

# Secure Design

**고려대학교 (Korea Univ.)**

사이버국방학과 · 정보보호대학원 (CIST)

보안성분석평가연구실 (Security Analysis aNd Evaluation Lab.)

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[www.kimlab.net](http://www.kimlab.net)

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# 보안서부서평가연구실



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## 주요 경력 :

1990.3~1999.2) 성균관대학교 공학 학사·석사·박사  
 1998.12~2004.2) KISA 암호기술팀장 및 CC평가1팀장  
 2004.3~2011.2) 성균관대학교 정보통신공학부 부교수  
 2011.3~현재) 고려대학교 사이버국방학과 정보보호대학원 정교수  
 Founder of (사)HARU & SECUIINSIDE

前) 육군사관학교 초빙교수  
 前) 선관위 DDoS 특별검사팀 자문위원  
 前) SBS 드라마 '유령' 및 영화 '베를린' 자문 / KBS '명견만리' 강연  
 現) 한국정보보호학회 이사  
 現) 대검찰청 디지털수사 자문위원  
 現) 개인정보분쟁조정위원회 위원

- '96: Convertible group signatures (AsiaCrypt)
- '97: Proxy signatures, revisited (ICICS): 670회 이상 인용
- '06: 국가정보원 암호학술논문공모전 우수상
- '07: 국가정보원장 국가사이버안전업무 유공자 표창
- '12, '16: 고려대학교 석탑강의상
- '13: Smart TV Security (Black Hat USA): 스마트TV 해킹(도청·도촬) 및 해적방송 송출 시연

# Security Analysis and Evaluation Lab

[www.KimLab.net](http://www.KimLab.net) / [www.SecEng.net](http://www.SecEng.net)

## 연구분야

- Security Eng. for High-Assurance Trustworthy Systems
- High-Assurance Cryptography
- Security Testing (including End-to-End Provable Security, Formal Verification) and Security Evaluation (e.g. CMVP, CC, C&A, SSE-CMM)
- Usable Security

## 주요 R&D 성과



LG전자와 공동으로  
국내 최초 스마트TV 보안 인증 획득 (2015년)

삼성전자와 공동으로  
국내 최초 프린터복합기 보안 인증 획득 (2008년)

# Cryptography & Secure Design

# Cryptography & Secure Design

- Cryptography has a **firmer** theoretical foundation than other security techniques.
  - So if you study this, you will be able to have an insight to design and analyze other security systems more systematically.

# Emphases of Modern Cryptography

- **Modern** cryptography, which is distinguished from classical cryptography by
  - Its emphasis on ( ),
    - If you don't know what it is you are trying to achieve, how can you hope to know when you have achieved it?
  - Precise ( ), and
    - Many cryptographic constructions cannot currently be proven secure in an unconditional sense. Security often relies, instead, on some widely-believed (albeit unproven) assumption. The modern cryptographic approach dictates that any such assumptions must be clearly and unambiguously defined.
  - ( ) of security.
    - This is the essence of modern cryptography, and was responsible for the transformation of cryptography from an art to a science.

# Symmetric Ciphers

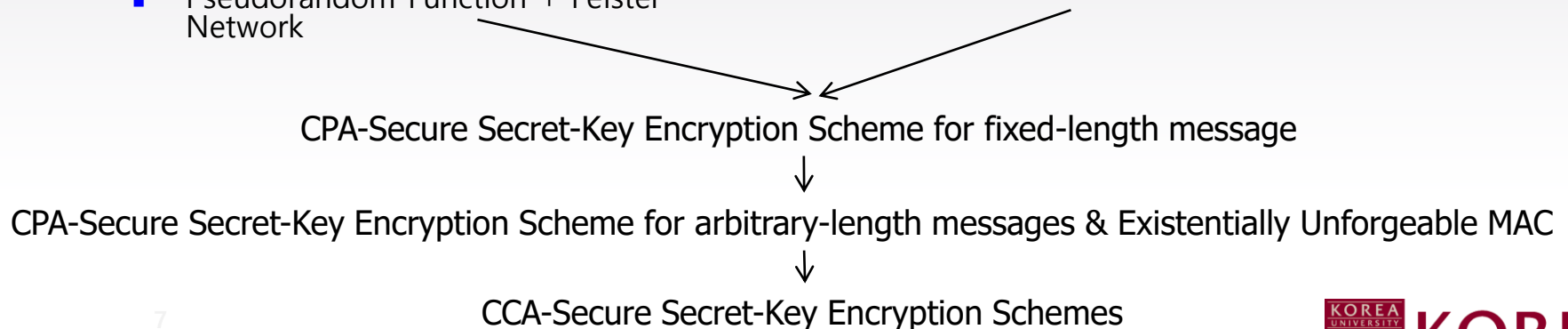
# The World of Symmetric Ciphers

## Theoretical Construction

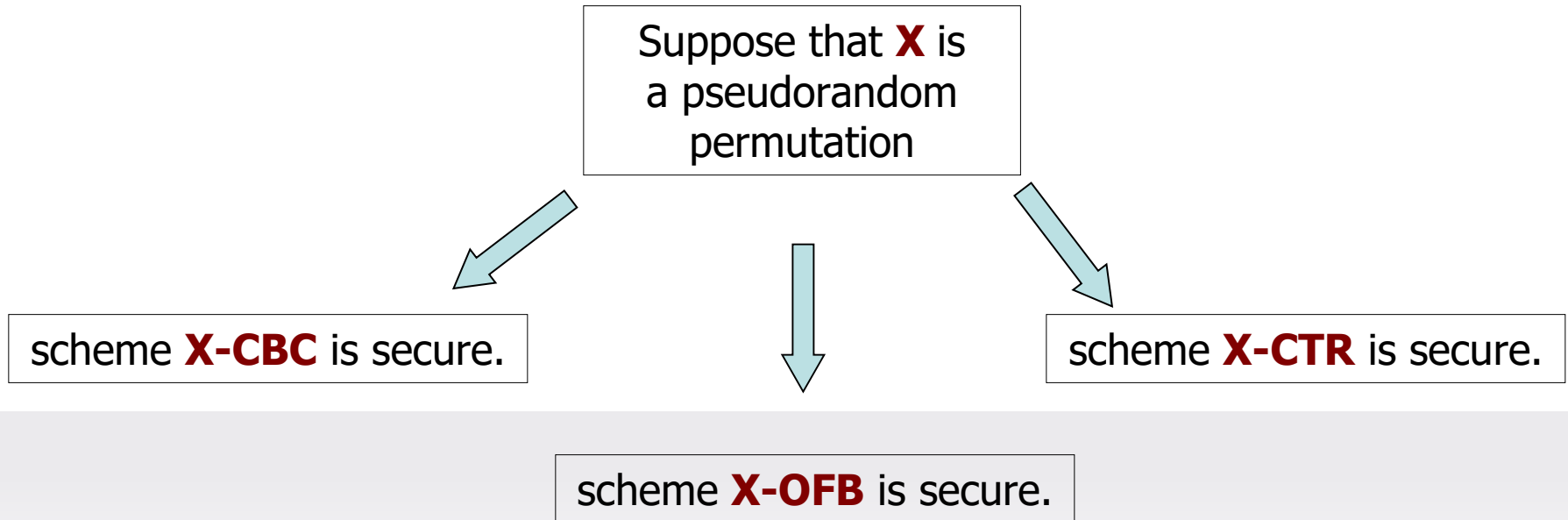
- RSA, Discrete Log, Factoring ...
- One-Way Function (or One-Way Permutation)
- Hard-Core Predicate
- Pseudorandom Generator with +1 Expansion
- Pseudorandom Generator with Arbitrary Expansion
- Pseudorandom Function
- (Strong) Pseudorandom Permutation
  - Pseudorandom Function + Feistel Network

## Practical Construction

■ Block Ciphers



# Modes of Operation



Of course, to get any information about practical relevance of these results one needs to look at the concrete parameters hidden in the “asymptotics”.



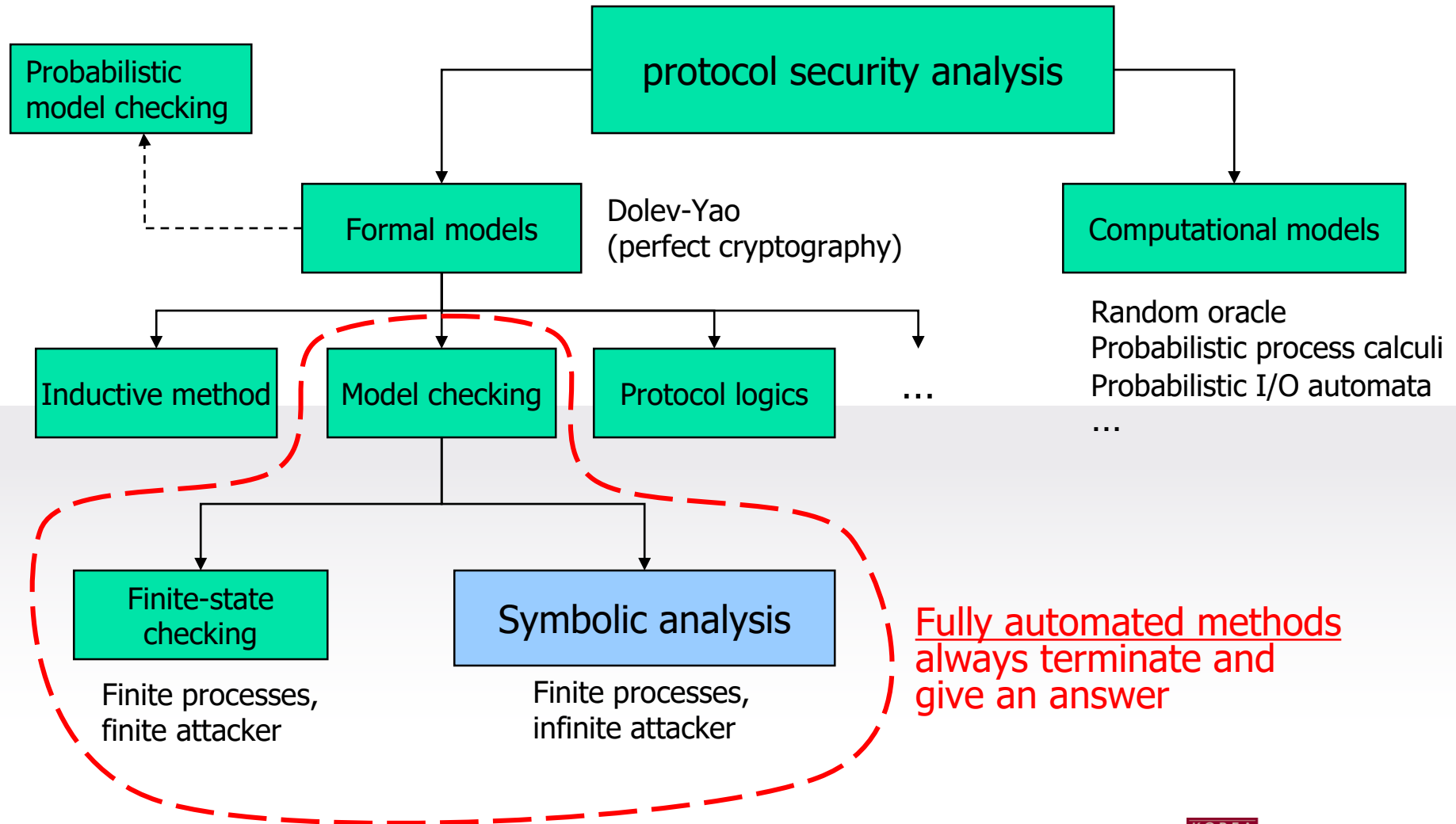
# Asymmetric Ciphers

# Ideal Properties of a Proof

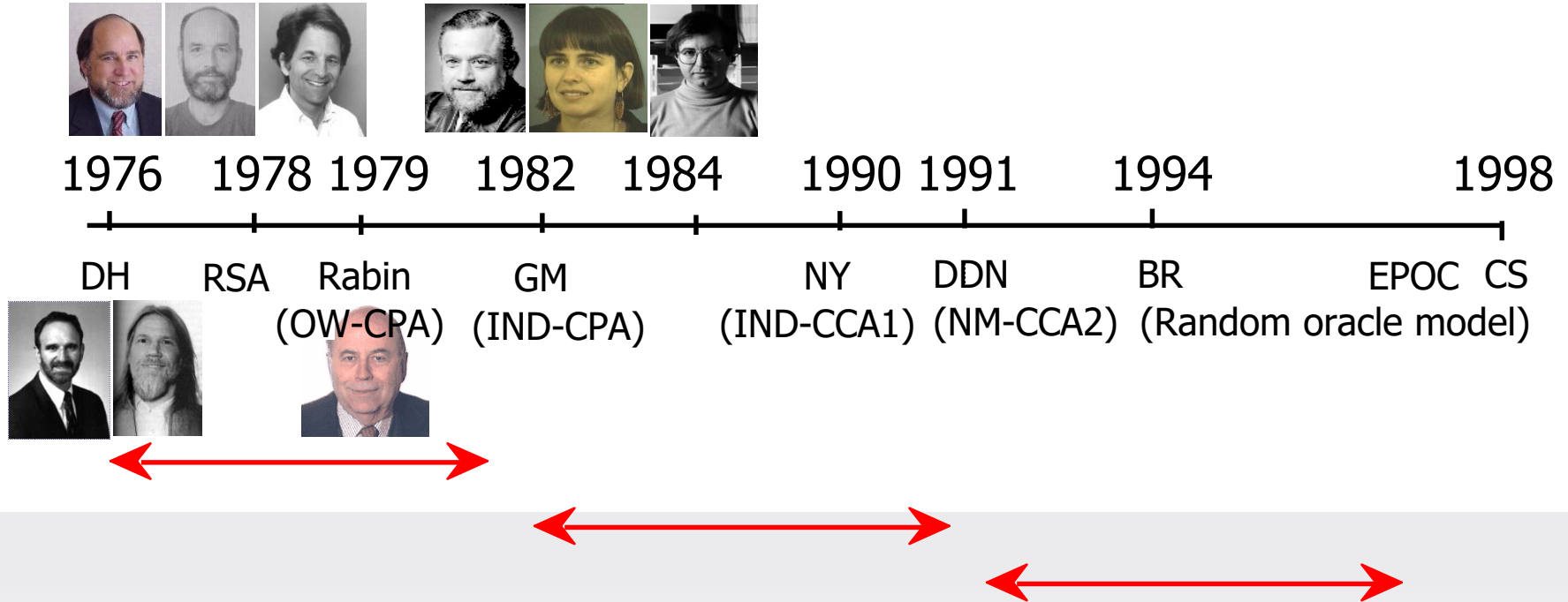
- The challenge(target) for the adversary should be as ( ) as possible
- The adversary should be as ( ) as possible
- The assumptions should be as ( ) as possible
- Quality of security reduction should be as ( ) as possible

※ Cited from B.Kaliski and J.Jonsson(@ RSA Lab)'s Presentation Material

# Protocol Analysis Techniques



# Brief History of Provable Security



※ Cited from Dr. T.Okamoto's Presentation Material in KISA

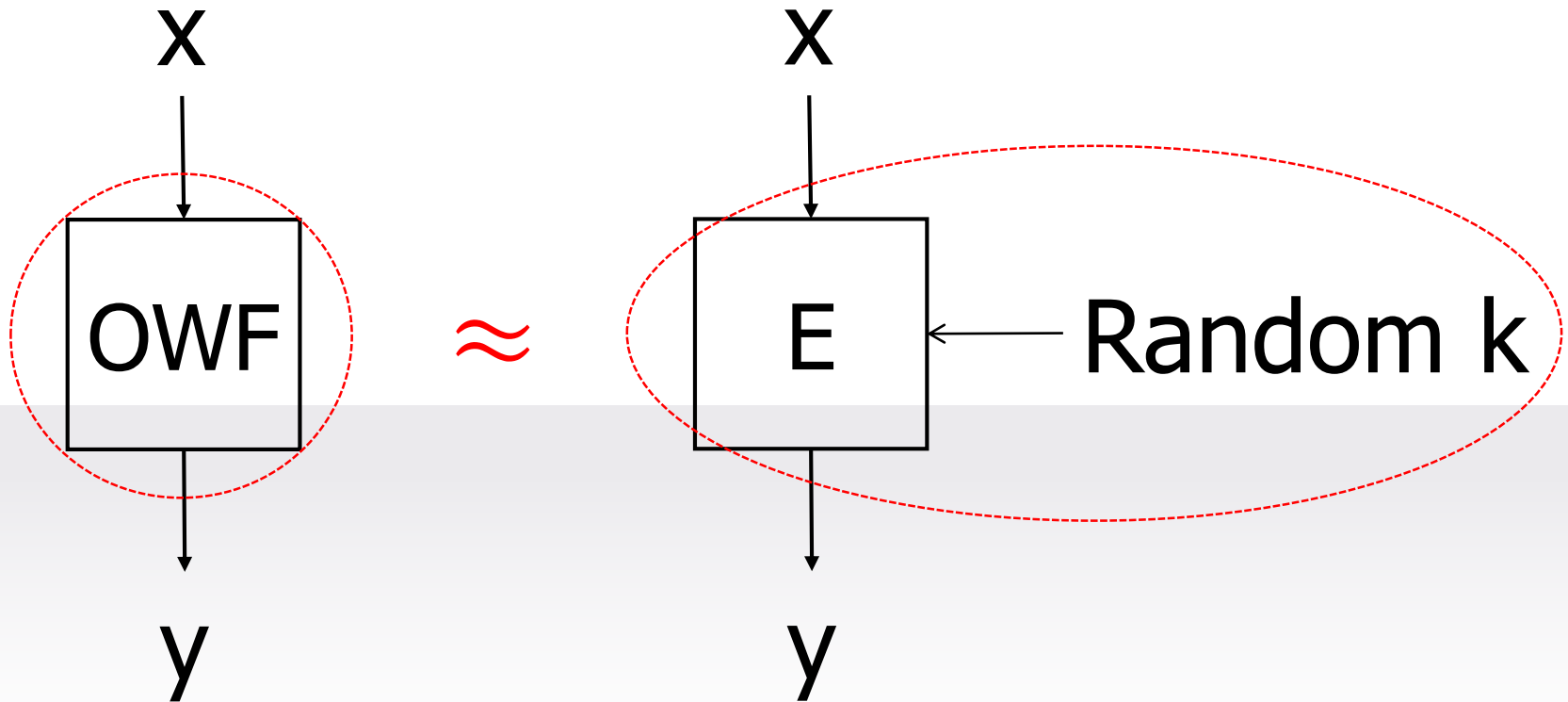
# Brief History of Provable Security

- Blum, Goldwasser & Micali (1982~1988) :  
Mathematical definitions of security



- Encryption [Goldwasser, Micali 86]
- Signatures [Goldwasser, Micali, Rivest 88]
- Now a common requirement to support emerging standards (IEEE P1363, ISO, Cryptrec, NESSIE).

# Design Secure Asymmetric Cipher



# One-Way Function

□ **One-Way Function** : A function

$$f : \{0,1\}^* \rightarrow \{0,1\}^*$$

is called “**one-way**” if there is an efficient algorithm that on input  $x$  outputs  $f(x)$ , whereas any feasible algorithm that tries to find a preimage of  $f(x)$  under  $f$  may succeed only with negligible probability.

- **Any Feasible Algorithm** :

- HW : DTM / NDTM / PTM
- SW : COA / KPA / CPA / CCA

- **Preimage** :

- Whole / Partial / Correlated

# One-Way Function

- **Preimage (Goal)**

- **One-Way (OW)** : Hard to invert the encryption function
- **Semantically Secure (IND)** : Hard to obtain any partial information of a plaintext from the ciphertext
- **Non-Malleability (NM)** : For any non-trivial relation  $R$ ,  $E(M) \rightarrow E(R(M))$  is hard



# One-Way Function

- **Algorithm (HW Attack Method)**
  - FA (Finite Automata)
  - PDA (Pushdown Automata)
  - TM (Turing Machine)
  - PTM (Probabilistic TM)
  - von Neumann Machine

# One-Way Function

- **Algorithm (SW Attack Method)**

- **Passive Attack (CPA)**

- Ciphertext Only Attack (COA)
    - Chosen Plaintext Attack (CPA)

- **Active Attack (CCA)**

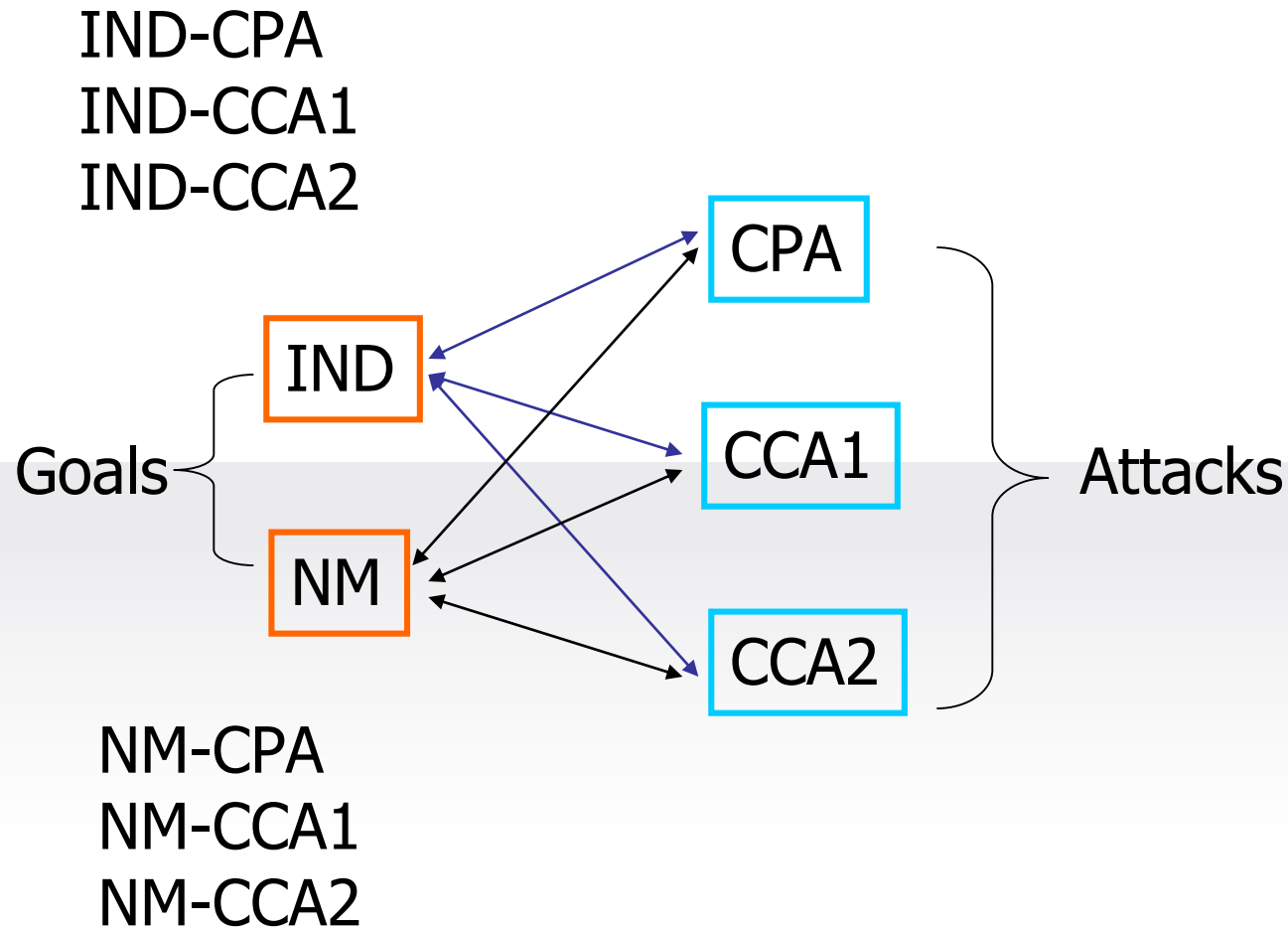
- Chosen Ciphertext Attack (CCA)
    - **1990)** Static Chosen-Ciphertext Attack (Lunch time attack, Naor & Yung)
    - **1991)** Adaptive Chosen-Ciphertext Attack (Rackoff & Simon)

# One-Way Function

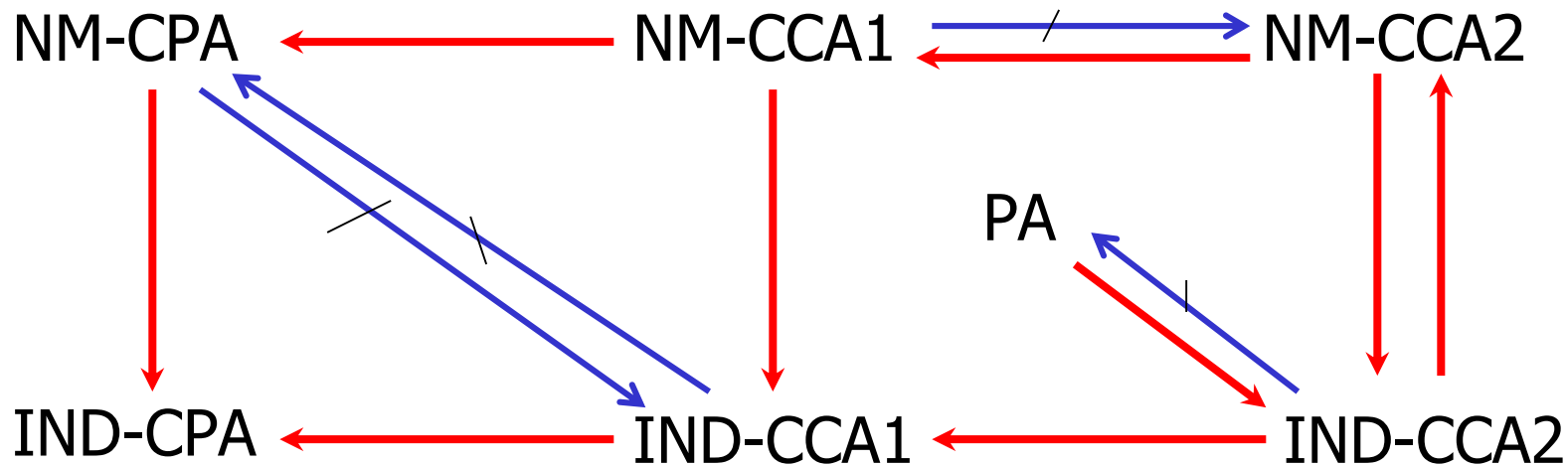
## ■ Algorithm (SW Attack Method)

Type of attack	Known to cryptanalyst
Ciphertext only	<ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext</li></ul>
Known plaintext	<ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext</li><li>•Several pairs plaintext-ciphertext</li></ul>
Chosen plaintext	<ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext</li><li>•Several pairs plaintext-ciphertext, where the plaintext was chosen by the attacker</li></ul>
Chosen ciphertext	<ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext</li><li>•Several pairs plaintext-ciphertext, where the ciphertext was chosen by the attacker</li></ul>
Chosen text	<ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext</li><li>•Several pairs plaintext-ciphertext, where the plaintext or the ciphertext was chosen by the attacker</li></ul>

# 6 Notions of Security



# Relations



A  $\rightarrow$  B: proven that meeting notion A implies meeting B

A  $\not\rightarrow$  B: proven that meeting notion A implies **not** meeting B

**NOTE: A implies B iff there is a path from A to B**

# One-Wayness (OW-CPA)

## Security Goal : One-wayness

- Easy to compute ciphertext from plaintext but hard to invert.

## Attacker Model :



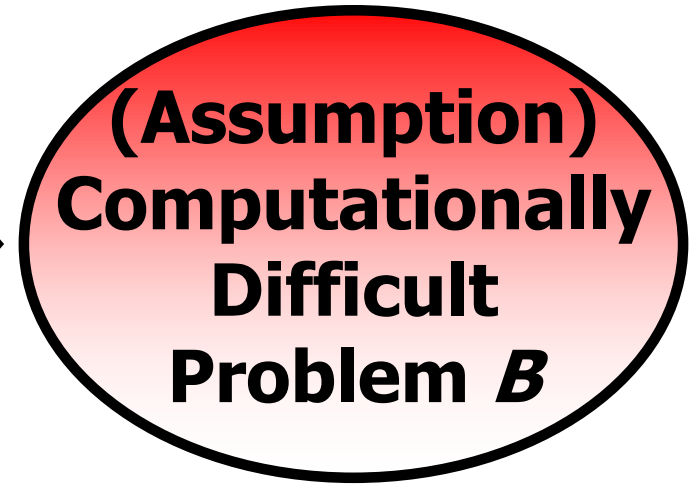
**Security Proof :** Relative complexity by reduction

# One-Wayness (OW-CPA)

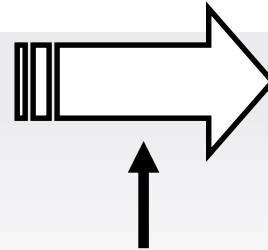
Encryption Algorithm



Complexity Theory



If an adversary  
can break the  
secrecy of  $A$



Then we can break  
The problem  $B$

**Contradicting Assumption**

- ※ ***Partial information problem*** : Leak partial information if the plaintext comes from small plaintext space!

# OW-CPA Example : Rabin Scheme



- **Private Key** :  $p = q = 3 \pmod{4}$
- **Public Key** :  $n = pq$
- **Encryption** :  $C = M^2 \pmod{n}$
- **Decryption** :
  - $m_1 = C^{(p+1)/4} \pmod{p}$ ,  $m_2 = (p - C^{(p+1)/4}) \pmod{p}$ ,  
 $m_3 = C^{(q+1)/4} \pmod{q}$ ,  $m_4 = (q - C^{(q+1)/4}) \pmod{q}$ .
  - $a = q(q^{-1} \pmod{p})$ ,  $b = p(p^{-1} \pmod{q})$ .
  - $M_1 = (am_1 + bm_3) \pmod{n}$ ,  $M_2 = (am_1 + bm_4) \pmod{n}$ ,  
 $M_3 = (am_2 + bm_3) \pmod{n}$ ,  $M_4 = (am_2 + bm_4) \pmod{n}$ .
  - $M$  is one of  $\{M_1, M_2, M_3, M_4\}$



# Proof Sketch of Rabin Scheme

Algorithm A' solving IFP

Algorithm A cryptanalyzing Rabin

Let A be an adversary that breaks the Rabin scheme. Then A can be used to solve IFP. If so, we say solving IFP reduces to breaking the Rabin scheme.

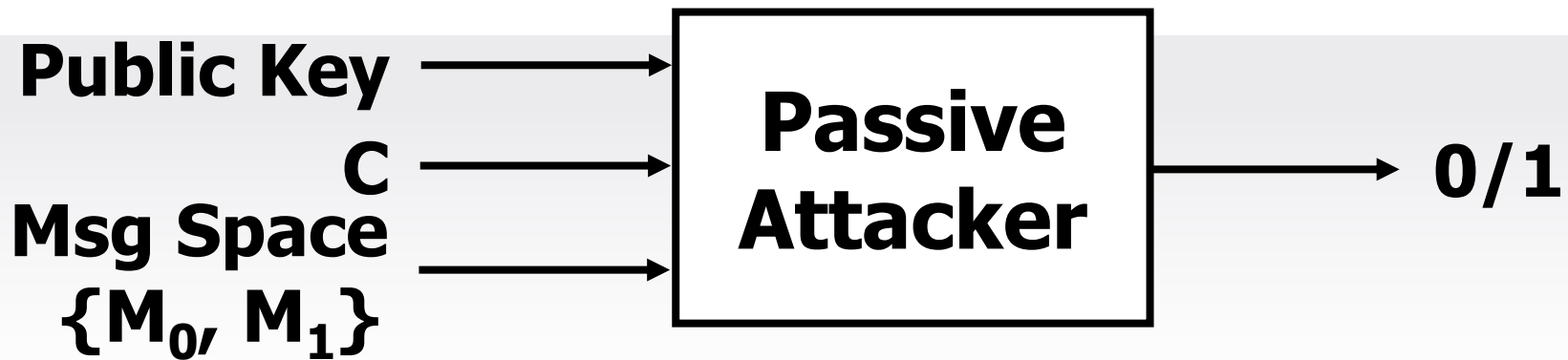
→ Conclusion: If IFP untractable then Rabin scheme is unbreakable!

