Bi-Weekly Contest 120

```
2970. Count the Number of Incremovable Subarrays I

Example 1:

Input: nums = [1,2,3,4]
Output: 10
Explanation: The 10 incremovable subarrays are: [1], [2], [3], [4], [1,2], [2,3], [3,4], [1,2,3], [2,3,4], and [1,2,3,4], because on removing any one of these subarrays nums becomes strictly increasing. Note that you cannot select an empty subarray.

Example 2:

Input: nums = [6,5,7,8]
Output: 10
Explanation: The 10 incremovable subarrays are: [5], [6], [5,7], [6,5], [5,7,8], [6,5,7] and [6,5,7,8].
It can be shown that there are only 7 incremovable subarrays in nums.
```

```
Example 3:

Input: nums = [8,7,6,6]
Output: 3
Explanation: The 3 incremovable subarrays are: [8,7,6], [7,6,6], and [8,7,6,6]. Note that [8,7] is not an incremovable subarray because after removing [8,7] nums becomes [6,6], which is sorted in ascending order but not strictly increasing.

Constraints:
    1 <= nums.length <= 50
    1 <= nums[i] <= 50</pre>
```

Solution 1:

```
class Solution {
    public:
        int incremovableSubarrayCount(vector<int>& nums) {
            int ans = 0; // Initialize the answer variable to 0.

        // Iterate through all possible subarrays defined by the indices i and j.
        for (int i = 0; i < nums.size(); ++i) {
            for (int j = i; j < nums.size(); ++j) {
                int last = -1, flag = 1; // Initialize variables to track the last element and a flag indicating whether the subarray is incremovable.
```

// Iterate through the array to check if removing the subarray defined by i and j makes the array strictly increasing.

```
for (int k = 0; k < nums.size(); ++k) {
             if (k \ge i \&\& k \le j) continue; // Skip the elements within the subarray
defined by i and j.
             if (last >= nums[k]) { // If the current element violates the increasing order,
set the flag to 0 and break the loop.
                flag = 0;
                break;
             last = nums[k]; // Update the last element.
           }
           // If the flag is still 1, the subarray is incremovable, so increment the answer.
           if (flag) {
             ans++;
          }
        }
     }
     return ans: // Return the final answer.
  }
};
```

Outer Loop (i): This loop iterates through all possible starting indices of the subarray.

Inner Loop (j): This loop iterates through all possible ending indices of the subarray. It starts from the current i to the end of the array.

Subarray Check (k): The innermost loop checks whether the subarray defined by the current i and j is incremovable. It skips the elements within this subarray and compares each element to the previous one (last). If at any point the order is violated, the flag is set to 0, indicating that the subarray is not incremovable. Result Update: If the flag remains 1 after the innermost loop, it means the subarray is incremovable, and the answer is incremented.

Return: The final count of incremovable subarrays is returned as the result.

Note: While this solution works, it is not efficient, and there are more optimized algorithms to solve this problem. The given code has a time complexity of $O(n^3)$, where n is the length of the input array, making it inefficient for larger inputs.

```
Solution 2:
class Solution {
public:
  // Function to check if a subarray is strictly increasing
  bool check(vector<int> cnums) {
     for (int i = 1; i < cnums.size(); i++) {
       if (cnums[i] <= cnums[i - 1])
          return false;
     }
     return true;
  }
  // Main function to find the total number of incremovable subarrays
  int incremovableSubarrayCount(vector<int>& nums) {
     int n = nums.size();
     int ans = 0;
     // Iterate through all possible subarrays defined by the indices i and j
     for (int i = 0; i < n; i++) {
       for (int j = i; j < n; j++) {
          vector<int> cnums;
          // Construct a new array excluding elements between i and j
          for (int k = 0; k < i; k++) {
             cnums.push back(nums[k]);
          }
          for (int k = j + 1; k < n; k++) {
             cnums.push back(nums[k]);
          }
          // Check if the constructed subarray is strictly increasing
          if (check(cnums))
             ans++;
     }
```

```
return ans; // Return the final answer }
};
```

check Function: This function takes a vector cnums as input and checks if it is strictly increasing. It does so by iterating through the elements of cnums and returning false if any adjacent pair violates the increasing order.

