

# Using Embeddings to Correct for Unobserved Confounding in Networks

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## Setup

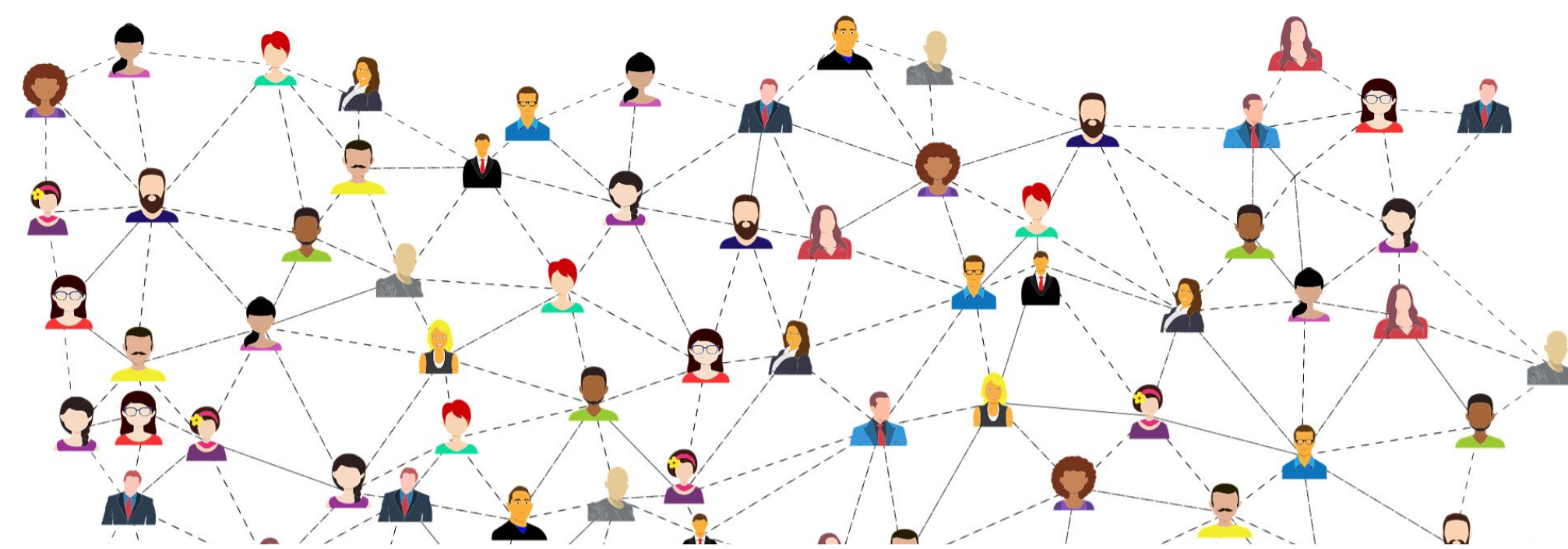
- Goal: infer (causal) average treatment effect  $\psi$  of treatment  $T$  on outcome  $Y$

$$\psi = \mathbb{E}[Y \mid \text{do}(T = 1)] - \mathbb{E}[Y \mid \text{do}(T = 0)]$$

- Problem: unobserved confounder  $Z$  might affect  $T$  and  $Y$
- Salvation: we observe a surrogate  $X$  for  $Z$

## The surrogate is nasty

- Network (non-iid) structure  
 $\implies$  standard non-parametrics = :(
- no plausible generative model for  $(X, \{Z_i\}, \{T_i\}, \{Y_i\})$ :  
 $\implies$  standard parametrics = :(



## Example: Social Network

- Have treatments and outcomes of people in a social network.
- Maybe latent confounders; age, sex, affinity for punk rock.
- These are associated with the social network itself.

## If life was easy, we'd observe $\{Z\}$

- estimate  $\hat{Q}_n(t, z) \approx Q(t, z) = \mathbb{E}[Y \mid t, z]$
- estimate  $\hat{g}_n(z) \approx g(z) = \mathbb{P}(T = 1 \mid z)$
- plug-in to (non-parametrically efficient, robust) estimator

## Or at least have a good generative model

- estimate  $\{\hat{z}_{n,i}\}$ .
- plug-in as though  $z$  observed.
- works if  $\hat{z}_{n,i}$  is really good estimate.
- but generative models for networks suck  $\implies$  :(

[1] V. Veitch, M. Austern, W. Zhou, D.M. Blei, and P. Orbanz. Empirical Risk Minimization and Stochastic Gradient Descent for Relational Data. 2018.