# Polynomial Security (IND-CPA)

## Security Goal : Polynomial Security

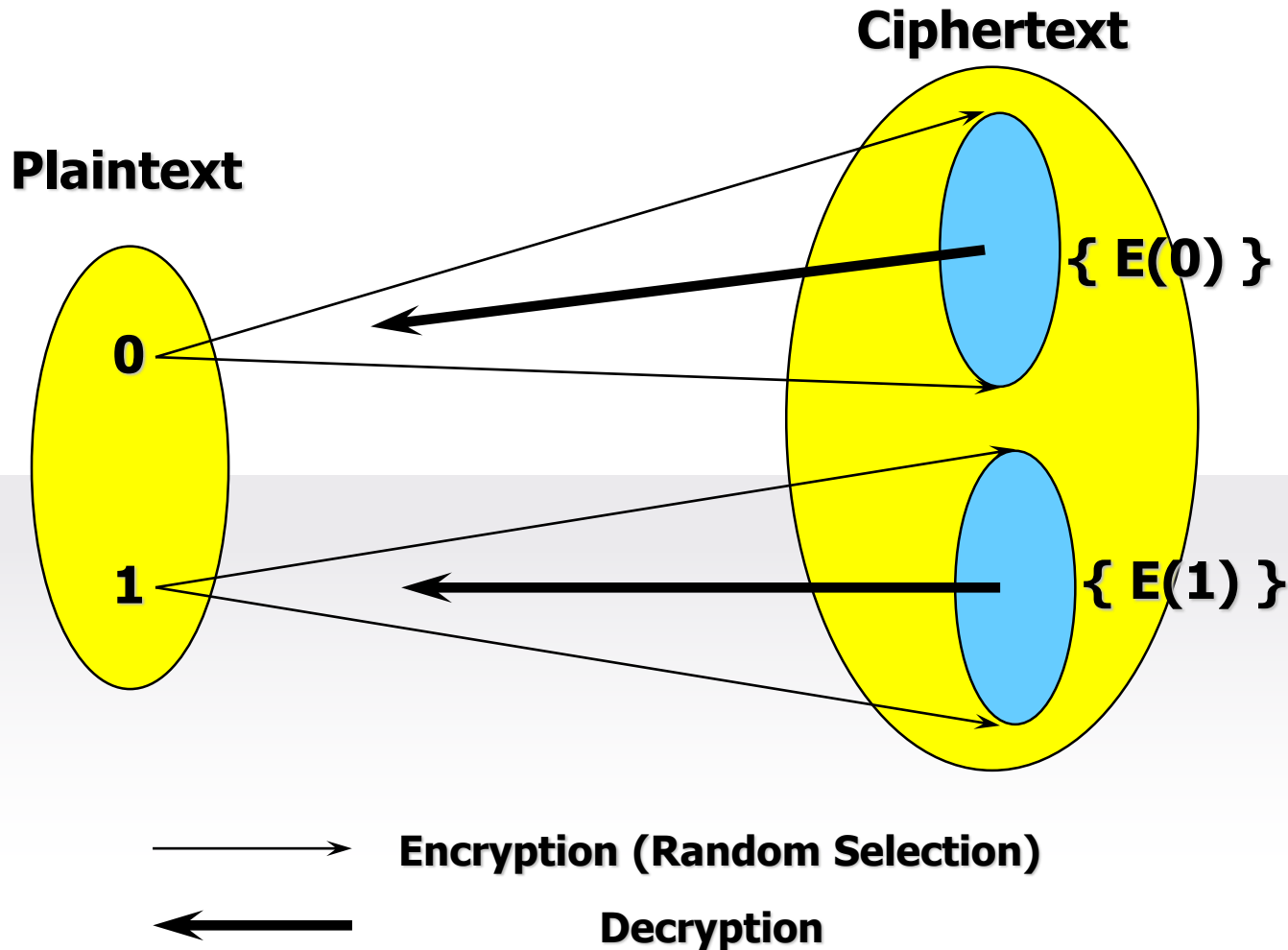
- Cannot distinguish 2 ciphertexts (Indistinguishability)

## Attacker Model :

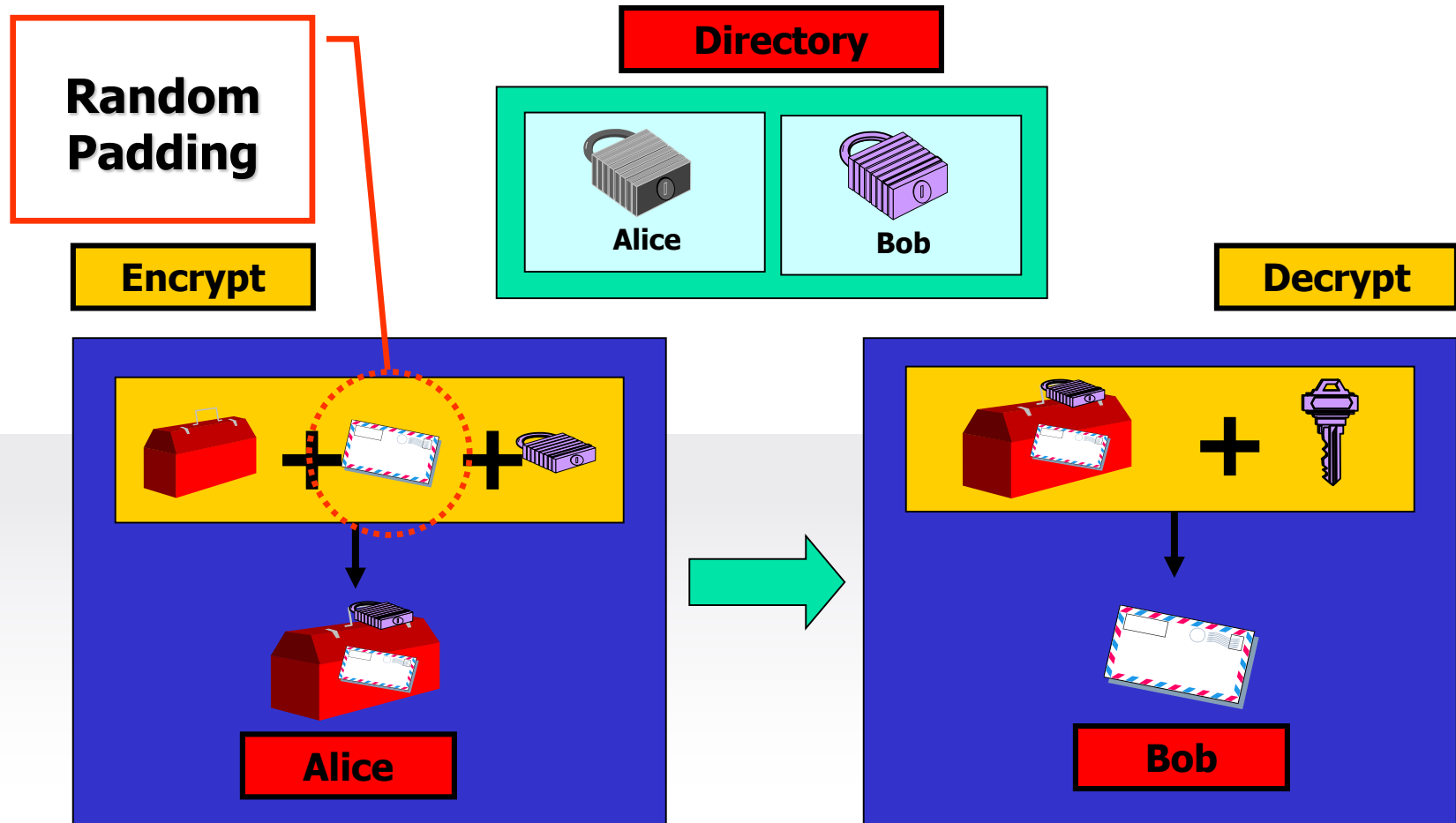


→ **Encryption Alg. : *must be probabilistic!***

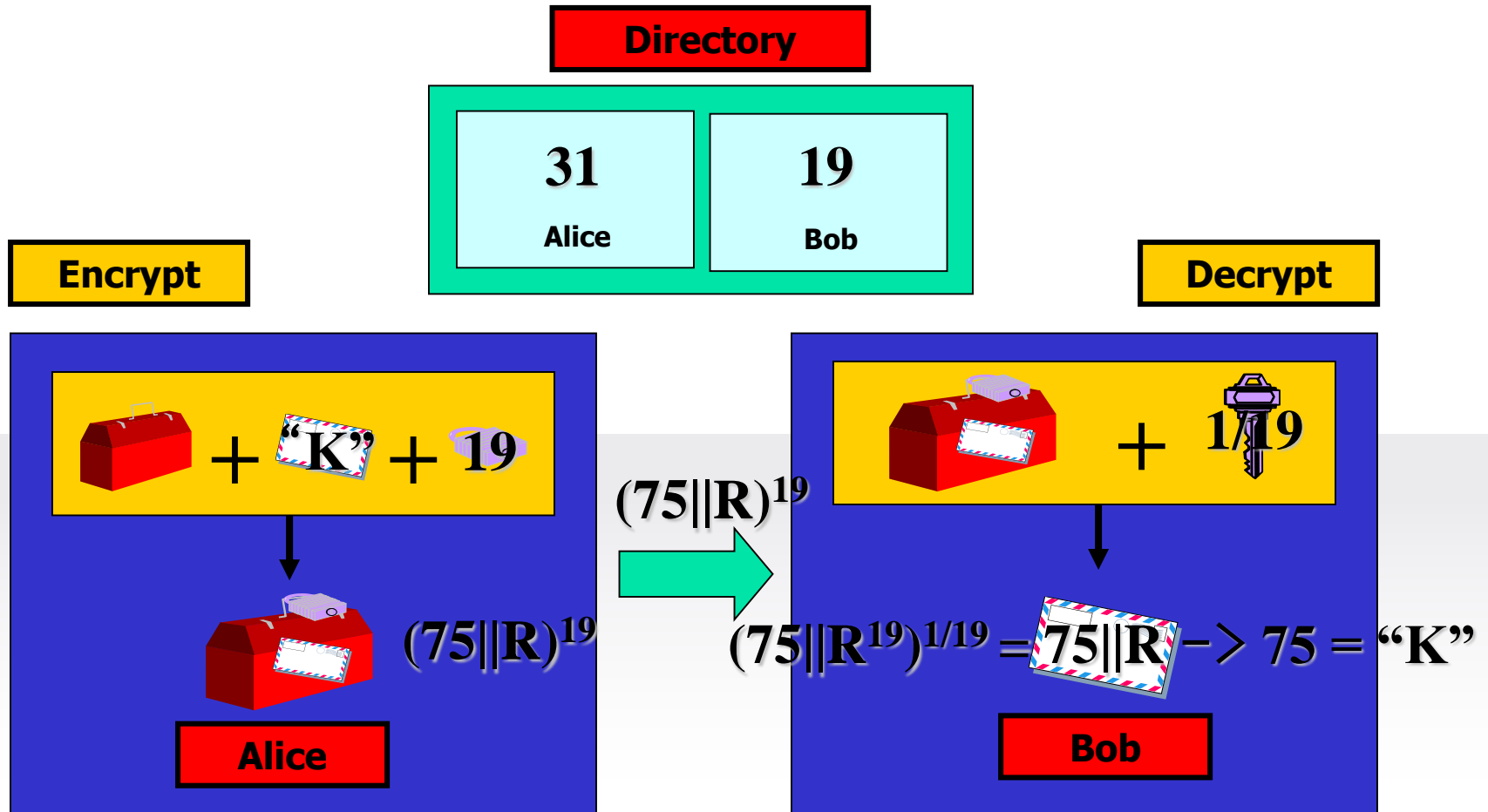
# Probabilistic Encryption



# Probabilistic Encryption



# Probabilistic Encryption



# Semantic Security

- Semantic Security (= Polynomial Security) is a ( ) of Shannon's "perfect secrecy".

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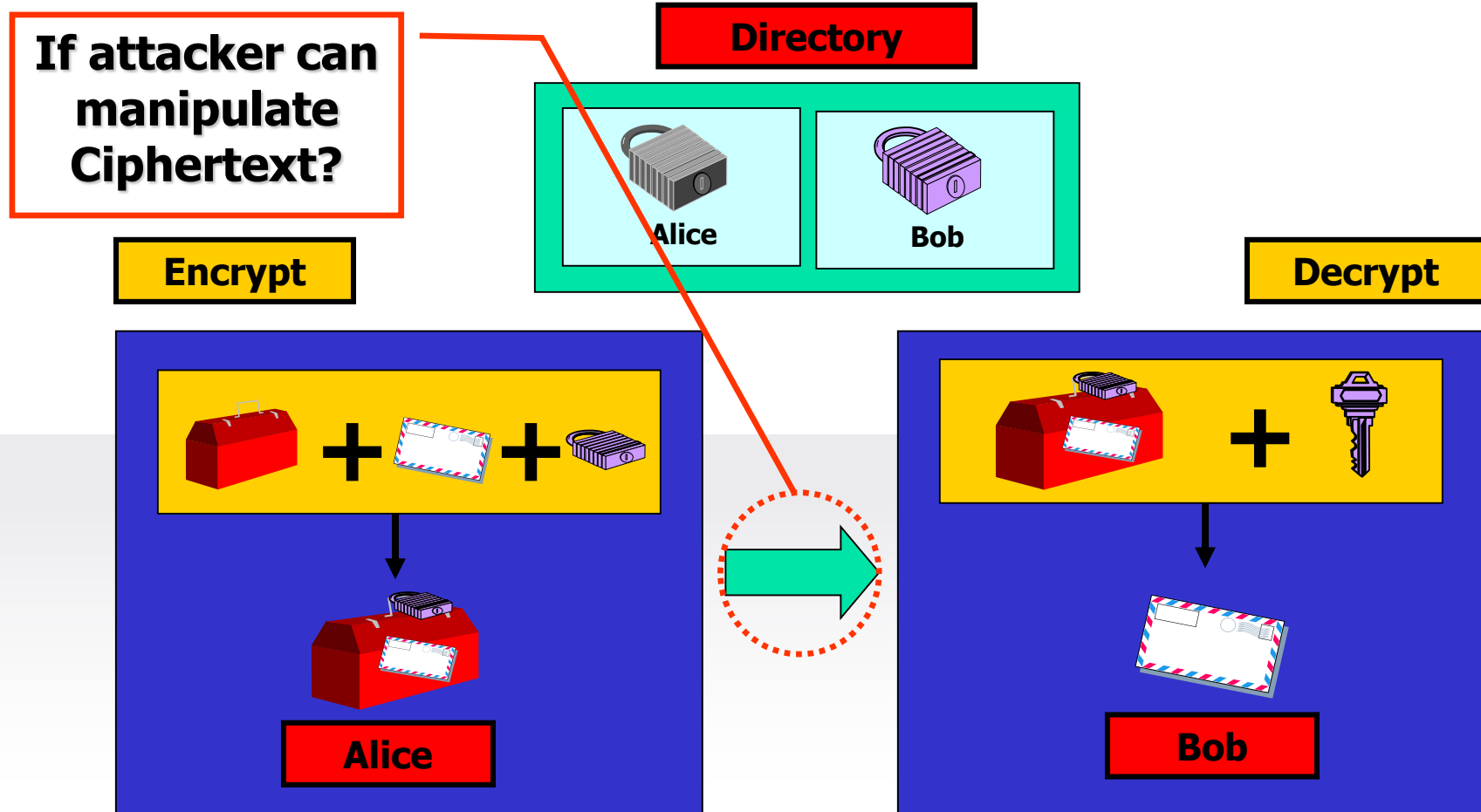
**How to define  
this goal formally?**

# How to Make Semantic Secure Cipher?

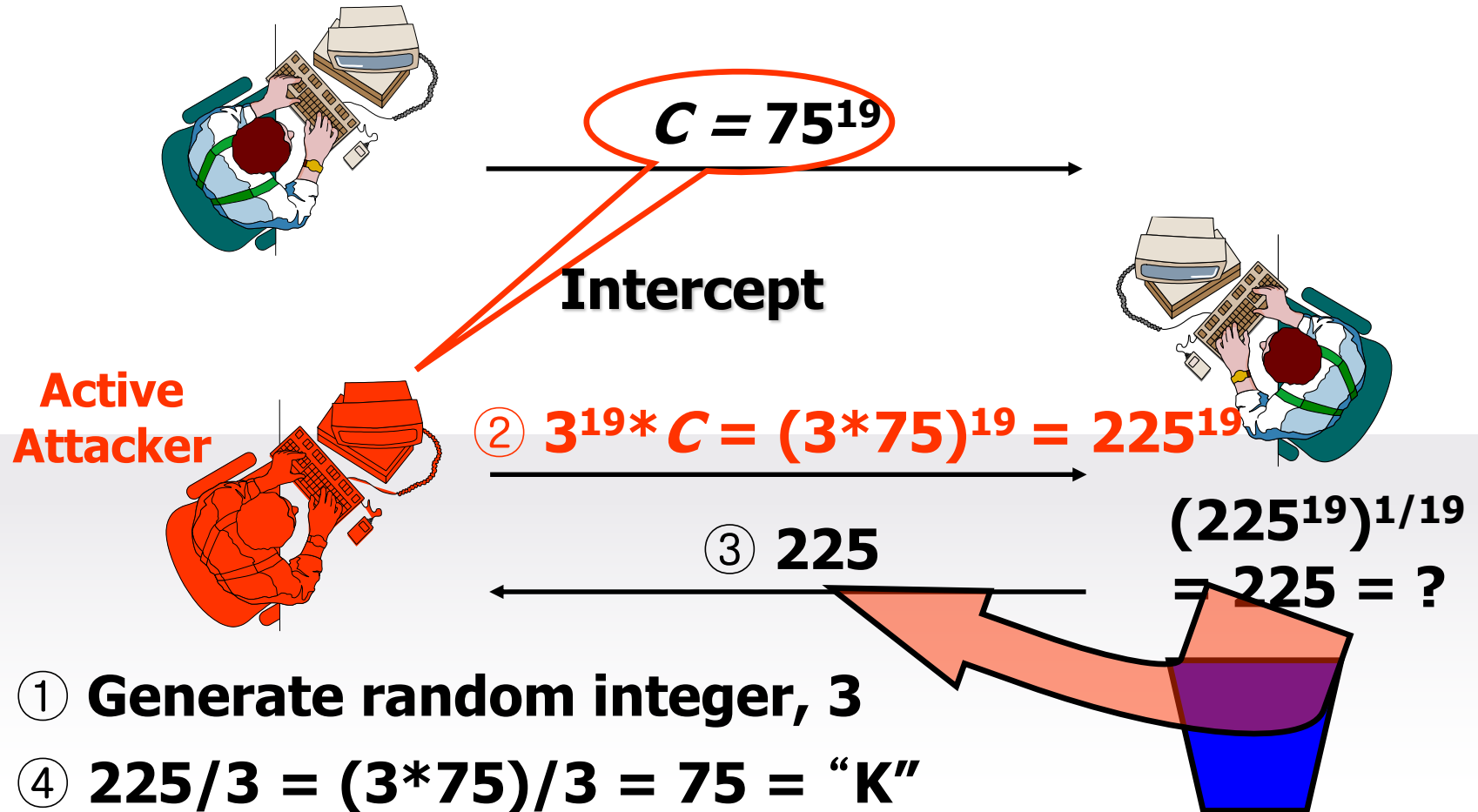
# How to make it?