Main Function (incremovableSubarrayCount):

- Outer Loop (i): Iterates through all possible starting indices of the subarray.
- Inner Loop (j): Iterates through all possible ending indices of the subarray, starting from the current i.
- Subarray Construction (cnums): Constructs a new vector cnums by excluding elements between the current i and j.
- Check if Subarray is Incremovable: Calls the check function to verify if the constructed subarray is strictly increasing. If it is, increments the answer.

Return: Returns the final count of incremovable subarrays as the answer.

While this code is correct, it is also not efficient, with a time complexity of O(n^3) due to the three nested loops. There are more optimized algorithms to solve this problem with better time complexity.

Solution 3:

```
class Solution {
public:
    int incremovableSubarrayCount(vector<int>& nums) {
        int n = nums.size();
        int count = 0;

    // Handle the case of a single-element array
        if (n == 1) return 1;

    // Iterate through all possible subarrays defined by the indices i and j
        for (int i = 0; i < n; i++) {
                  unordered_map<int, int> mp; // Map to store indices to be excluded
```

```
for (int j = i; j < n; j++) {
          vector<int> temp; // Temporary vector to construct the subarray
          // Mark the index j to be excluded
          mp[j]++;
          bool helpme = false;
          // Construct a new array excluding elements marked in the map
          for (int k = 0; k < n; k++) {
             if (mp.find(k) == mp.end()) {
               temp.push_back(nums[k]);
            }
          }
          // Check if the constructed subarray is incremovable
          if (temp.size() == 1 || temp.size() == 0) {
             count += 1;
          } else {
            for (int m = 0; m < temp.size() - 1; m++) {
               if (temp[m] \ge temp[m + 1]) {
                  helpme = true;
               }
            }
             if (helpme == false) {
               count += 1;
          }
       }
     }
     return count; // Return the final answer
  }
};
Explanation:
```

<u>Initialization:</u> Initialize variables, including count to keep track of the number of incremovable subarrays.

<u>Handling Single Element Array</u>: If the array has only one element, return 1 because a single element is considered strictly increasing.

Main Loop (\underline{i}): Iterate through all possible starting indices of the subarray. Nested Loop (\underline{i}): Iterate through all possible ending indices of the subarray, starting from the current \underline{i} .

 $\underline{\text{Map (mp)}}$: Use an unordered map to mark the indices that should be excluded from the subarray.

<u>Subarray Construction (temp)</u>: Construct a new vector temp by excluding elements marked in the map.

<u>Incremovable Check</u>: Check if the constructed subarray is incremovable. If it has only one or no elements, increment the count. Otherwise, check if the elements are strictly increasing. If so, increment the count.

Return: Return the final count of incremovable subarrays as the answer.

While this code is correct, it is not efficient, with a time complexity of $O(n^4)$ due to the four nested loops. There are more optimized algorithms to solve this problem with better time complexity.

Solution 4-

```
class Solution {
public:
    long long incremovableSubarrayCount(vector<int>& nums) {
    int n = nums.size();
    vector<int> start, end;

    // Construct the increasing subarray from the beginning
    for (int i = 0; i < n; ++i) {
        if (start.empty() || start.back() < nums[i]) {
            start.push_back(nums[i]);
        } else {</pre>
```

```
break;
       }
    }
    // Construct the increasing subarray from the end
    for (int i = n - 1; i >= 0; --i) {
       if (end.empty() || end.back() > nums[i]) {
         end.push_back(nums[i]);
       } else {
         break;
      }
    }
    // If the combined size of start and end is greater than n, return the total possible
subarrays
    if (start.size() + end.size() > n) {
       return 1LL * n * (n + 1) / 2;
    }
    long long ans = start.size() + end.size();
    int i = 0, j = 0;
```

```
// Reverse the end vector to compare elements easily
reverse(end.begin(), end.end());
// Merge the increasing subarrays and count the incremovable subarrays
while (i < start.size() && j < end.size()) {
  if (start[i] < end[j]) {</pre>
    ans += end.size() - j;
     ++i;
  } else {
     ++j;
  }
}
return ans + 1; // Add 1 to include the case of an empty subarray
```

}

};

Constructing Increasing Subarrays (start and end):

• The first loop (i from 0 to n-1) constructs an increasing subarray (start) from the beginning of the array.

