

Lecture 5: Sequence Models II

Alan Ritter

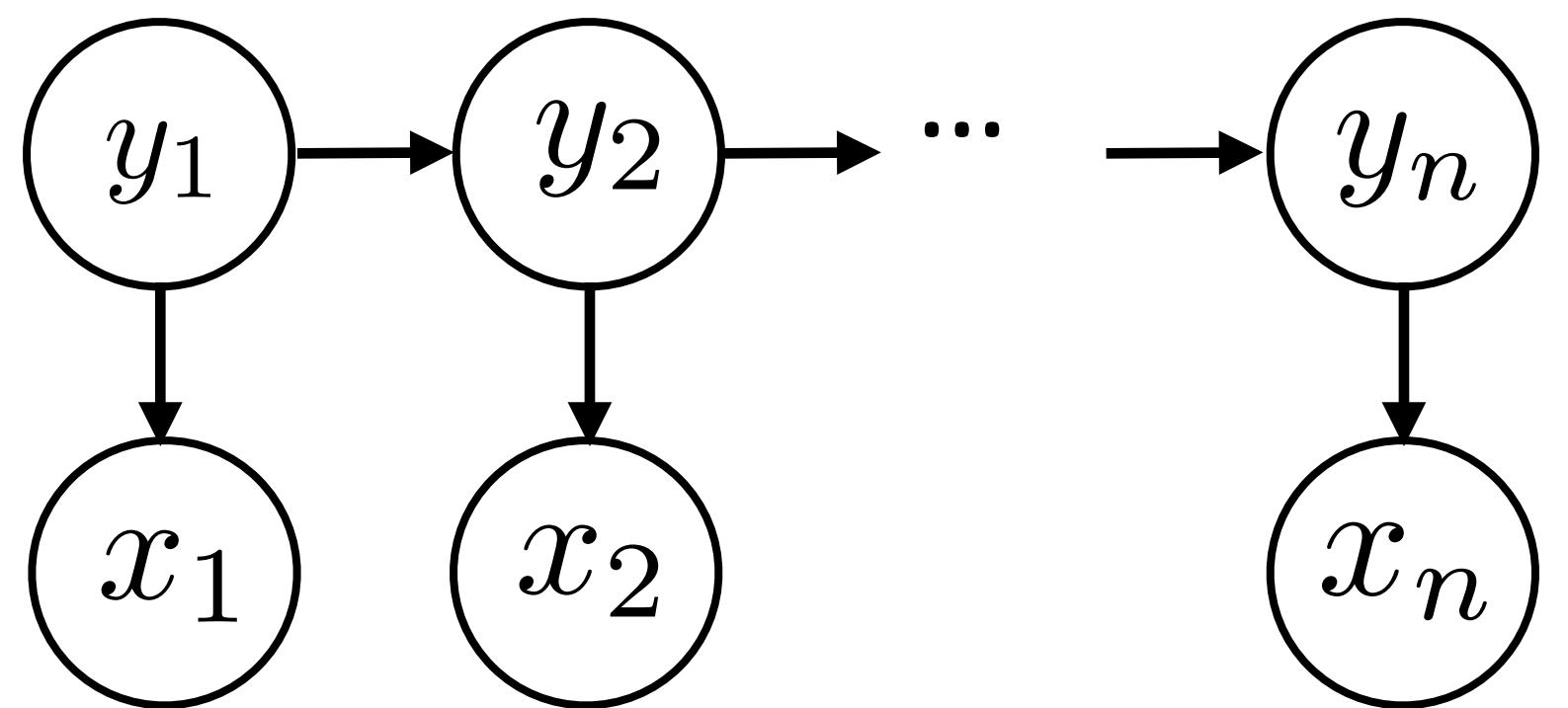
(many slides from Greg Durrett, Dan Klein, Vivek Srikumar, Chris Manning, Yoav Artzi)

Recall: HMMs

- ▶ Input $\mathbf{x} = (x_1, \dots, x_n)$ Output $\mathbf{y} = (y_1, \dots, y_n)$

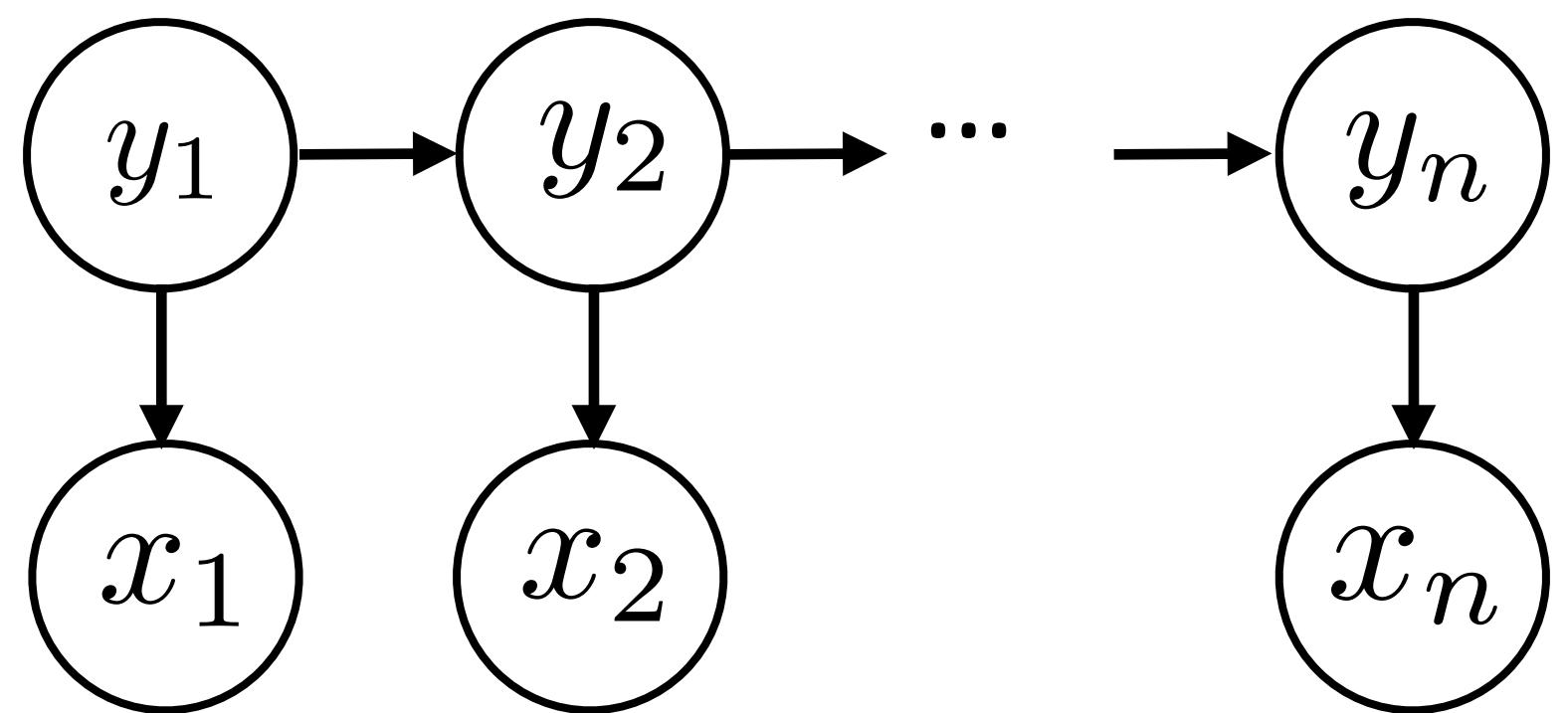
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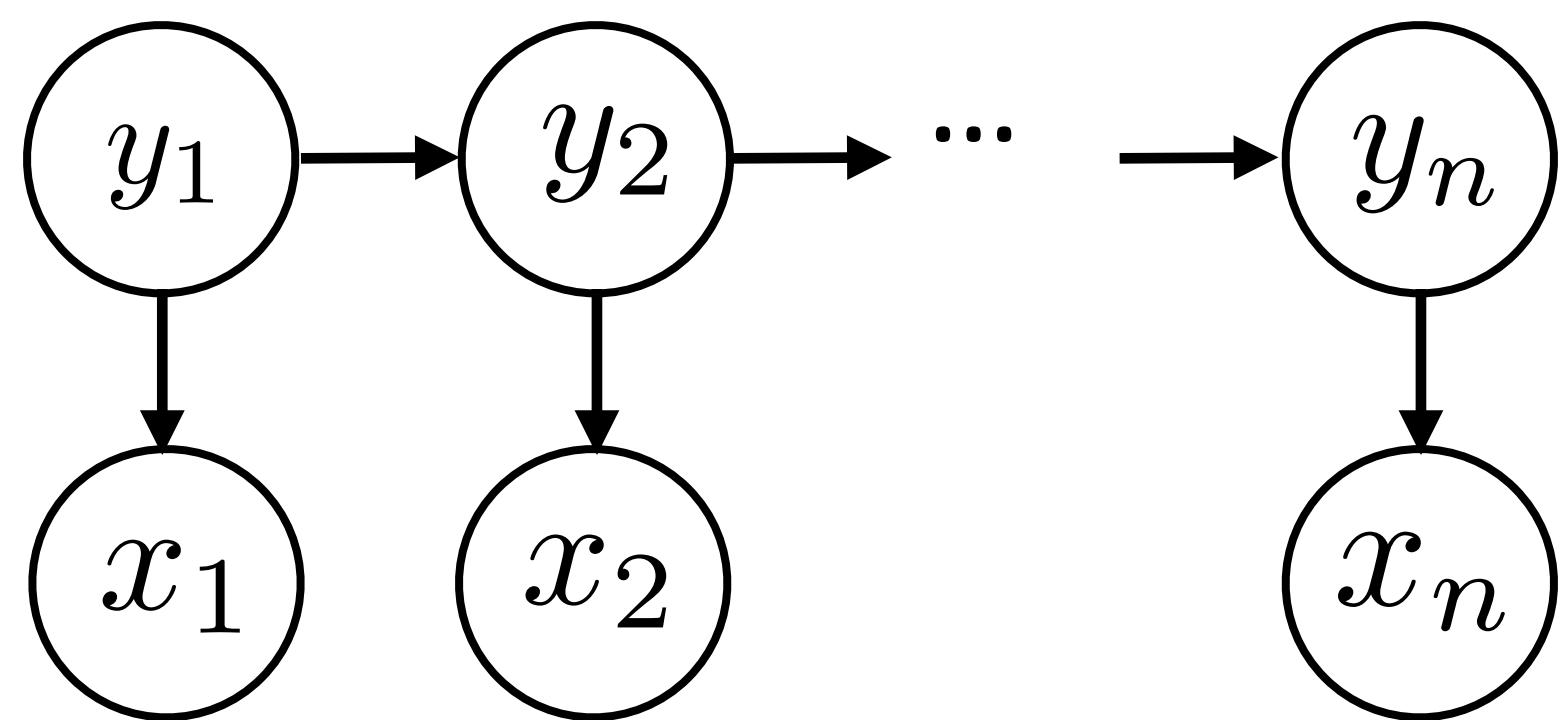


Output $\mathbf{y} = (y_1, \dots, y_n)$

$$P(\mathbf{y}, \mathbf{x}) = P(y_1) \prod_{i=2}^n P(y_i|y_{i-1}) \prod_{i=1}^n P(x_i|y_i)$$

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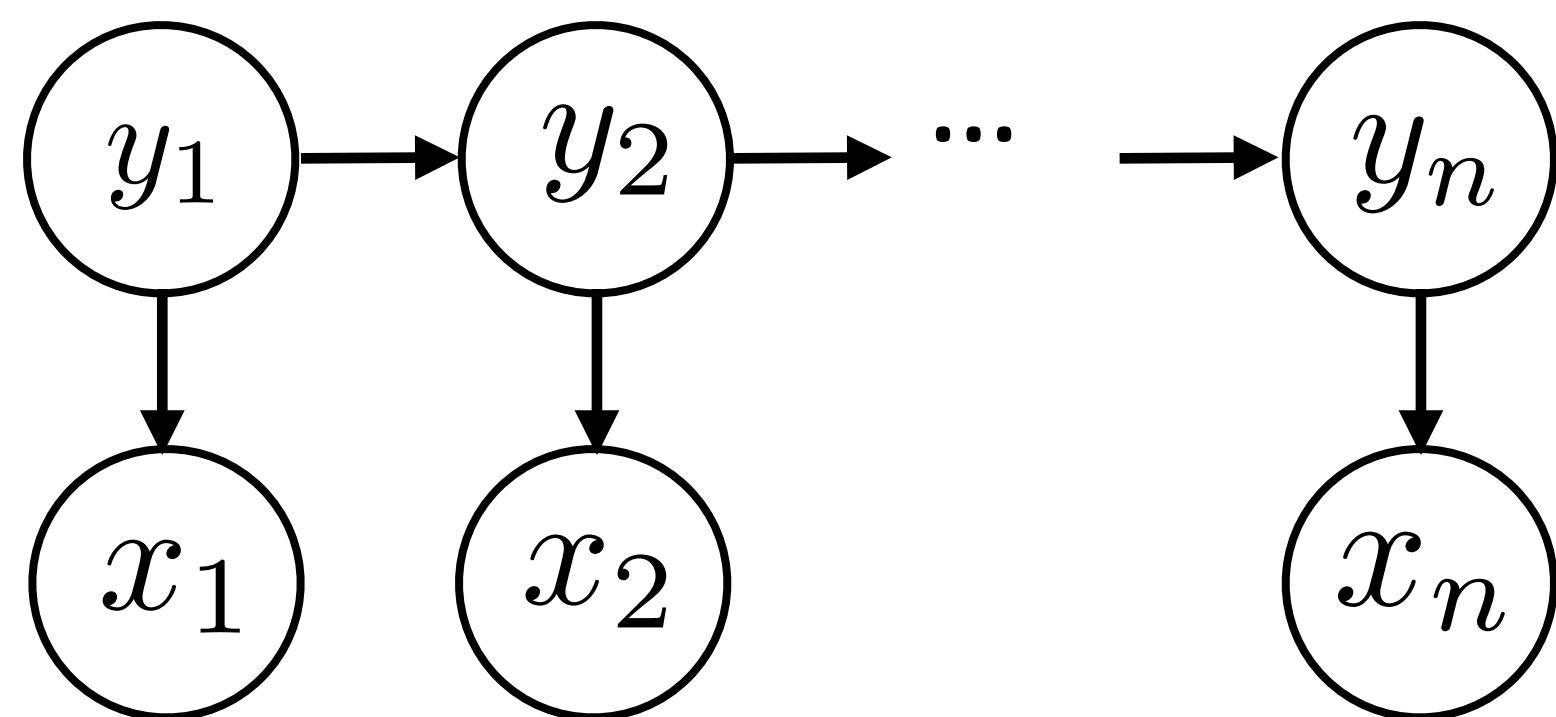
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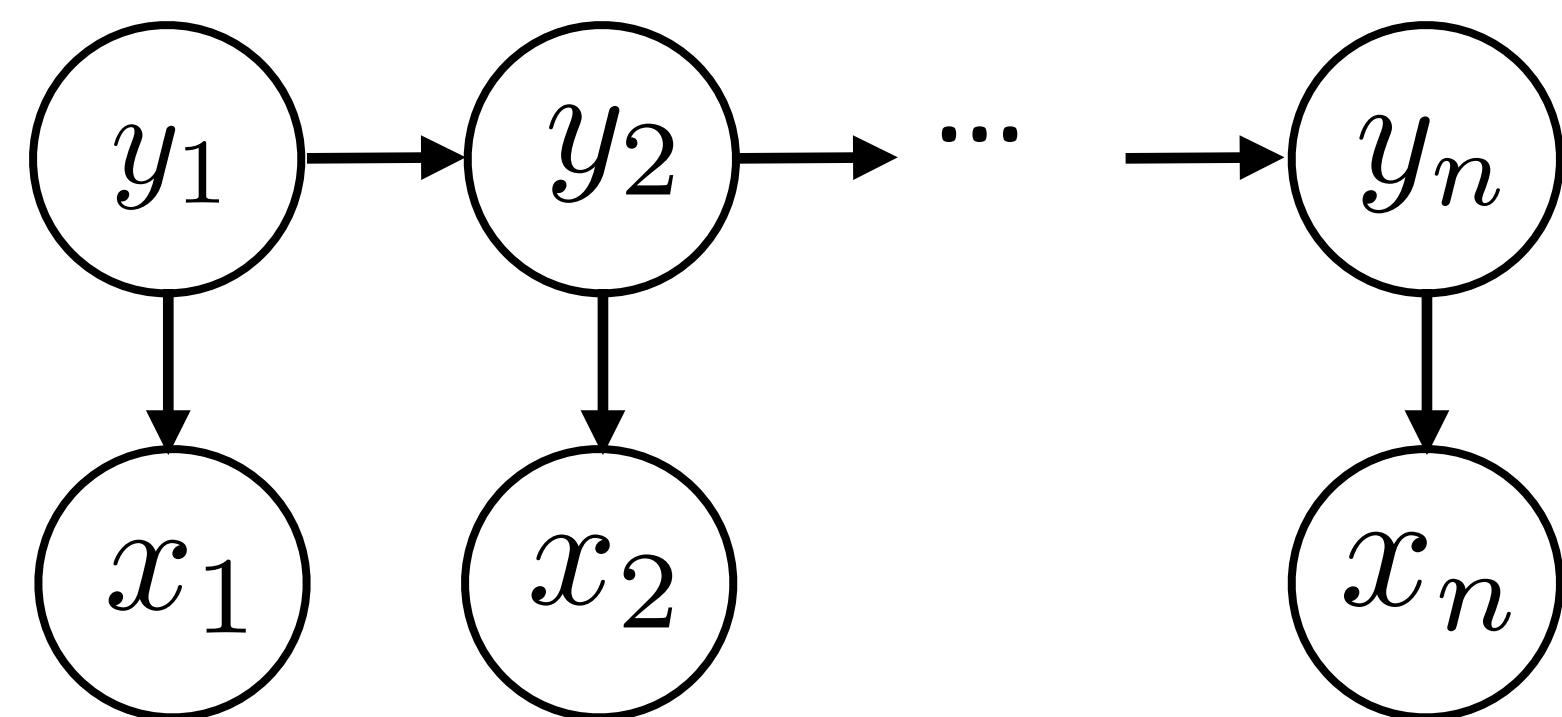
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► Inference problem: $\text{argmax}_{\mathbf{y}} P(\mathbf{y}|\mathbf{x}) = \text{argmax}_{\mathbf{y}} \frac{P(\mathbf{y}, \mathbf{x})}{P(\mathbf{x})}$

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► Viterbi: $\text{score}_i(s) = \max_{y_{i-1}} P(s|y_{i-1}) P(x_i|s) \text{score}_{i-1}(y_{i-1})$

This Lecture

- ▶ CRFs: model (+features for NER), inference, learning
- ▶ Named entity recognition (NER)
- ▶ (if time) Beam search

Named Entity Recognition

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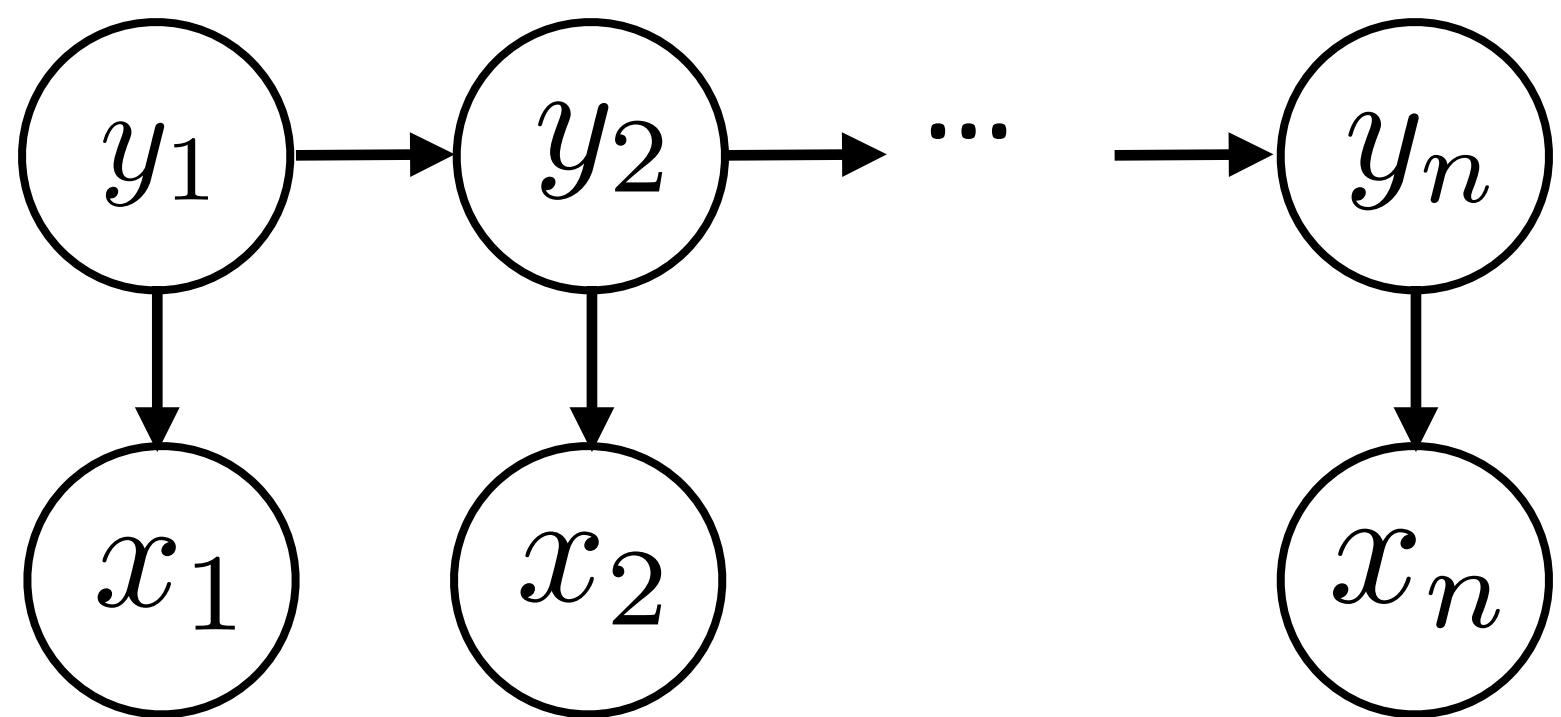
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- ▶ BIO tagset: begin, inside, outside
- ▶ Sequence of tags – should we use an HMM?
- ▶ Why might an HMM not do so well here?
 - ▶ Lots of O's, so tags aren't as informative about context
 - ▶ Insufficient features/capacity with multinomials (especially for unks)

CRFs

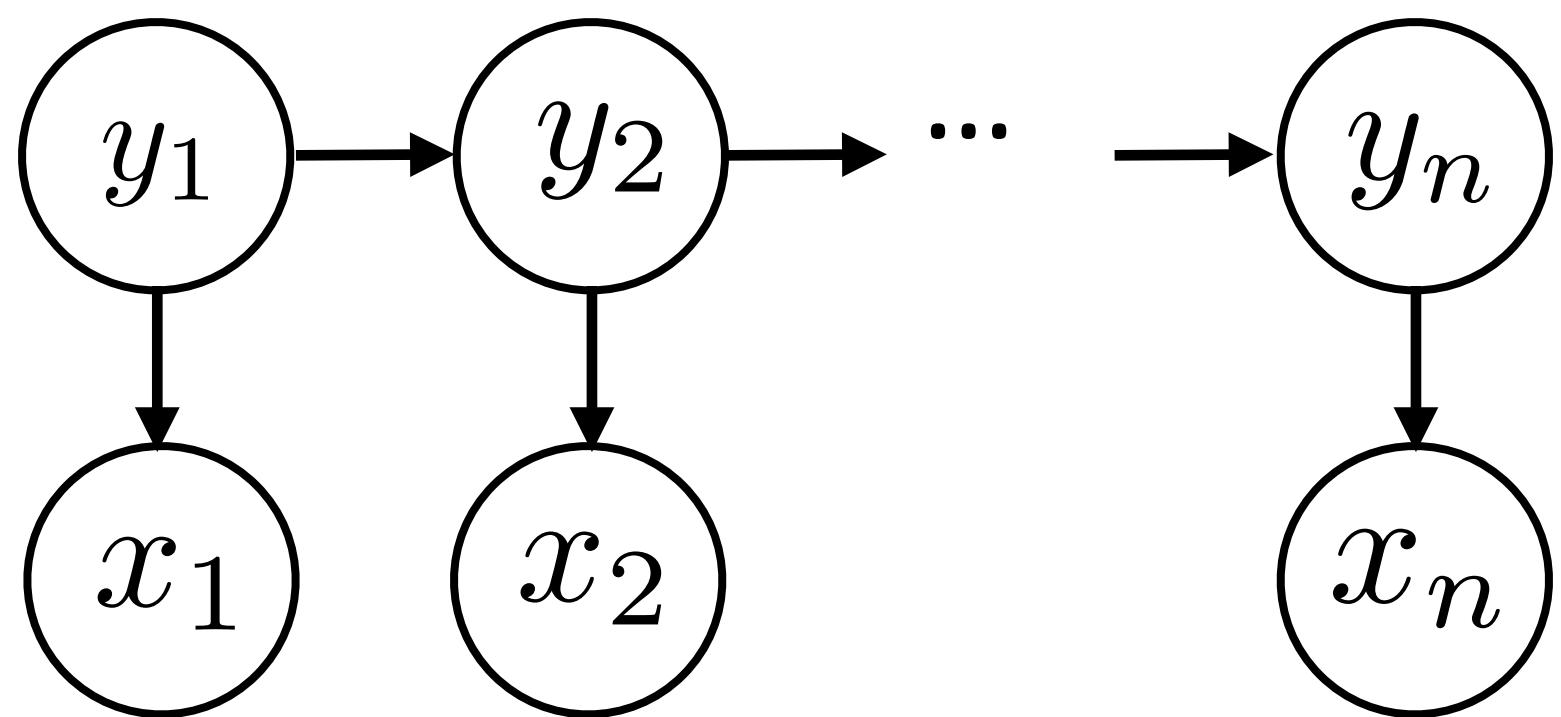
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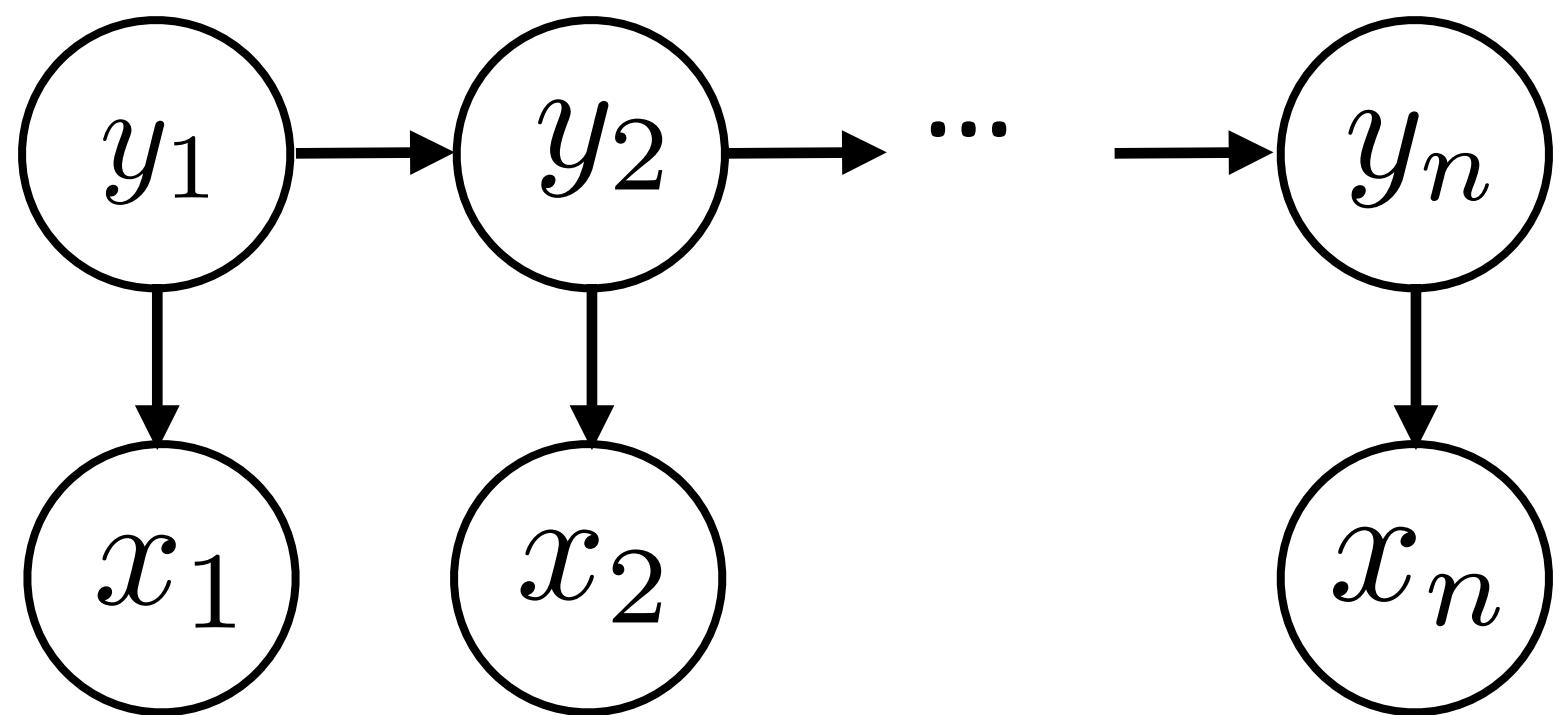