# Chosen Ciphertext Attack

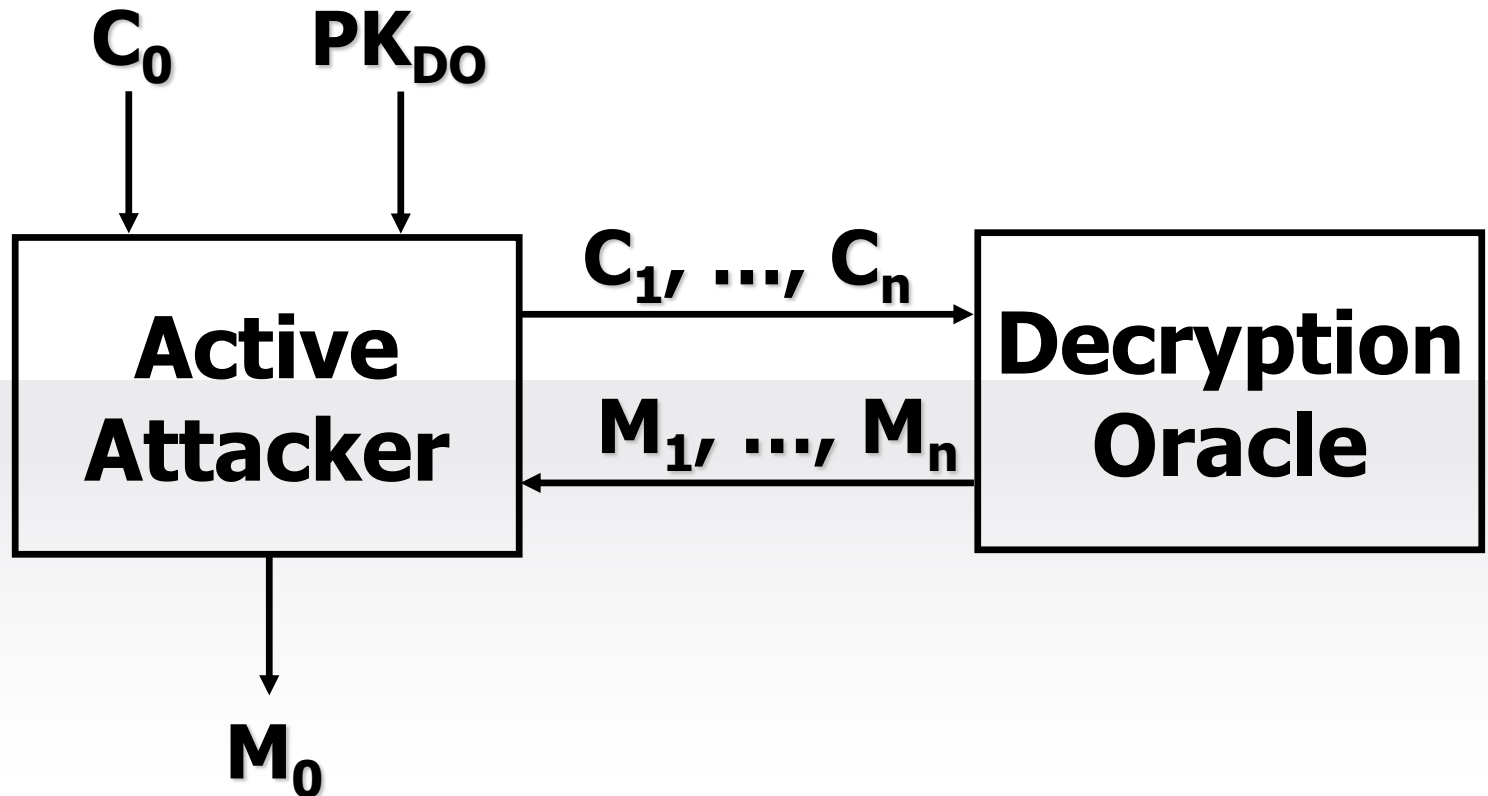


# Chosen Ciphertext Attack



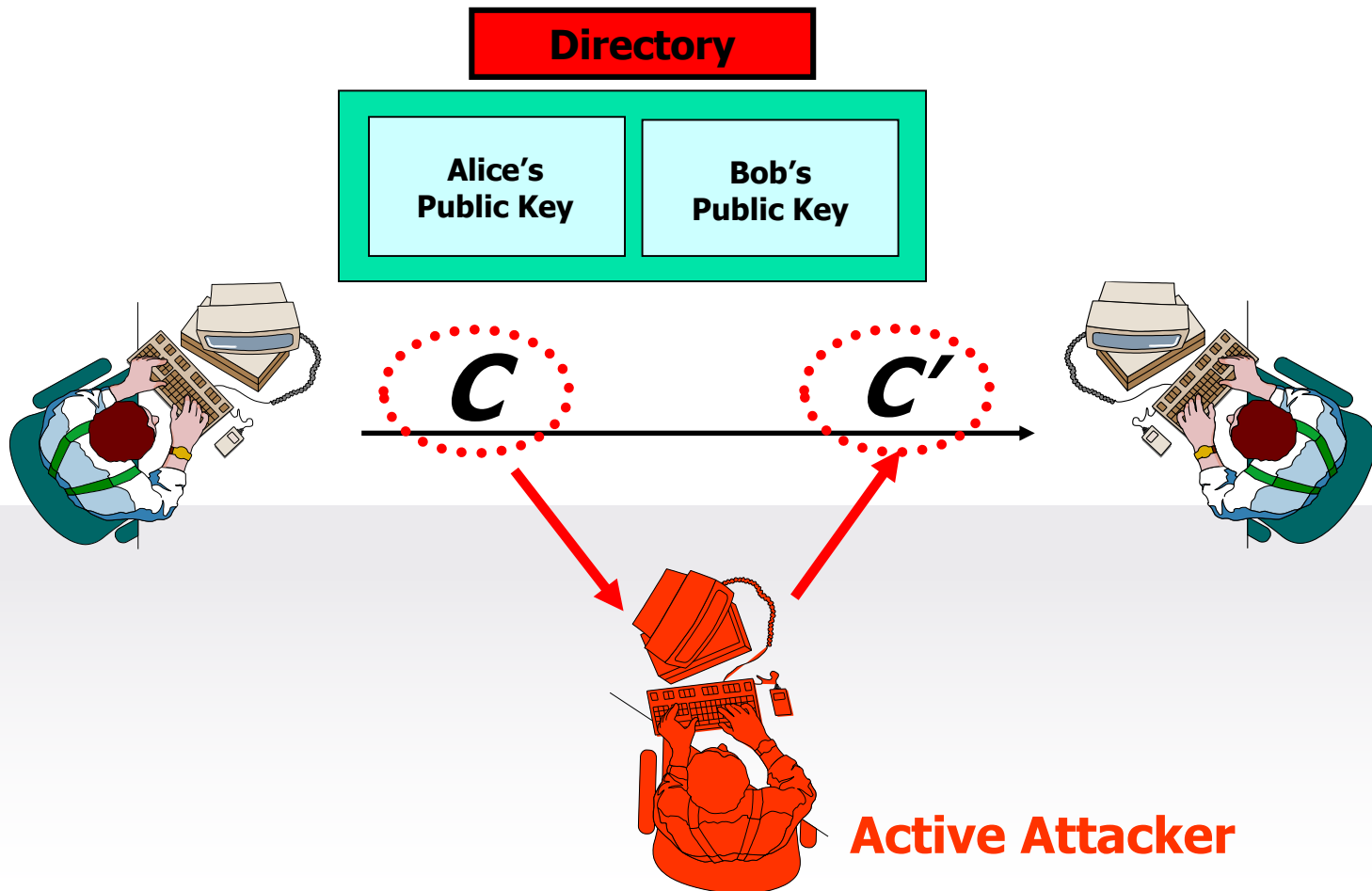
# Chosen Ciphertext Attack

- **After** queries to  $DO$
- **Before** queries to  $DO$



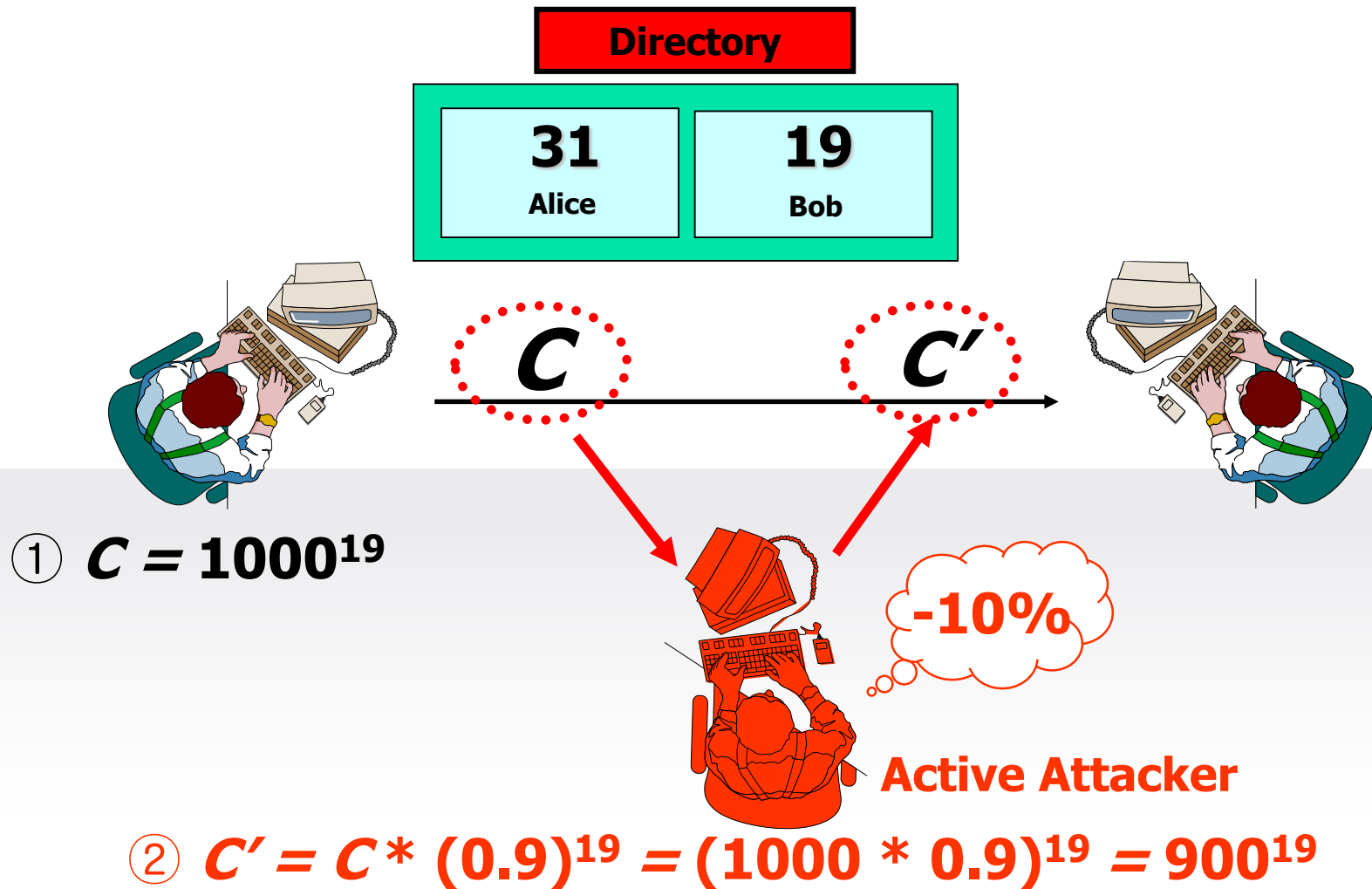
※ **RULE :  $C_0 \neq C_1, \dots, C_n$**

# Non-Malleability



$m'$  is unknown, but related in some known way to  $m$

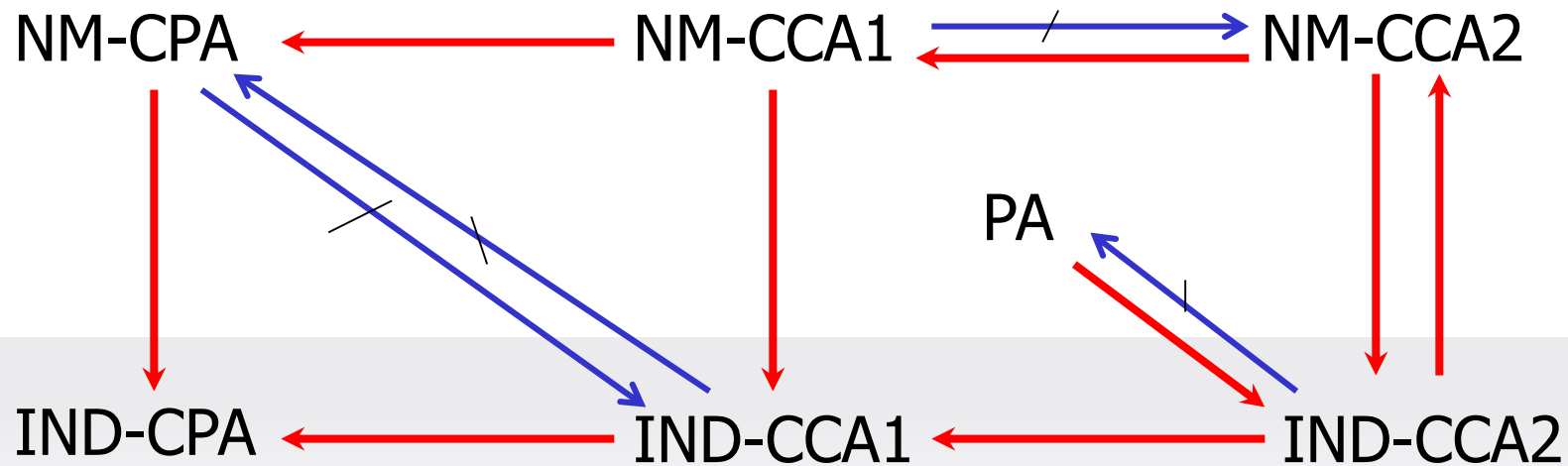
# Non-Malleability



# How to Make Non-Malleable Cipher?

# How to make it?

# How to Make Non-Malleable Cipher?

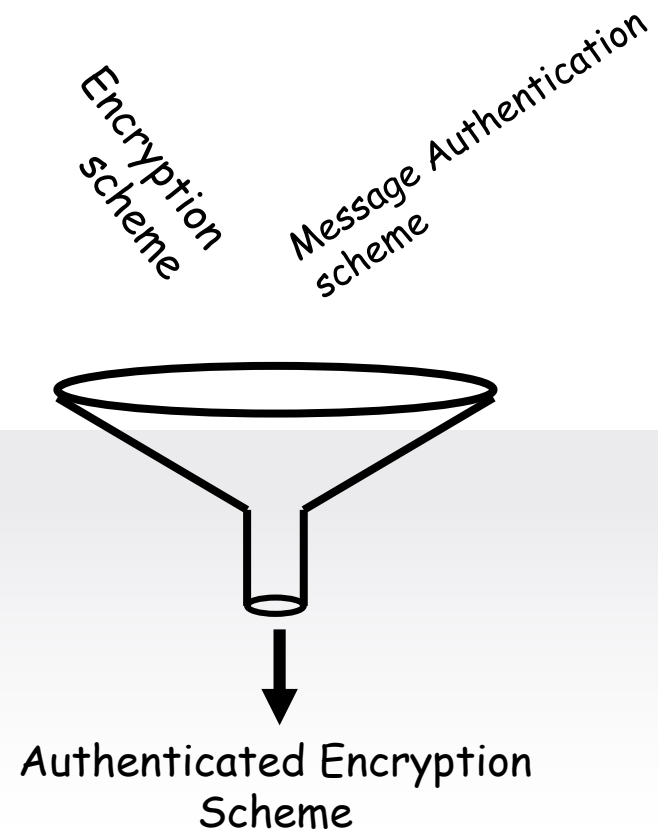


# How to Make Non-Malleable Cipher?

- Authenticated Encryption
- Plaintext Awareness



# Authenticated Encryption



# Relevance to Internet Security

- Many popular Internet protocols rely on authenticated encryption schemes for privacy and authenticity.
  - Examples: SSL, TLS, SSH, IPSEC, ...
- Many applications on the Internet require both privacy and authenticity.
  - Examples: online banking, online retail, online auctions, instant messaging, remote login, secure file transfer, ...

# Generic Composition Methods

- **Encrypt-and-MAC**

- $\bar{E}_{Ke,Km}(M) = E_{Ke}(M) || T_{Km}(M)$

- **MAC-then-Encrypt**

- $\bar{E}_{Ke,Km}(M) = E_{Ke}(M || T_{Km}(M))$

- **Encrypt-then-MAC**

- $\bar{E}_{Ke,Km} = E_{Ke}(M) || T_{Km}(E_{Ke}(M))$

# Generic Composition Results

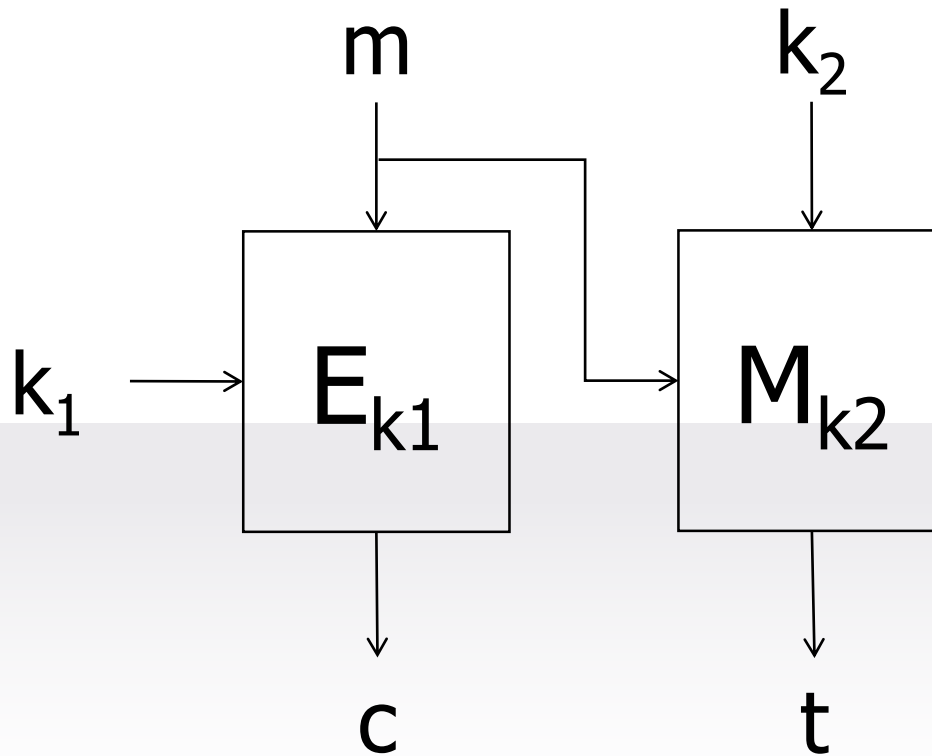
## ■ Question:

- Assuming the base encryption scheme is secure (IND-CPA) and the base MAC scheme is secure (UF-CMA),
- is the composed scheme CCA-secure?

# Generic Composition Results

Composition Method	Security
1) Encrypt-and-MAC $E_{Ke,Km}(M) = E_{Ke}(M)    T_{Km}(M)$	
2) MAC-then-Encrypt $E_{Ke,Km}(M) = E_{Ke}(M    T_{Km}(M))$	
3) Encrypt-then-MAC $E_{Ke,Km}(M) = E_{Ke}(M)    T_{Km}(E_{Ke}(M))$	

# Encrypt-then-MAC



# Plaintext Awareness

- PA is merely a ( ) rather than a ( ).
- A scheme with IND-CPA security is plaintext aware (PA) if an adversary cannot produce a valid ciphertext without knowing the corresponding plaintext.
  - The adversary has access to an encryption oracle and random oracles but no decryption oracle.
- PA implies IND-CCA2 security.
  - Decryption queries give no information since the adversary already “knows” the plaintext.

# PA & Random Oracle Model

- Sometimes it is helpful to consider models where some tools (primitives) used by cryptographic schemes such as,
  - Hash functions
  - Block ciphers
  - Finite groupsare considered to be ideal, that is, the adversary can only use (attack) them in a certain way.
- Idealized Security Models:
  - Hash function  $\rightarrow$  Random oracle
  - Block ciphers  $\rightarrow$  Ideal cipher
  - Finite groups  $\rightarrow$  Generic group
- Standard model: no idealized primitives (sort of)



# PA & Random Oracle Model

- A paradigm for designing efficient provably secure protocols (M.Bellare and P.Rogaway, 1993)
- In cryptography, a RO is an oracle (a theoretical black box) that responds to every query with a (truly) random response chosen uniformly from its output domain, except that for any specific query, it responds the same way every time it receives that query.

# PA & Random Oracle Model

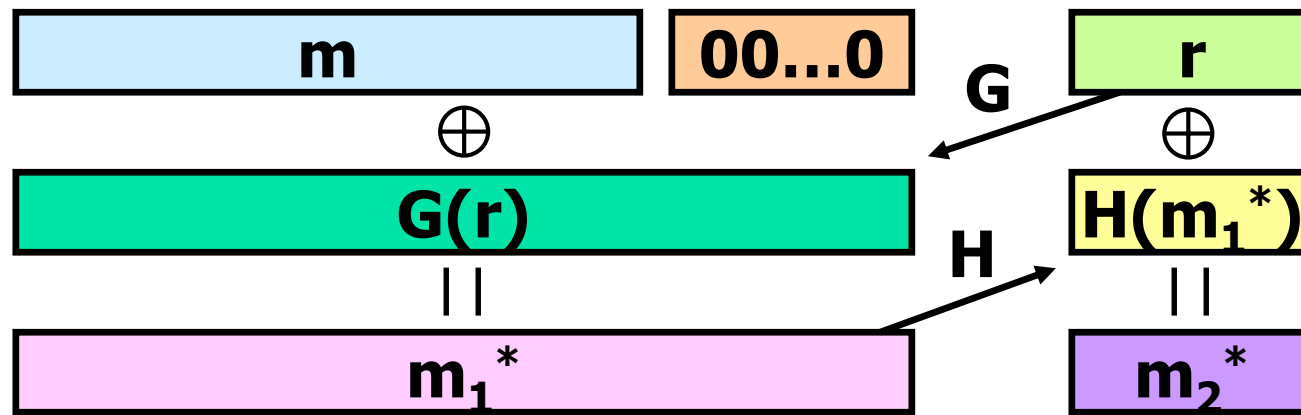
- PA makes sense only in the ROM!
  - The RO is used in the definition of plaintext awareness to give the extractor a “window” into the internal state of the adversary (as revealed through its queries). If the external RO is replaced by an internal algorithm, then this window is closed.
  - In the standard model, the adversary can encrypt a plaintext and then “forget” it.

# OAEP



- Optimal Asymmetric Encryption Padding
- The main drawback of the previous scheme is that ciphertexts are longer than a single element of  $Z_N^*$ , even when short messages are encrypted.
- The encoding function OAEP is designed so that the only way to find an element in the image of OAEP is to choose  $m$  and  $r$  and then explicitly compute  $\text{OAEP}(m, r)$ .
- OAEP is essentially a ( ).

# RSA-OAEP



$f(\cdot)$  : one-way permutation

$$C = f(\text{OAEP}(m, r)) = (m_1^* || m_2^*)^e \bmod N$$

# OAEP++

- A new padding scheme OAEP++ was proposed by Jonsson (2002).
  - The one-time pad on the OAEP (xor between random and output of H) is replaced by a strong block cipher (ideal cipher model).
- Ideal Cipher Model
  - Consider block cipher E as a family of perfectly random and independent permutations.

# Limits of Provable Security

- Provable security does not yield proofs
  - Proofs are relative (to computational assumptions) and to the definition of the scheme's goal
  - Proofs often done in ideal models (Random Oracle Model, Ideal Cipher Model, Generic Group Model) with debatable meaning.
  - Definitions and proofs need time for acceptance.

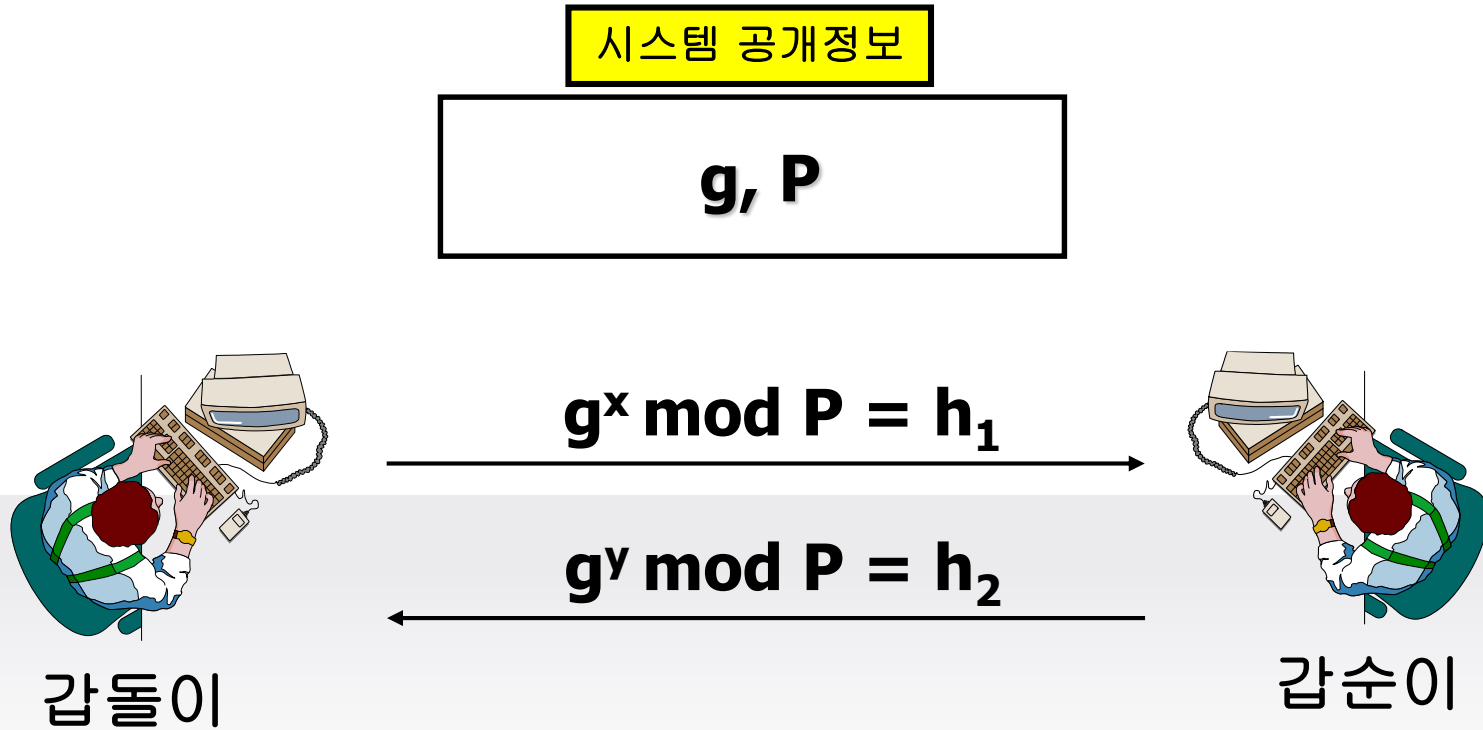
# Limits of Provable Security

- Still, provable security
  - Provides some form of guarantee that the scheme is not flawed
  - Motivates us to spell out (clarify) definitions and models formally, a process that, in itself, may help us to better understand the problem!
  - Gives well-defined reductions from which we can distill practical implications of the result (exact security)

# Key Management



# Diffie-Hellman Key Exchange



$$K = h_2^x = (g^y)^x = g^{xy} \pmod{P}$$

$$K = h_1^y = (g^x)^y = g^{xy} \pmod{P}$$

# Definition of Security

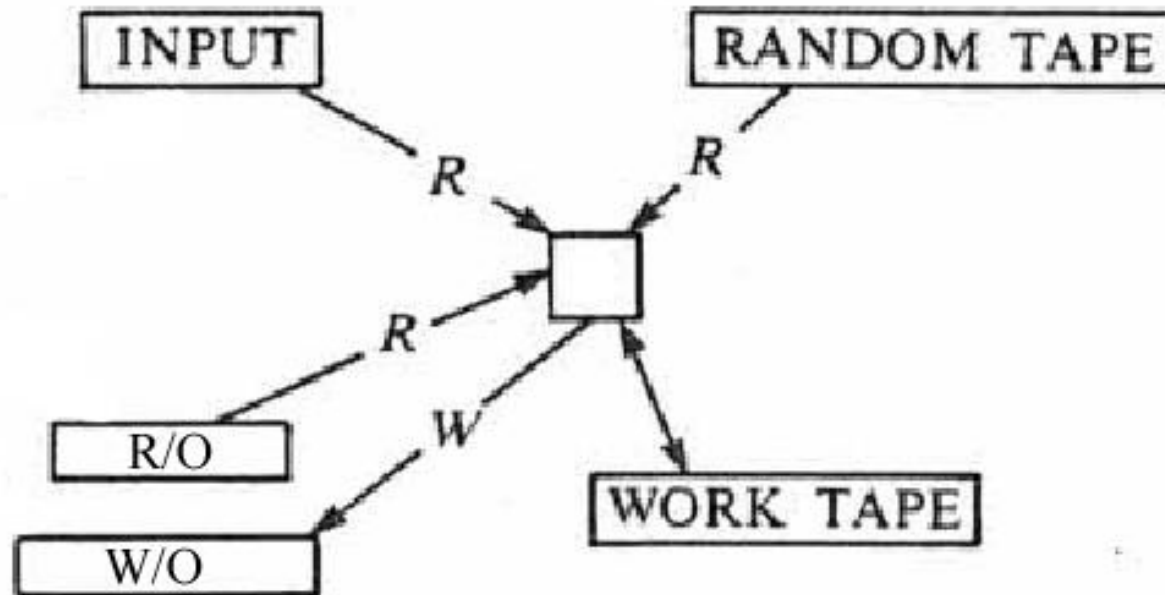


- ***This is much stronger than simply requiring that the adversary be unable to compute  $K$  exactly.***
  - *Can compute  $K \rightarrow$  Can distinguish  $K$*

# 2-Party Protocols

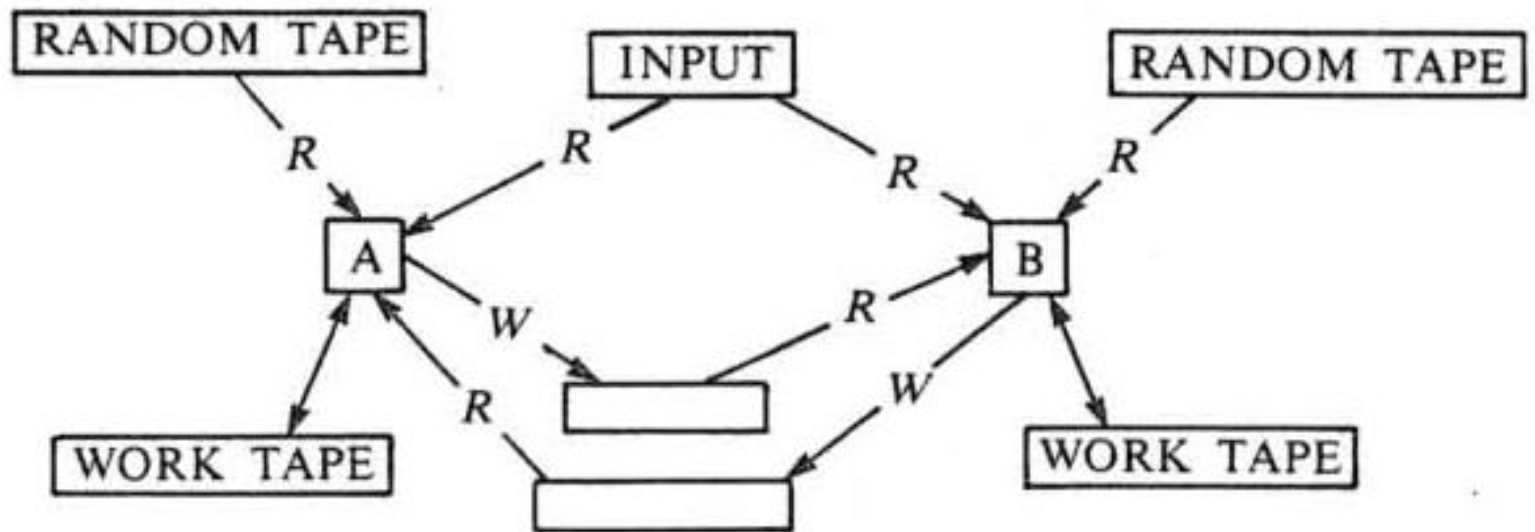
# Interactive Protocol

- Interactive Turing Machine



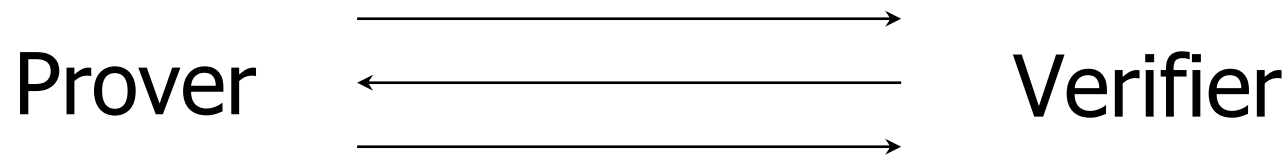
# Interactive Protocol

- Interactive Turing Machines



# Zero-Knowledge Proofs

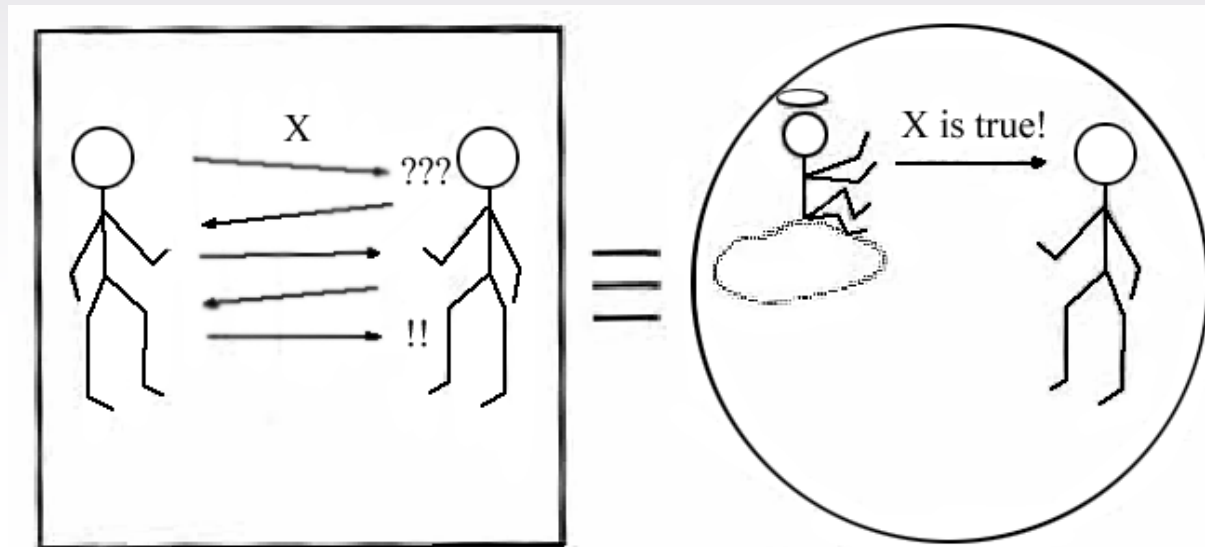
- An interactive proof system involves a prover and a verifier



(Interactive proofs)

# Zero-Knowledge Proofs

- **Idea:** the prover proves a statement to the verifier without revealing anything except the fact that the statement is true
- **Zero-Knowledge Proof of Knowledge (ZKPK):** prover convinces verifier that he knows a secret without revealing the secret



# Properties of ZKPK

## ■ Completeness

- If both prover and verifier are honest, protocol succeeds with overwhelming probability

## ■ Soundness

- No one who does not know the secret can convince the verifier with nonnegligible probability
  - Intuition: the protocol should not enable prover to prove a false statement

## ■ Zero-Knowledge

- The proof does not leak any information

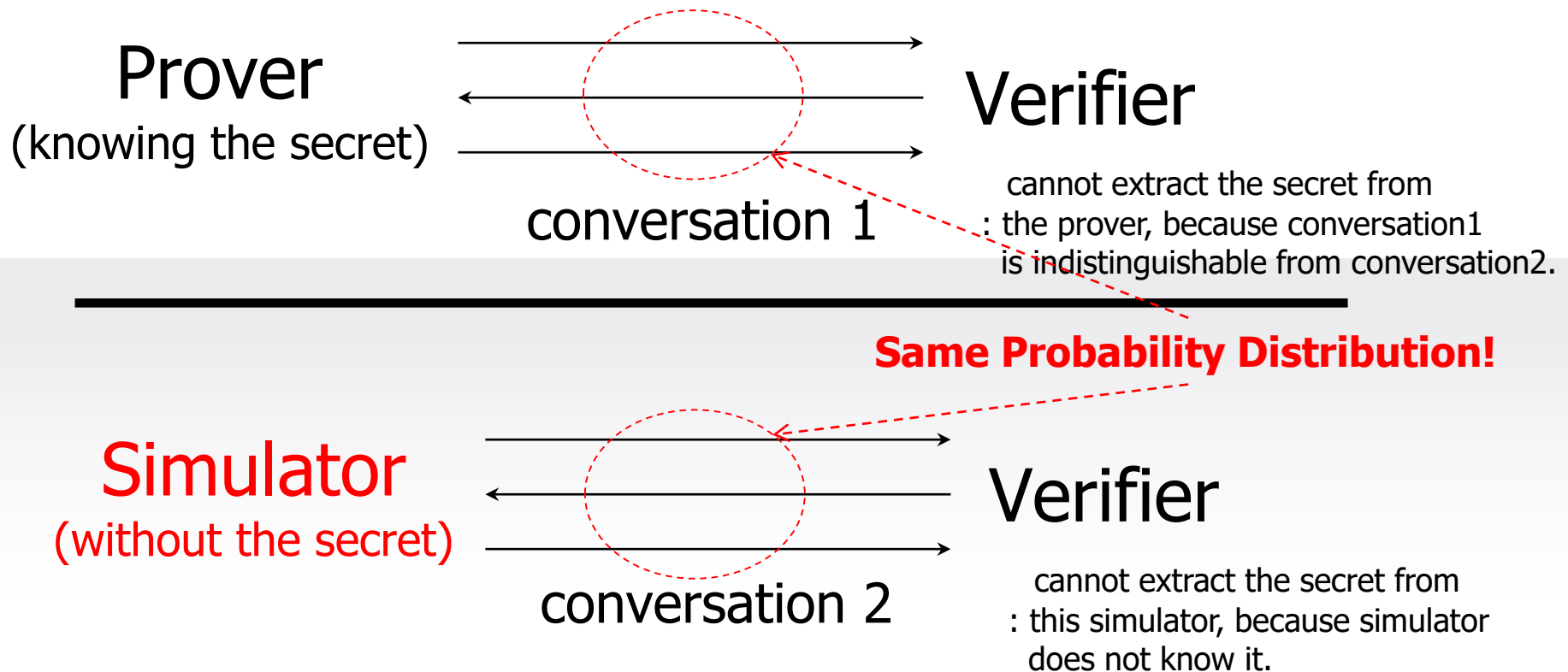


# Zero-Knowledge Property

- The proof does not leak any information
- There exists a **simulator** that, taking what the verifier knows before the protocol starts, produces a fake “transcript” of protocol messages that is **indistinguishable** from actual protocol messages
  - Because all messages can be simulated from verifier’s initial knowledge, verifier does not learn anything that he didn’t know before
  - **Indistinguishability**: perfect, statistical, or computational
- Honest-verifier ZK only considers verifiers that follow the protocol

# Zero-Knowledge Property

- Zero knowledge proofs are simulatable (conversation distributions are **indistinguishable**)

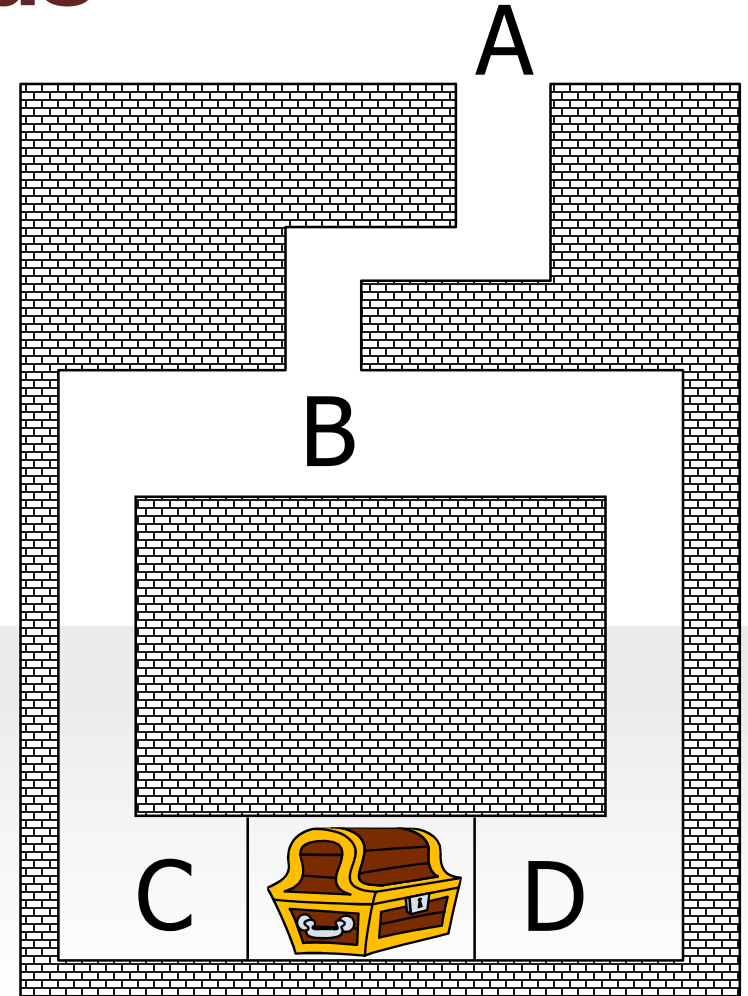


# Zero-Knowledge Property

- No one who does not know the secret can convince the verifier with nonnegligible probability.
- Let  $A$  be any prover who convinces the verifier ...
- ... there must exist a **knowledge extractor** algorithm that, given  $A$ , extracts the secret from  $A$ .
  - **Intuition:** if there existed some prover  $A$  who manages to convince the verifier that he knows the secret without actually knowing it, then no algorithm could possibly extract the secret from this  $A$ .

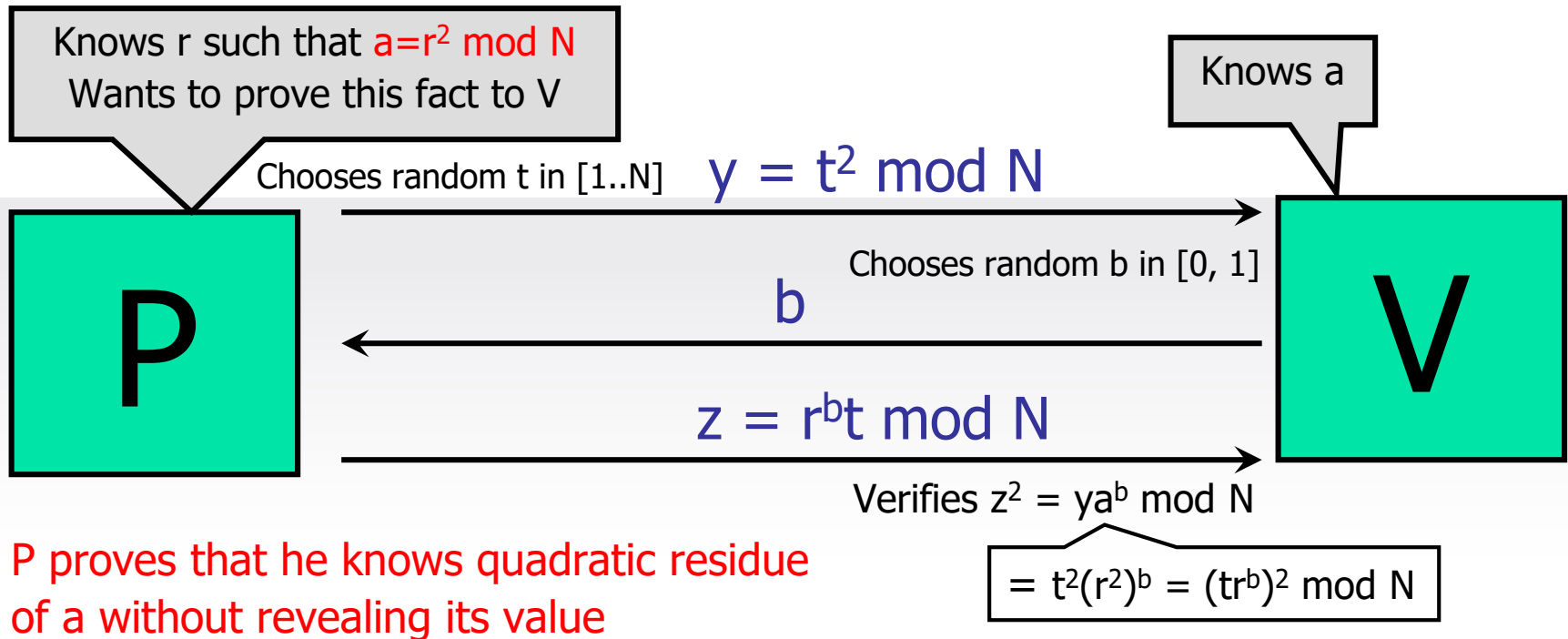
# Zero-Knowledge for Kids

1. V stands at A.
2. P walks to C or D.
3. V walks to B.
4. V asks P to come L or R.
5. P follows the request.
6. Repeat 1 ~ 5, n times.



