

Lattice  $L \times L$  with Periodic Boundary Conditions (PBCs).

Since we have an  $L \times L$  spin matrix, in order to impose PBCs but most important! taking into account the Von-Neumann neighbors then in order to calculate the neighbors sum  $S_o(\vec{x})$  we create an extended spin matrix "e-spins" which is  $(L+2) \times (L+2)$  where at the corners is zero and has the following structure.:

