

## Tutorial #6. Sorting

### Theoretical part

Sorting allows us to do multiple tasks:

- Sorted elements can be found in  $O(\log(n))$  for search using binary/interpolation search (or even a place they should be inserted)
- They allow us to select linked areas of data in  $O(n)$  time (SELECT \* FROM T where C1 > V1).
- They allow us to make cool math (Principal Component Analysis include sorts, create a polygon of points, compression with loss algorithms involve sorting)
- They allow us to represent data for humans.

### Faster sorts

There's a class of sorts that allow us to do it in  $T(n \cdot \log(n))$  time: **quick sort**, that involves recursive strategy, **heap sort** and **merge sort**. Some of them provide  $O(n \cdot \log(n))$ , some –  $\Omega(n \cdot \log(n))$ .

### $O(n)$ -sorts

Unlike bubble and insertion sort, there's a class of algorithms that does not involve comparison. All  $O(n)$  sorts are non-comparative, because it is proven, that comparative sorts cannot perform better than  $\Omega(n \cdot \log(n))$ . We already know **counting sort**, it takes  $O(n+k)$ . There are also two well-known non-comparative sorts:

- **Bucket sort (Explain)**. Idea is to
  - o Split the range of values into buckets [1-50, 51-100, ...].
  - o Then **Scatter**: place items in the buckets according to the value (value /  $N_{\text{buckets}}$ ).
  - o Sort each non-empty bucket.
  - o Then **Gather**: collect values back into array
    - Worst case:  $O(n^2)$ ,
    - best/average case  $E(n+k)$  (use count sort inside the bucket)
  - o Study this sort and try to implement it for integers.
- **Radix sort (Just mention)**. Similar idea: use digits as buckets.

### Practical part (for Students)

- 1) Implement **insertion sort** using **Comparator** object for case insensitive string sorting.
- 2) Embed your implementation into **MyFramework.sort(...)** method, reuse the *Comparable.compareTo(...)* in comparator object.
- 3) Run tests in **MyFramework** class. See the output.
- 4) Uncomment line 22 in **MyFrameworkTests**. Measure **select** operation speed before and after this operation.
- 5) \*Try to implement  $O(n)$  sort