• The second loop (i from n-1 to 0) constructs an increasing subarray (end) from the end of the array.

Total Possible Subarrays Check:

• If the combined size of start and end is greater than n, it means that the array itself is strictly increasing, so the total number of subarrays is returned using the formula for the sum of the first n natural numbers.

Merging and Counting:

- The code then merges the increasing subarrays (start and end) and counts the incremovable subarrays.
- It uses two pointers (i and j) to iterate through start and end vectors.
- It compares elements at the pointers, and if an element from start is less than an element from end, it increments the answer by the remaining size of end (end.size() j).
- This is because if start[i] < end[j], then all subarrays with start[i] and elements in end from end[j] to the end are incremovable.
- The pointers are then appropriately incremented.

Return:

• The final answer is returned by adding 1 to include the case of an empty subarray.

This solution has a time complexity of O(n), making it more efficient compared to the previous solutions.

```
2971. Find Polygon With the Largest Perimeter
You are given an array of positive integers nums of length n.
A polygon is a closed plane figure that has at least 3 sides. The longest side of a polygon is smaller than the sum of its other sides.
Conversely, if you have k (k >= 3) positive real numbers a_1, a_2, a_3, ..., a_k where a_1 <= a_2 <= a_3 <= \ldots <= a_k and a_1 + a_2 + a_3 + \ldots + a_{k-1} > a_k, then there
always exists a polygon with k sides whose lengths are a_1, a_2, a_3, ..., a_k.
The perimeter of a polygon is the sum of lengths of its sides.
Return the largest possible perimeter of a polygon whose sides can be formed from nums, or -1 if it is not possible to create a polygon.
Example 1:
  Input: nums = [5,5,5]
  Output: 15
 Explanation: The only possible polygon that can be made from nums has 3 sides: 5, 5, and 5. The perimeter is 5 + 5 + 5 = 15.
Example 2:
  Input: nums = [1,12,1,2,5,50,3]
  Output: 12
  Explanation: The polygon with the largest perimeter which can be made from nums has 5 sides: 1, 1, 2, 3, and 5. The
  We cannot have a polygon with either 12 or 50 as the longest side because it is not possible to include 2 or more smaller
```

```
Example 3:

Input: nums = [5,5,50]
Output: -1
Explanation: There is no possible way to form a polygon from nums, as a polygon has at least 3 sides and 50 > 5 + 5.

Constraints:

• 3 <= n <= 10<sup>5</sup>
• 1 <= nums[i] <= 10<sup>9</sup>
```

Solution-1

class Solution {

public:

long long largestPerimeter(vector<int>& nums) {

```
long long sum = 0; // Initialize a variable to store the sum of all elements
sort(nums.begin(), nums.end()); // Sort the elements in non-decreasing order
// Calculate the sum of all elements in the input vector
for (auto i : nums) {
  sum += i;
}
int n = nums.size(); // Get the size of the input vector
// Loop through the sorted vector from the end to find the largest perimeter
for (int i = n - 1; i >= 2; i--) {
  sum -= nums[i]; // Remove the largest element from the sum
  // Check if the sum of two smaller sides is greater than the largest side
  if (sum > nums[i]) {
    return sum + nums[i]; // If true, return the largest perimeter
```

```
}

return -1; // If no valid triangle is possible, return -1
}
```

Sorting the Array: The input array nums is sorted in non-decreasing order. Sorting helps in identifying the largest sides of the potential polygon towards the end of the array.

Calculating the Sum: The sum of all elements in the array is calculated.

Finding the Largest Perimeter:

- The code then loops through the sorted array from the end (i = n 1) to the beginning (i >= 2). It starts from the end because we are looking for the largest sides.
- In each iteration, the largest element (nums[i]) is removed from the total
 sum (sum -= nums[i]).
- The code then checks if the sum of the two remaining smaller sides is greater than the largest side (if (sum > nums[i])).
- If the condition is true, it means a valid triangle is possible, and the function returns the largest perimeter (return sum + nums[i]).

