Pondering on the God Equation

Arithmoi Foundation

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Imagine Infinite Power

Imagine an equation so profound that it encodes the logic of existence itself. In the philosophy of ontological mathematics, as articulated by Mike Hockney, reality is not built from matter or energy, but from mathematics—living, generative, and eternal. At the heart of this vision is the God Equation: a simple formula that unfolds into the infinite complexity of the universe.

The God Equation: Euler's Formula

The journey begins with one of the most celebrated equations in mathematics:

$$e^{ix} = \cos(x) + i\sin(x)$$

where:

- e (Euler's number, pronounced "OY-ler's number") is the base of natural logarithms, approximately 2.71828.
- i (the imaginary unit, pronounced "eye") is defined by $i^2 = -1$.
- $\cos(x)$ and $\sin(x)$ are the cosine and sine trigonometric functions.

This elegant formula is more than a bridge between exponentials and trigonometry—it is, in Hockney's framework, the fundamental pattern from which existence emerges.

The God Equation via Euler's Identity

A particularly striking case of Euler's formula appears when $x = \pi$:

$$e^{i\pi} + 1 = 0$$

or, rearranged:

$$e^{i\pi} = -1$$

where:

• π (the Greek letter "pi," pronounced "pie") is the mathematical constant, approximately 3.14159, representing the ratio of a circle's circumference to its diameter.

This identity unites the five most important numbers in mathematics: e, i, π , 1, and 0. As Hockney emphasizes, this identity is a powerful and elegant mathematical statement, celebrated for its beauty and its ability to capture the unity of mathematics in a single expression. It shows how the God Equation, even in its simplest form, contains the seeds of all reality.

The Generalized God Equation: The Living Frequency

To express the full generative power of mathematical existence, Hockney presents the generalized God Equation as the most abstract and universal form of Euler's formula:

$$A e^{i\theta} = A\cos(\theta) + iA\sin(\theta)$$

where:

- A is the amplitude (maximum value or strength of the wave).
- θ (the Greek letter "theta," pronounced "THAY-tuh") is a phase parameter that may encode frequency, position, time, or any combination thereof.

This generalization emphasizes the timeless, frequency-based nature of reality. In the language of pure frequency, it is sometimes written as:

$$A e^{if} = A\cos(f) + iA\sin(f)$$

where:

• f is the frequency parameter.

For particular physical phenomena, θ can represent a combination of variables such as:

$$\theta = \omega t + kx + \phi$$

where:

- ω (the Greek letter "omega," pronounced "oh-MAY-guh") is the angular frequency, describing how rapidly the phase oscillates, measured in radians per unit time.
- k is the wave number, relating to the spatial frequency (number of wave cycles per unit distance).
- ϕ (the Greek letter "phi," pronounced "fye" or sometimes "fee") is the phase offset, determining the initial angle or shift of the wave.

leading to the familiar wave form:

$$A e^{i(\omega t + kx + \phi)} = A \cos(\omega t + kx + \phi) + iA \sin(\omega t + kx + \phi)$$

where all variables are as explained above.

However, Hockney's ontological mathematics maintains that the **core reality** is the superposition of all possible frequency-based terms, each of the fundamental form $Ae^{i\theta}$, with their corresponding sine and cosine components.

Sinusoidal Waves: The Fabric of Existence

In ontological mathematics, everything—matter, mind, energy, and even space and time—is ultimately made of sinusoidal waves. These waves are combinations of the sine and cosine functions, as revealed in Euler's formula. Sine and cosine are not just mathematical abstractions; they are the very basis of energy and reality itself.

Every phenomenon is constructed from these fundamental waves. When combined in different ways—varying amplitude (A), frequency $(\omega \text{ or } f)$, and phase (ϕ) —they form

the infinite diversity of structures we observe in the universe. The interplay of sine and cosine underpins all vibration, oscillation, and energy flow. In this view, energy is a manifestation of these mathematical waveforms, and reality is the superposition of all possible sinusoidal modes.

Fourier Mathematics: The Architecture of Reality

This vision is made rigorous through Fourier analysis, which states that any function—any signal, structure, or process—can be expressed as a sum of sinusoidal waves:

$$f(x) = \sum_{n = -\infty}^{\infty} c_n e^{in\omega x} = \sum_{n = -\infty}^{\infty} (c_n \cos(n\omega x) + ic_n \sin(n\omega x))$$

where:

- \sum (the Greek capital letter "sigma," pronounced "SIG-muh") denotes summation, meaning to add up terms over a given range.
- c_n are complex coefficients encoding amplitude and phase for each frequency component.
- ω ("omega") is the angular frequency, as above.
- i is the imaginary unit, as above.

This mathematical principle shows that the God Equation, through the sine and cosine basis, is sufficient to build any possible reality. Every entity—whether a particle, a field, or a thought—is ultimately a unique combination of these waves.

Why the God Equation Matters

- The God Equation, in its basic and generalized forms, is the mathematical source code of existence.
- Euler's formula and its identity reveal the unity and power of mathematics at the heart of reality.
- The generalized God Equation $Ae^{i\theta} = A\cos(\theta) + iA\sin(\theta)$ unveils the living, dynamic, and frequency-based structure underpinning everything.
- All existence, energy, and phenomena are constructed from sinusoidal waves—sine and cosine—the true fabric of being.

Understanding these equations is to glimpse the mathematical architecture of reality itself.

Best Practices for Exploring Ontological Mathematics

- Develop a strong foundation in complex numbers and the relationships between exponential and trigonometric functions.
- Study Fourier analysis to understand how complex patterns arise from simple waves.
- Explore the philosophy of mathematical ontology, which posits mathematics as the fabric of reality.
- Consider the implications for physics, information theory, and consciousness as emanating from these mathematical principles.

Where to Go Next

To explore the full depth of these ideas, start with the **God Series** by Mike Hockney—a comprehensive journey through the philosophy and mathematics of existence from the perspective of ontological mathematics.

For those seeking to understand the unified mathematical foundations of reality—with a focus on equations and rigorous reasoning—the **Arithmoí** series by Jason Glowney is an excellent path. This six-part series investigates mathematics, physics, and metaphysics through a cohesive framework rooted in ontological mathematics.

• Mathematics Book I: Arithmoí – Mathematical Foundations and the Singularity

The opening volume explores existence as a mathematical construct, presenting mathematics not merely as a tool, but as the very language in which reality is written.

• Physics Book I: Arithmoí – Phenomenology and the Geometry of Light The second volume will examine how phenomena arise from mathematical light and geometric synthesis, laying the groundwork for a unified understanding of physical reality.

As stated in the Emerald Tablet:

"That which is above is from that which is below, and that which is below is from that which is above, working the miracles of one."

In the end, we are not discovering mathematics—we are remembering it.

Learn more at arithmoi.org