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$$P(\mathbf{y}, \mathbf{x}) = P(y_1)P(x_1|y_1)P(y_2|y_1)P(x_2|y_2)\dots$$

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- ▶ Locally normalized model: each factor is a probability distribution that normalizes

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local vs. global normalization <-> generative vs. discriminative

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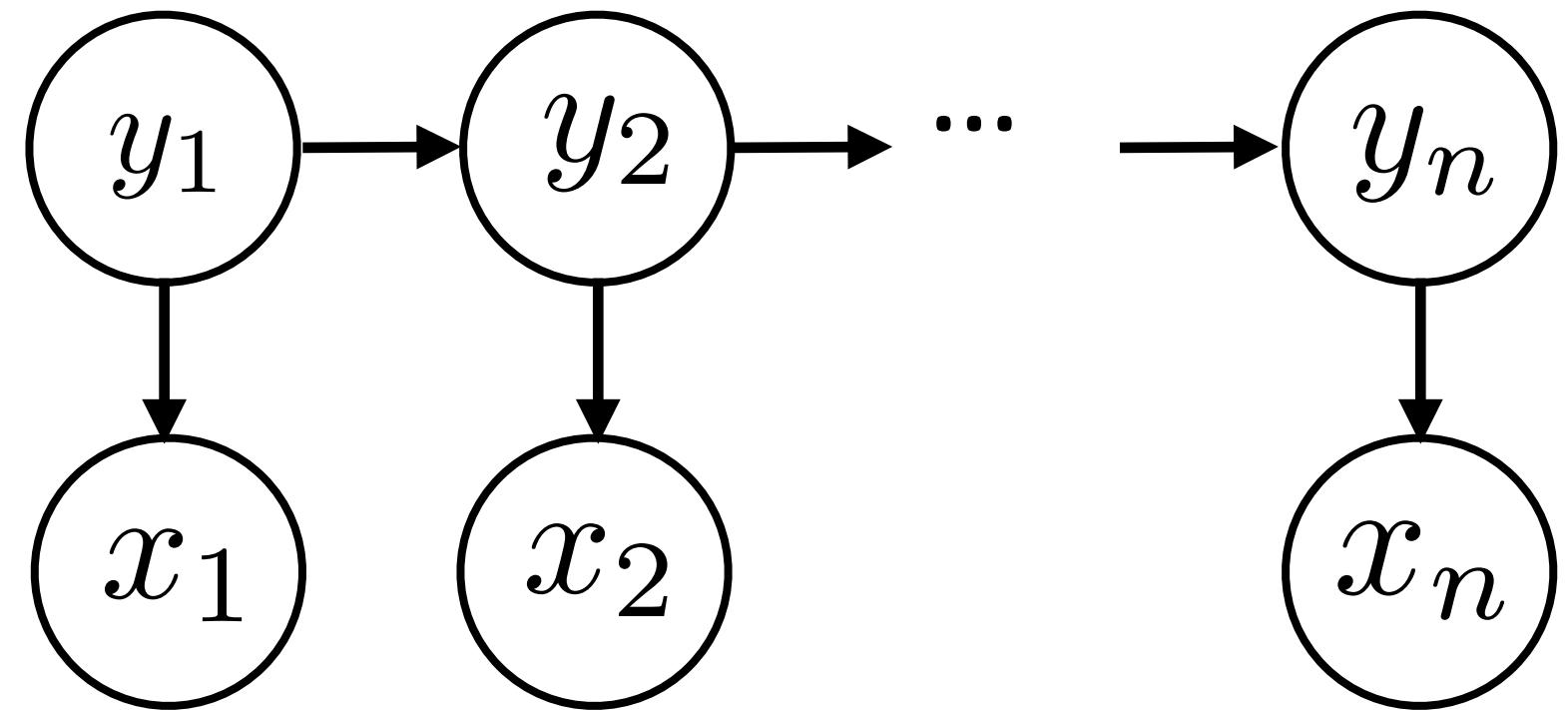
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local vs. global normalization \leftrightarrow generative vs. discriminative
- ▶ Locally normalized discriminative models do exist (MEMMs)
- ▶ How do we max over \mathbf{y} ? Intractable in general — can we fix this?

Sequential CRFs

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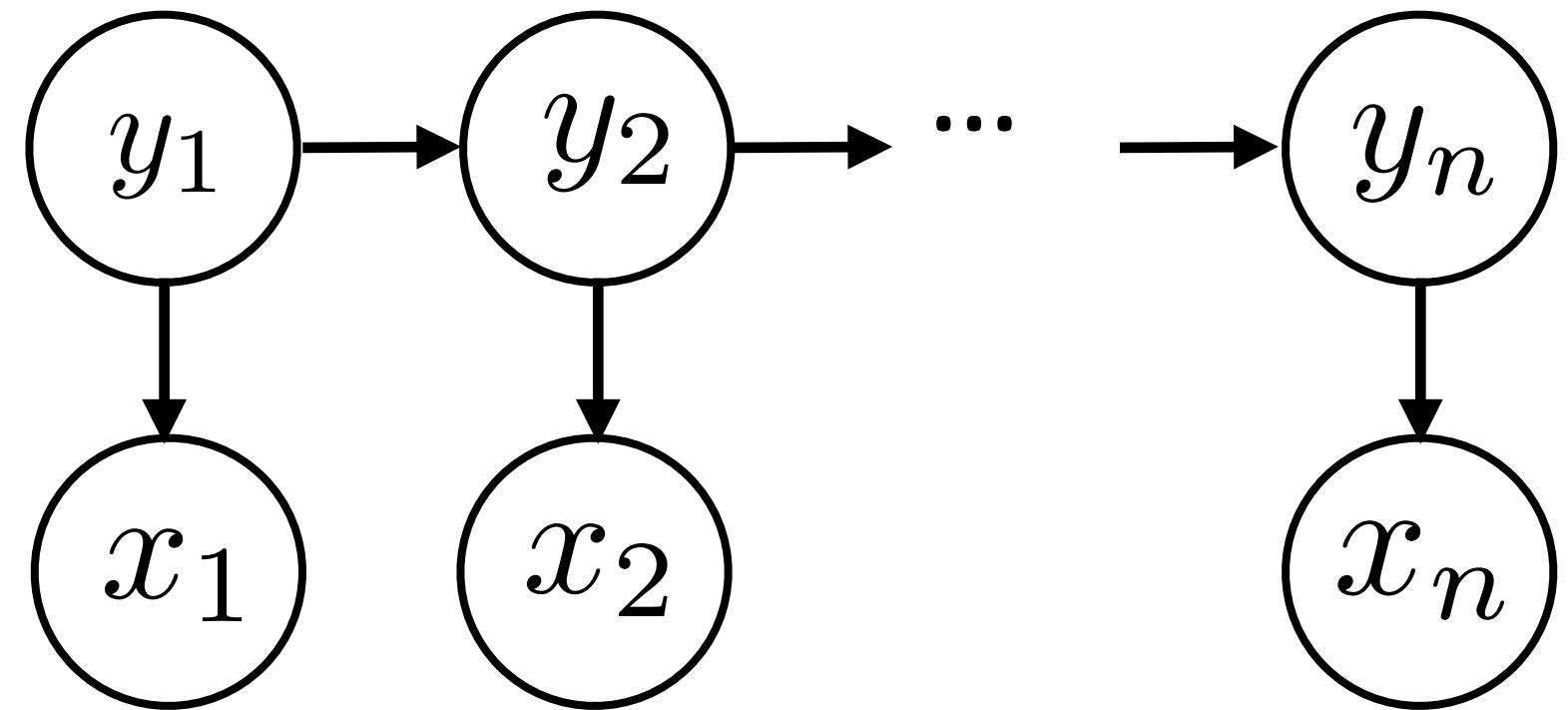


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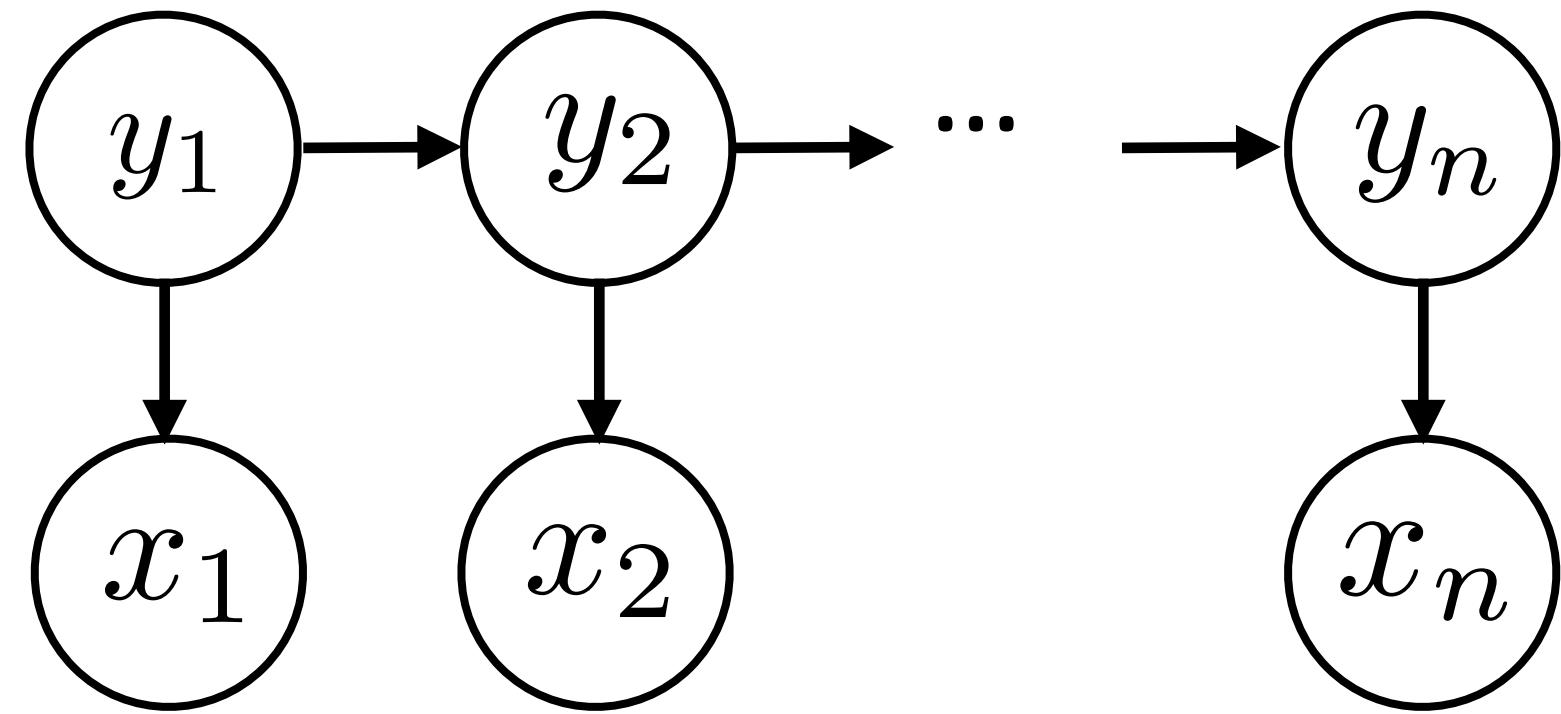
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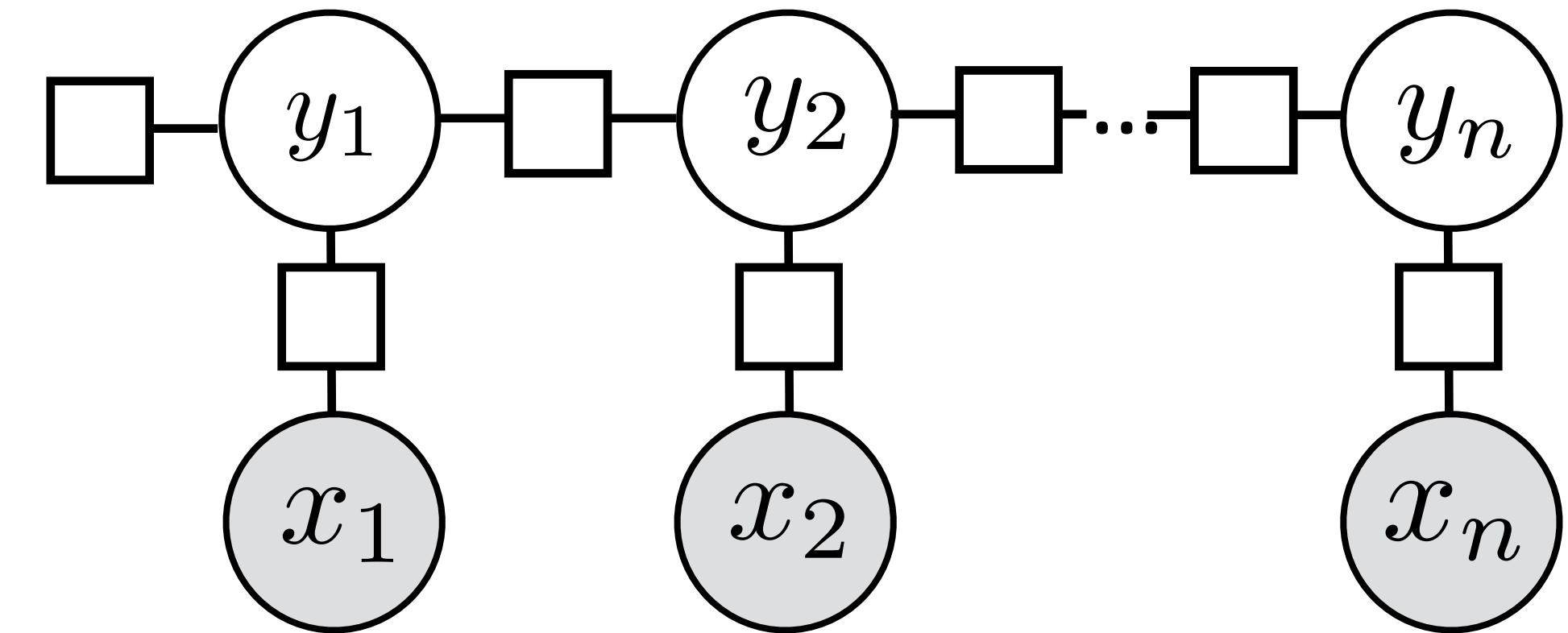
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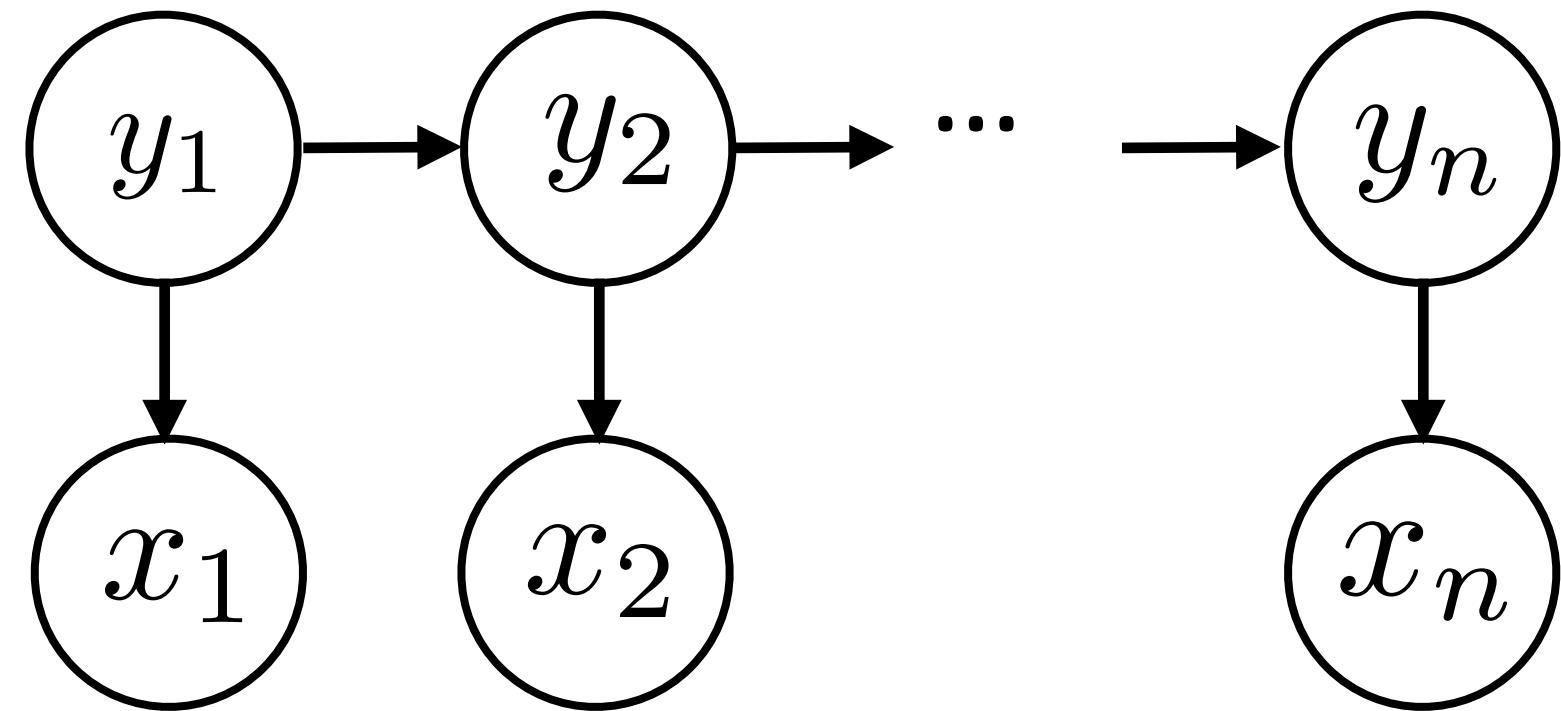
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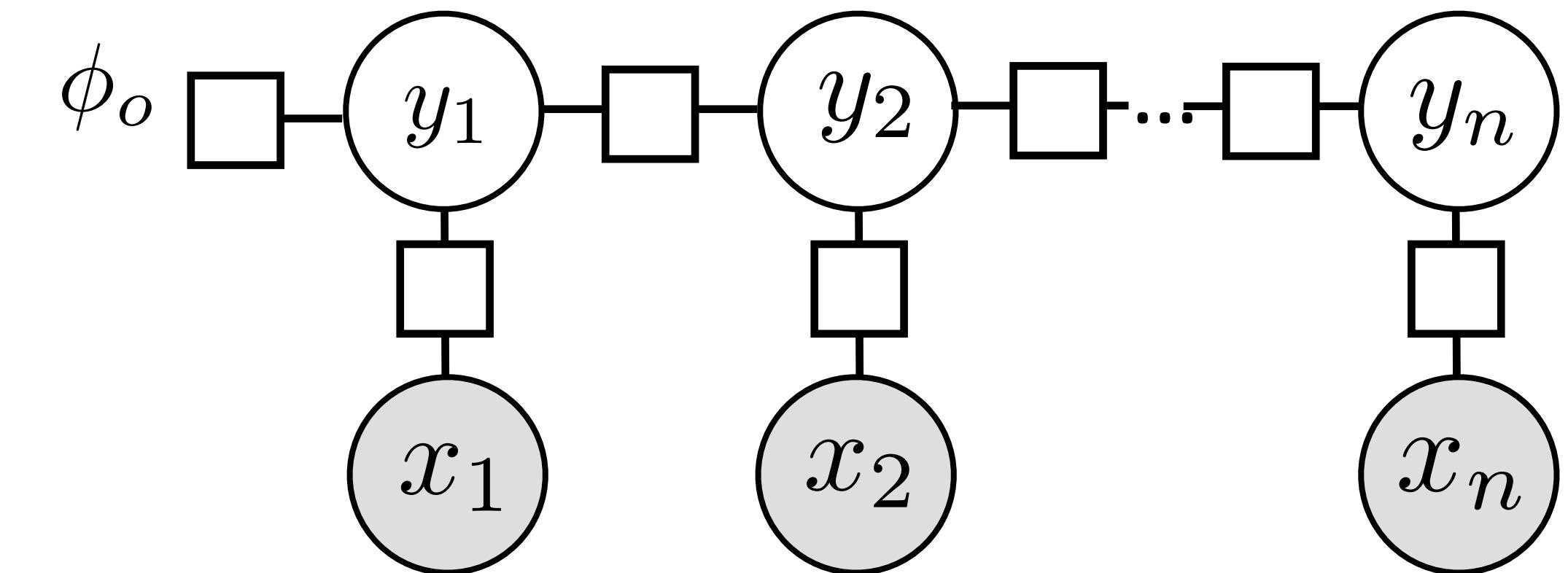
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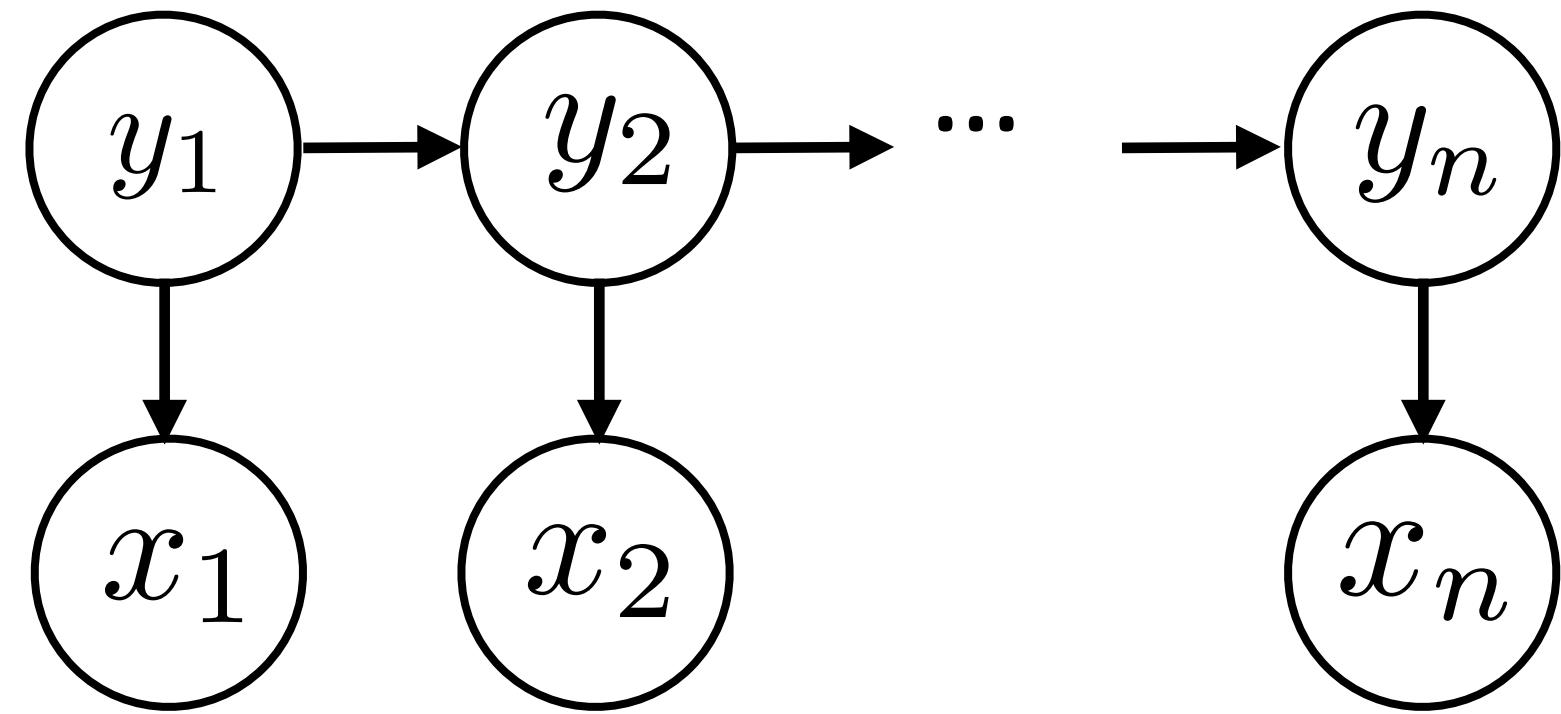
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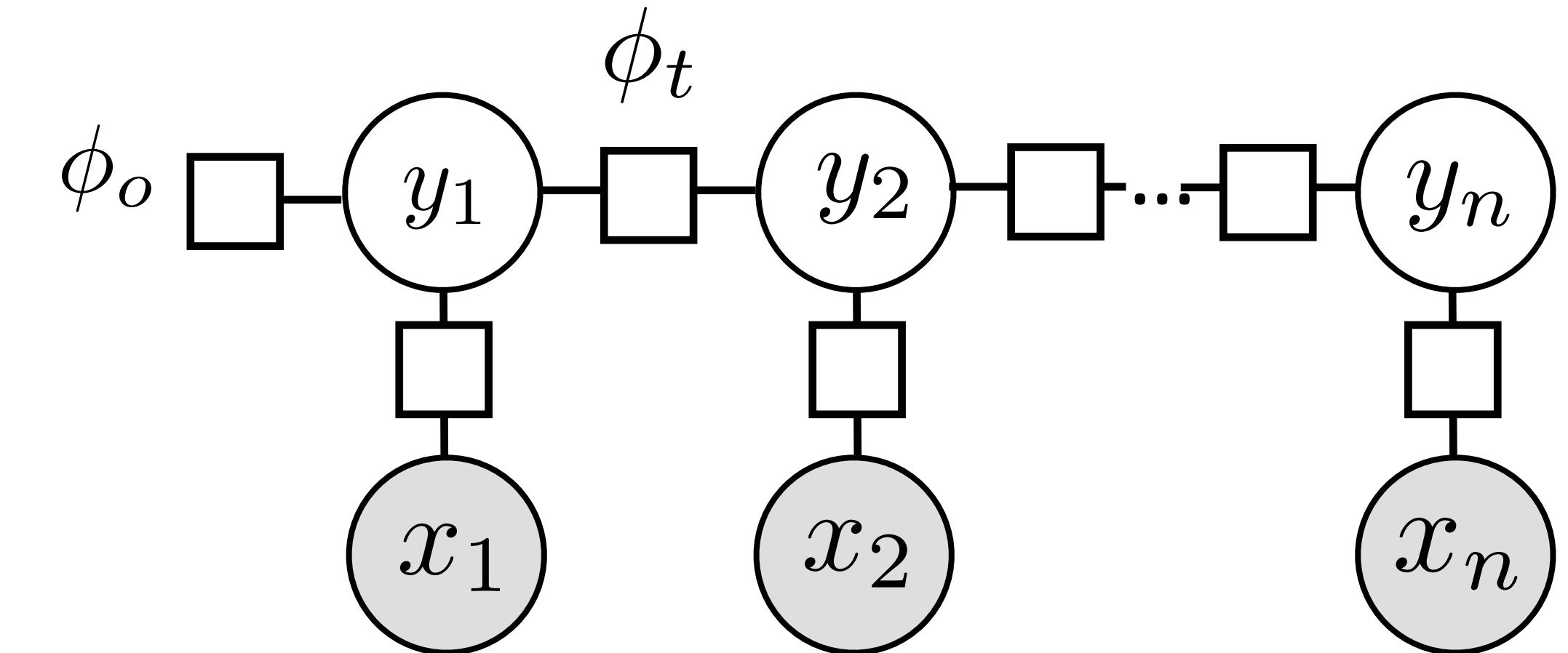
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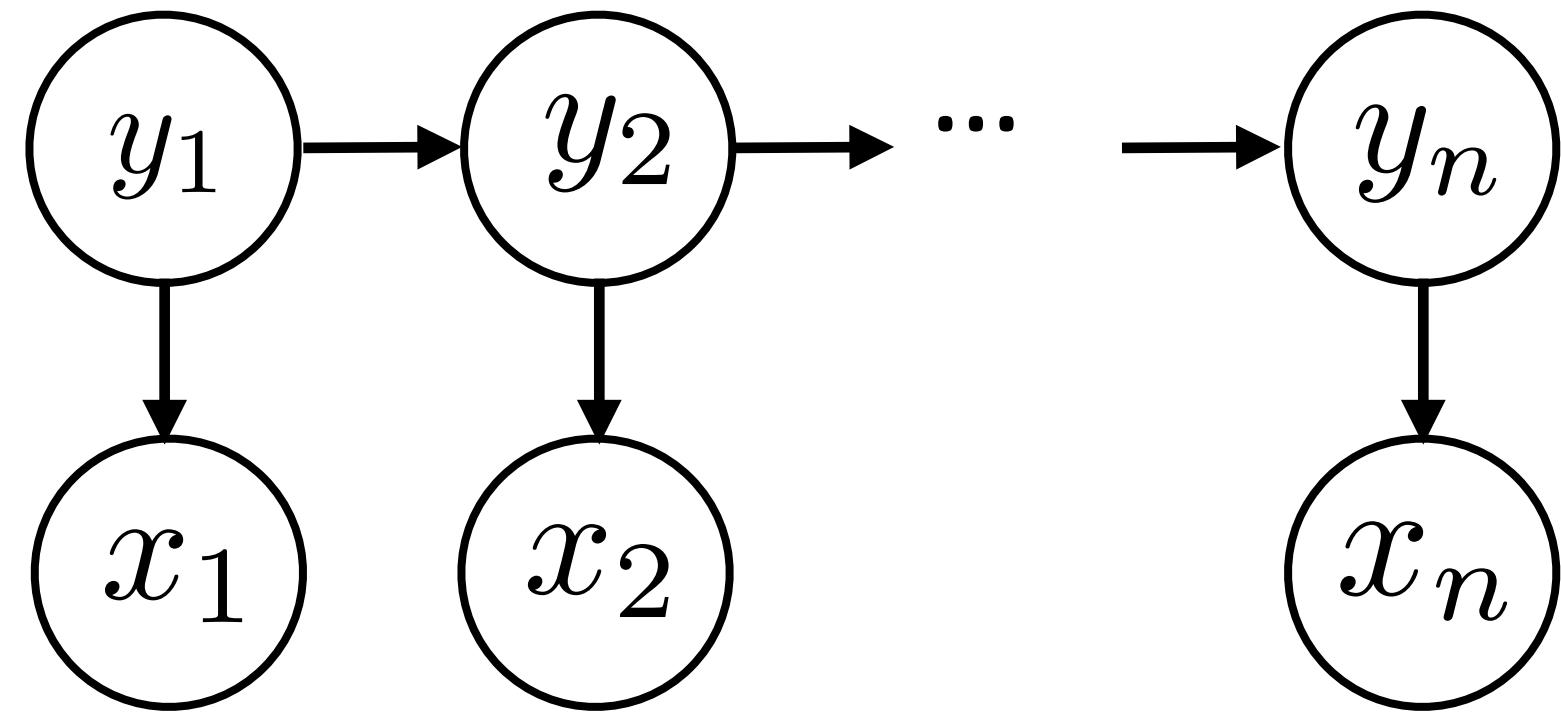
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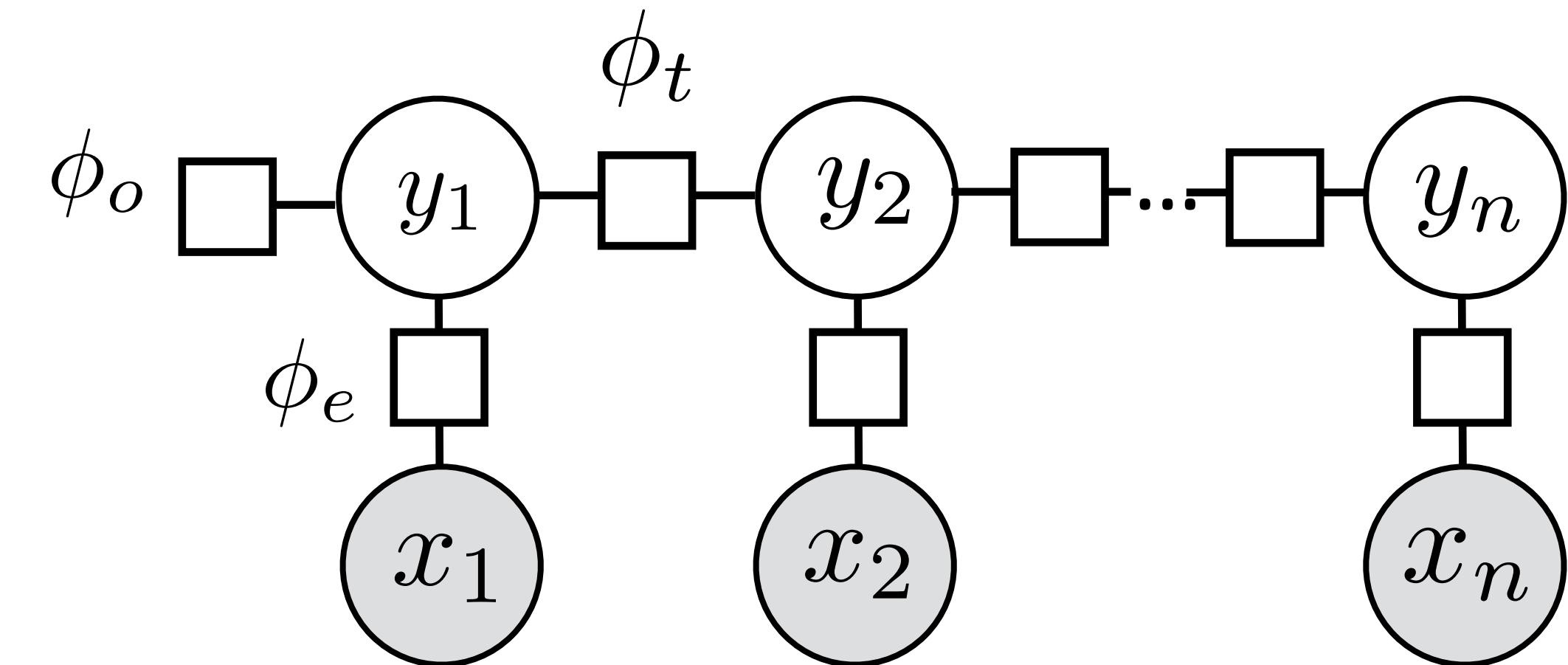
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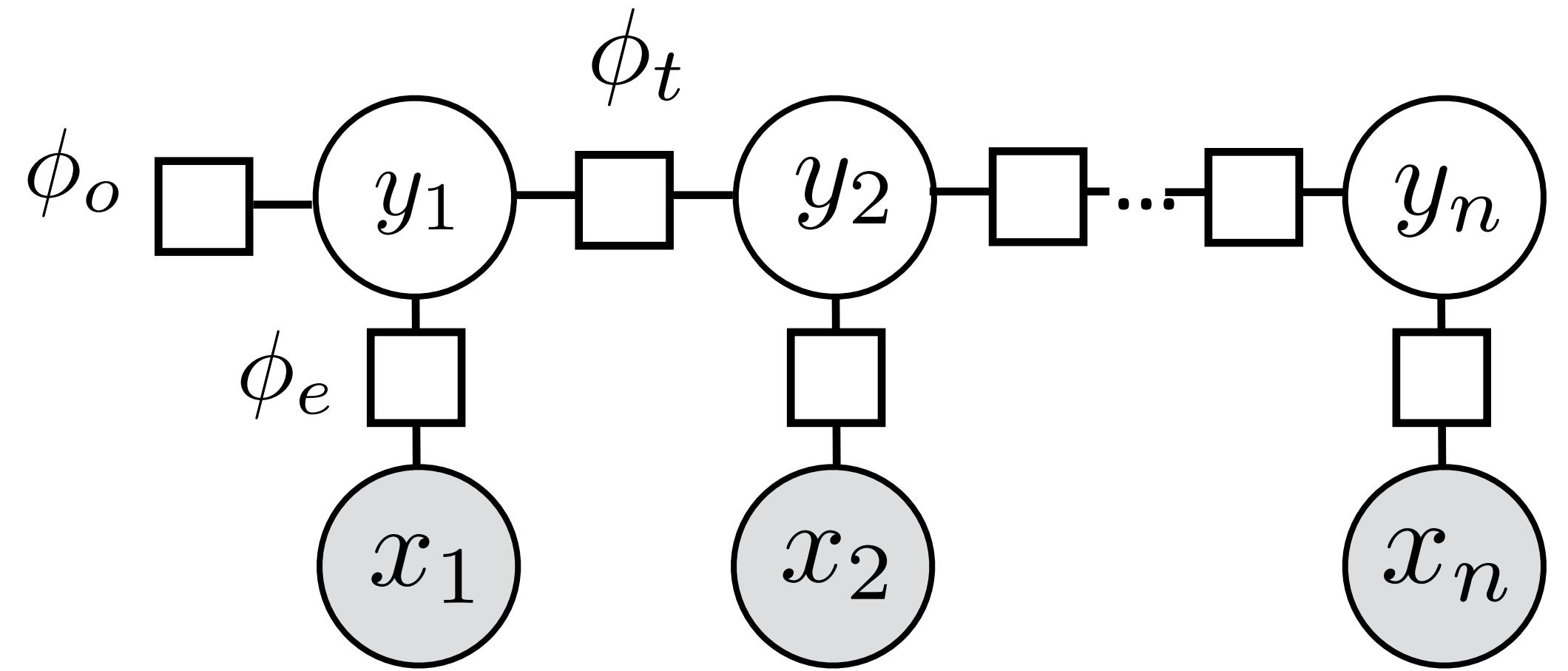
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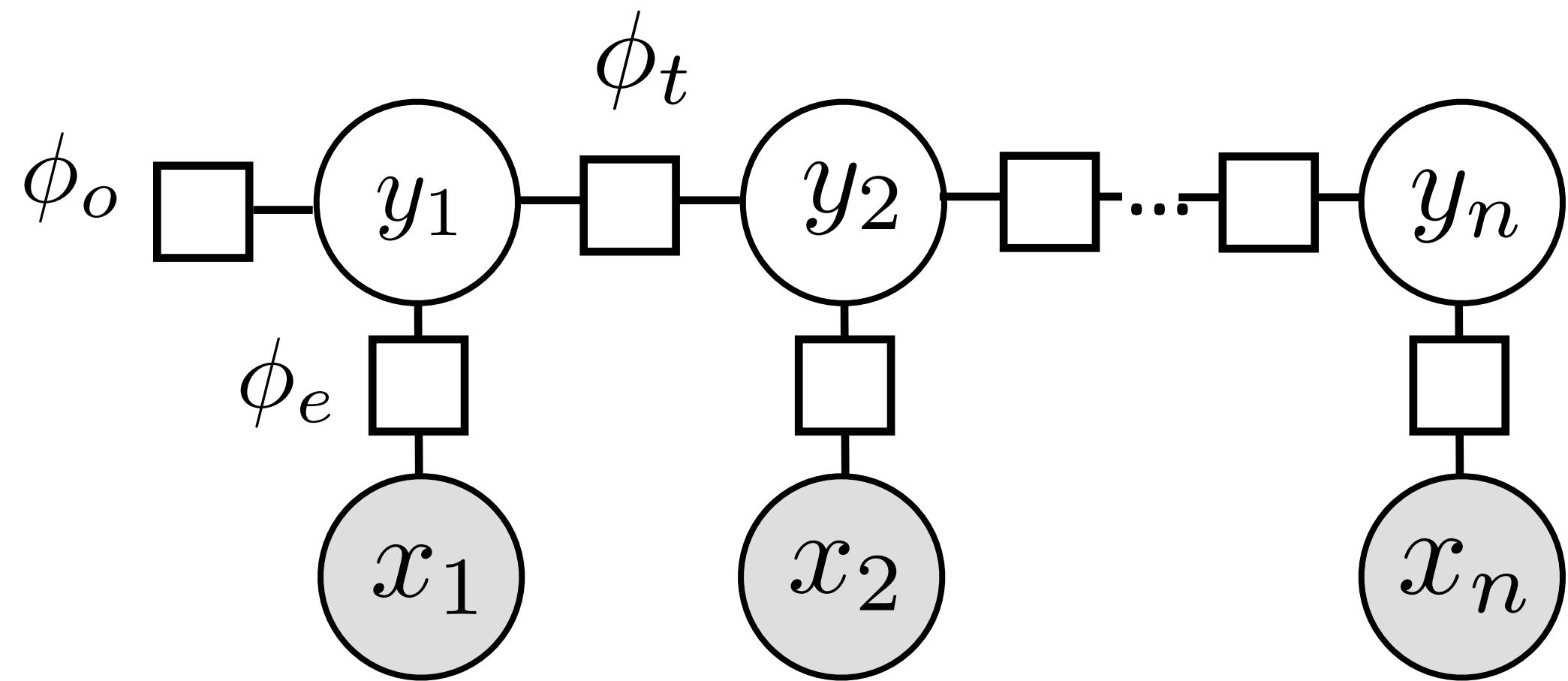