Returning -1 if No Valid Triangle: If no valid triangle is found after the loop, the function returns -1.

The time complexity of this solution is $O(n \log n)$ due to the sorting operation. The loop has a time complexity of O(n), resulting in an overall time complexity of $O(n \log n)$.

Solution-2

```
# define II long long
class Solution {
public:
  long long largestPerimeter(vector<int>& nums) {
    sort(nums.begin(), nums.end()); // Sort the elements in non-decreasing order
    II prefSum = nums[0] + nums[1]; // Initialize a variable to store the sum of the two
smallest elements
    Il ans = 0; // Initialize the variable to store the largest perimeter
    // Iterate through the sorted array from the third element
    for(int i = 2; i < nums.size(); i++) {
```

```
if(prefSum > nums[i]) {
         ans = max(ans, prefSum + nums[i]); // Check if the sum of two smaller sides is
greater than the third side
      }
      prefSum += nums[i]; // Update the sum by adding the current element
    }
    return (ans == 0) ? -1 : ans; // If no valid triangle is possible, return -1; otherwise,
return the largest perimeter
  }
};
```

Sorting the Array: The input array nums is sorted in non-decreasing order.

Initializing Variables:

- prefsum: This variable is initialized with the sum of the two smallest elements in the sorted array.
- ans: This variable is initialized to 0 and will be used to store the largest perimeter.

Iterating Through the Sorted Array:

- The code iterates through the sorted array starting from the third element
 (i = 2).
- In each iteration, it checks if the sum of the two smallest elements
 (prefSum) is greater than the current element (nums[i]).
- If the condition is true, it means a valid triangle is possible, and the code updates the ans with the maximum perimeter.

Updating the Sum:

The prefsum is updated by adding the current element (prefsum += nums[i]).

Returning the Result:

- If no valid triangle is found (i.e., ans remains 0), the function returns -1.
- Otherwise, it returns the largest perimeter stored in the ans variable.

The time complexity of this solution is $O(n \log n)$ due to the sorting operation. The loop has a time complexity of O(n), resulting in an overall time complexity of $O(n \log n)$. The use of 11 (long long) suggests that the code accounts for potential large values, ensuring correct results for edge cases.

Solution-3

```
class Solution {
  typedef long long II; // Define a type alias for long long
public:
  long long largestPerimeter(vector<int>& nums) {
    Il sum = 0; // Initialize a variable to store the sum of all elements
    // Calculate the sum of all elements in the input vector
    for(auto & it: nums) {
      sum += it;
    }
    priority_queue<|l> pq; // Initialize a max heap (priority queue) to efficiently get the
largest elements
    // Push all elements into the priority queue
```

```
for(auto & it: nums) {
  pq.push(it);
}
// Loop until the priority queue is empty
while(!pq.empty()) {
  II val = pq.top(); // Get the largest element from the priority queue
  sum -= val; // Remove the largest element from the sum
  // Check if the sum of two smaller sides is greater than the largest side
  if(sum > val) {
    return sum + val; // If true, return the largest perimeter
  } else {
    pq.pop(); // If not true, try another value by removing the largest element
  }
}
```

```
return -1; // If no valid triangle is possible, return -1
}
};
```

Calculating the Sum: The code calculates the sum of all elements in the input array nums.

Initializing the Priority Queue (Max Heap): It initializes a priority queue (pq) as a max heap, which ensures that the largest elements are at the top.

Pushing Elements into the Priority Queue: All elements from the input array are pushed into the priority queue.

Main Loop:

- The code then enters a loop that continues until the priority queue is empty.
- In each iteration, it gets the largest element from the priority queue (val)
 and removes it from the sum.
- It checks if the sum of the two remaining smaller sides is greater than the largest side.
- If the condition is true, it means a valid triangle is possible, and the function returns the largest perimeter.
- If not true, it tries another value by removing the largest element from the priority queue.

Returning -1 if No Valid Triangle: If no valid triangle is found after the loop, the function returns -1.