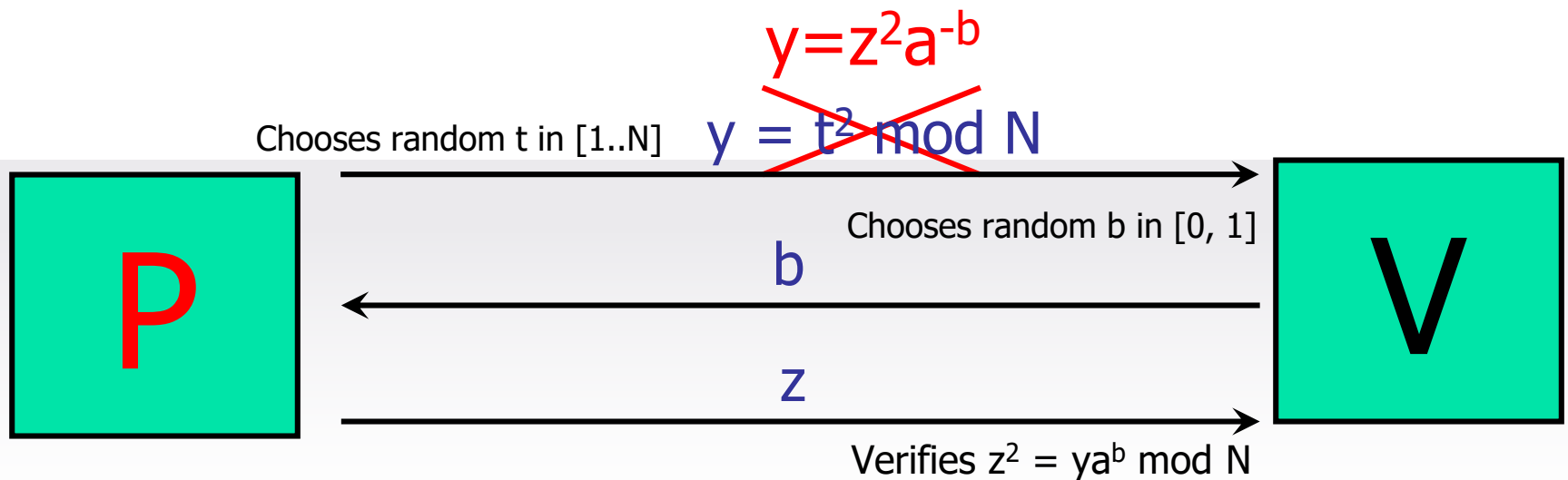
# ZKIP for QRP

- System parameters
  - $N$



# Cheating against ZKIP for QRP

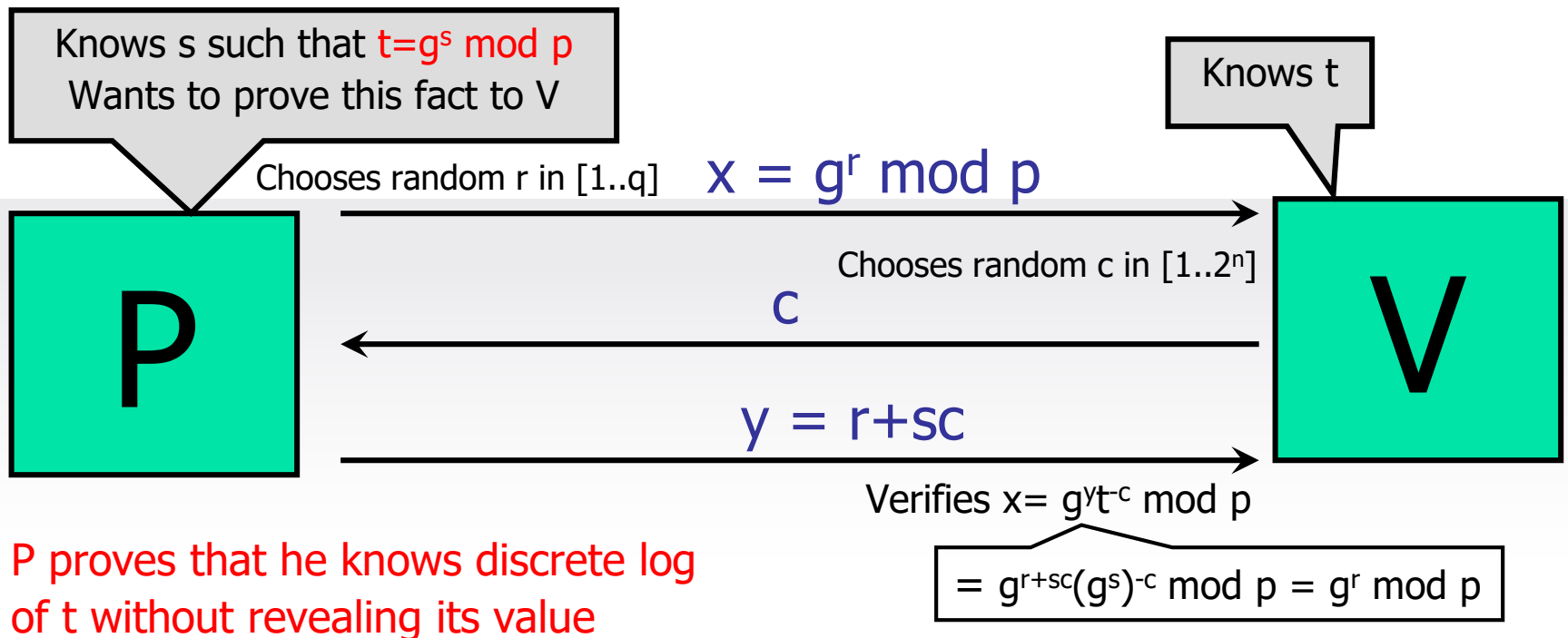
- Prover can cheat if he can guess  $b$  in advance
  - Guess  $b$ , set  $y = z^2 a^{-b}$  for random  $z$  in 1<sup>st</sup> message
  - What is the probability of guessing  $b$ ?



P proves that he "knows" quadratic residue of  $a$  even though he does not know  $r$

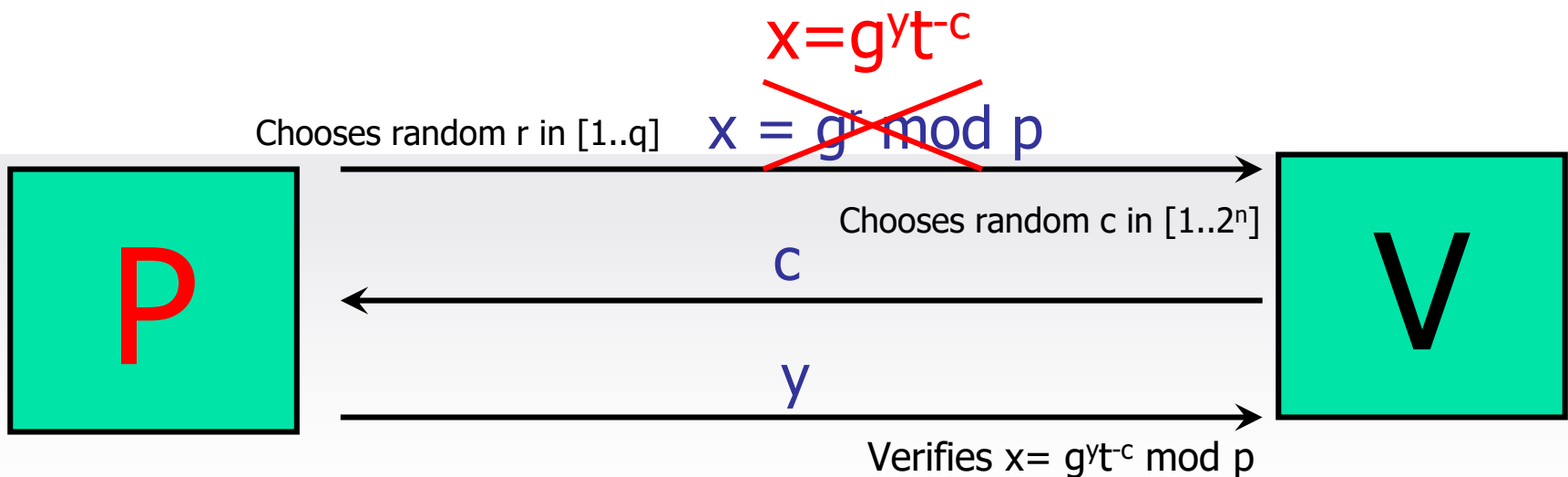
# Schnorr's Id Protocol (ZKIP for DLP)

- System parameters
  - Prime  $p$  and  $q$  such that  $q$  divides  $p-1$
  - $g$  is a generator of an order- $q$  subgroup of  $Z_p^*$



# Cheating against Schnorr's Id Protocol

- Prover can cheat if he can guess  $c$  in advance
  - Guess  $c$ , set  $x = g^y t^{-c}$  for random  $y$  in 1<sup>st</sup> message
  - What is the probability of guessing  $c$ ?

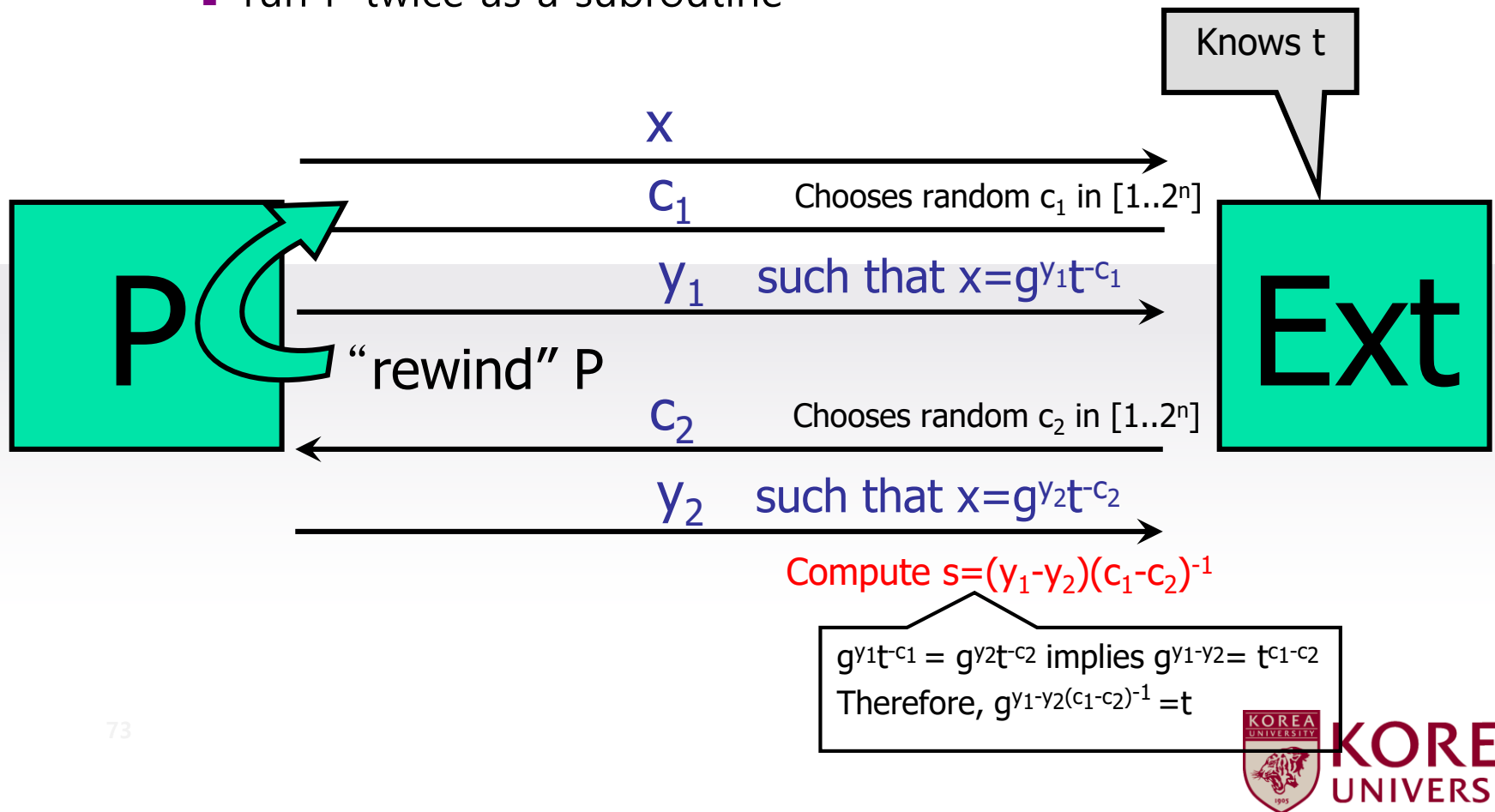


P proves that he "knows" discrete log of  $t$  even though he does not know  $s$



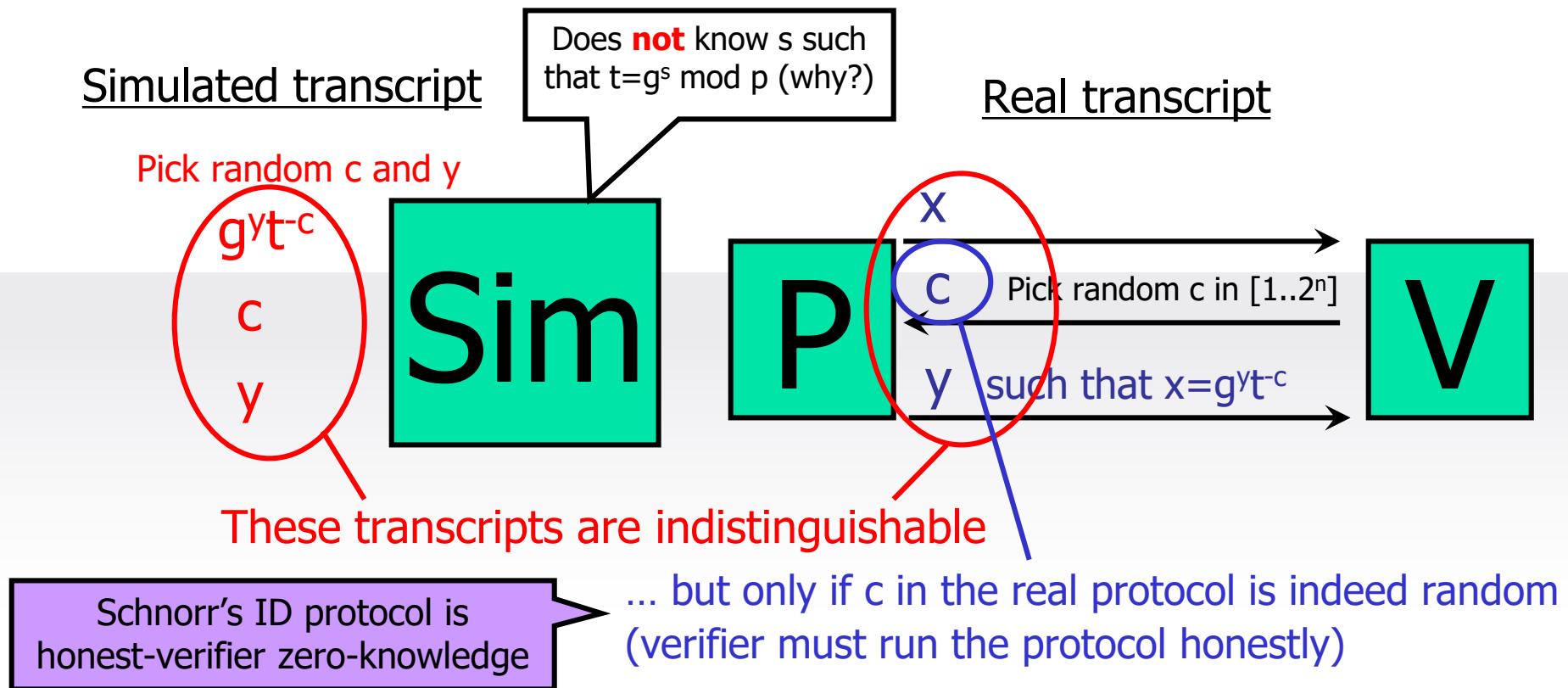
# But Schnorr's Id Protocol Is Sound

- Prover can cheat if he can guess  $c$  in advance
  - Given  $P$  who successfully passes the protocol, extract  $s$  such that  $t = g^s \pmod p$ 
    - run  $P$  twice as a subroutine



# Schnorr's Id Protocol Is HVZK

- Simulator produces a transcript which is indistinguishable from the real transcript



# Digital Signatures

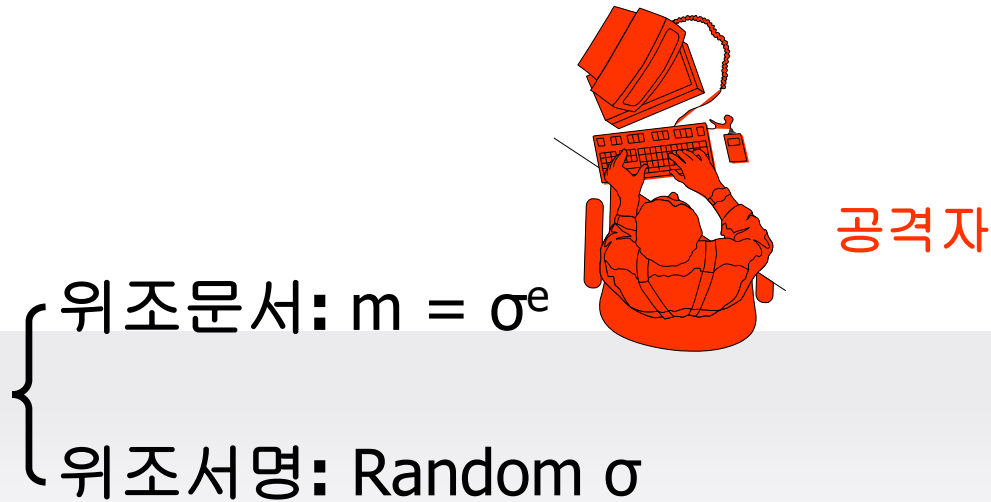
# Security Goal & Attack Model

- Target
  - **Total Break** : Find private key
  - **Selective Forgery** : Signature on selected message
  - **Existential Forgery** : Signature on some message