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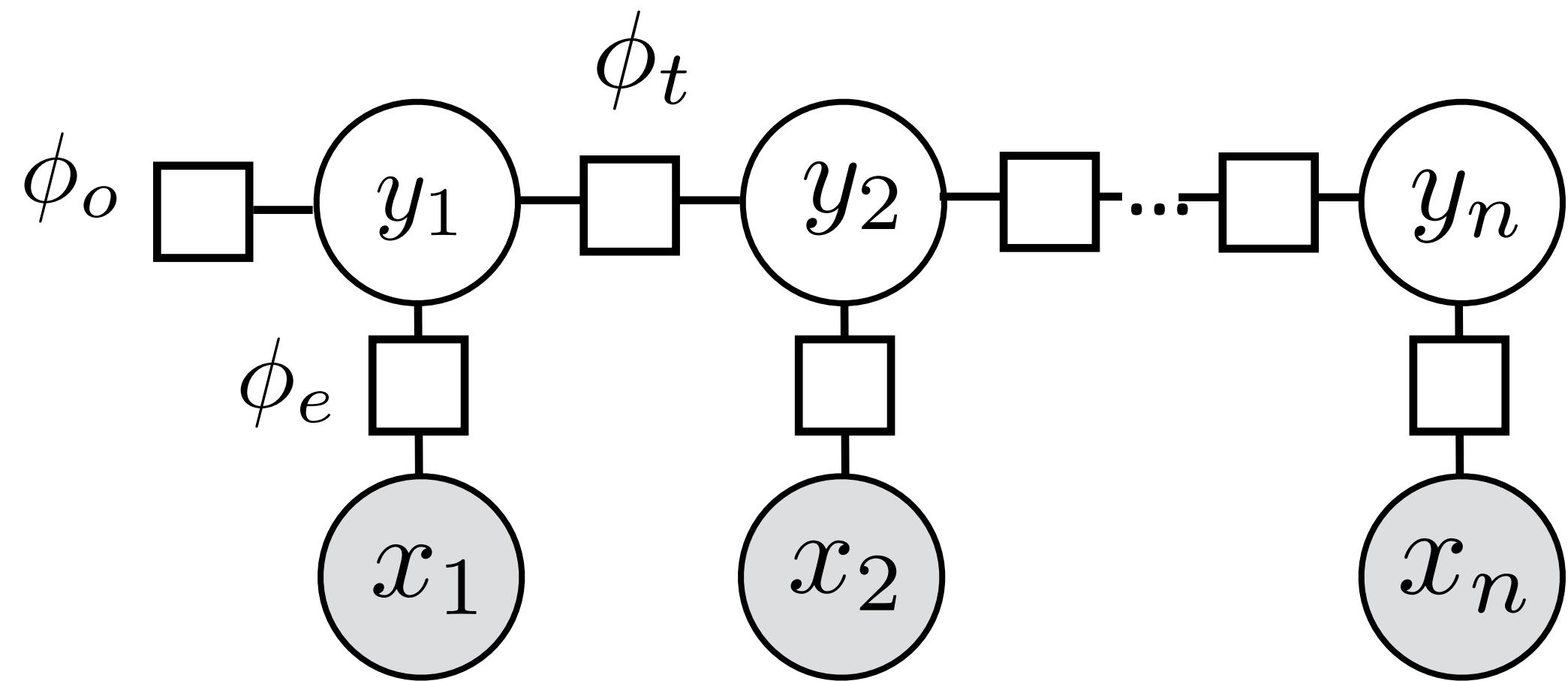
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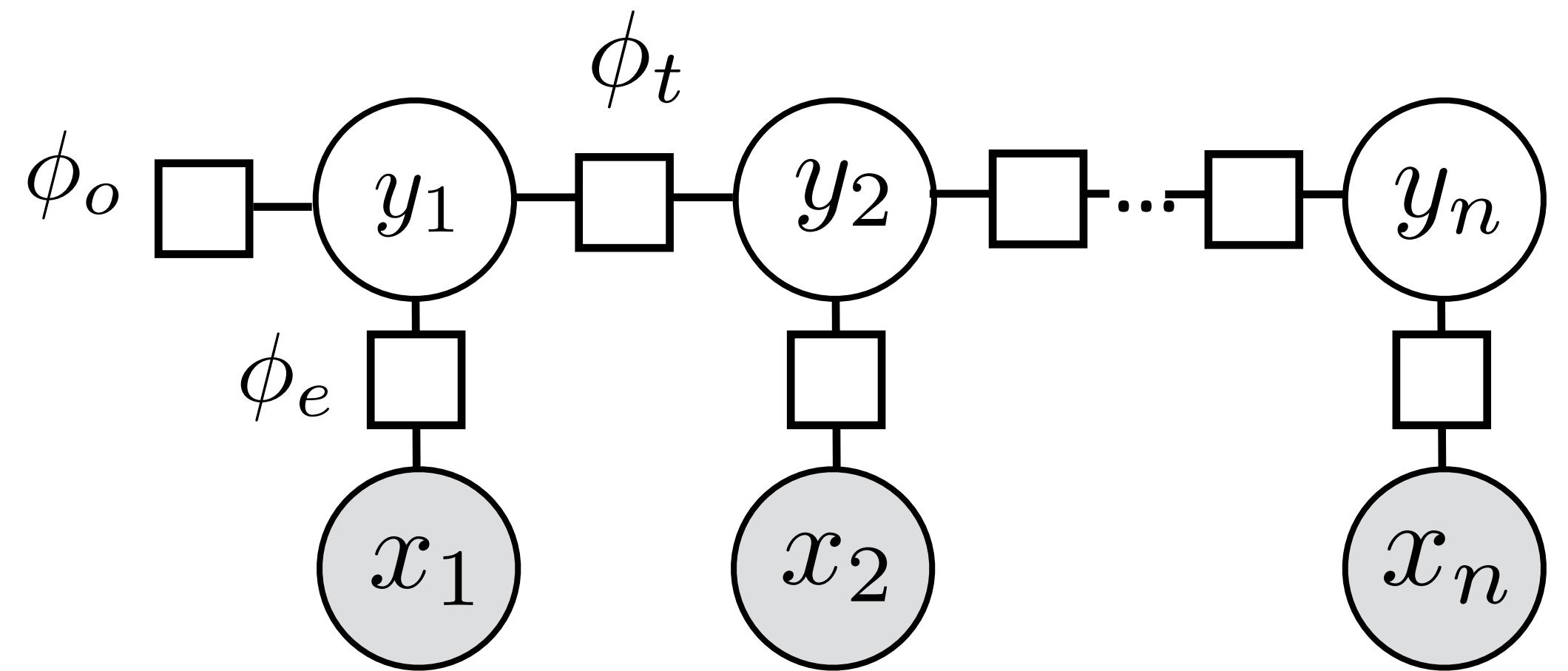
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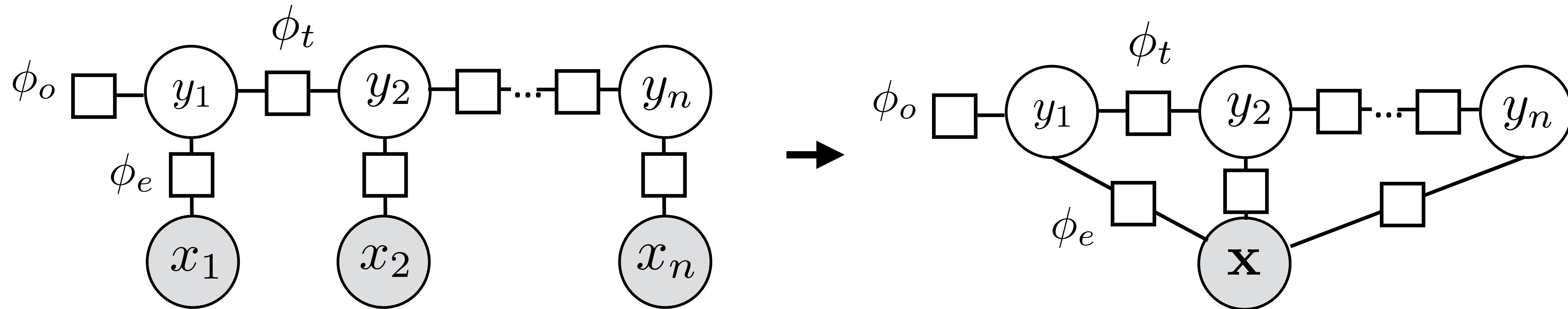
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token index — lets us look at current word

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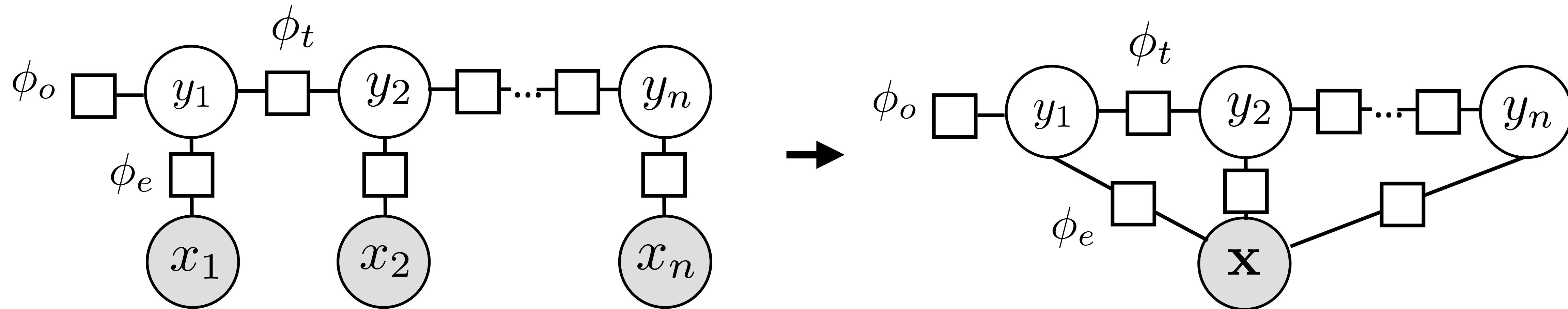
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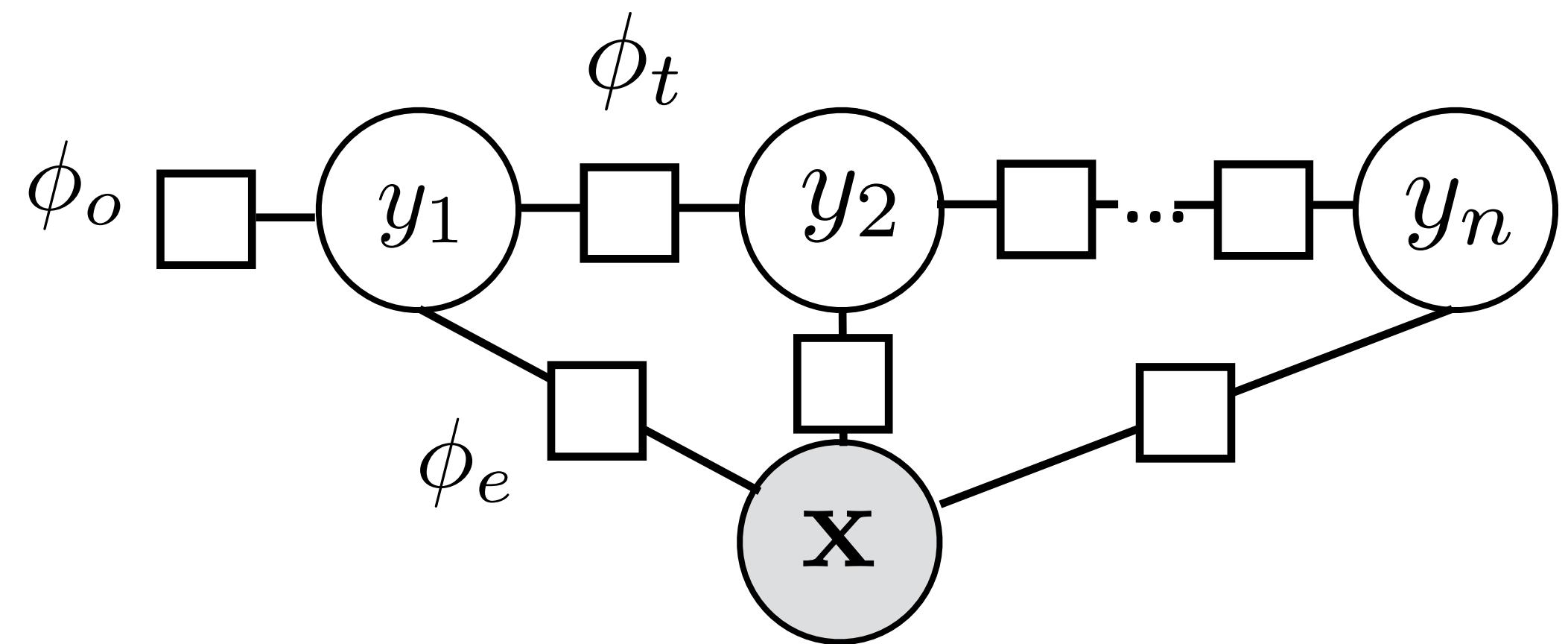
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- ▶ We condition on \mathbf{x} , so every factor can depend on all of \mathbf{x} (including transitions, but we won't do this)
- ▶ \mathbf{y} can't depend arbitrarily on \mathbf{x} in a generative model

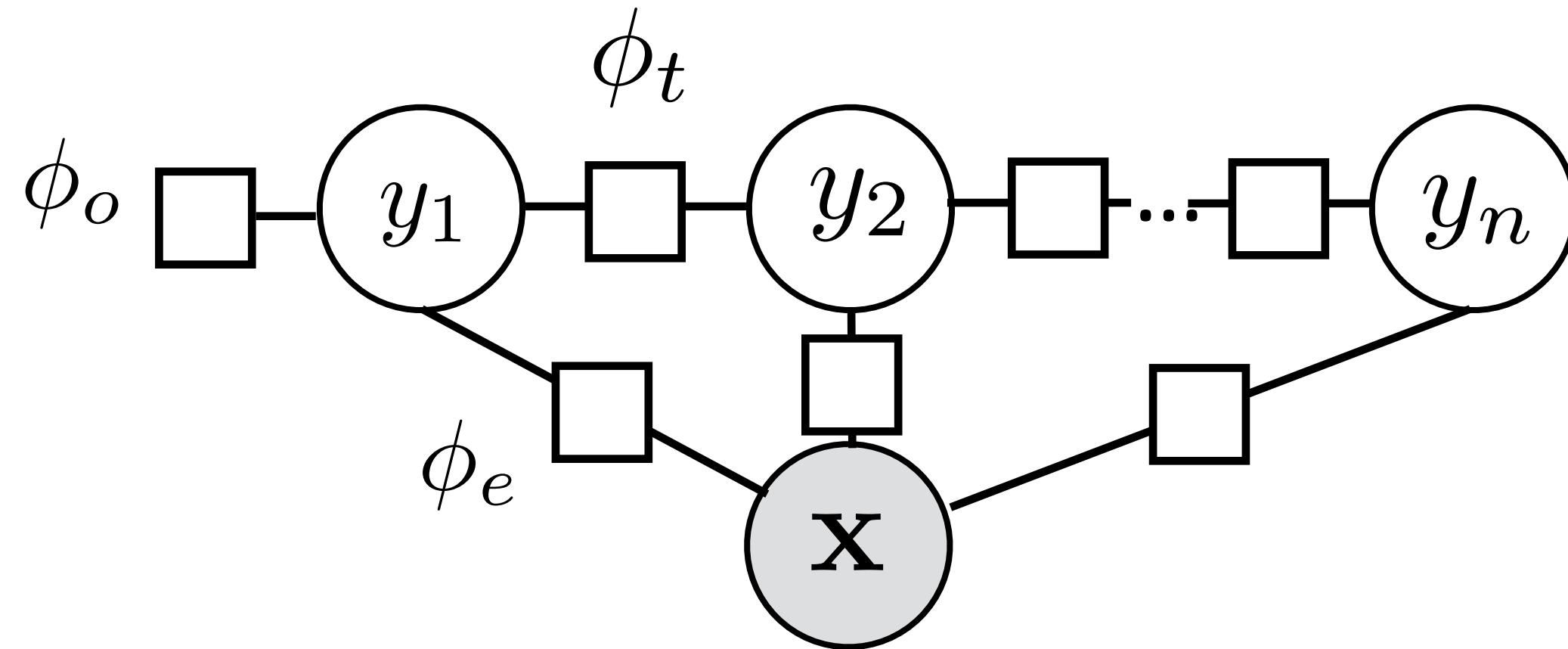
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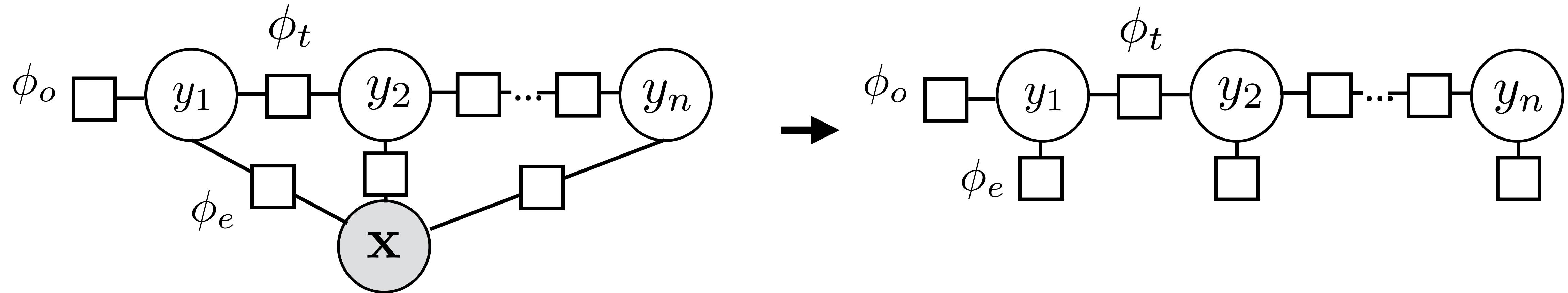


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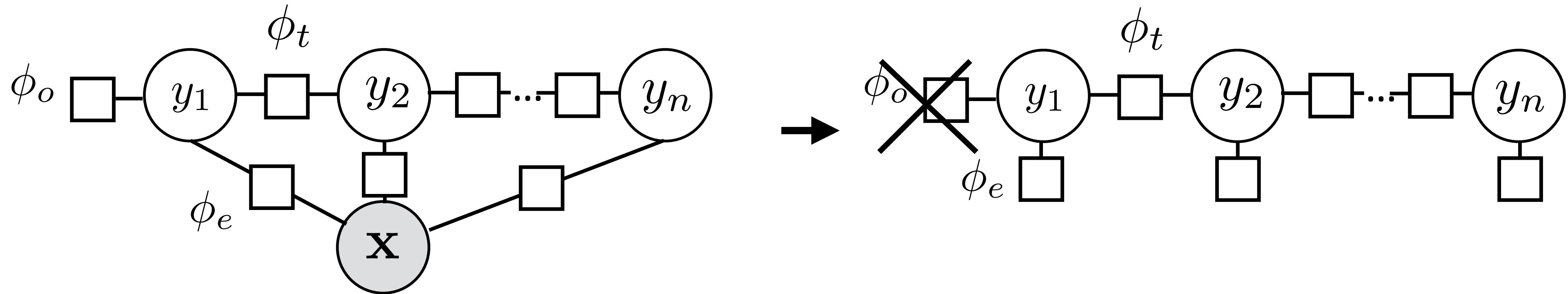
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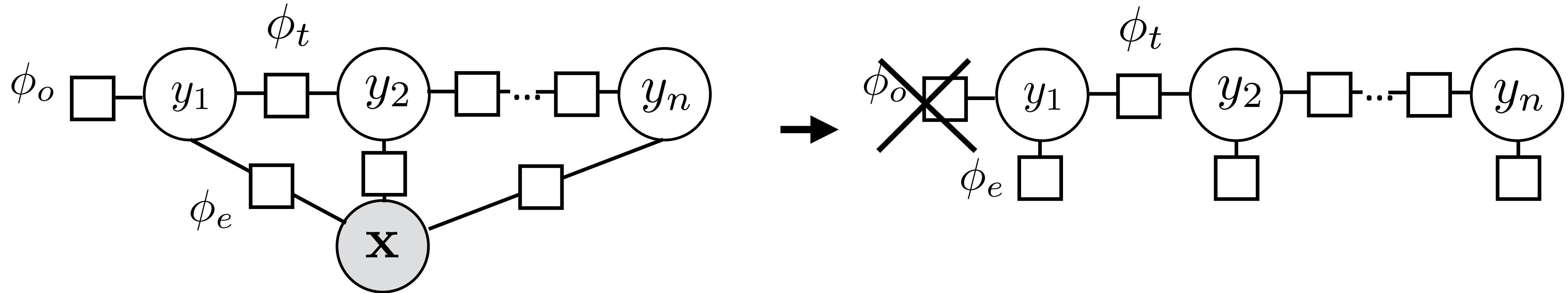
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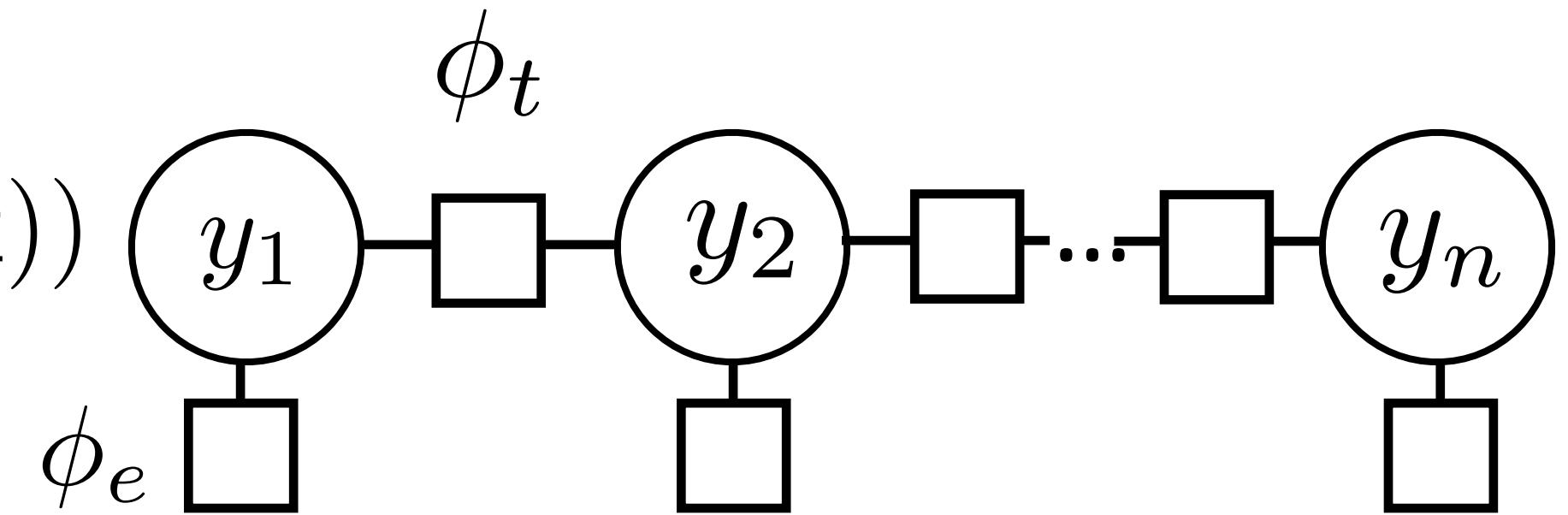
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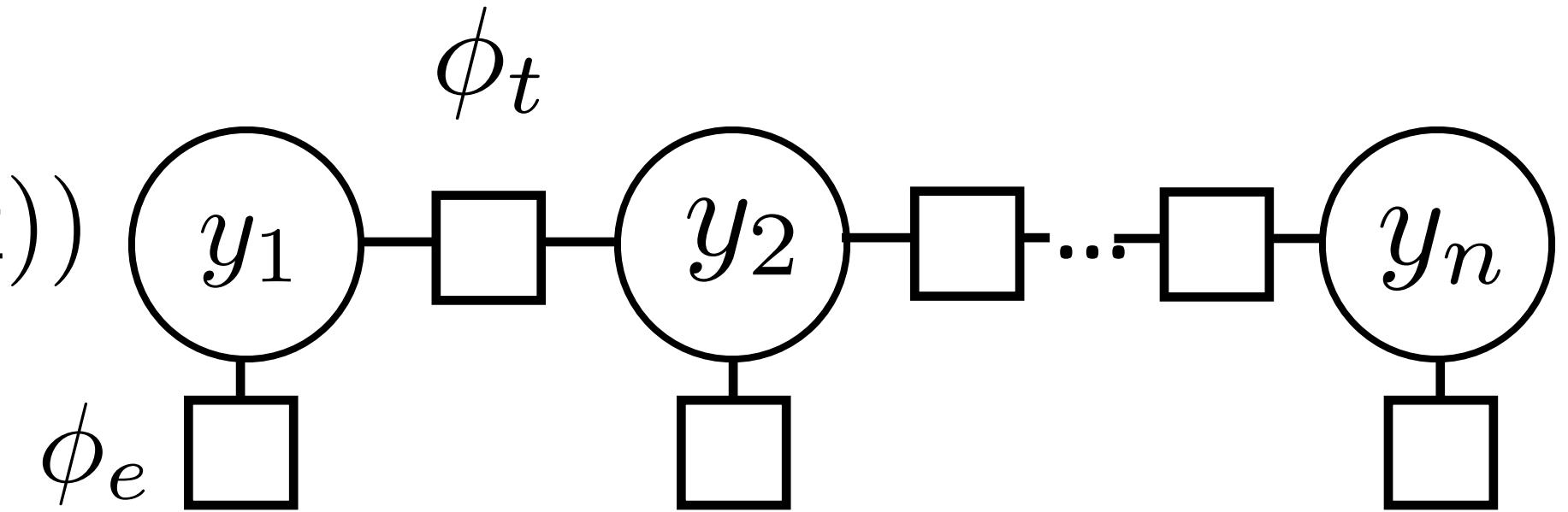
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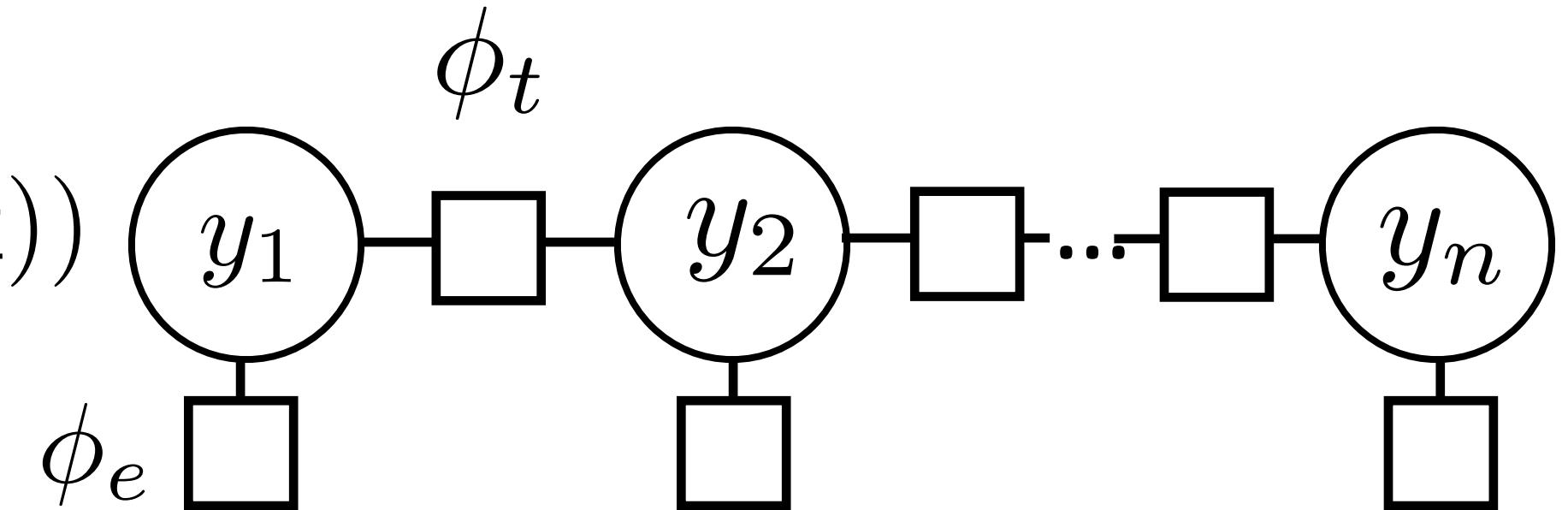
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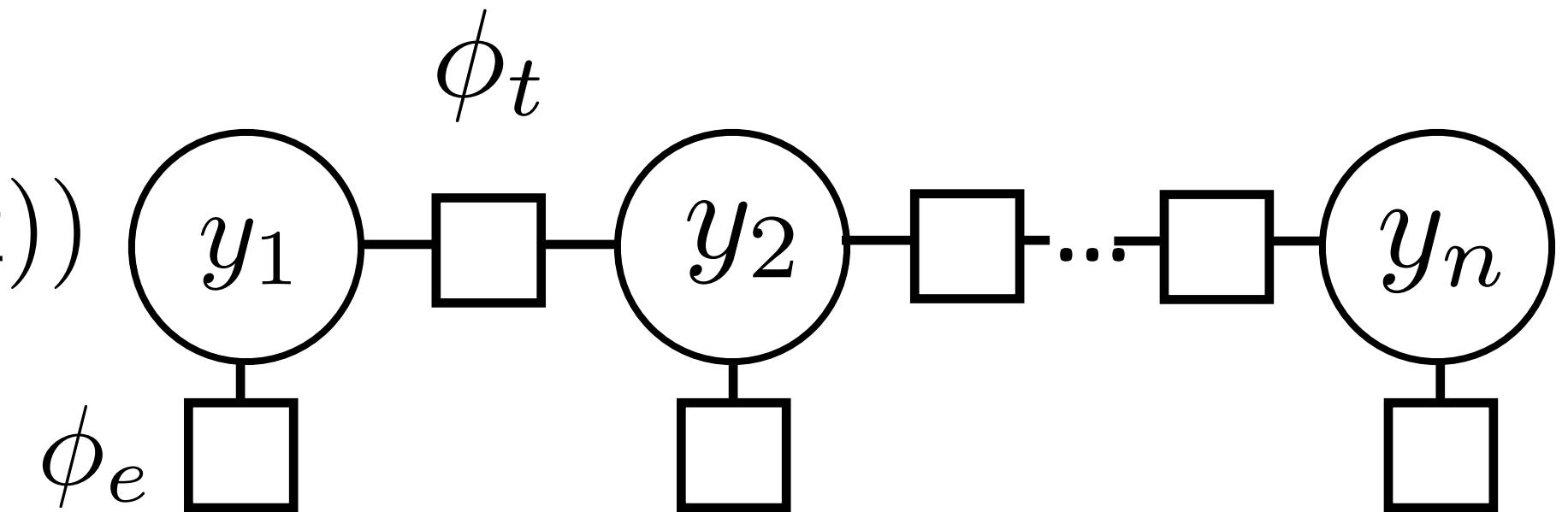


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$$\phi_e(y_i, i, \mathbf{x}) = w^\top f_e(y_i, i, \mathbf{x})$$

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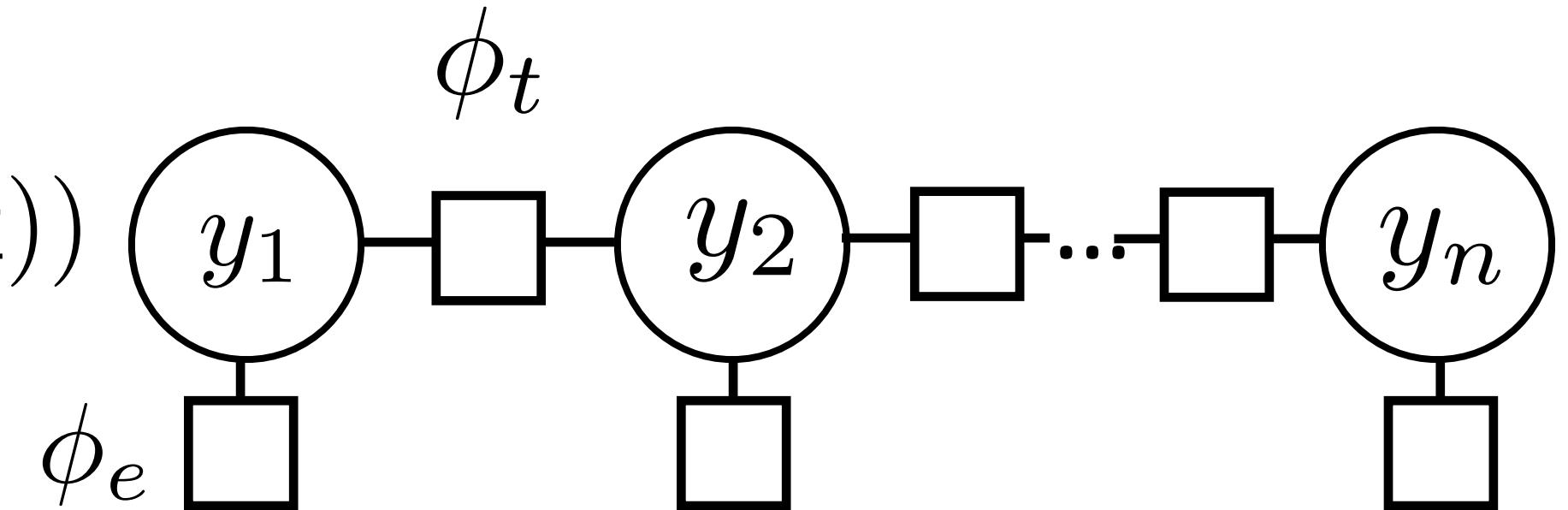


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$$\phi_e(y_i, i, \mathbf{x}) = w^\top f_e(y_i, i, \mathbf{x}) \quad \phi_t(y_{i-1}, y_i) = w^\top f_t(y_{i-1}, y_i)$$

Feature Functions

$$P(\mathbf{y}|\mathbf{x}) = \frac{1}{Z} \prod_{i=2}^n \exp(\phi_t(y_{i-1}, y_i)) \prod_{i=1}^n \exp(\phi_e(y_i, i, \mathbf{x}))$$



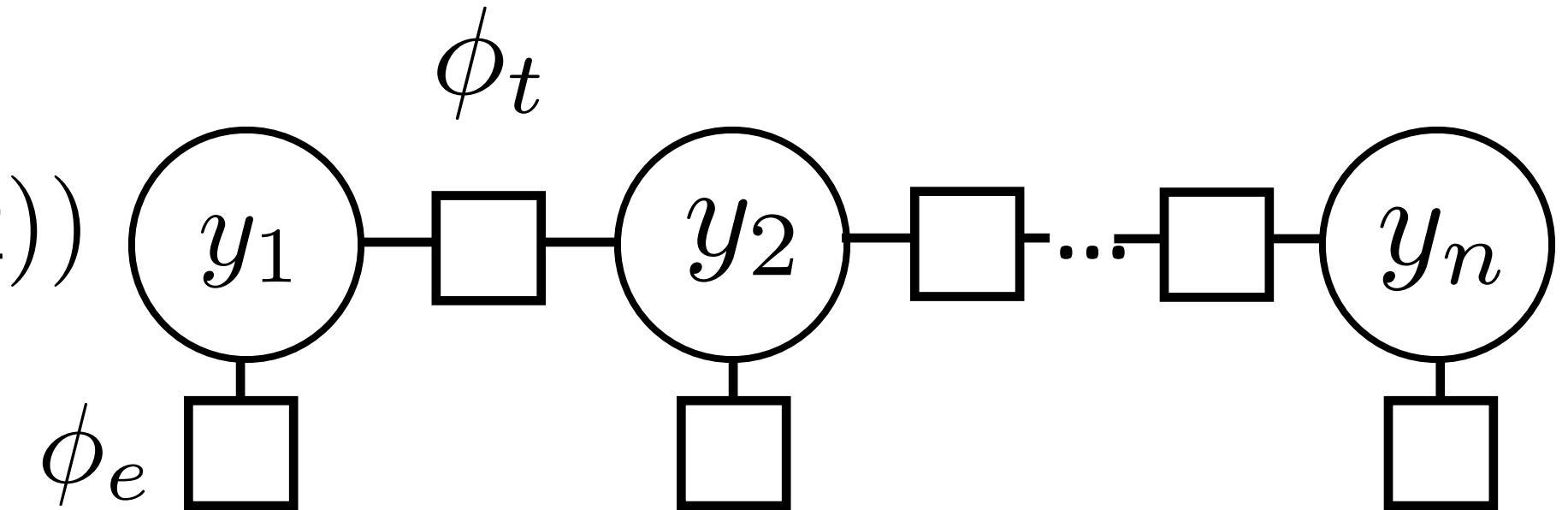
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$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

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- ▶ Looks like our single weight vector multiclass logistic regression model

Basic Features for NER

$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

Barack Obama will travel to Hangzhou today for the G20 meeting .

Basic Features for NER

$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

O B-LOC
Barack Obama will travel to Hangzhou today for the G20 meeting .

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O B-LOC
Barack Obama will travel to Hangzhou today for the G20 meeting .

Transitions: $f_t(y_{i-1}, y_i) = \text{Ind}[y_{i-1} \& y_i] = \text{Ind}[O - B-LOC]$

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$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

O B-LOC
*Barack Obama will travel to **Hangzhou** today for the G20 meeting .*

Transitions: $f_t(y_{i-1}, y_i) = \text{Ind}[y_{i-1} \& y_i] = \text{Ind}[O - B-LOC]$

Emissions: $f_e(y_6, 6, \mathbf{x}) =$

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Emissions: $f_e(y_6, 6, \mathbf{x}) = \text{Ind}[B-LOC \& \text{Current word} = Hangzhou]$

Basic Features for NER

$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

O B-LOC
*Barack Obama will travel to **Hangzhou** today for the G20 meeting .*

Transitions: $f_t(y_{i-1}, y_i) = \text{Ind}[y_{i-1} \& y_i] = \text{Ind}[O - B-LOC]$

Emissions: $f_e(y_6, 6, \mathbf{x}) = \text{Ind}[B-LOC \& \text{Current word} = Hangzhou]$
 $\text{Ind}[B-LOC \& \text{Prev word} = to]$

Features for NER

LOC

Leicestershire is a nice place to visit...

$\phi_e(y_i, i, \mathbf{x})$

PER

Leonardo DiCaprio won an award...

LOC

I took a vacation to Boston

ORG

Apple released a new version...

LOC

Texas governor Greg Abbott said

PER

According to the New York Times...

ORG

Features for NER

- ▶ Word features (can use in HMM)
 - ▶ Capitalization
 - ▶ Word shape
 - ▶ Prefixes/suffixes
 - ▶ Lexical indicators
- ▶ Context features (can't use in HMM!)
 - ▶ Words before/after
 - ▶ Tags before/after
- ▶ Word clusters
- ▶ Gazetteers

Leicestershire

Boston

Apple released a new version...

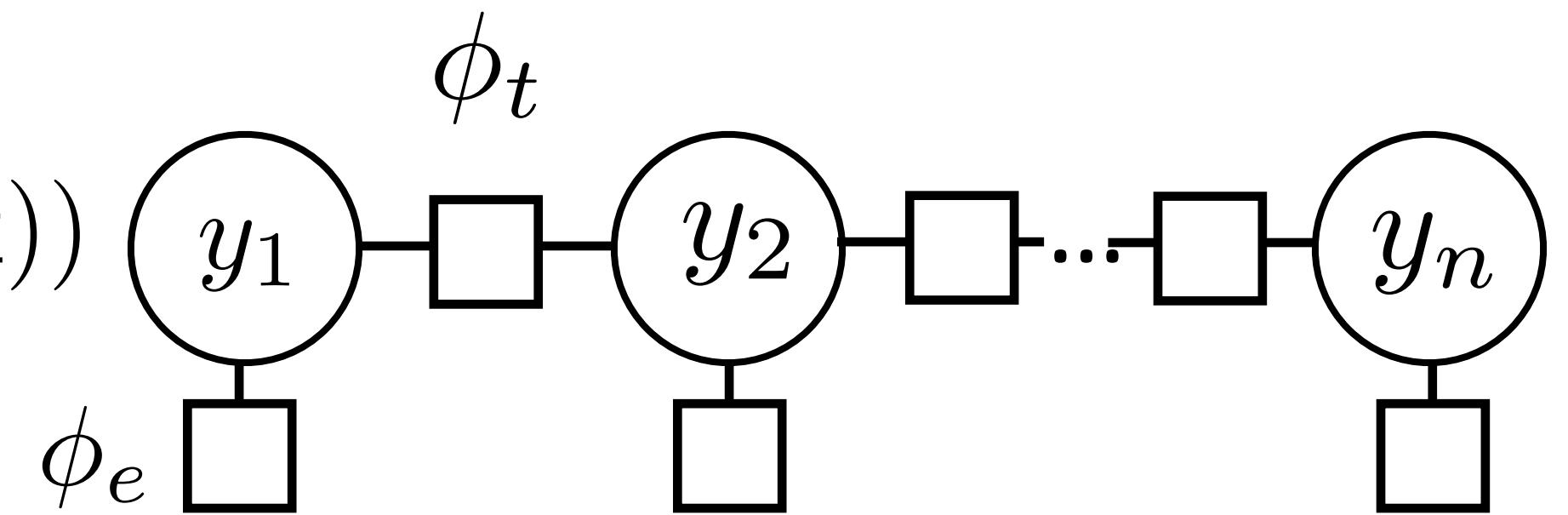
According to the New York Times...

CRFs Outline

- Model:
$$P(\mathbf{y}|\mathbf{x}) = \frac{1}{Z} \prod_{i=2}^n \exp(\phi_t(y_{i-1}, y_i)) \prod_{i=1}^n \exp(\phi_e(y_i, i, \mathbf{x}))$$
$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$
- Inference
- Learning

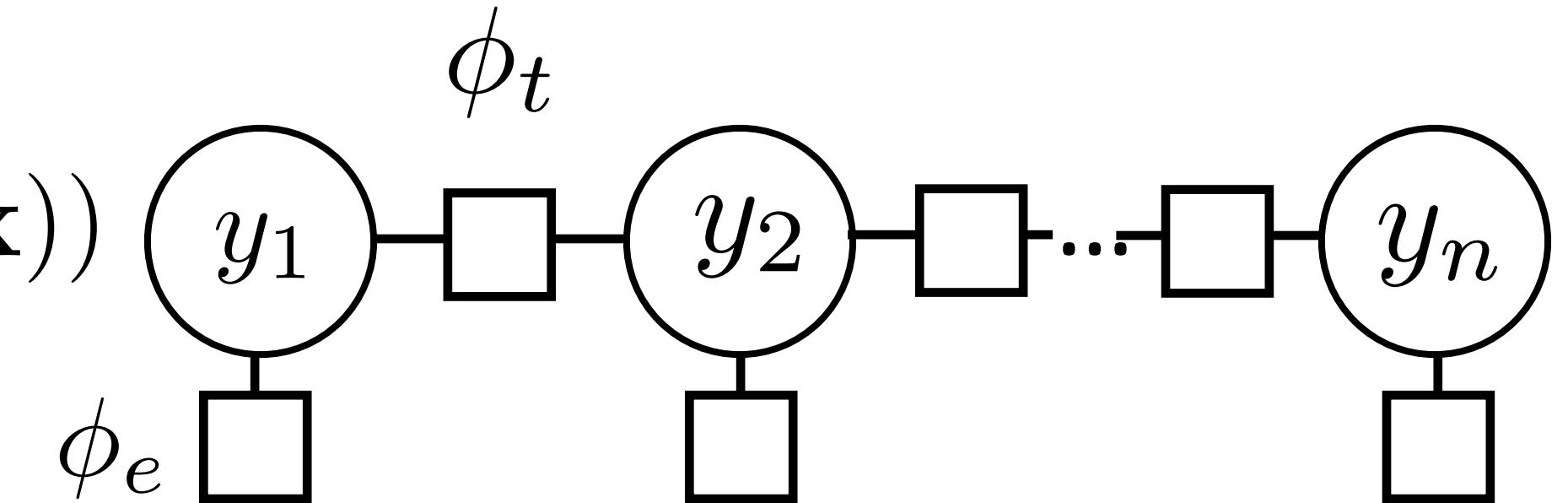
Computing (arg)maxes

$$P(\mathbf{y}|\mathbf{x}) = \frac{1}{Z} \prod_{i=2}^n \exp(\phi_t(y_{i-1}, y_i)) \prod_{i=1}^n \exp(\phi_e(y_i, i, \mathbf{x}))$$



Computing (arg)maxes

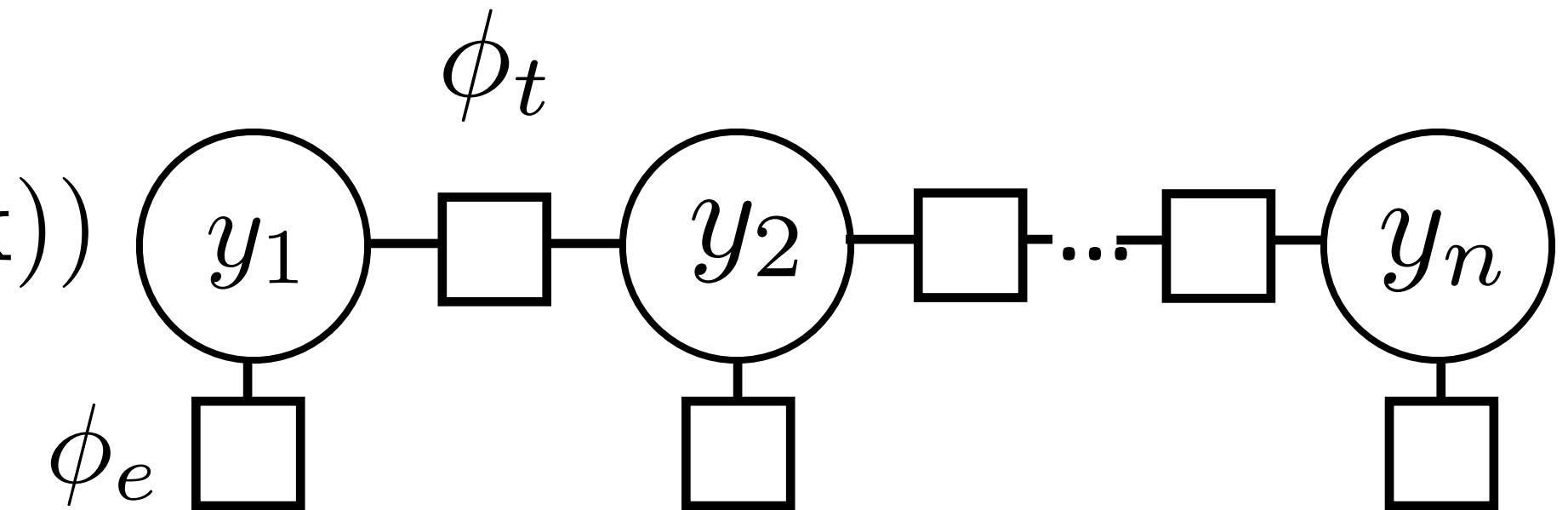
$$P(\mathbf{y}|\mathbf{x}) = \frac{1}{Z} \prod_{i=2}^n \exp(\phi_t(y_{i-1}, y_i)) \prod_{i=1}^n \exp(\phi_e(y_i, i, \mathbf{x}))$$



- ▶ $\text{argmax}_{\mathbf{y}} P(\mathbf{y}|\mathbf{x})$: can use Viterbi exactly as in HMM case

Computing (arg)maxes

$$P(\mathbf{y}|\mathbf{x}) = \frac{1}{Z} \prod_{i=2}^n \exp(\phi_t(y_{i-1}, y_i)) \prod_{i=1}^n \exp(\phi_e(y_i, i, \mathbf{x}))$$

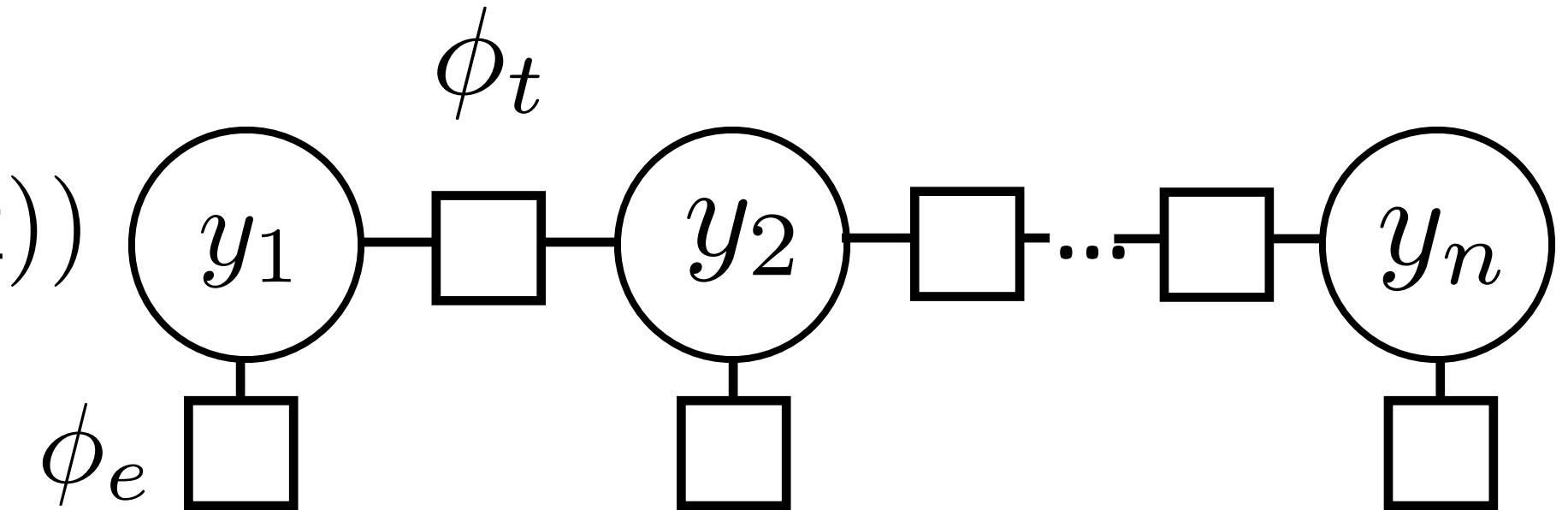


- $\text{argmax}_{\mathbf{y}} P(\mathbf{y}|\mathbf{x})$: can use Viterbi exactly as in HMM case

$$\max_{y_1, \dots, y_n} e^{\phi_t(y_{n-1}, y_n)} e^{\phi_e(y_n, n, \mathbf{x})} \dots e^{\phi_e(y_2, 2, \mathbf{x})} e^{\phi_t(y_1, y_2)} e^{\phi_e(y_1, 1, \mathbf{x})}$$

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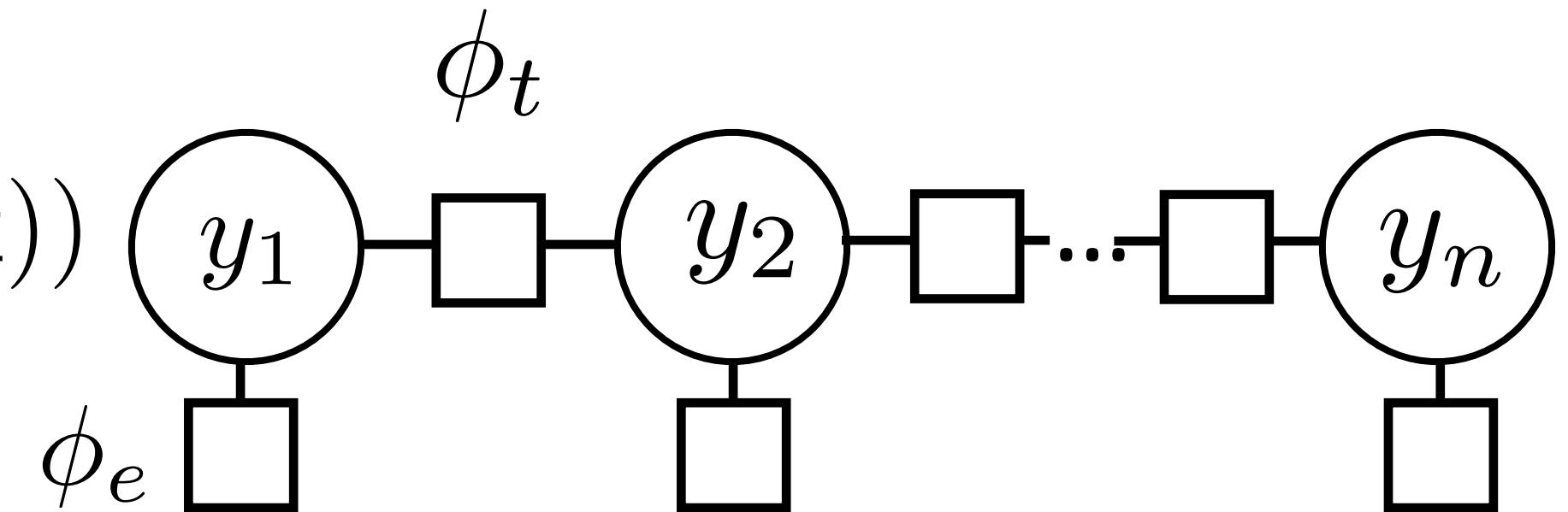
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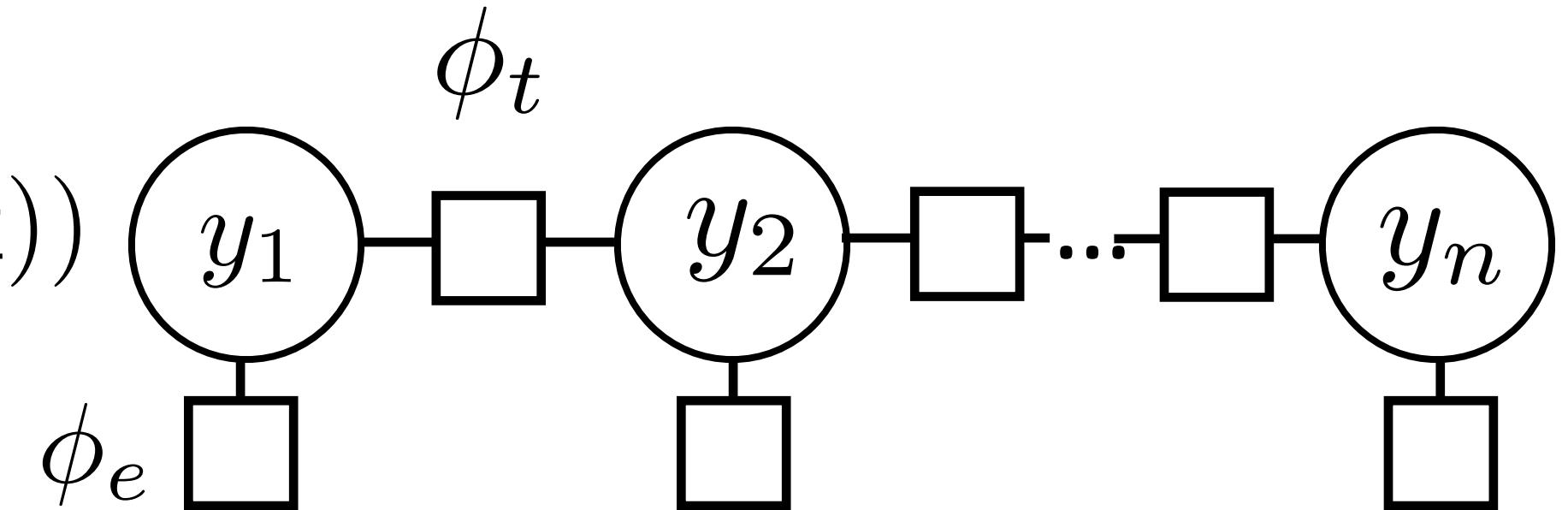
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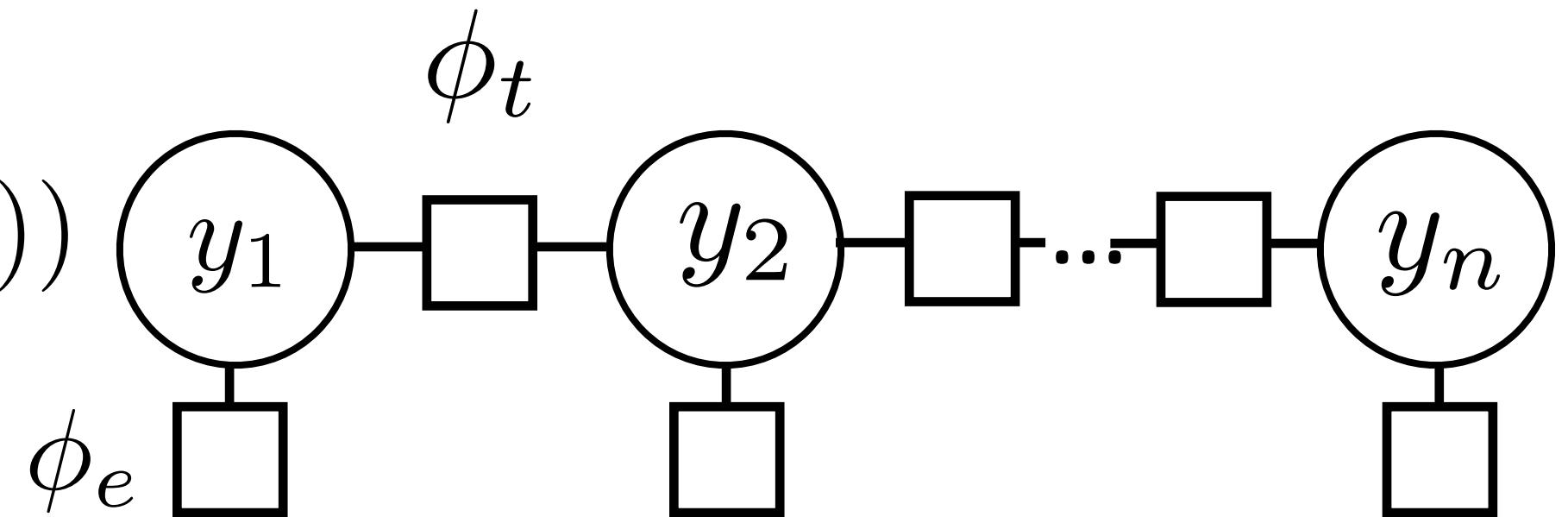
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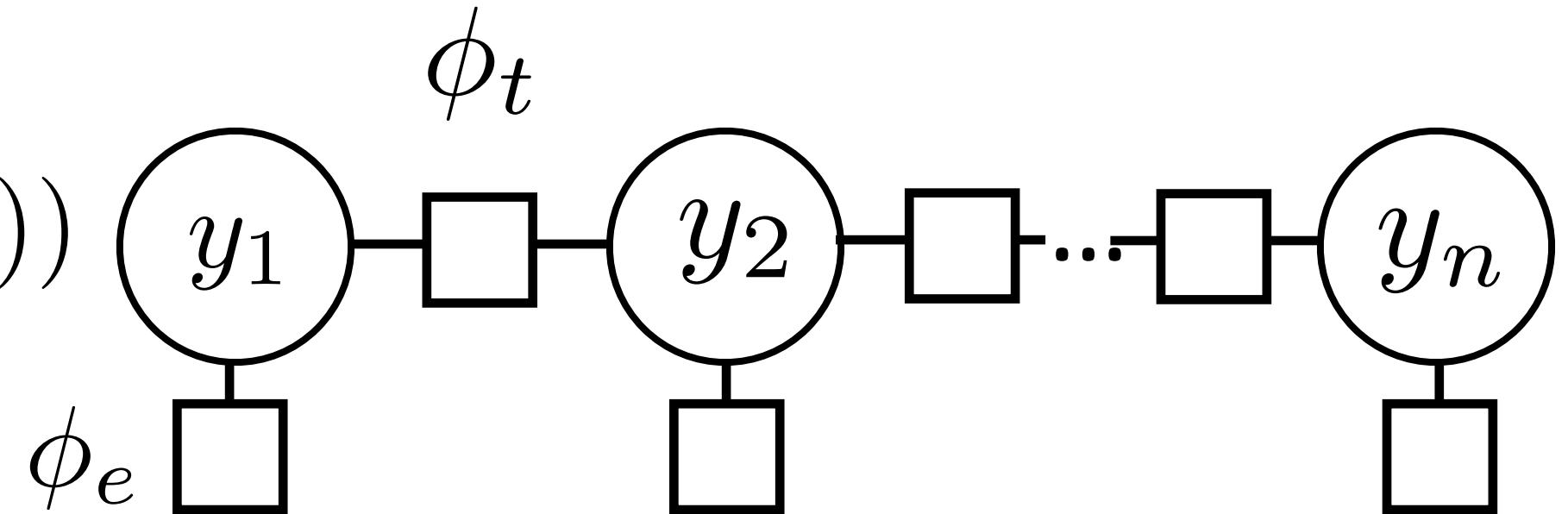


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Computing (arg)maxes

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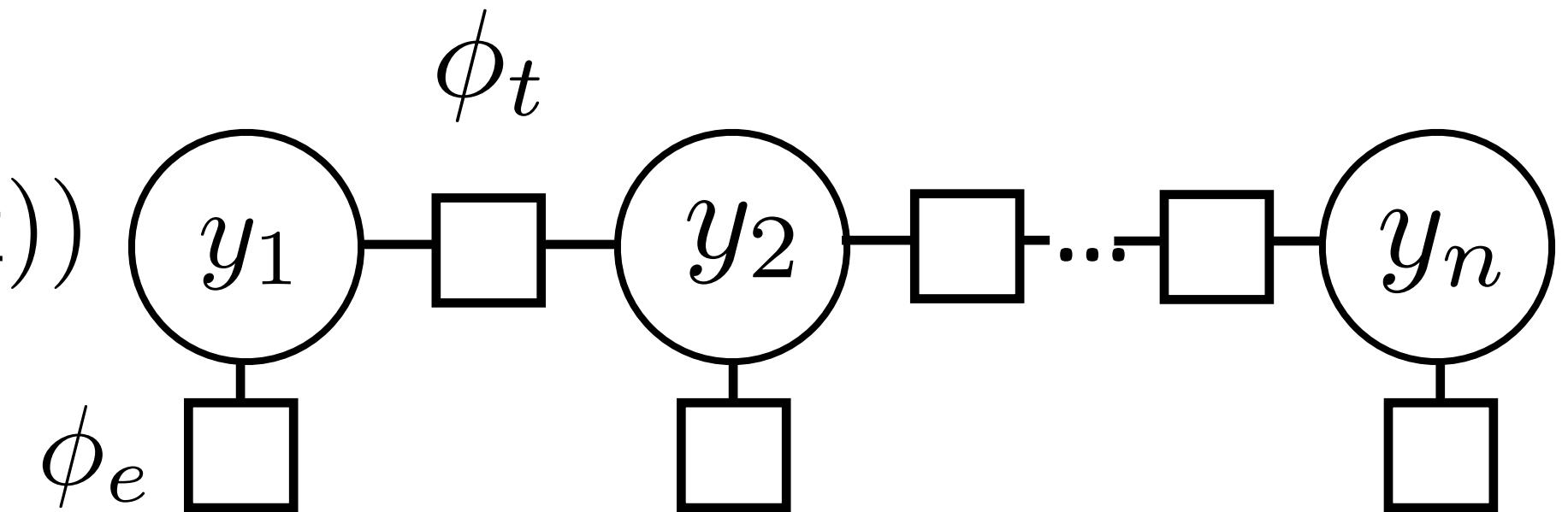


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Computing (arg)maxes

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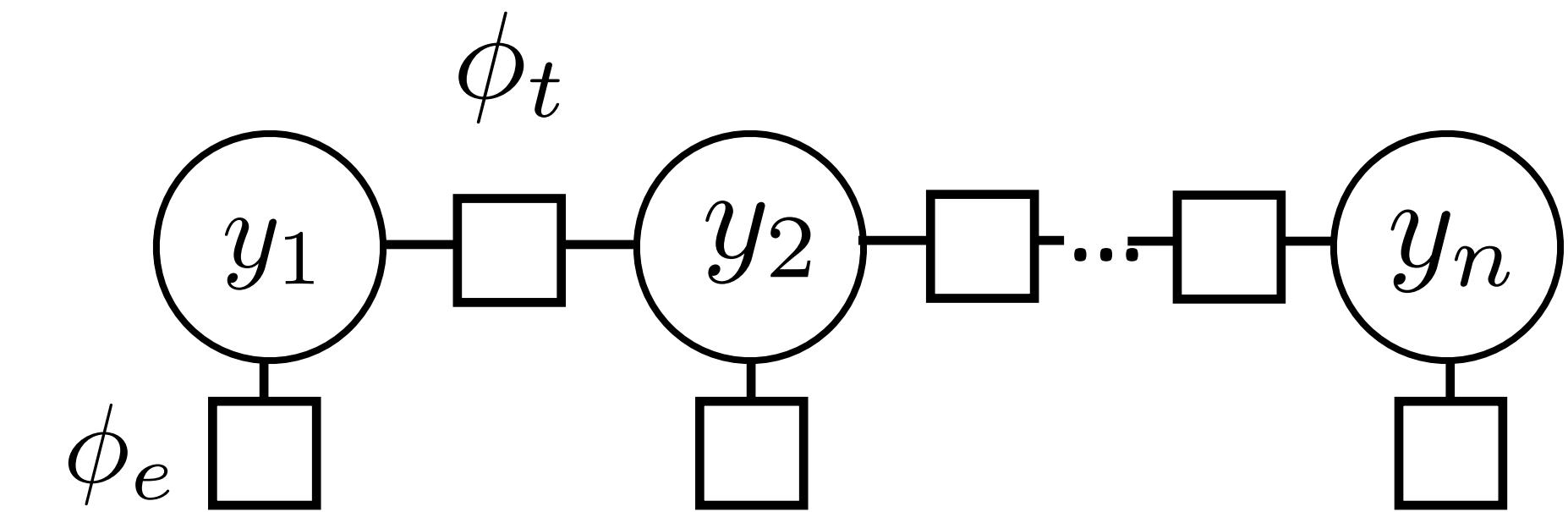


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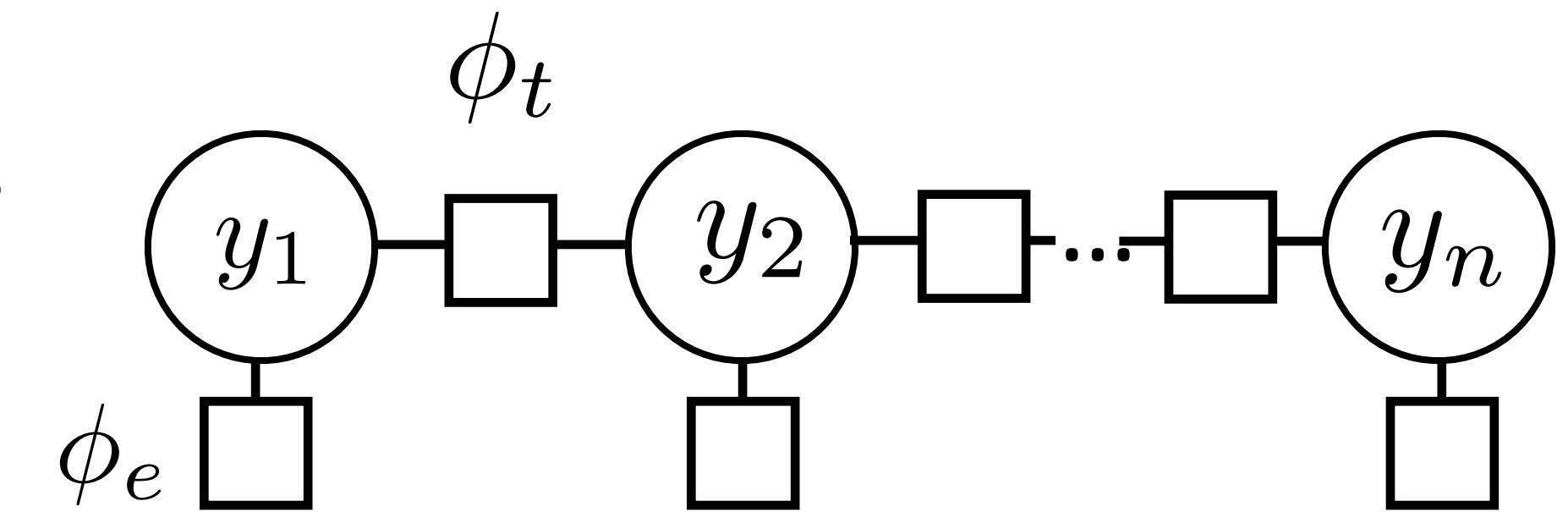
- $\exp(\phi_t(y_{i-1}, y_i))$ and $\exp(\phi_e(y_i, i, \mathbf{x}))$ play the role of the Ps now, same dynamic program

Inference in General CRFs



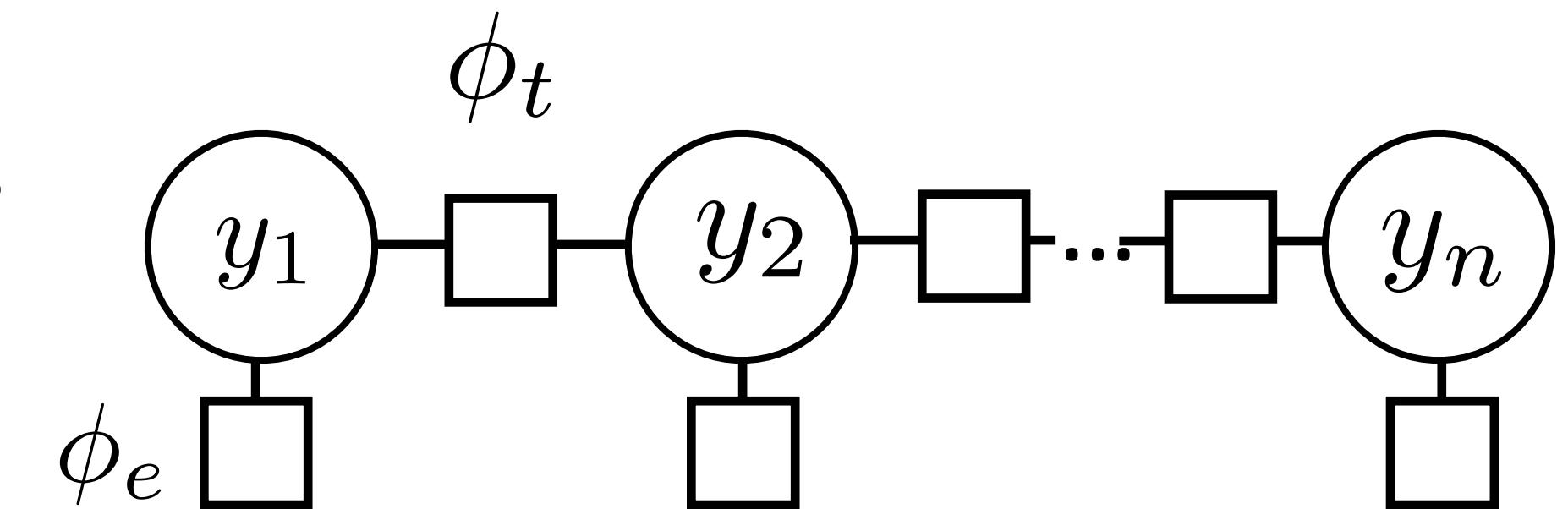
Inference in General CRFs

- ▶ Can do inference in any tree-structured CRF



Inference in General CRFs

- ▶ Can do inference in any tree-structured CRF



- ▶ Max-product algorithm: generalization of Viterbi to arbitrary tree-structured graphs (sum-product is generalization of forward-backward)

CRFs Outline

- Model: $P(\mathbf{y}|\mathbf{x}) = \frac{1}{Z} \prod_{i=2}^n \exp(\phi_t(y_{i-1}, y_i)) \prod_{i=1}^n \exp(\phi_e(y_i, i, \mathbf{x}))$
$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$
- Inference: argmax $P(\mathbf{y}|\mathbf{x})$ from Viterbi
- Learning

Training CRFs

$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

Training CRFs

$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

- ▶ Logistic regression: $P(y|x) \propto \exp w^\top f(x, y)$

Training CRFs

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- ▶ Maximize $\mathcal{L}(\mathbf{y}^*, \mathbf{x}) = \log P(\mathbf{y}^*|\mathbf{x})$

Training CRFs

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- ▶ Gradient is completely analogous to logistic regression:

Training CRFs

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$$\begin{aligned} \frac{\partial}{\partial w} \mathcal{L}(\mathbf{y}^*, \mathbf{x}) &= \sum_{i=2}^n f_t(y_{i-1}^*, y_i^*) + \sum_{i=1}^n f_e(y_i^*, i, \mathbf{x}) \\ &\quad - \mathbb{E}_{\mathbf{y}} \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right] \end{aligned}$$

Training CRFs

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$$\frac{\partial}{\partial w} \mathcal{L}(\mathbf{y}^*, \mathbf{x}) = \sum_{i=2}^n f_t(y_{i-1}^*, y_i^*) + \sum_{i=1}^n f_e(y_i^*, i, \mathbf{x})$$

intractable! $\xrightarrow{-\mathbb{E}_{\mathbf{y}} \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]}$

Training CRFs

$$\begin{aligned} \frac{\partial}{\partial w} \mathcal{L}(\mathbf{y}^*, \mathbf{x}) &= \sum_{i=2}^n f_t(y_{i-1}^*, y_i^*) + \sum_{i=1}^n f_e(y_i^*, i, \mathbf{x}) \\ &\quad - \mathbb{E}_{\mathbf{y}} \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right] \end{aligned}$$

Training CRFs

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- ▶ Let's focus on emission feature expectation

Training CRFs

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► Let's focus on emission feature expectation

$$\mathbb{E}_{\mathbf{y}} \left[\sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

Training CRFs

$$\begin{aligned}\frac{\partial}{\partial w} \mathcal{L}(\mathbf{y}^*, \mathbf{x}) &= \sum_{i=2}^n f_t(y_{i-1}^*, y_i^*) + \sum_{i=1}^n f_e(y_i^*, i, \mathbf{x}) \\ &\quad - \mathbb{E}_{\mathbf{y}} \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]\end{aligned}$$

► Let's focus on emission feature expectation

$$\mathbb{E}_{\mathbf{y}} \left[\sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right] = \sum_{\mathbf{y} \in \mathcal{Y}} P(\mathbf{y} | \mathbf{x}) \left[\sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

Training CRFs

$$\begin{aligned}\frac{\partial}{\partial w} \mathcal{L}(\mathbf{y}^*, \mathbf{x}) &= \sum_{i=2}^n f_t(y_{i-1}^*, y_i^*) + \sum_{i=1}^n f_e(y_i^*, i, \mathbf{x}) \\ &\quad - \mathbb{E}_{\mathbf{y}} \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]\end{aligned}$$

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Training CRFs

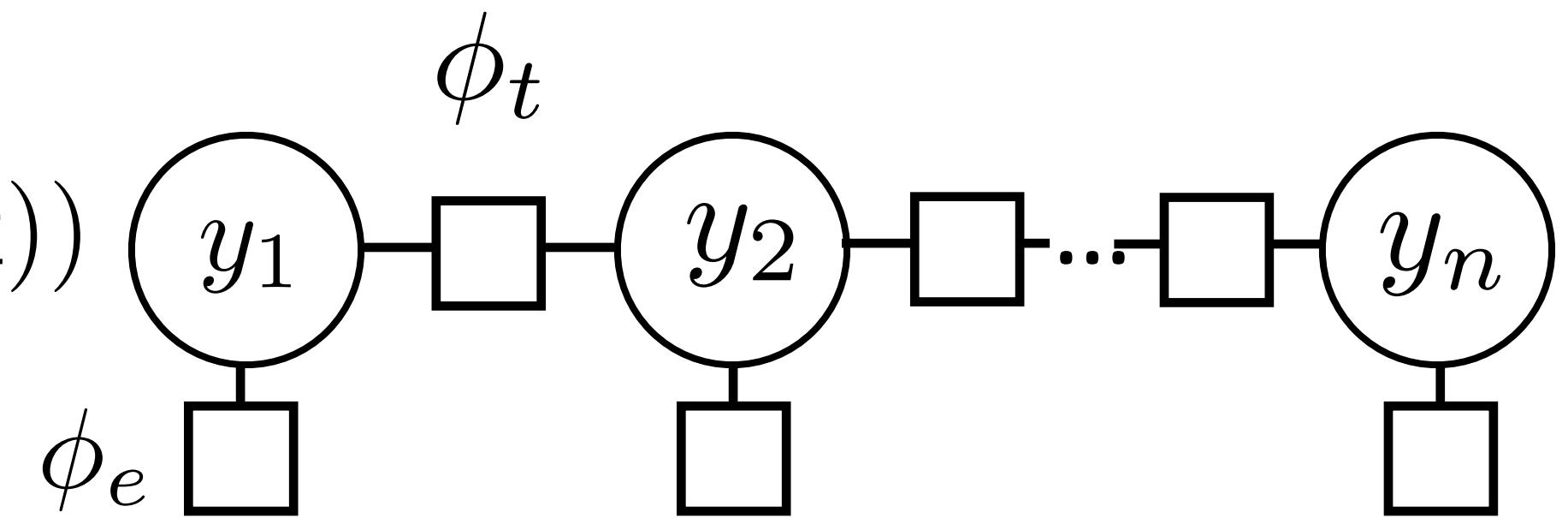
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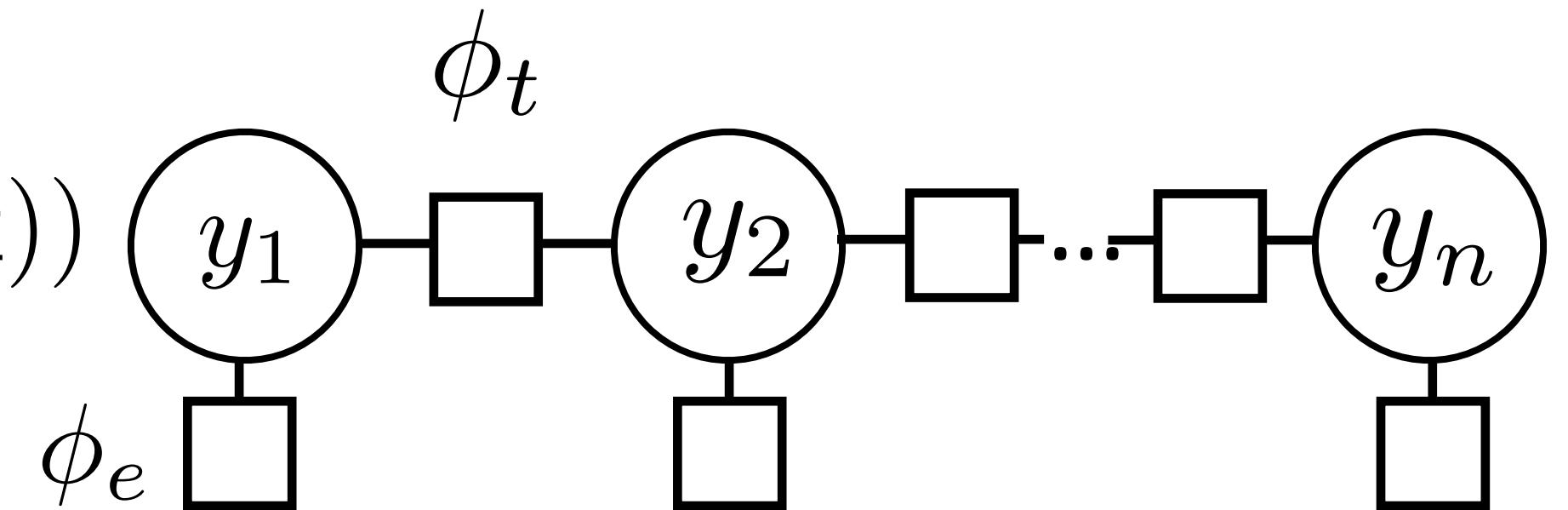
Computing Marginals

$$P(\mathbf{y}|\mathbf{x}) = \frac{1}{Z} \prod_{i=2}^n \exp(\phi_t(y_{i-1}, y_i)) \prod_{i=1}^n \exp(\phi_e(y_i, i, \mathbf{x}))$$



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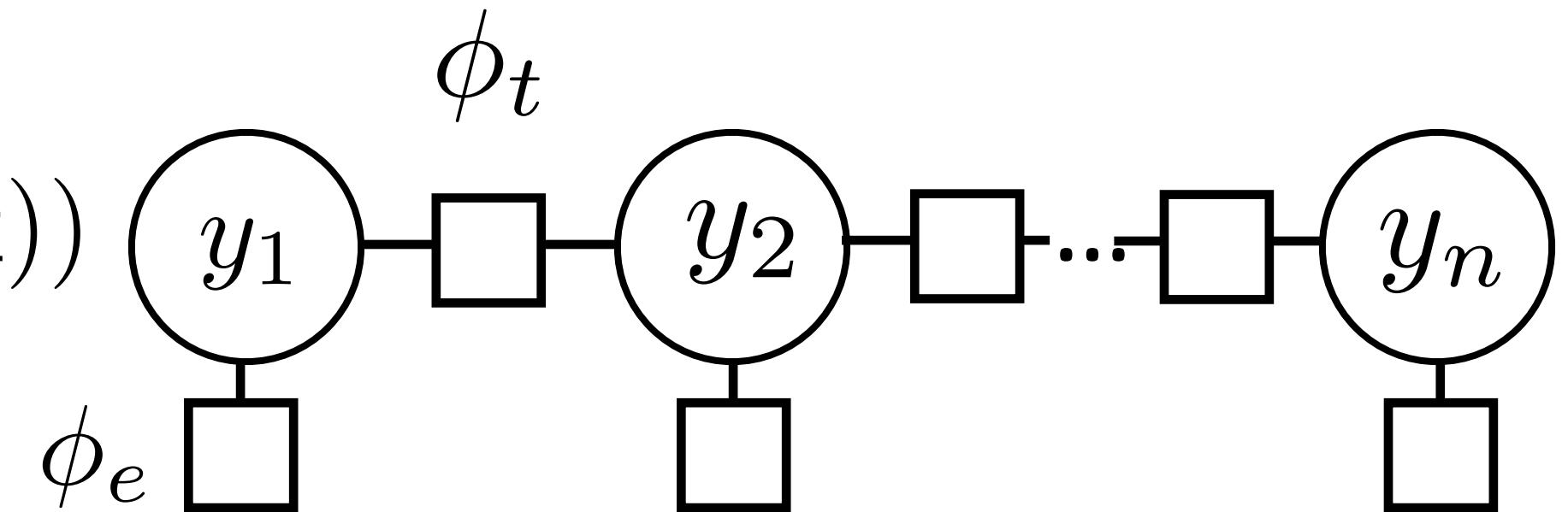
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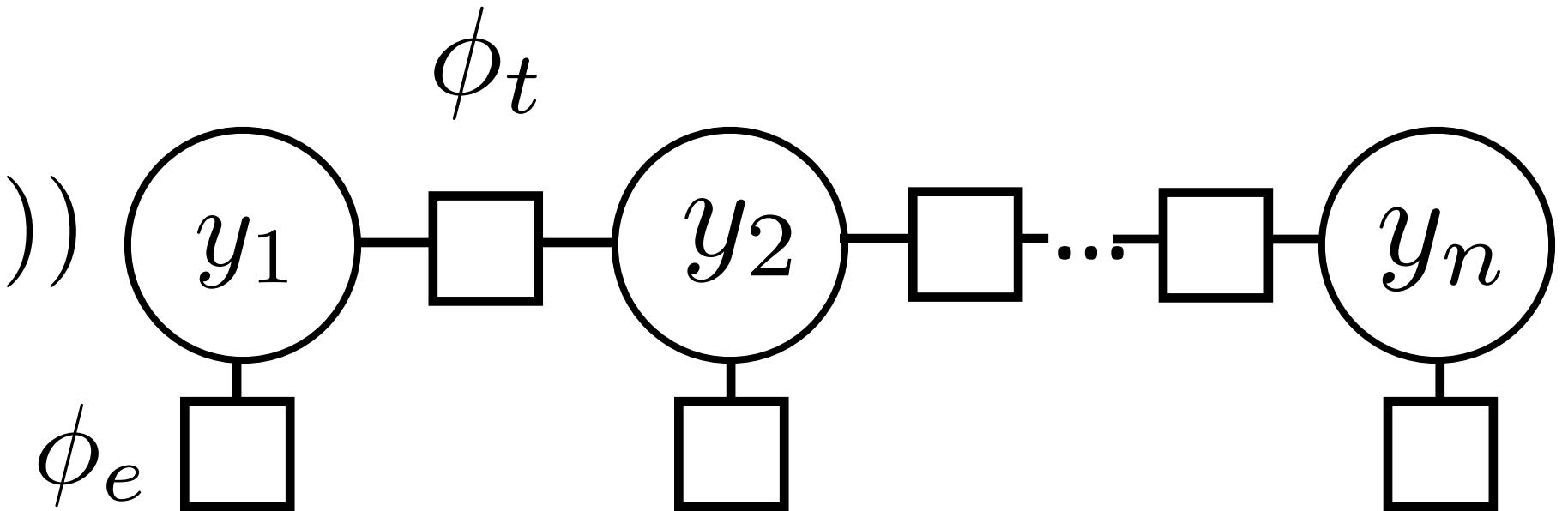
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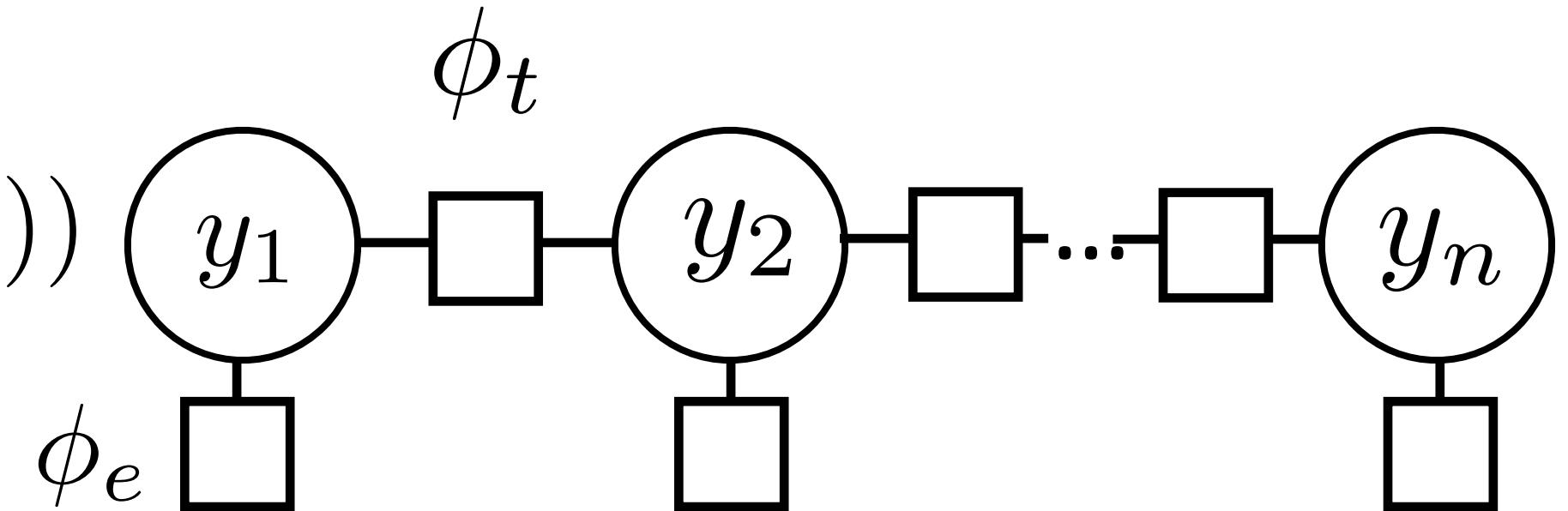


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- ▶ Transition features: need to compute $P(y_i = s_1, y_{i+1} = s_2 | \mathbf{x})$ using forward-backward as well

CRFs Outline

- Model:
$$P(\mathbf{y}|\mathbf{x}) = \frac{1}{Z} \prod_{i=2}^n \exp(\phi_t(y_{i-1}, y_i)) \prod_{i=1}^n \exp(\phi_e(y_i, i, \mathbf{x}))$$
$$P(\mathbf{y}|\mathbf{x}) \propto \exp w^\top \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$
- Inference: argmax $P(\mathbf{y}|\mathbf{x})$ from Viterbi
- Learning: run forward-backward to compute posterior probabilities; then

$$\frac{\partial}{\partial w} \mathcal{L}(\mathbf{y}^*, \mathbf{x}) = \sum_{i=1}^n f_e(y_i^*, i, \mathbf{x}) - \sum_{i=1}^n \sum_s P(y_i = s | \mathbf{x}) f_e(s, i, \mathbf{x})$$

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    for each example
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        compute potentials phi based on features + weights
        compute marginal probabilities with forward-backward
        accumulate gradient over all emissions and transitions
```

Structured Perceptron

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► Structured Perceptron Update:

$$\hat{y} = \operatorname{argmax}_{y \in \mathcal{Y}} w^\top f(x, y)$$

$$w = w + f(x, y^*) - f(x, \hat{y})$$

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Replaces Expectation
With argmax

$$- \mathbb{E}_y \left[\sum_{i=2}^n f_t(y_{i-1}, y_i) + \sum_{i=1}^n f_e(y_i, i, \mathbf{x}) \right]$$

NER

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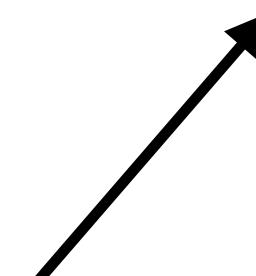
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Tanjug

From Wikipedia, the free encyclopedia

Tanjug (/tʌnjʊg/) ([Serbian Cyrillic](#): Танјуг) is a Serbian state news agency based in [Belgrade](#).^[2]



Nonlocal Features

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Nonlocal Features

ORG?
PER?

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- More complex factor graph structures can let you capture this, or just decode sentences in order and use features on previous sentences

Semi-Markov Models

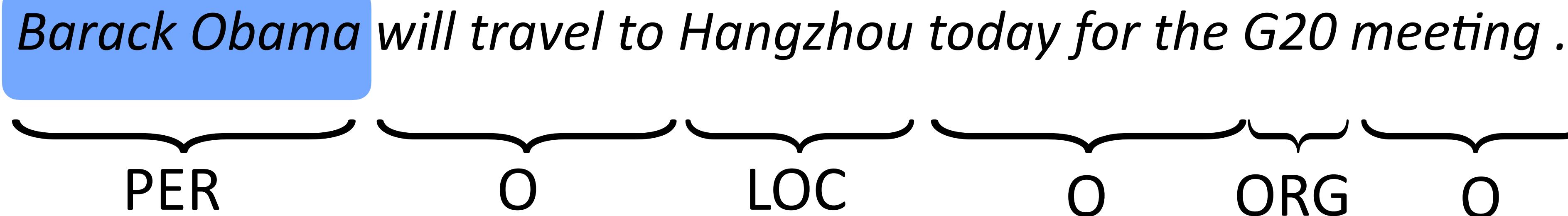
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Semi-Markov Models

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- ▶ Chunk-level prediction rather than token-level BIO

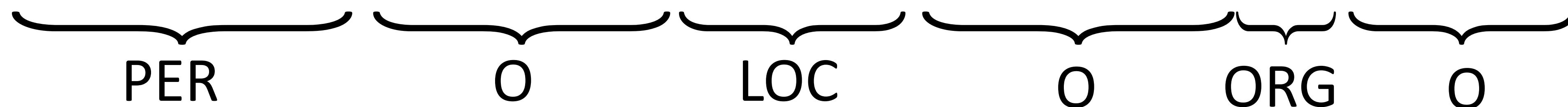
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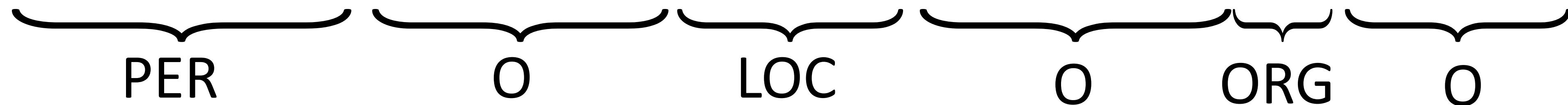
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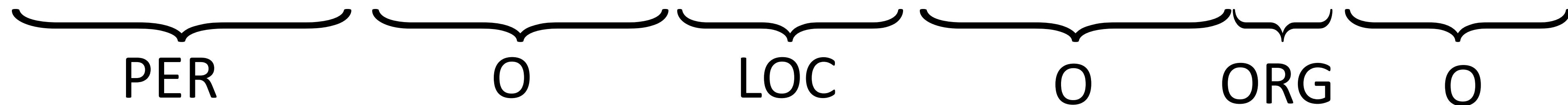
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- ▶ Cons: there's an extra factor of n in the dynamic programs

Evaluating NER

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- ▶ F-measure: harmonic mean of these two

How well do NER systems do?

	System	Resources Used	F_1
+	LBJ-NER	Wikipedia, Nonlocal Features, Word-class Model	90.80
-	(Suzuki and Isozaki, 2008)	Semi-supervised on 1G-word unlabeled data	89.92
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Beam Search

Viterbi Time Complexity

VBD

VBN VBZ

NNP NNS

VB

VBP VBZ

NN NNS CD NN

Fed raises interest rates 0.5 percent

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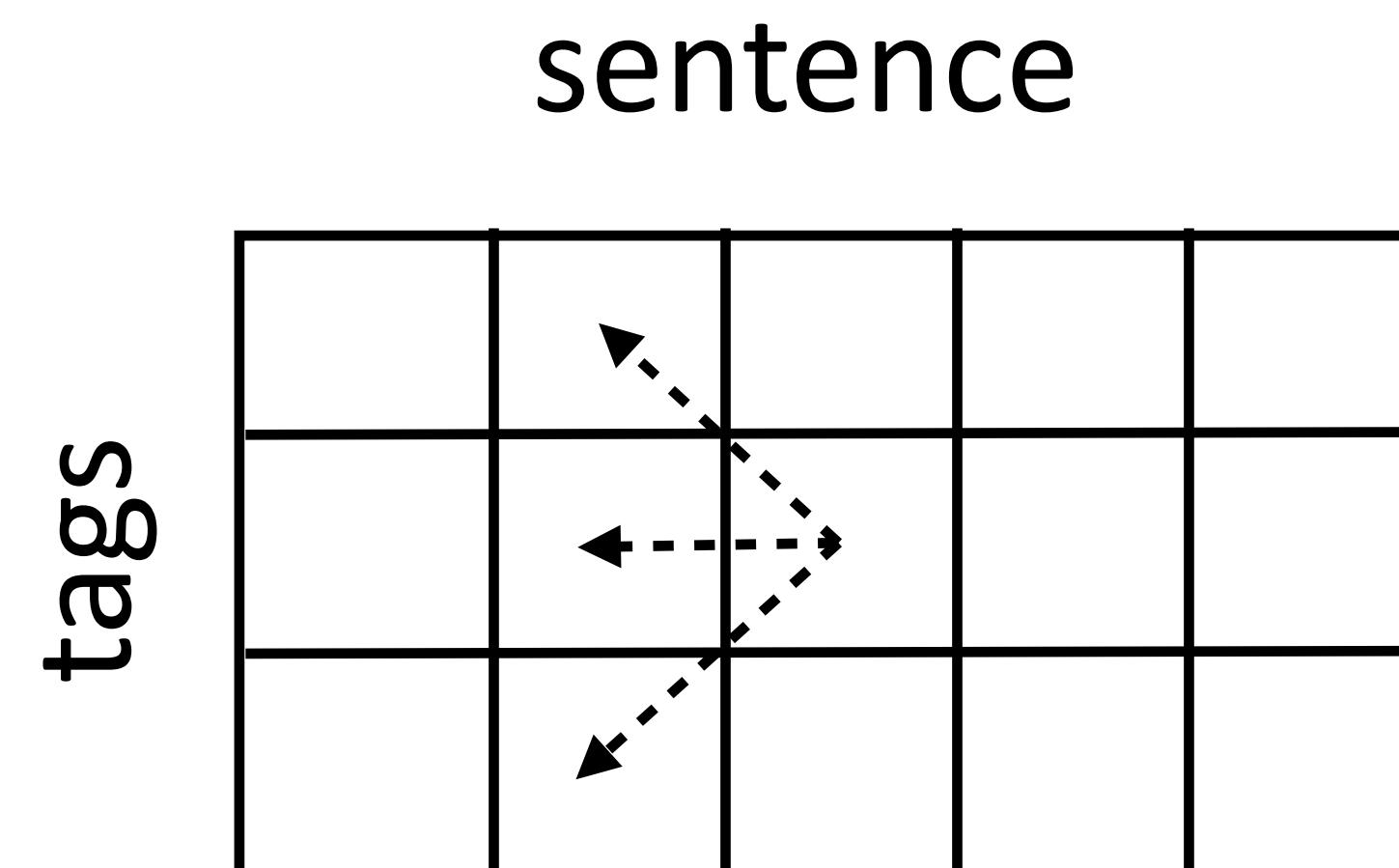
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Fed raises interest rates 0.5 percent

