

02458 Cognitive Modelling – Bayes Exercise 1

In this exercise we'll try and solve a perceptual problem using the Bayesian approach. The problem is to infer the 3-dimensional structure of a wireframe from a 2-dimensional projection image. The structure is called S and the image is called I . The Bayesian approach is to maximize the posterior probability $P(S|I)$. For practical reasons we will minimize the negative logarithm of the posterior probability instead.

We'll use Matlab and the first thing you have to do is to get all the Matlab files that comes with the exercise and put them in your active directory.

Question 1

We'll first work with a cube. Open the Matlab function `NeckerExercise.m`. It is commented so try and read it to see what it does. It can almost solve the problem by numerically maximizing the posterior probability $P(S|I)$. We use Matlab's optimization routine `fminunc` (function *minimization unconstrained*). This routine calls the function `NeckerError` which is nested in the `NeckerExercise` function. The program is almost ready to run only the `NeckerError` function is not quite ready. All you have to do is specifying the negative logarithm of the posterior probability in the variable `NegLogPost` on line 77. Start with a uniform prior probability so that the posterior is simply the likelihood. That won't work, but it'll be illustrative. Then try using some clever prior. If you want you can use the calculation of the angles of the wireframe structure calculated in the variable `Angels` (a prior for right angles will work well for the cube).

Question 2

Do the same thing with a hexagon cylinder to test whether the prior you came up with for the cube also works for a different structure. Open the Matlab function `HexagonalExercise.m`. It works just like `NeckerExercise.m`. Try a flat prior and try the prior you found in 5.1. Why doesn't it work? Can you come up with a prior that works? Is it a realistic model for how the brain works.

Question 3

Evolution gave us two eyes for a reason. So far you've solved the problem using only one eye. Now solve it using two. Do you still need the prior? Explain why/why not.