[2] L. Takac and M. Zabovsky. Data Analysis in Public Social Networks. 2012

## Overview

- A network connecting units can be a surrogate for unobserved confounding
- Insight: identification only requires treatment and outcome predictions
- Causal adjustment achieved by adapting black-box node embeddings
- IF [pure homophily] and [black-box predictor works]  
 THEN correct estimation at parametric rate

## So What?

- Doesn't require knowledge of relationship between network and confounding
- Stop worrying and love the black box

## Method

- Assign embedding  $\lambda_i \in \mathbb{R}^p$  for each unit  $i$
- Not justified by generative model, but kickass for prediction
- Train by *jointly* minimizing (we use [1] default)
  - graph reconstruction on subgraphs
  - predictor  $\hat{g}^T(\lambda)$  for  $T$  from embedding (minimize CrossEnt)
  - predictor  $\hat{Q}^Y(t, \lambda)$  for  $Y$  from treatment  $t$  and  $\lambda$  (minimize MSE)
- Plug into modified A-IPTW estimator

$$\begin{aligned} \hat{\psi}_n^A &= \frac{1}{n} \sum_i \hat{Q}_n(1, z_i) - \hat{Q}_n(0, z_i) \\ &+ \frac{1}{n} \sum_i \left( \frac{I[t_i = 1]}{\hat{g}_n(z_i)} - \frac{I[t_i = 0]}{1 - \hat{g}_n(z_i)} \right) (y_i - \hat{Q}_n(t_i, z_i)) \end{aligned}$$

## Assumptions and Validity

- IF Many technical conditions
- IF Pure homophily and observing  $Z$  would make identifiable
- IF The model learns something, eventually. For  $t \in \{0, 1\}$ :

$$\|\mathbb{E}[Y \mid T = t, Z] - \tilde{Q}(t, \hat{\lambda}_{n,i}, \hat{\gamma}_n^Q)\|_2 \|\mathbb{P}(T = 1 \mid Z) - \tilde{g}(\hat{\lambda}_{n,i}, \hat{\gamma}_n^g)\|_2 = o\left(\frac{1}{\sqrt{n}}\right)$$

- Asymptotically, the embeddings are independent-ish. For all bounded continuous  $f$  with mean 0,  $\mathbb{E}[f(\hat{\lambda}_i)f(\hat{\lambda}_j)] = o(\frac{1}{n})$

THEN

$\hat{\psi}_n^A$  converges to the ATE  $\psi$  at  $\sqrt{n}$ -rate.

## Example: Pokec

Semi-synthetic data using a large social network (Pokec) [2].

Conf.	age		district		join date	
	Low	High	Low	High	Low	High
Unadjusted	1.32 $\pm$ 0.02	4.34 $\pm$ 0.05	1.34 $\pm$ 0.03	4.51 $\pm$ 0.05	1.29 $\pm$ 0.03	4.03 $\pm$ 0.06
Parametric	1.30 $\pm$ 0.00	4.06 $\pm$ 0.01	1.21 $\pm$ 0.00	3.22 $\pm$ 0.01	1.26 $\pm$ 0.00	3.73 $\pm$ 0.01
Two-stage	1.33 $\pm$ 0.02	4.55 $\pm$ 0.05	1.34 $\pm$ 0.02	4.55 $\pm$ 0.05	1.30 $\pm$ 0.03	4.16 $\pm$ 0.06
$\hat{\psi}_n^A$	1.24 $\pm$ 0.04	3.40 $\pm$ 0.04	1.09 $\pm$ 0.02	2.03 $\pm$ 0.07	1.21 $\pm$ 0.05	3.26 $\pm$ 0.09

Outcome and propensity simulated using labeled attribute as hidden confounder. Ground truth is 1. Network adjustment always helps relative to baseline.