quantiles") +
  vlab("Standardized residuals")
# Create histogram for log10 transformed data
faithful |>
  ggplot(aes(x = log10(waiting))) +
  geom_histogram(bins = 30) +
```

```
xlab("Log10 transformed waiting time between Old Faithful's eruptions") +
ylab(paste0("Frequency (n = ", n_eruptions, ")"))

# Create Q-Q plot for log10 transformed data
faithful |>
ggplot(aes(sample = log10(waiting))) +
stat_qq() +
stat_qq_line() +
xlab("Theoretical Quantiles") +
ylab("Standardized residuals")
```

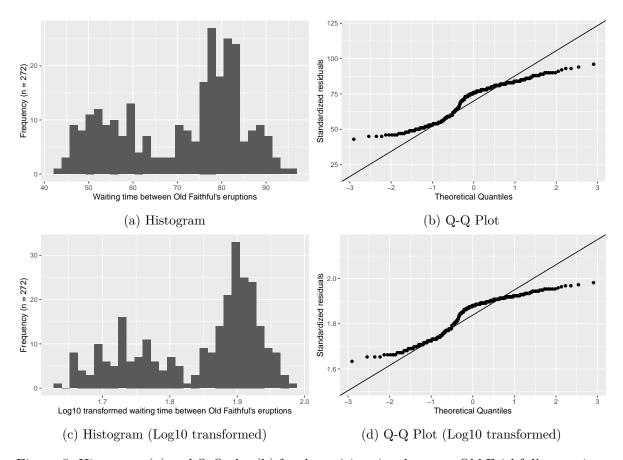


Figure 5: Histogram (a) and Q-Q plot (b) for the waiting time between Old Faithful's eruptions, and histogram (c) and Q-Q plot (d) of the corresponding log transformed data.

```
# Normal tests on rainfall data, sample realization, and Old Faithful
dago_mia_rain <- dagoTest(mia_rain_fraction$apr)
dago_mia_rain_log10 <- dagoTest(log10(mia_rain_fraction$apr))
dago_mia_rain_sample_1000 <- dagoTest(apr_rain_fraction_sample_1000)
dago_mia_rain_log10_sample_1000 <- dagoTest(apr_rain_fraction_log10_sample_1000)
dago_faithful <- dagoTest(faithful$waiting)
dago_faithful_log10 <- dagoTest(log10(faithful$waiting))</pre>
```

```
# Collect results in a tibble for table output
dagoTest_results <- tibble(</pre>
  test = c(
    "April fraction",
    "April log10(fraction)",
    "April Normal sample (n = 1000)",
    "April log10 Normal sample (n = 1000)",
    "Old Faithful waiting",
    "log10(Old Faithful waiting)"
 ),
  chi square = c(
    round(dago_mia_rain@test$statistic[1], 4),
    round(dago_mia_rain_log10@test$statistic[1], 4),
   round(dago_mia_rain_sample_1000@test$statistic[1], 4),
   round(dago_mia_rain_log10_sample_1000@test$statistic[1], 4),
   round(dago_faithful@test$statistic[1], 4),
   round(dago_faithful_log10@test$statistic[1], 4)
 ),
 p_value = c(
    round(dago_mia_rain@test$p.value[1], 4),
    round(dago_mia_rain_log10@test$p.value[1], 4),
    round(dago_mia_rain_sample_1000@test$p.value[1], 4),
    round(dago_mia_rain_log10_sample_1000@test$p.value[1], 4),
   round(dago_faithful@test$p.value[1], 4),
    round(dago_faithful_log10@test$p.value[1], 4)
 )
```

```
# Flextable
flextable(dagoTest_results) |>
    set_header_labels(test = "", chi_square = "2", p_value = "p-value") |>
    colformat_num(j = c("chi_square", "p_value"), digits = 4) |>
    theme_booktabs() |>
    fontsize(size = 9, part = "all") |>
    autofit()
```

Table 2: Chi-squared and p-value statistics from various normality tests conducted using the D'Agostino-Pearson omnibus normality test.

	χ²	p-value
April fraction	59.3249	0.0000
April log10(fraction)	24.3791	0.0000
April Normal sample (n = 1000)	0.7250	0.6959
April log10 Normal sample (n = 1000)	0.0705	0.9654
Old Faithful waiting	109.2417	0.0000
log10(Old Faithful waiting)	55.5880	0.0000

I also computed the ranks and return periods for April rainfall. When preparing the data for the plot, I noticed that it was necessary for the ranking to have a negative sign to generate a descending ranking. Lastly, in my first attempt of the plot with the logarithmic x-axis ticks, I realized I was accidentally doing log10 twice. When I use scale_x_log10 to adjust the x-axis scale, I noticed I need to read in the non-transformed data. That way the axis values in Figure 6 reflect the actual return periods in years, but the spacing is logarithmic.

```
# Rank April rainfall and compute return period
apr_rank <- mia_rain |>
 select(apr) |>
 # sort largest to smallest
 arrange(desc(apr)) |>
 # Create rank and compute return period
 mutate(
   rank = row_number(),
   recurrence = (n_years + 1) / rank,
   log10_recurrence = log10(recurrence)
 )
# Plot ranked rainfall amounts as a function of the log10 of the return period
ggplot(apr_rank, aes(x = recurrence, y = apr)) +
 geom_point() +
 scale_x_log10(
    breaks = c(1, 10, 100),
    labels = c("1", "10", "100")
 ) +
 labs(x = "Return period (years, log scale)", y = "Ranked April rainfall (inches)")
```

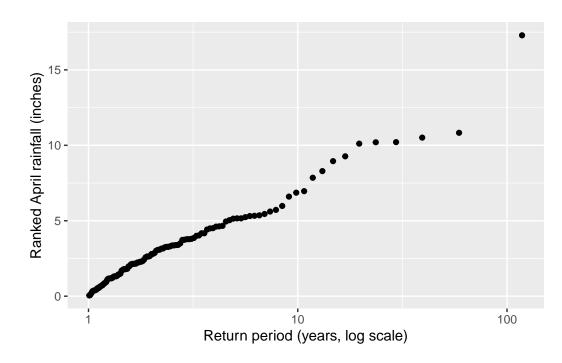


Figure 6: Ranked rainfall ammounts for the month of April as a function of the $\log 10$ of the returneriod in years.