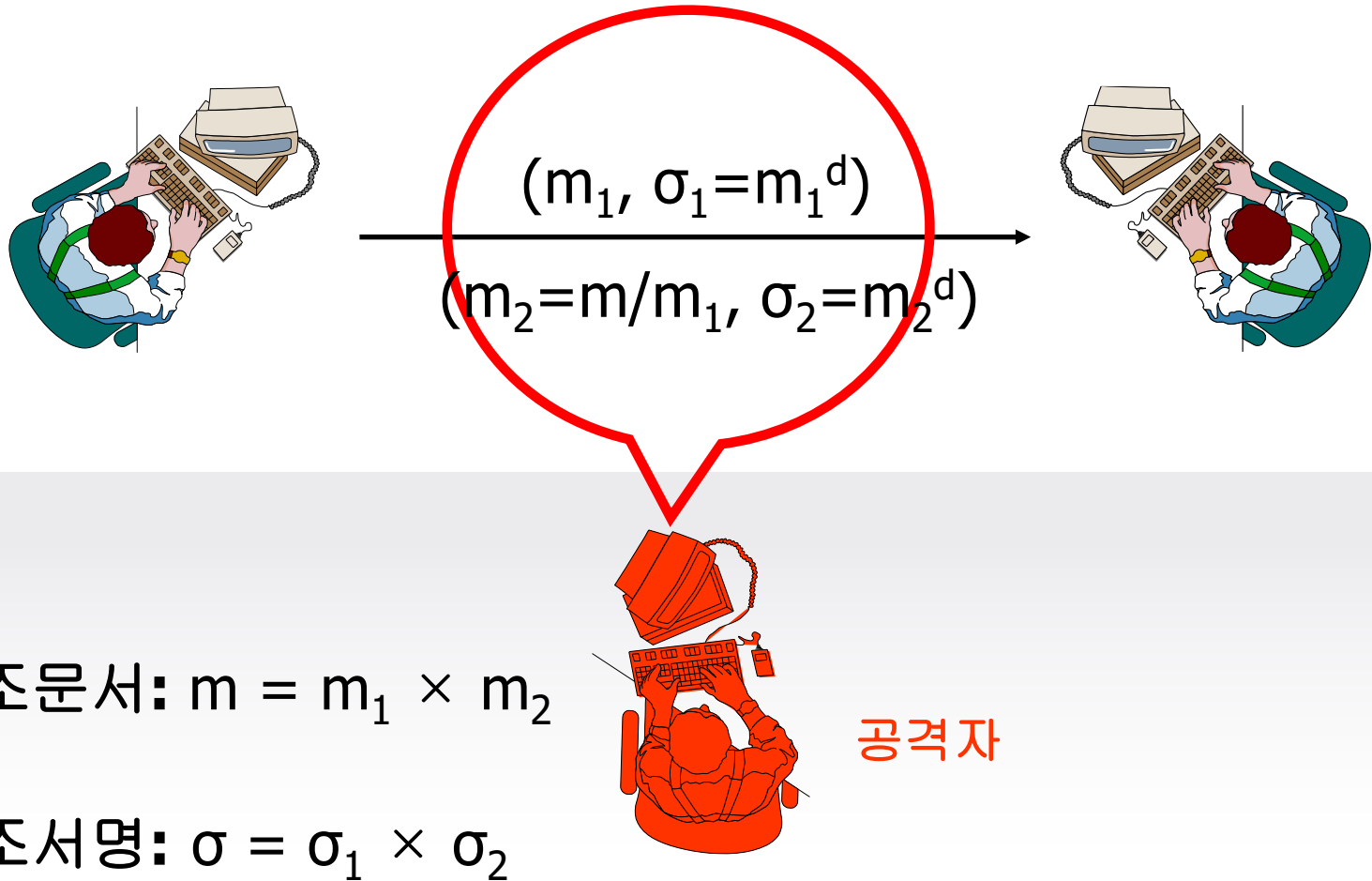
# Security Goal & Attack Model

- Attack
  - Key-Only Attack
  - Known Message Attack
  - Chosen Message Attack

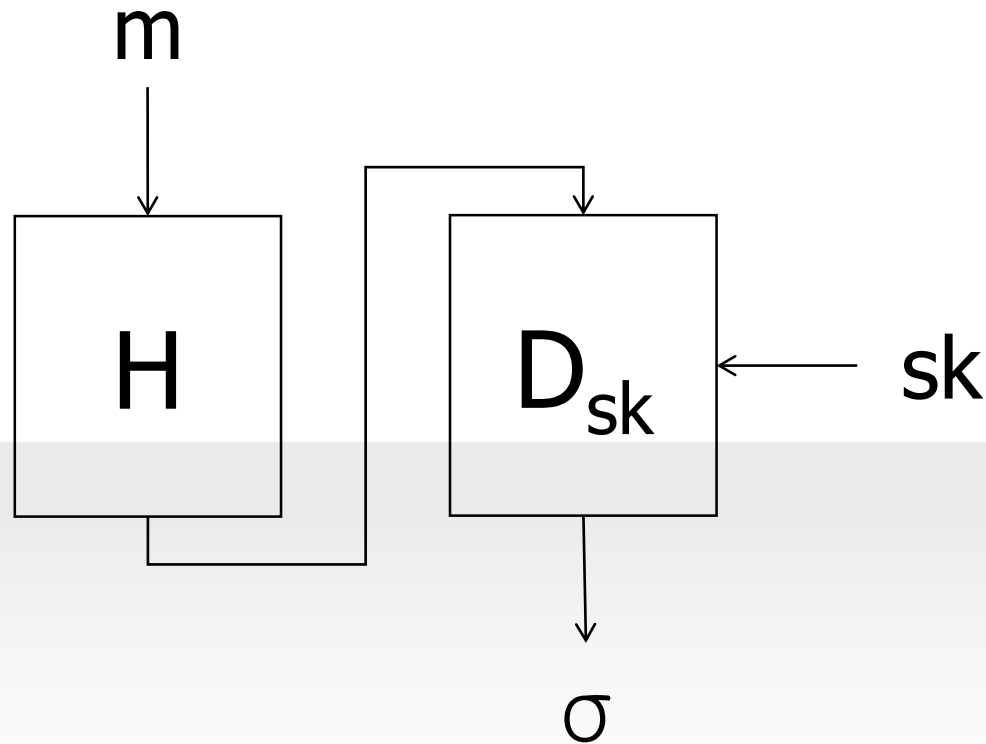
# Existential Forgery - KOA



# Selective Forgery - CMA

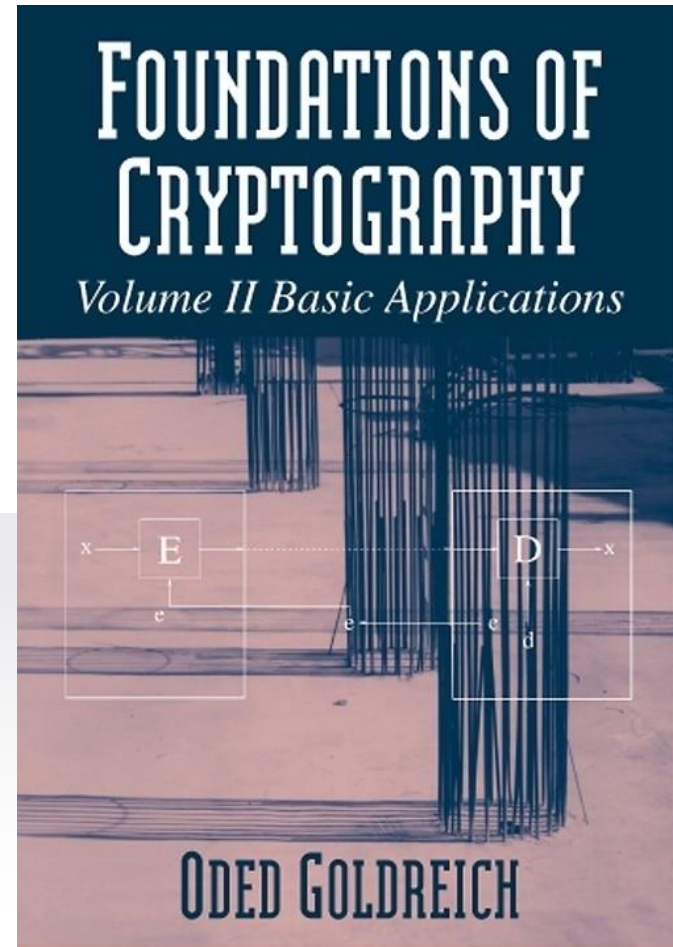
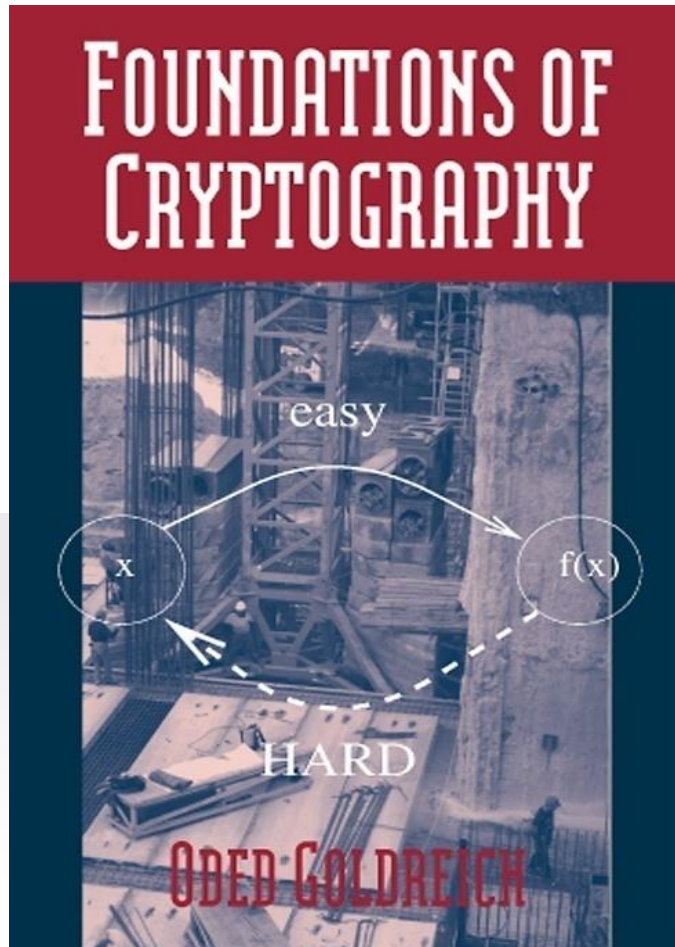


# Hash-and-Sign Paradigm

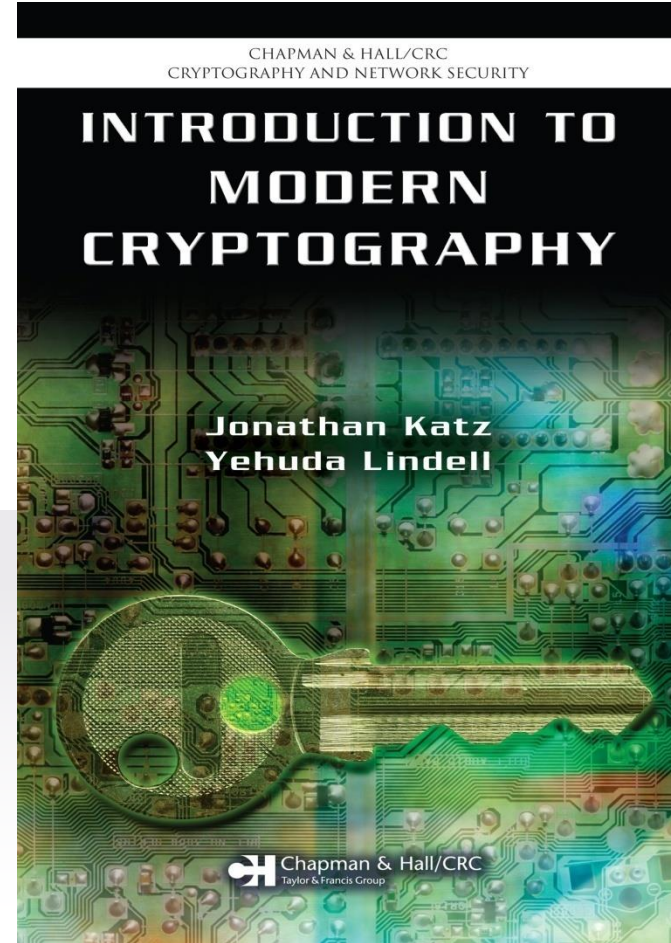
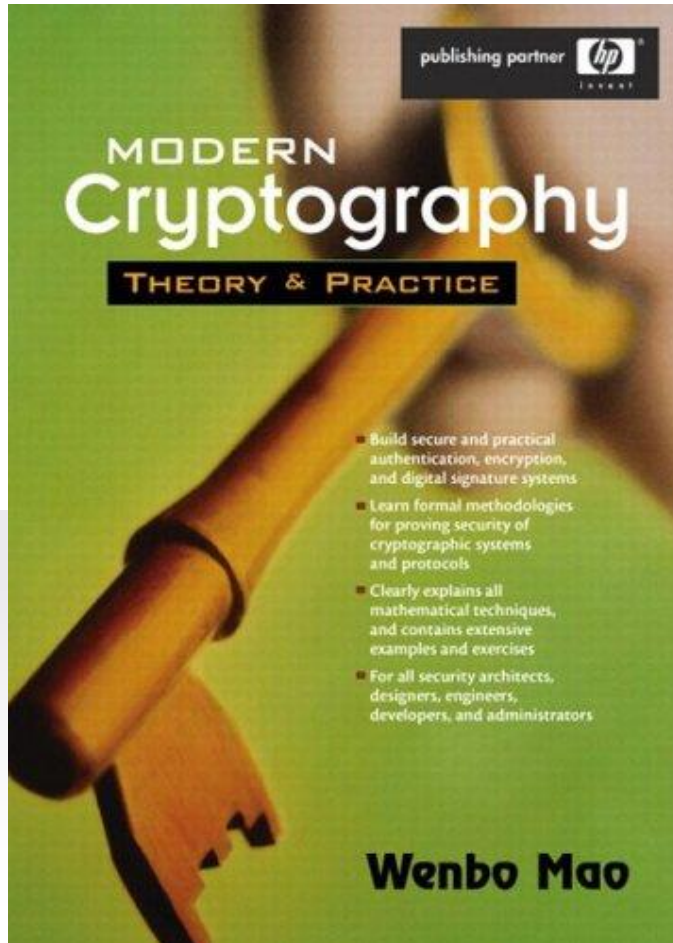




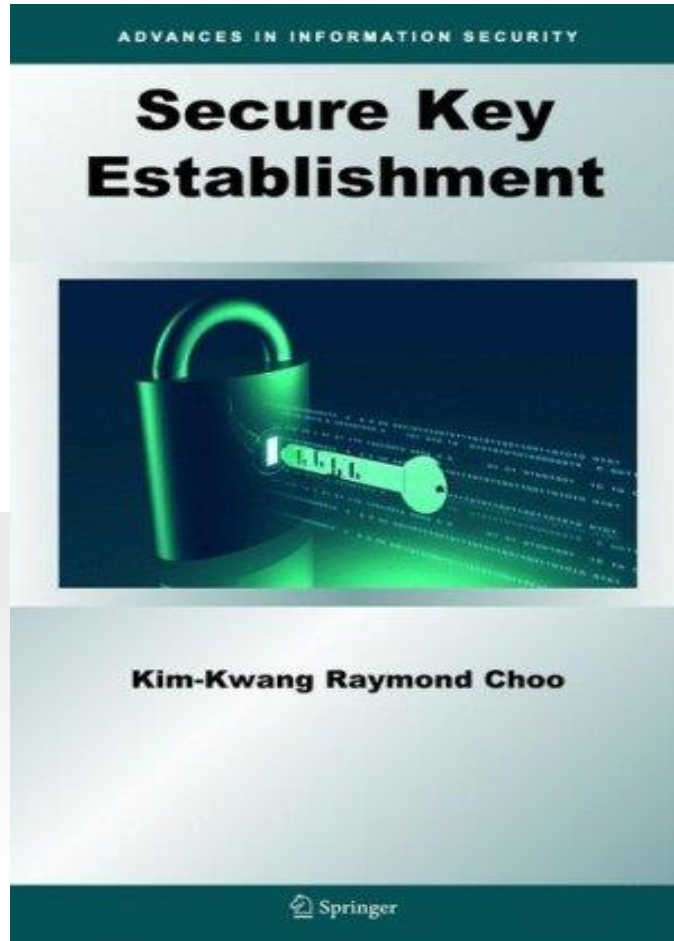
# To Learn More



# To Learn More



# To Learn More



# Secure Design

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