The use of 11 (long long) suggests that the code accounts for potential large values, ensuring correct results for edge cases. The priority queue efficiently handles the process of selecting the largest elements from the array. The overall time complexity of this solution is O(n log n), where n is the size of the input array.

2973. Find Number of Coins to Place in Tree Nodes

Hard ♠ Companies ♦ Hint

You are given an undirected tree with n nodes labeled from 0 to n - 1, and rooted at node 0. You are given a 2D integer array edges of length n - 1, where edges[i] = [a_1, b_1] indicates that there is an edge between nodes a_i and b_i in the tree.

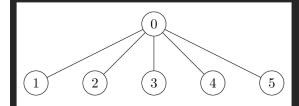
You are also given a **0-indexed** integer array cost of length n, where cost[i] is the cost assigned to the ith node.

You need to place some coins on every node of the tree. The number of coins to be placed at node ii can be calculated as:

- If size of the subtree of node i is less than 3, place 1 coin.
- Otherwise, place an amount of coins equal to the maximum product of cost values assigned to 3 distinct nodes in the subtree of node 3. If this product is negative, place 6 coins.

Return an array coin of size n such that coin[i] is the number of coins placed at node i.

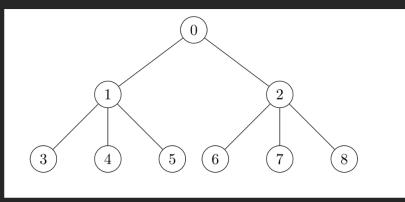
Example 1:



Input: edges = [[0,1],[0,2],[0,3],[0,4],[0,5]], cost = [1,2,3,4,5,6]
Output: [120,1,1,1,1,1]

Explanation: For node 0 place 6 * 5 * 4 = 120 coins. All other nodes are leaves with subtree of size 1, place 1 coin on each of them.

Example 2:



Input: edges = [[0,1],[0,2],[1,3],[1,4],[1,5],[2,6],[2,7],[2,8]], cost = [1,4,2,3,5,7,8,-4,2]Output: [280,140,32,1,1,1,1,1,1]Explanation: The coins placed on each node are:

- Place 8 * 7 * 5 = 280 coins on node 0. Place 7 * 5 * 4 = 140 coins on node 1. Place 8 * 2 * 2 = 32 coins on node 2.

0 <= a_i, b_i < n
 cost.length == n
 1 <= |cost[i]| <= 10⁴
 The input is generated such that edges represents a valid tree.

Solution-1-

class Solution {

public:

vector<long long> ans;

vector<long long> dfs(vector<vector<int>>& t, vector<int>& cost, int root, int par){

```
vector<long long> usefulCost = {cost[root]}; // Initialize the vector with the cost of
the current node
```

```
// Traverse through the children of the current node
    for(auto n: t[root]){
      if(n == par) continue; // Skip the parent node
      vector<long long> v = dfs(t, cost, n, root); // Recursively go deep into the leaf
nodes first
      for(auto e: v) usefulCost.push_back(e); // Accumulate all the costs from all its
child nodes at the root level
    }
    // After traversing all subtrees, sort the accumulated cost
    sort(usefulCost.begin(), usefulCost.end(), greater<long long>());
    long long sz = usefulCost.size();
    if(usefulCost.size() < 3) {</pre>
```

```
ans[root] = 1;
       return usefulCost;
    } // Check if the size of the subtree is less than 3, then set the cost to 1 and return
from here.
    if(usefulCost[1] * usefulCost[2] > usefulCost[sz - 1] * usefulCost[sz -2]) {
       ans[root] = usefulCost[0] * usefulCost[1] * usefulCost[2];
    }
    else {
       ans[root] = usefulCost[0] * usefulCost[sz - 1] * usefulCost[sz - 2];
    }
    if(ans[root] < 0) ans[root] = 0; // If the product is negative, set cost to 0
    // If the size of the subtree is less than or equal to 5, return the useful costs
    if(usefulCost.size() <= 5) return usefulCost;</pre>
```

```
// Return the largest 3 and smallest two items, only those can be useful in later
steps and discard others
    return {usefulCost[0], usefulCost[1], usefulCost[2], usefulCost[sz-2],
usefulCost[sz-1]};
  }
  vector<long long> placedCoins(vector<vector<int>>& edges, vector<int>& cost) {
    ans.resize(cost.size(), 0);
    vector<vector<int>> t(cost.size());
    // Build the tree from the given edges
    for(auto e : edges){
      t[e[0]].push_back(e[1]);
      t[e[1]].push_back(e[0]);
    }
    // Perform DFS to calculate the number of coins for each node
```

```
dfs(t, cost, 0, -1);

return ans; // Return the vector containing the number of coins for each node
}
```