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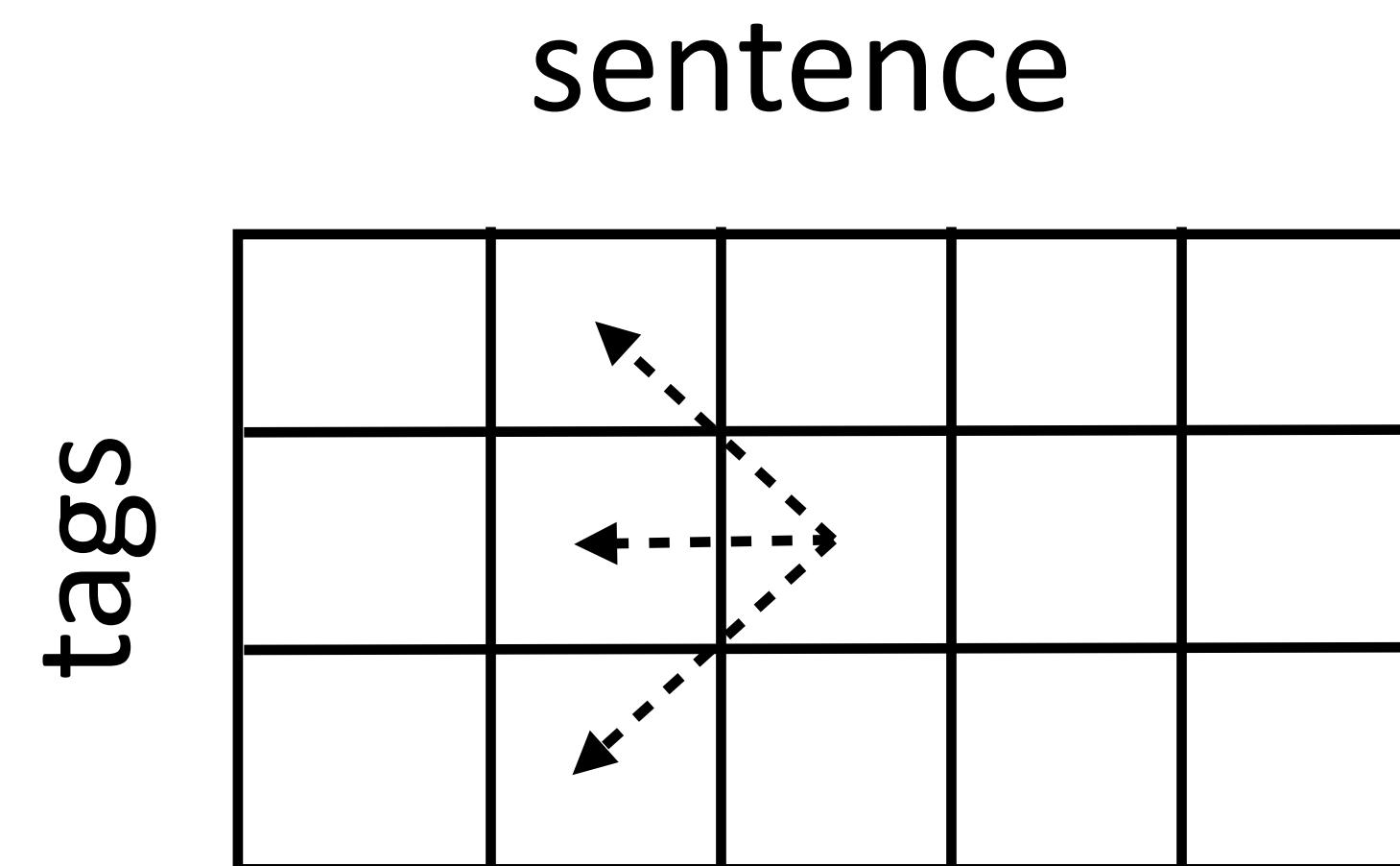


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- ▶ $O(ns^2)$ – s is ~40 for POS, n is ~20

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 - ▶ Prepositions?
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- ▶ Can any of these be:
 - ▶ Determiners?
 - ▶ Prepositions?
 - ▶ Adjectives?
- ▶ Features quickly eliminate many outcomes from consideration — don't need to consider these going forward

Beam Search

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- ▶ Maintain a beam of k plausible states at the current timestep

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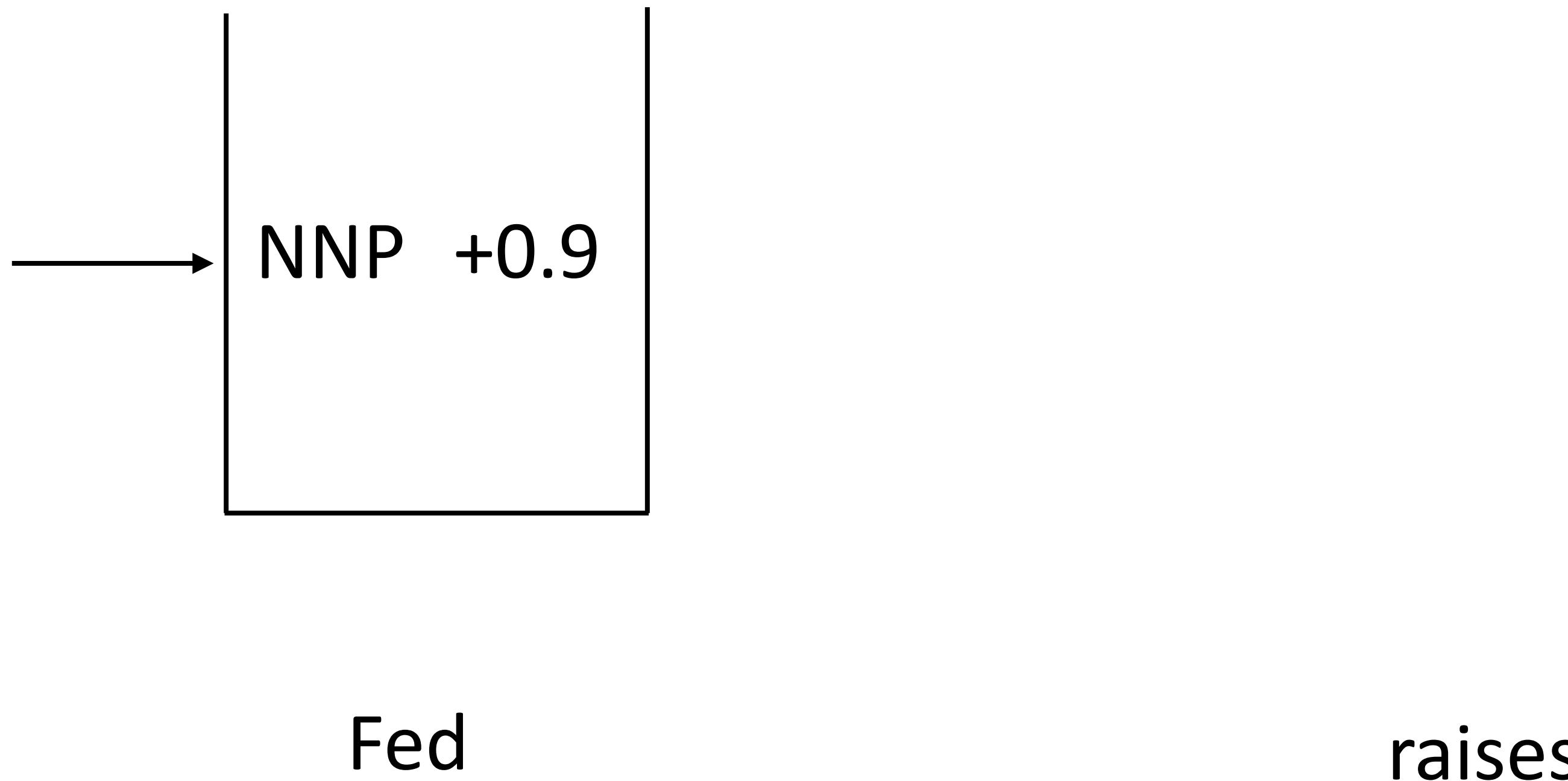


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→	VBD	+1.2
→	NNP	+0.9

Fed

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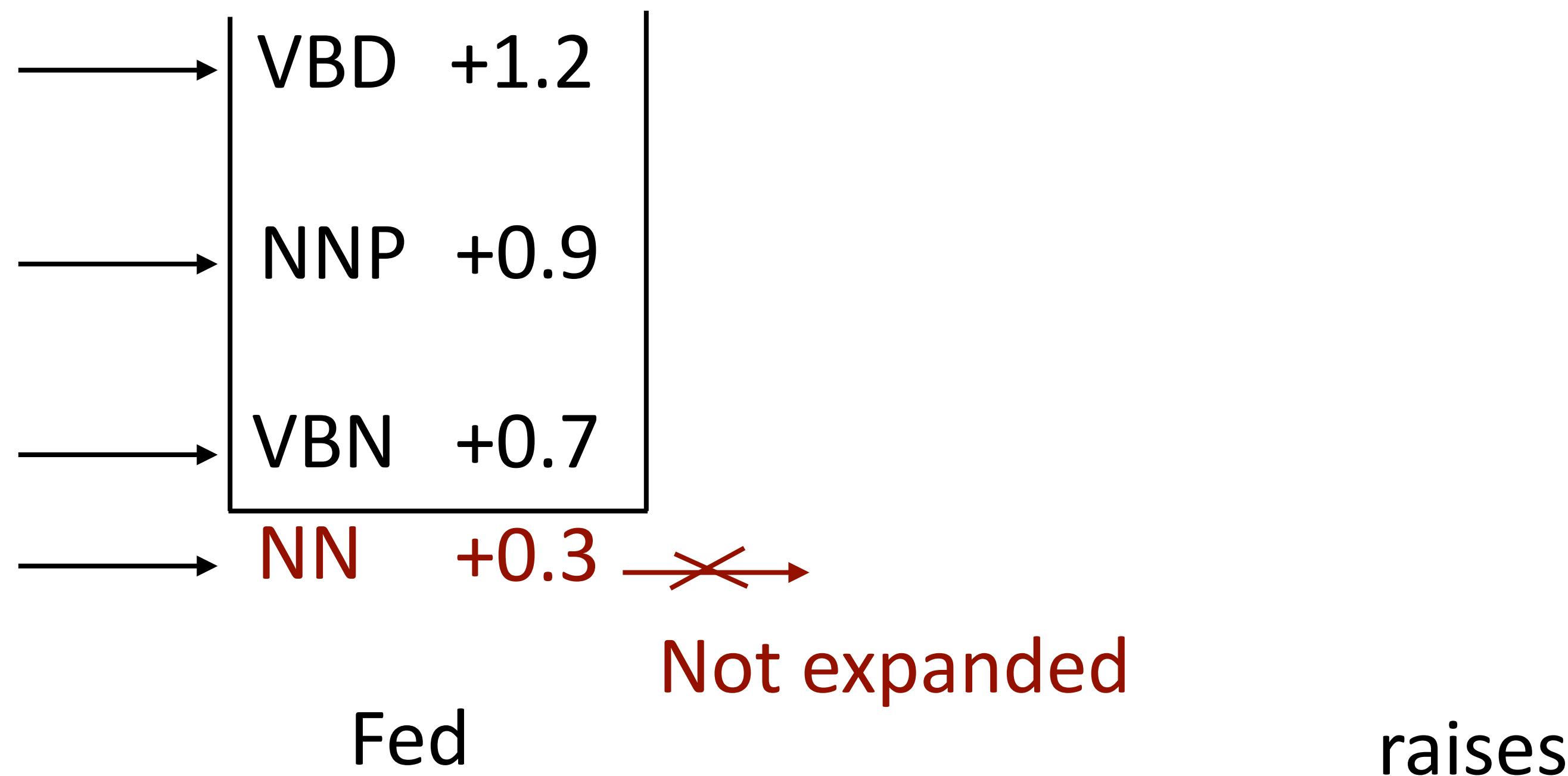
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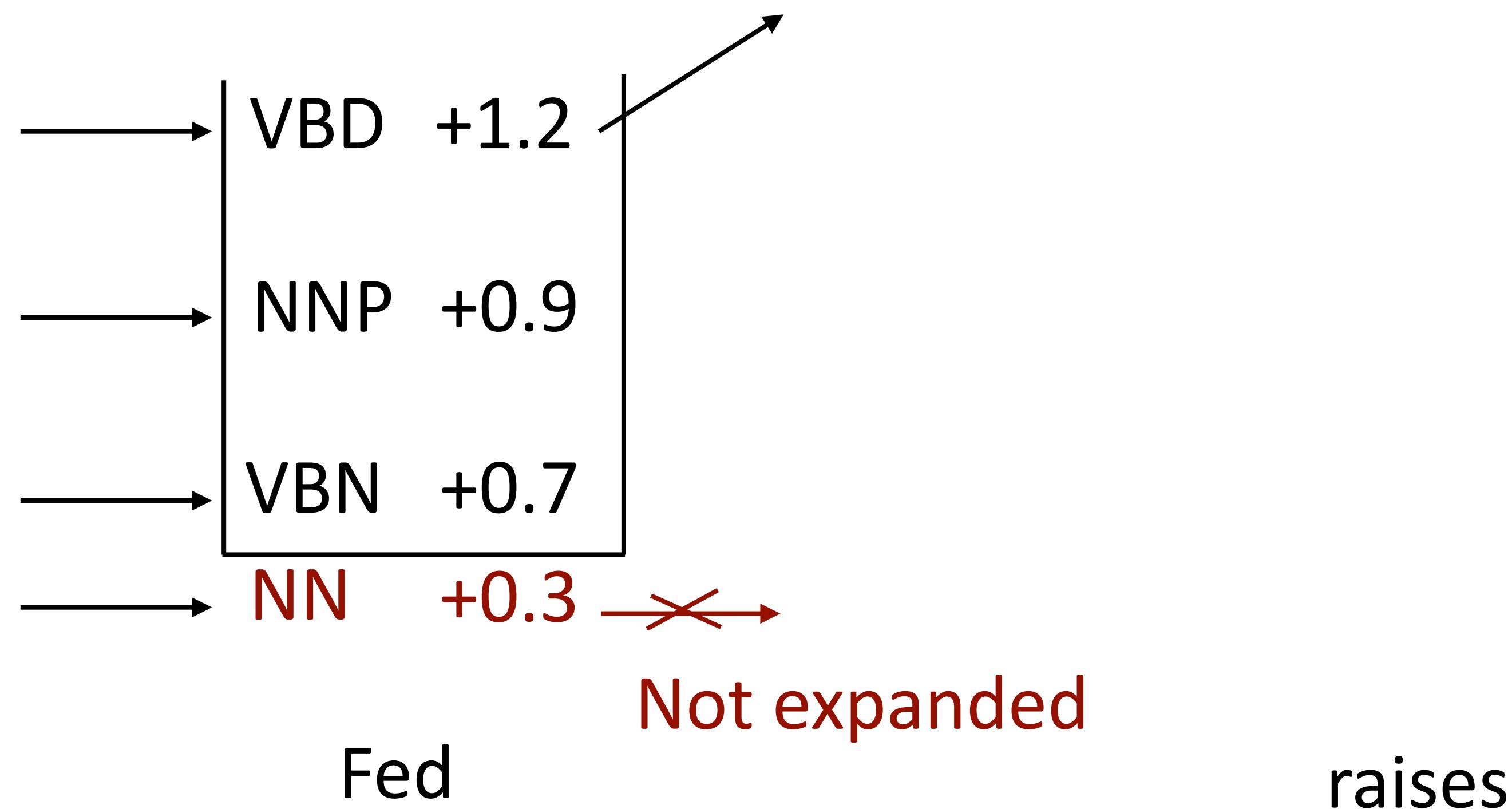
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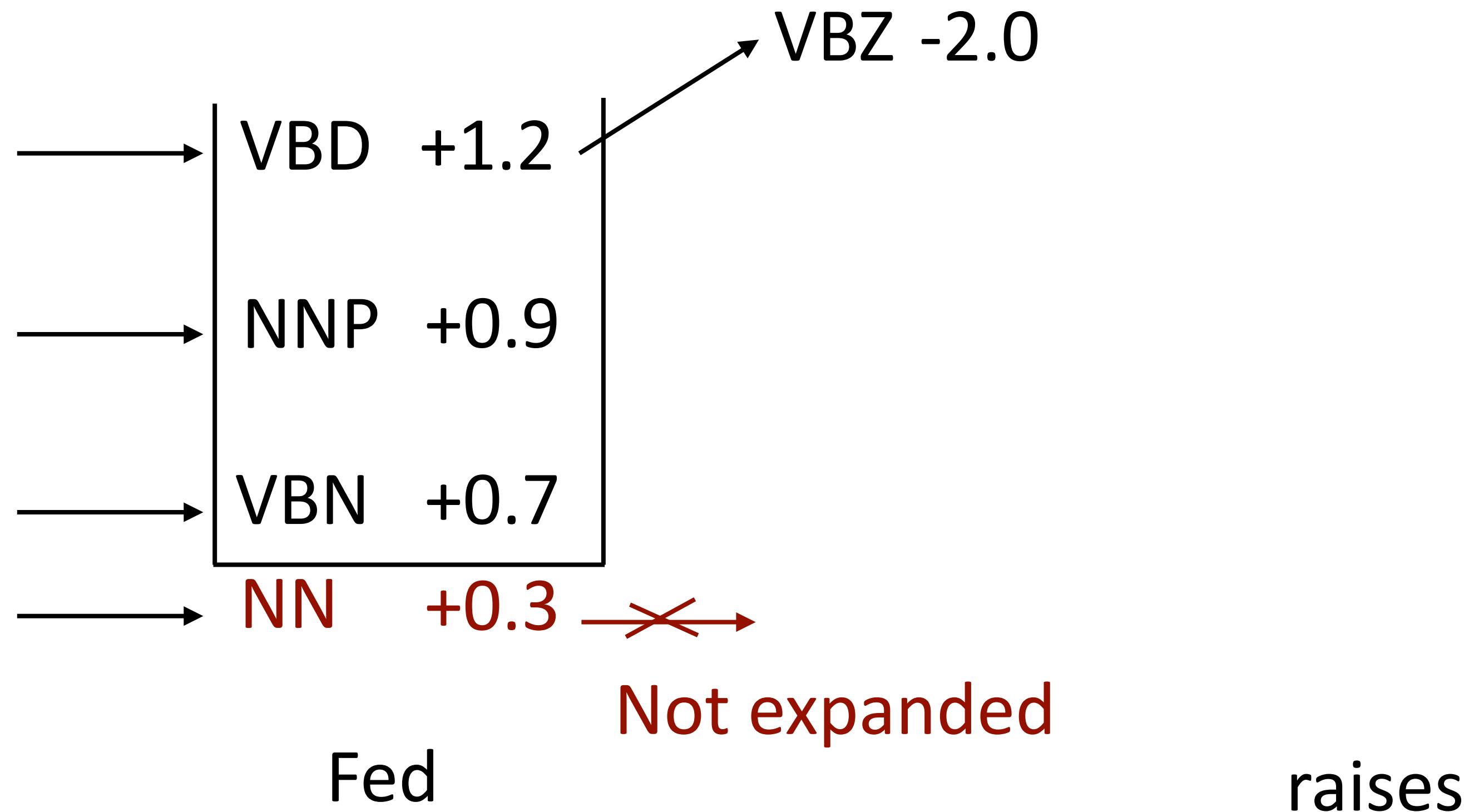
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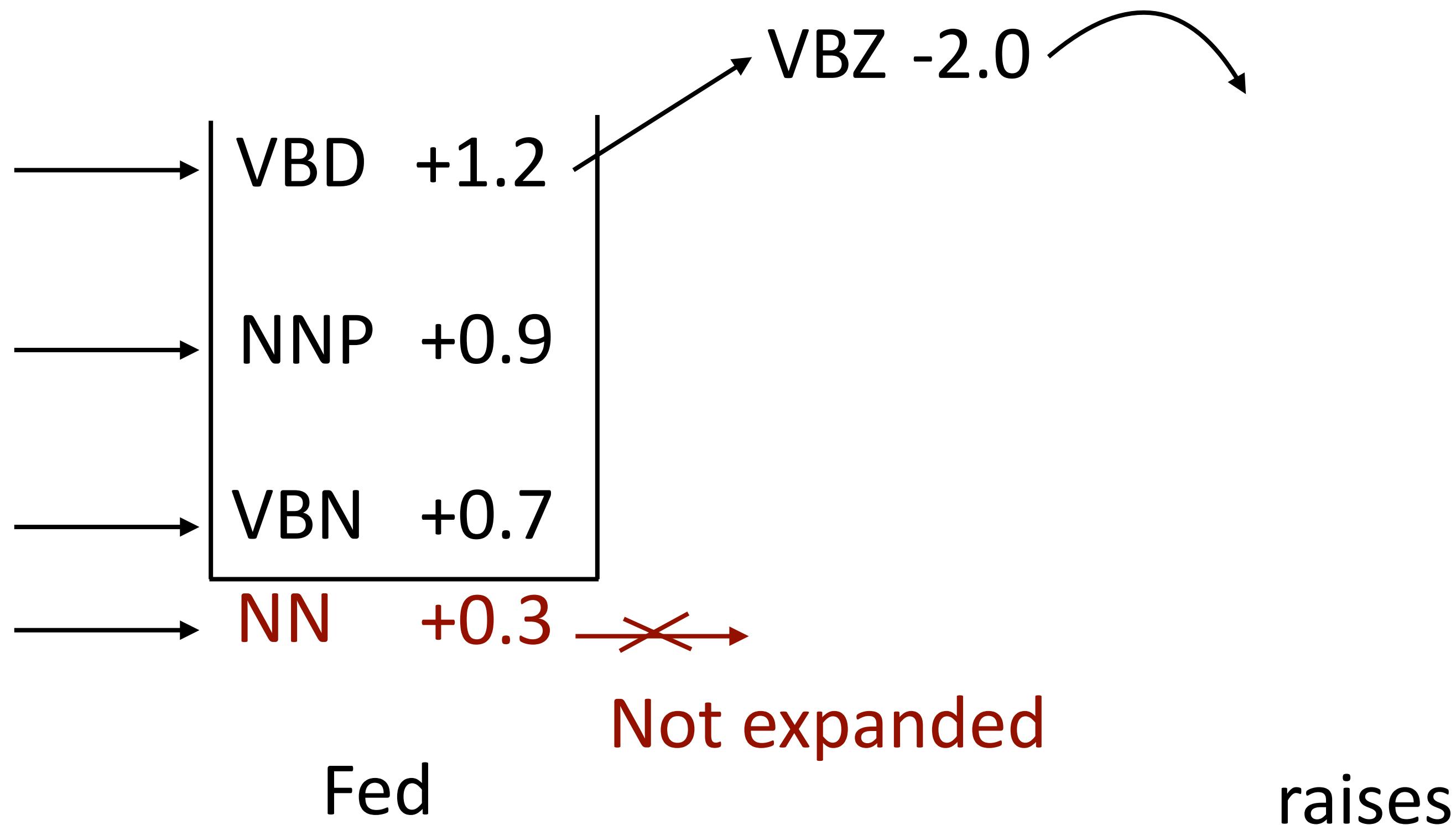
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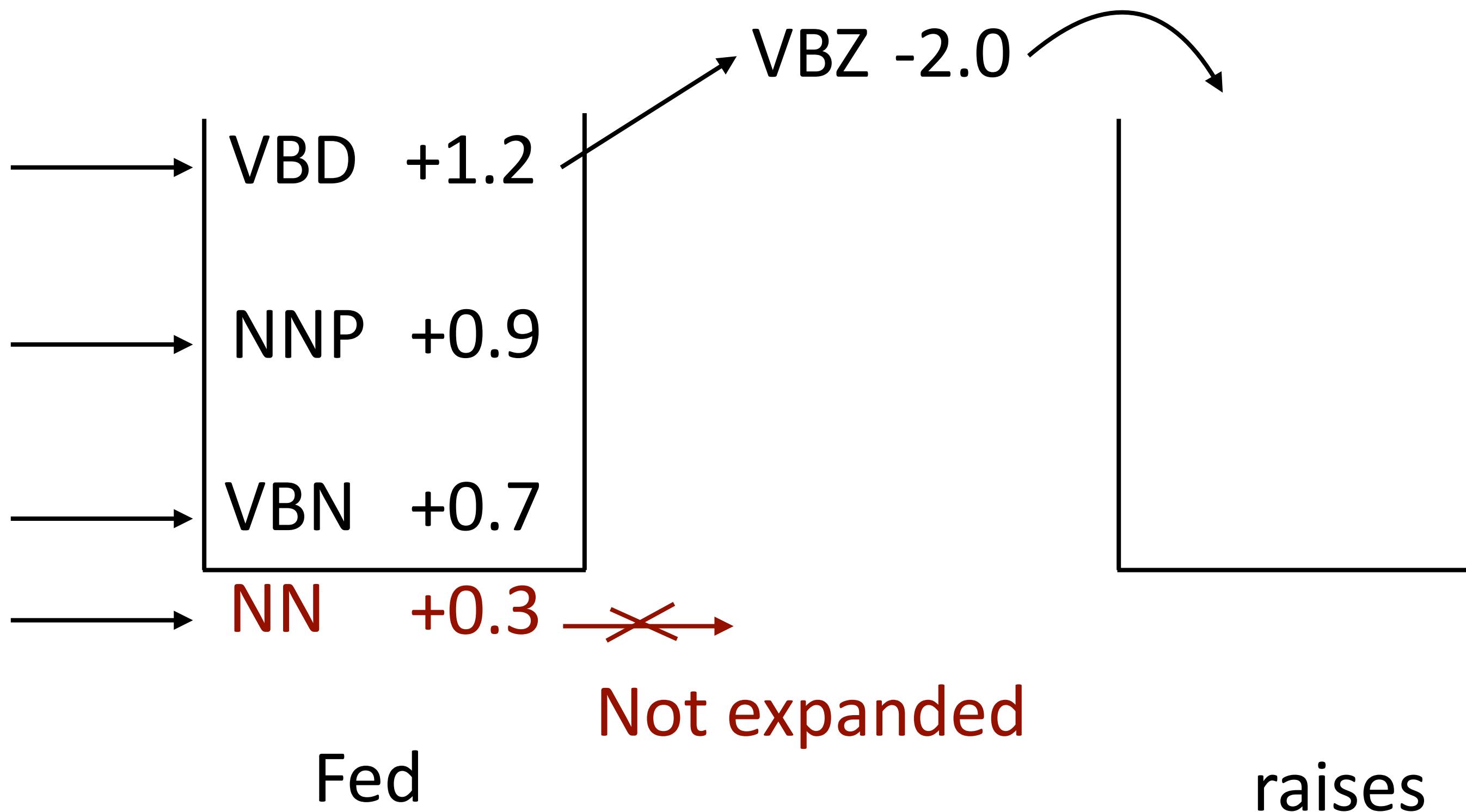
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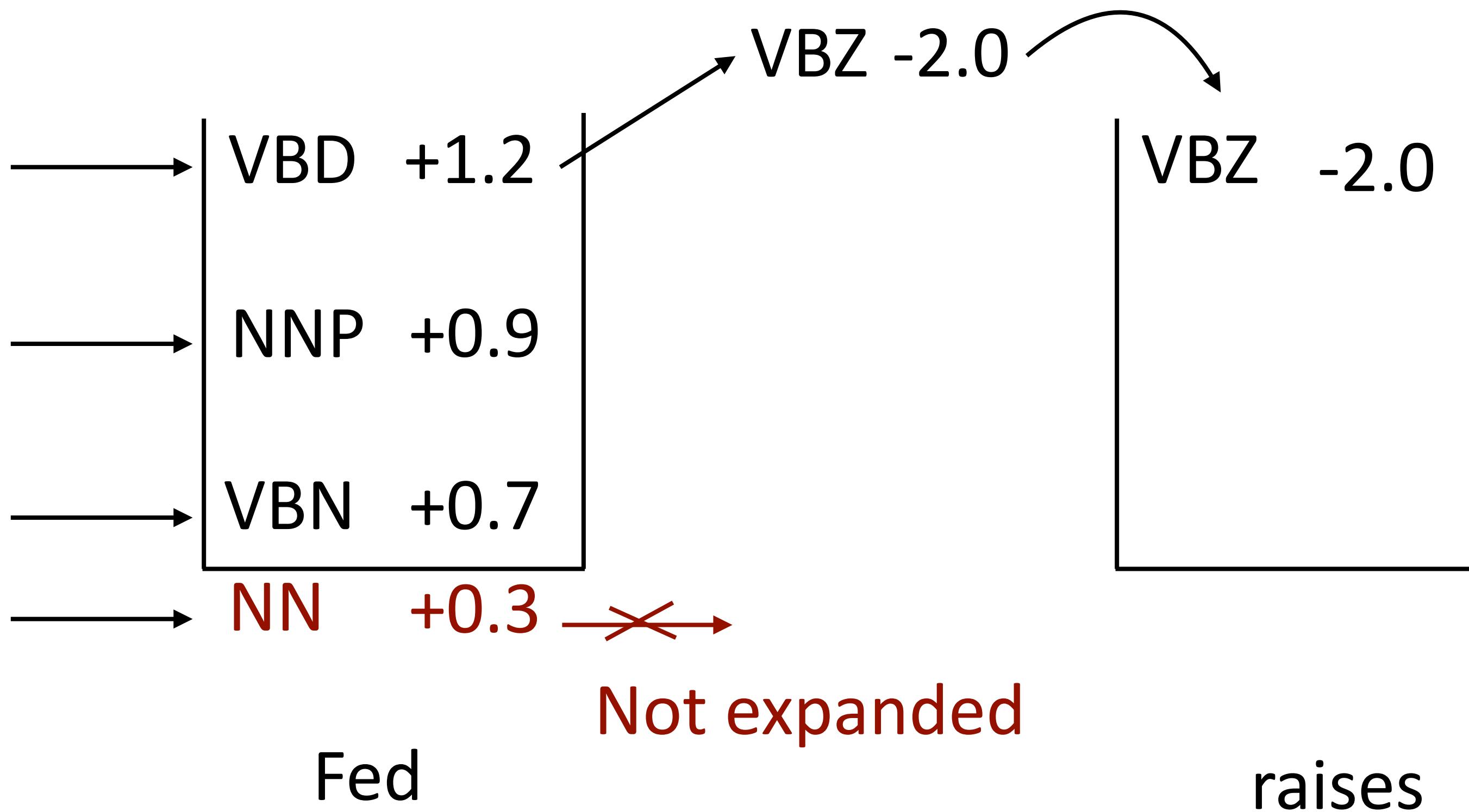
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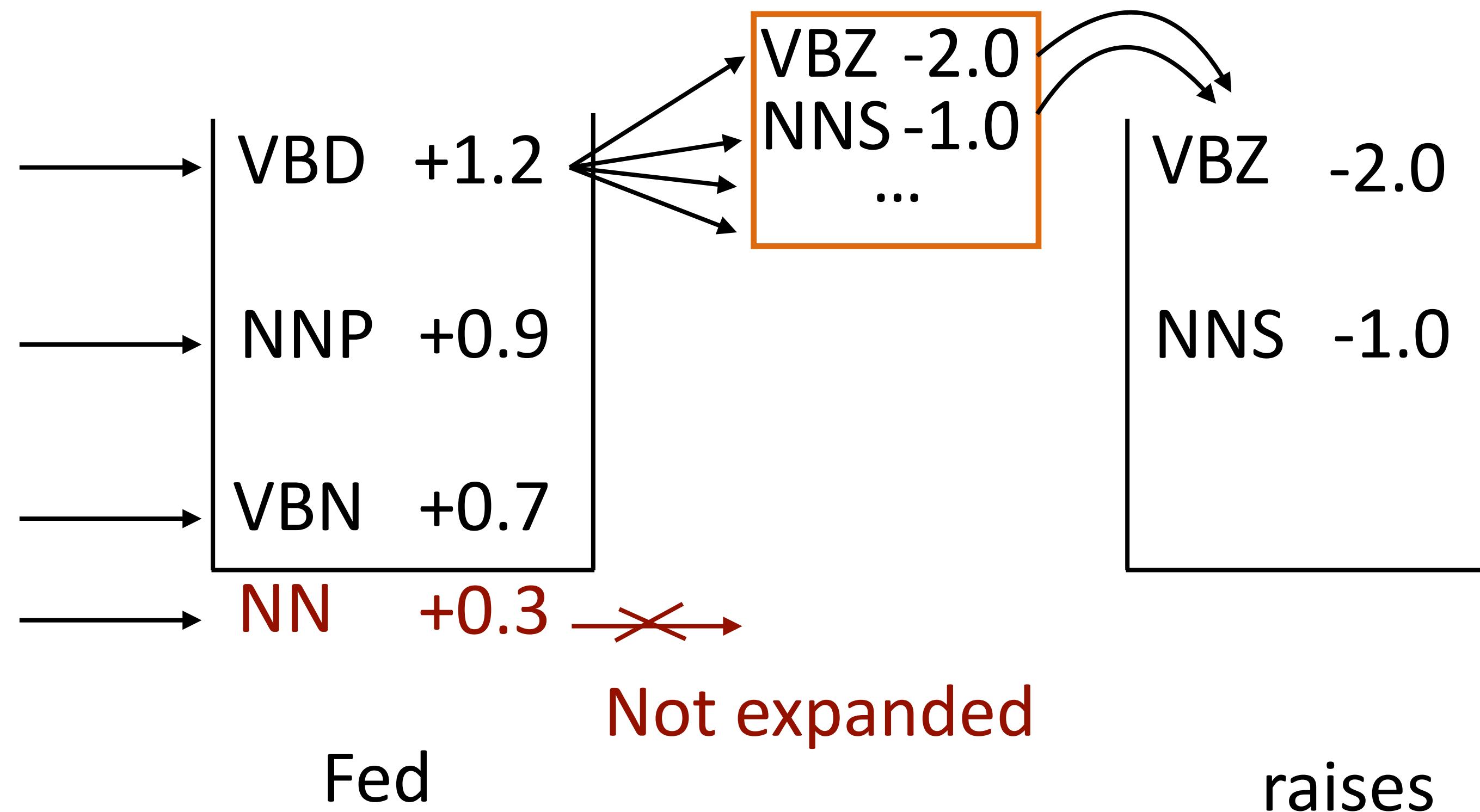
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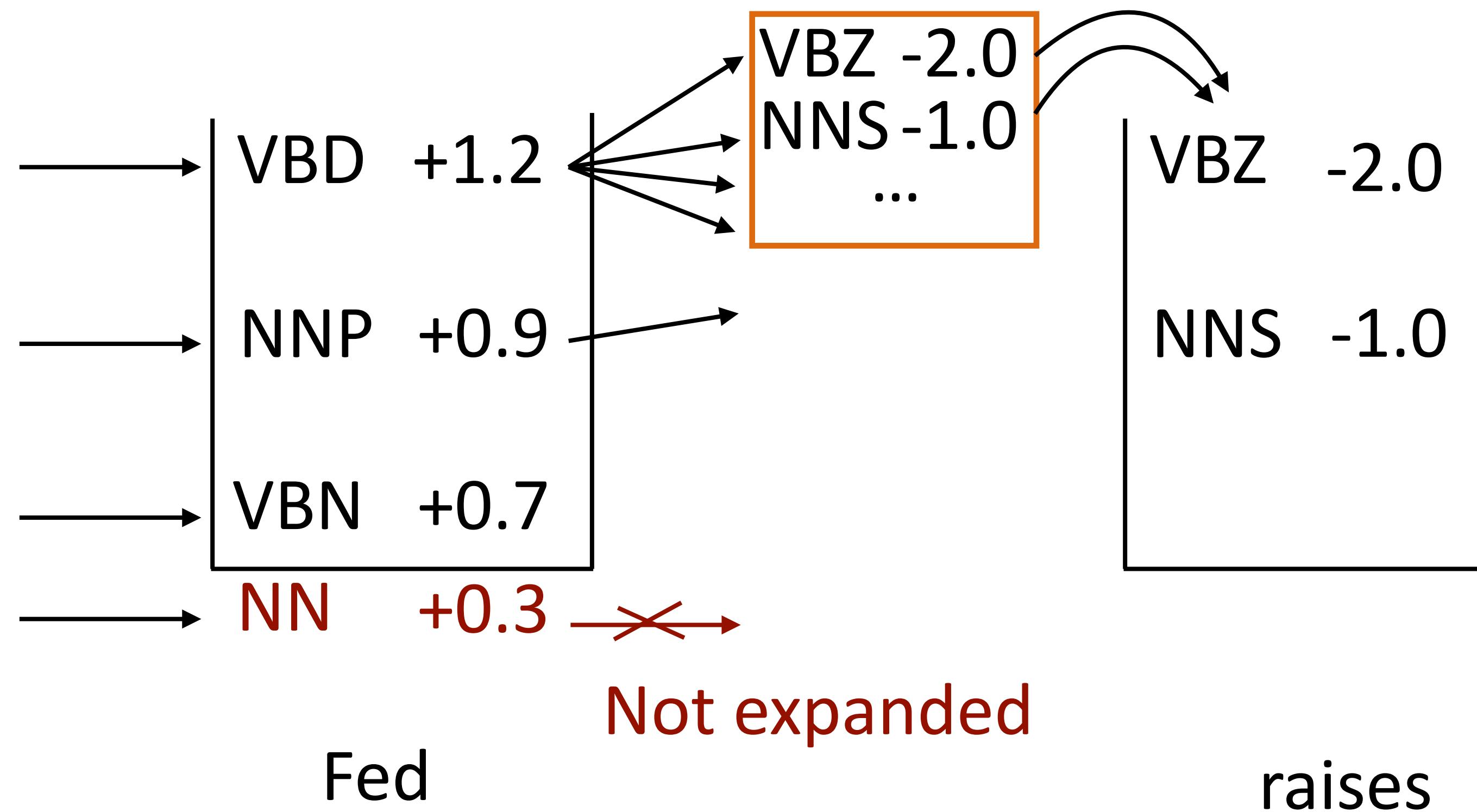
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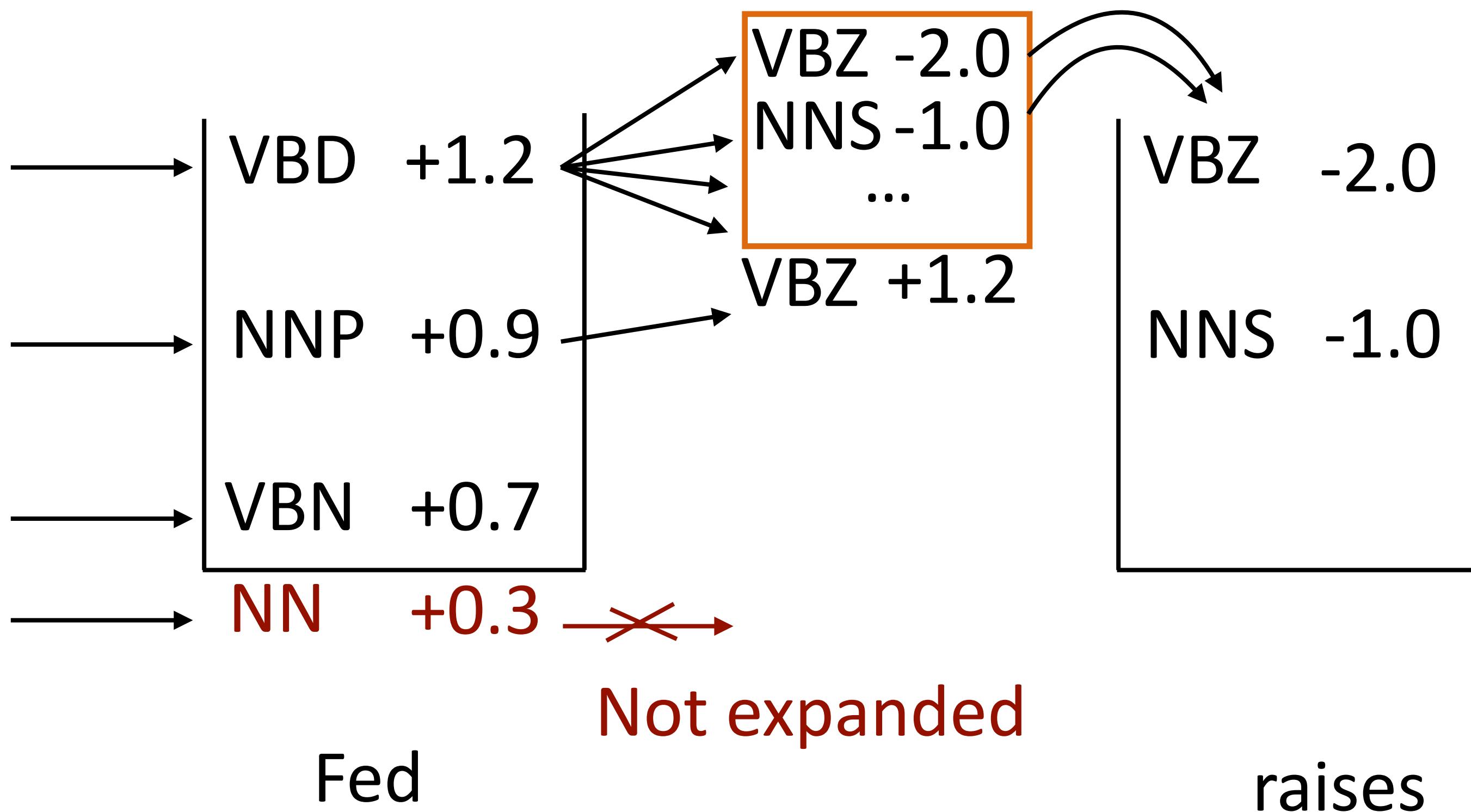
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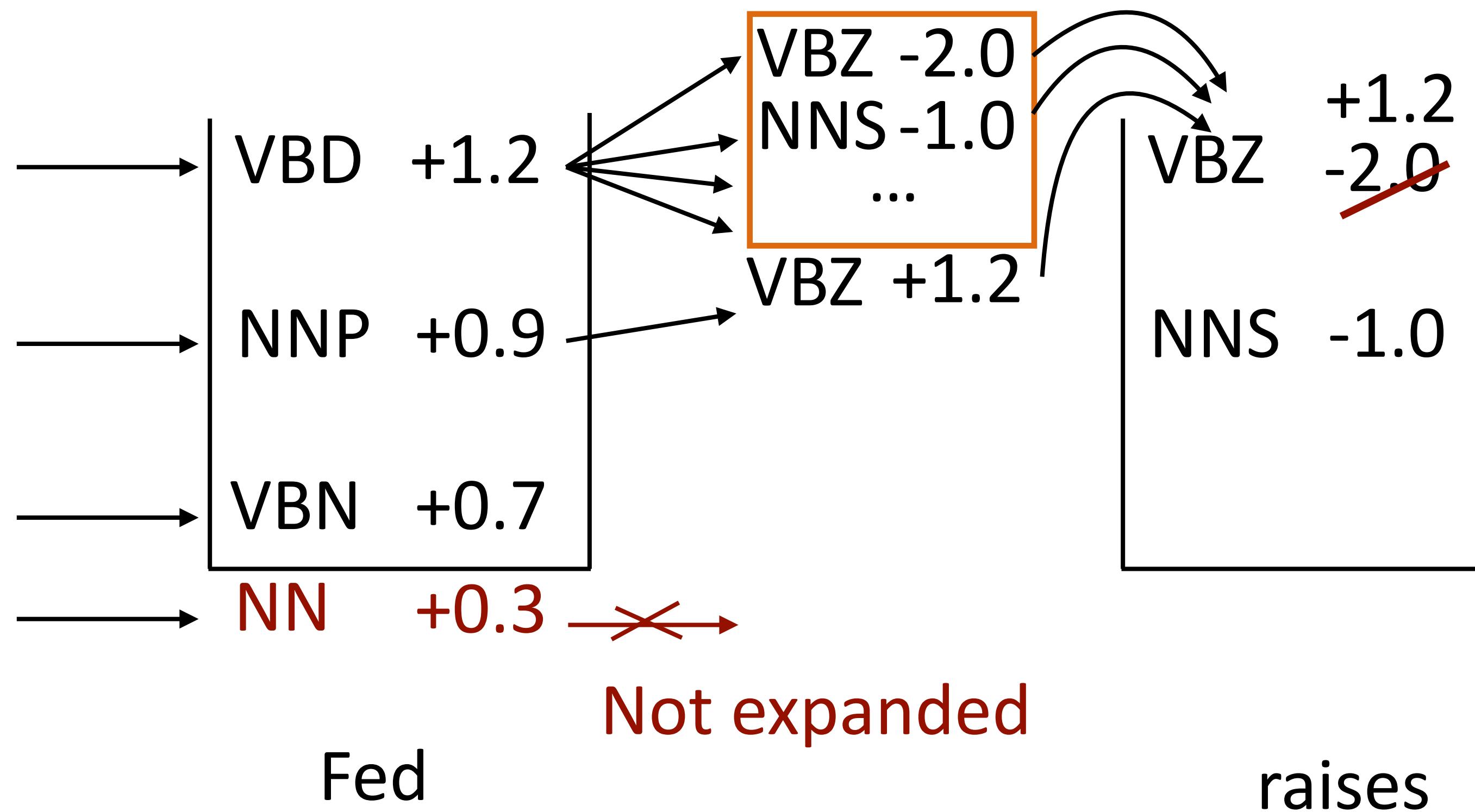
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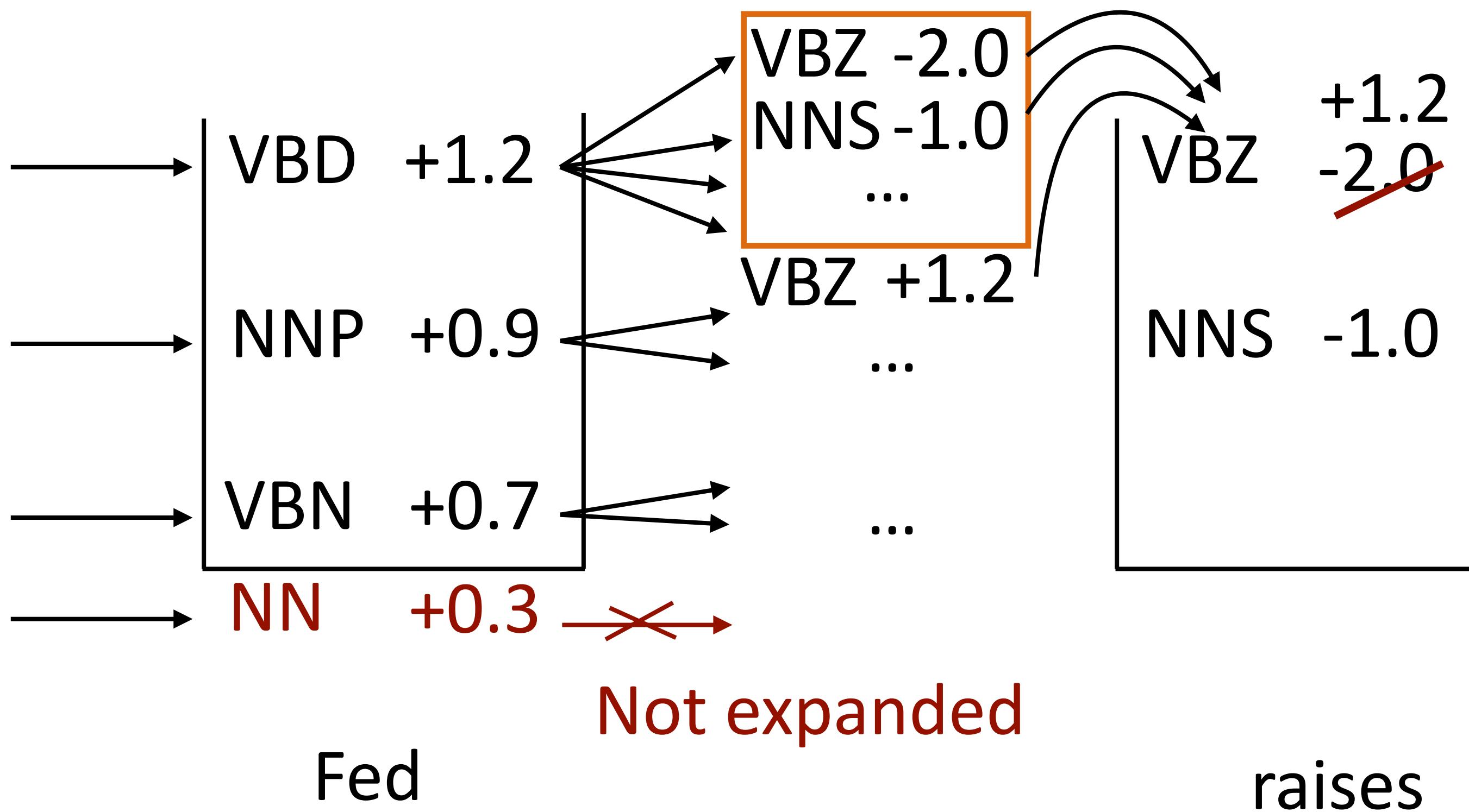
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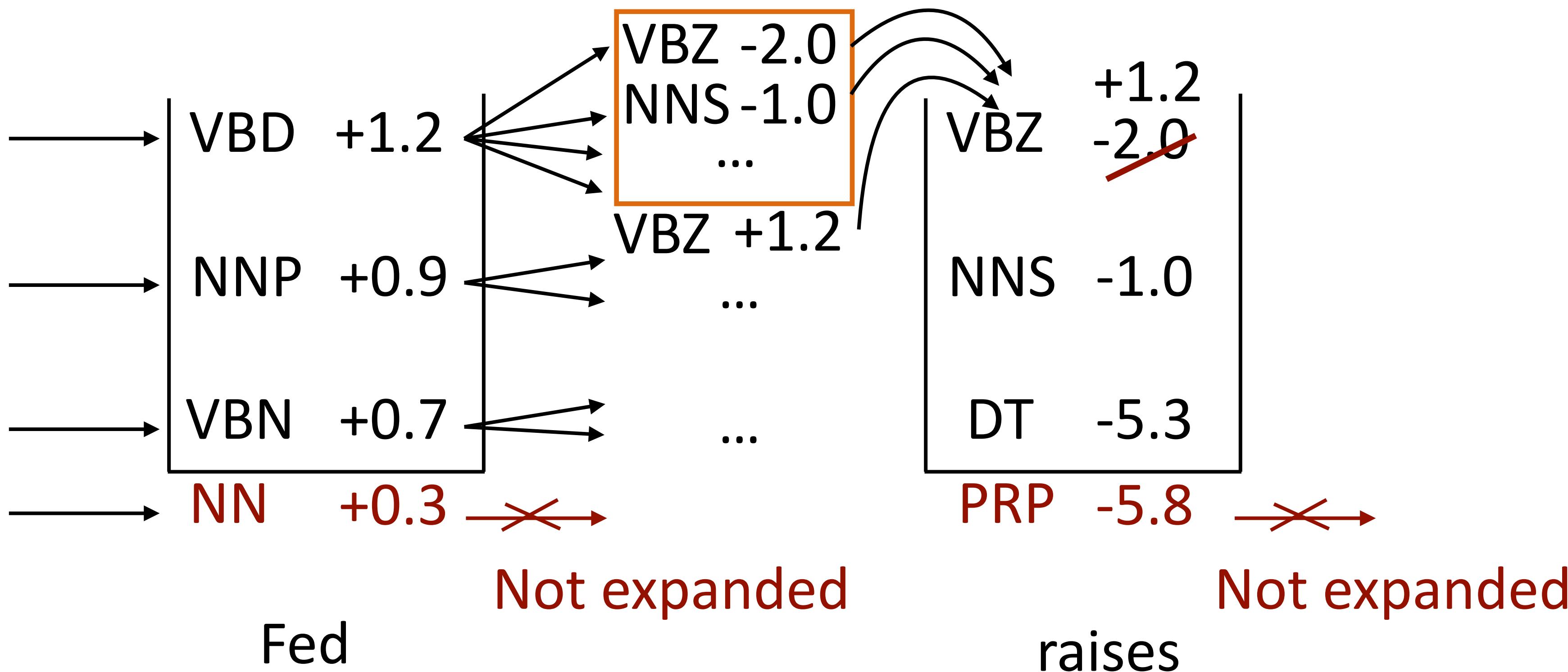
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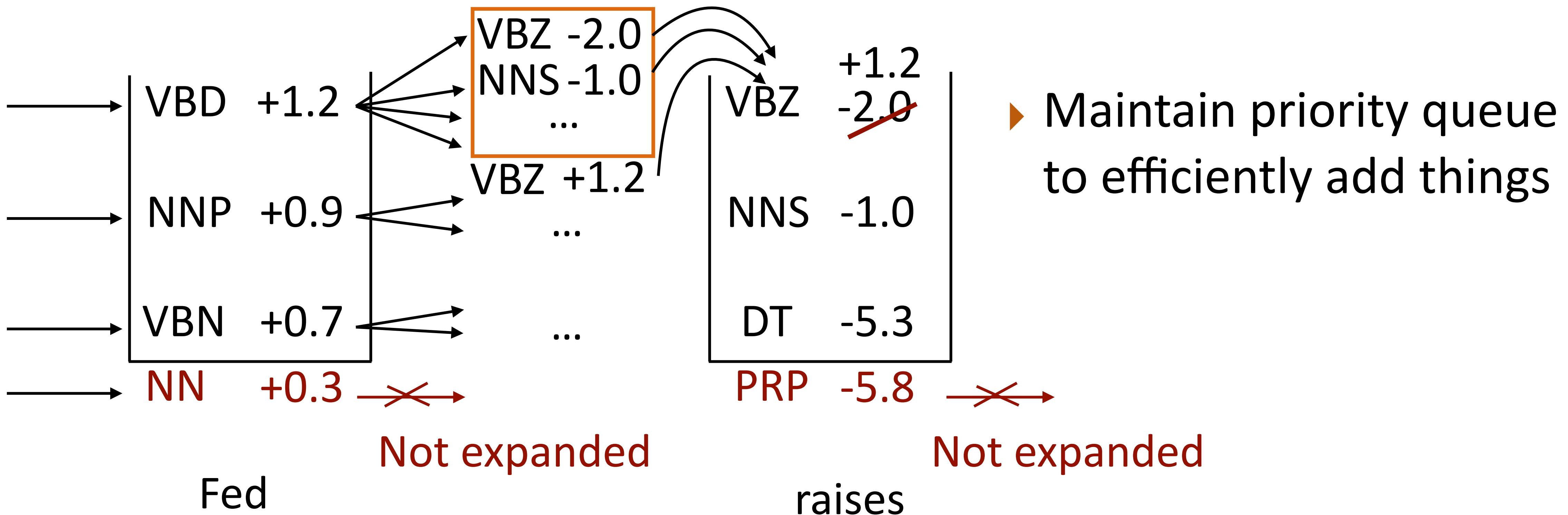
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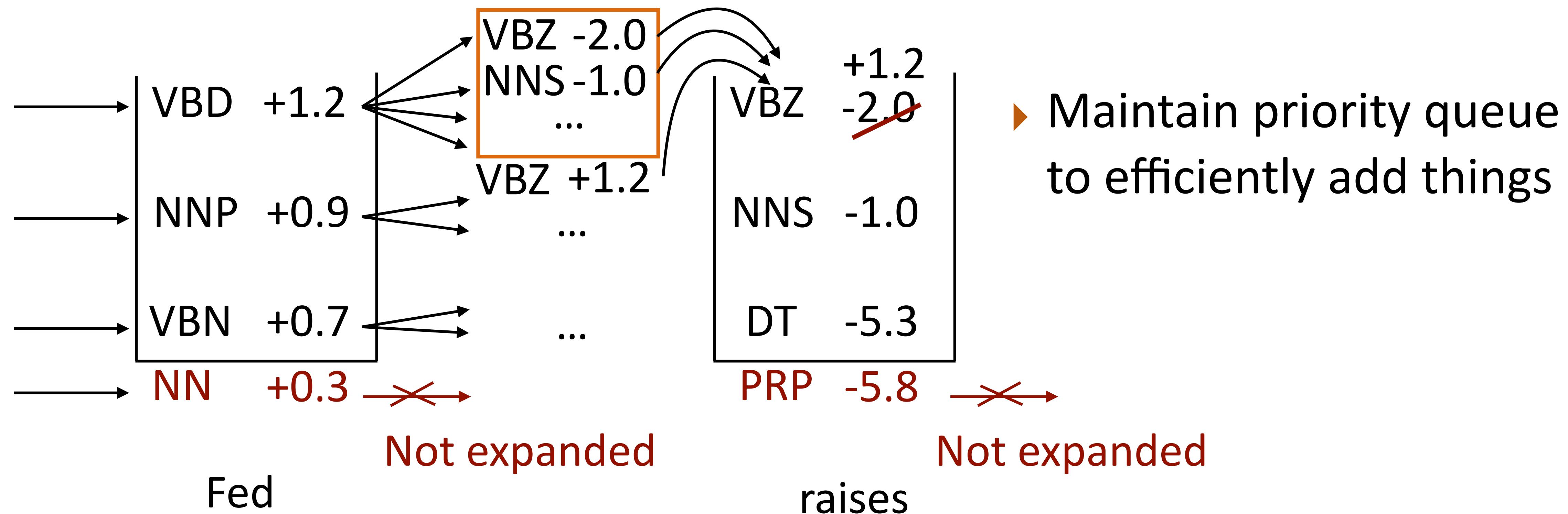
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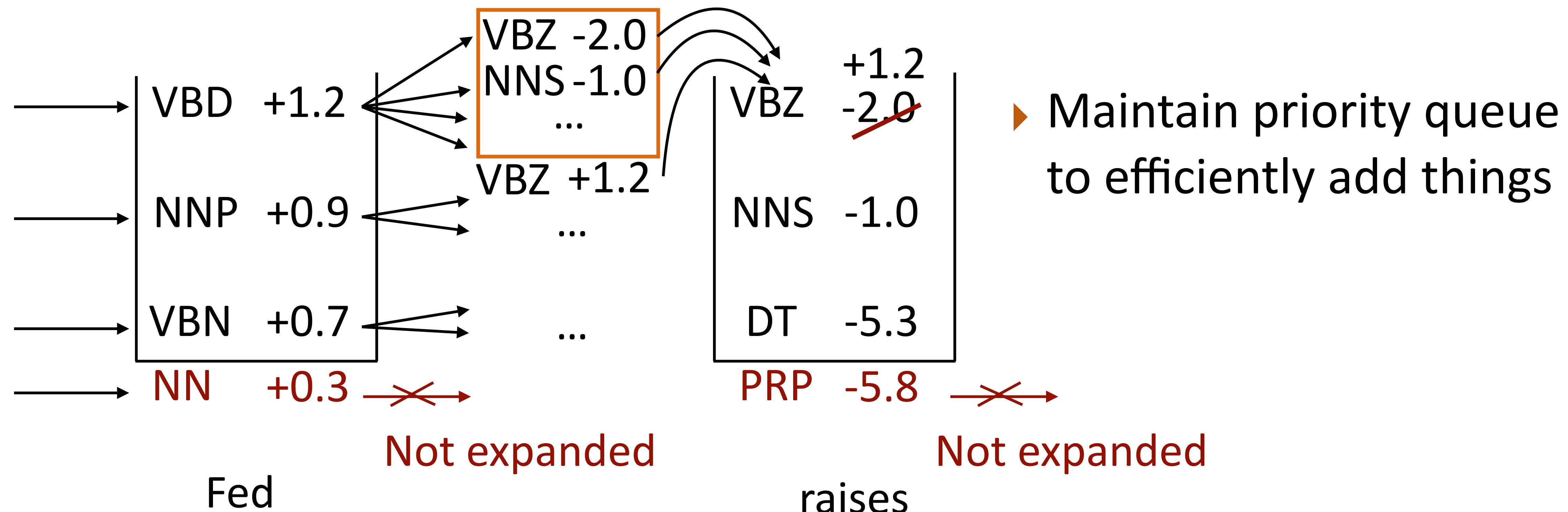
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- ▶ Beam size of k , time complexity $O(nks \log(ks))$

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- ▶ If beam search is much faster than computing full sums, can use structured perceptron SVM instead of CRFs
- ▶ Very similar to structured SVM