Exploring the Effects of Time Dilation on Formula 1 Drivers

Aging (or Not) at High Speeds

Ari Singh

March 29, 2023

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- 2 The Data
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Time Dilation?

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The lengthening of the time interval between two events for an observer in an inertial frame that is moving with respect to the rest frame.

$$T = \gamma T_0$$

Explained by Einstein's special relativity



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- Only noticeable in very fast things
- Always observed, though



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Formula 1 (F1) – the highest class of international racing...



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How much more time has passed for the audience over the course of a season than for the drivers, thanks to the effects of time dilation?



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How much more time has passed for the audience over the course of a season than for the drivers, thanks to the effects of time dilation?

How?

I'll use Formula 1 lap times from the 2020, 2021, and 2022 seasons to approximate the time delta.



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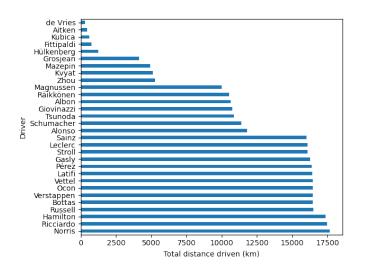
Warning

This approximation is the best it gets, but it isn't perfect.

- This estimated velocity is not really constant, relative to the spectators.
- The drivers follow the track's curves, accelerating and decelerating around.

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Meet the Drivers



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Meet the Drivers

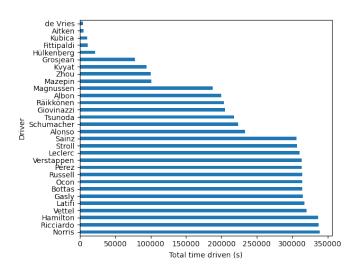


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$$T_0 = \left(\sqrt{1 - \frac{v^2}{c^2}}\right) T$$

Since I want the difference in the two intervals, my final result looks like:

$$\Delta T = T - T_0$$

$$\Delta T = T - \left(\sqrt{1 - \frac{v^2}{c^2}}\right) T$$

$$\Delta T = \left(1 - \sqrt{1 - \frac{v^2}{c^2}}\right) T$$

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```
c = 299792458 # in m/s

def time_finder(df):
   total_length = mp.fsum(df['length']) # in m
   total_seconds = mp.fdiv(mp.fsum(df['milliseconds']), 1000) # in s
   avg_speed = mp.fdiv(total_length, total_seconds) # in m/s

   time_factor = mp.fsub(1, mp.sqrt(mp.fsub(1, mp.power(mp.fdiv(avg_speed, c), 2))
   return mp.fmul(total_seconds, time_factor)
```

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Important consideration

With numbers this small, I need to use more precision in my math. I used the mpmath library to accomplish this.

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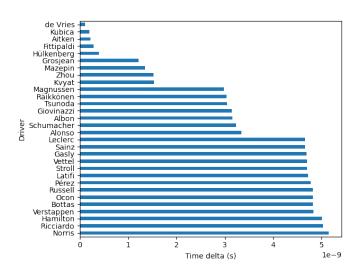


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Results

Season	Time Delta (10^{-8} s)
2020	2.92
2021	3.34
2022	3.36

Results



Results

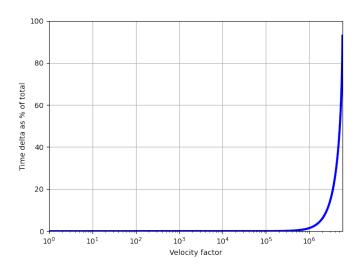




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- The effects of time dilation on F1 drivers are minimal, as expected
- Different answers could be reached with different assumptions
 - Aren't the spectators moving through space?
- Questions!

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Sources

- Ergast developer api.
- Length contraction.
- Welcome to mpmath's documentation!
- List of formula one circuits, Mar 2023.
- LIBRETEXTS, 5.4: Time dilation, Sep 2022.

Singh