Depth-First Search (DFS):

- The dfs function performs a depth-first search on the tree.
- It recursively traverses through the children of the current node and accumulates the costs from its child nodes.
- After traversing all subtrees, it sorts the accumulated costs in descending order.

Calculating Coins:

- If the size of the subtree is less than 3, the cost for the current node is set to 1.
- Otherwise, the cost is calculated as the maximum product of the cost values assigned to three distinct nodes in the subtree.
- If the product is negative, the cost is set to 0.

Returning Useful Costs:

 The function returns the largest 3 and smallest two items, as only those can be useful in later steps, and discards the others.

Building the Tree:

• The placedCoins function builds the tree from the given edges.

Overall Process:

 The DFS is performed to calculate the number of coins for each node, and the result is stored in the ans vector.

Returning the Result:

 The ans vector containing the number of coins for each node is returned as the final result.

The code ensures that the cost is calculated according to the specified conditions, and the time complexity is determined by the DFS traversal of the tree.

```
Solution2-
typedef long long int II;

const II NO_VALUE = 1e9;

class Solution {
  int n;
  vector<vector<int>> g;
  vector<int> cost;
```

```
vector<vector<ll>> val;
vector<II> coins;
void CalculateCoins (int src, int par) {
  vector<II> child_val = {cost[src]};
  // Traverse through the children of the current node
  for (auto i : g[src]) {
    if (i == par) continue;
    CalculateCoins (i, src);
    for (auto i : val[i]) child_val.push_back(i);
  }
  sort (child_val.begin(), child_val.end());
```

```
if (child_val.size() < 3) {</pre>
       coins[src] = 1;
       val[src] = child_val;
    }
    else {
       int n = child_val.size();
       II max_product = -1e18;
       max_product = max (max_product, child_val[0]*child_val[1]*child_val[n-1]);
       max_product = max (max_product, child_val[n-1]*child_val[n-2]*child_val[n-3]);
       coins[src] = max_product < 0? 0 : max_product;</pre>
       // If the size of the subtree is less than 6, return all values; otherwise, return the
largest 3 and smallest two items
       if (child_val.size() < 6) val[src] = child_val;</pre>
       else val[src] = {child_val[0], child_val[1], child_val[n-3], child_val[n-2],
child_val[n-1]};
```

```
}
  }
public:
  vector<long long> placedCoins(vector<vector<int>>& edges, vector<int>& _cost) {
    n = _cost.size();
    g.clear(), val.clear(), cost.clear(), coins.clear();
    val.resize(n), g.resize(n), cost.resize(n), coins.resize(n);
    cost = _cost;
    for (auto e: edges) {
      g[e[0]].push_back(e[1]);
      g[e[1]].push_back(e[0]);
    }
```

```
CalculateCoins(0, -1);

return coins; // Return the vector containing the number of coins for each node
}
```

CalculateCoins Function:

- The CalculateCoins function is a recursive function that calculates the number of coins for each node based on the given conditions.
- It traverses through the children of the current node, accumulates the costs from its child nodes, and sorts them.
- If the size of the subtree is less than 3, the cost for the current node is set to 1.
- Otherwise, the cost is calculated as the maximum product of the cost values assigned to three distinct nodes in the subtree.
- If the product is negative, the cost is set to 0.
- If the size of the subtree is less than 6, it returns all values; otherwise, it returns the largest 3 and smallest two items.

placedCoins Function:

• The placedCoins function initializes the necessary vectors and calls the calculateCoins function to calculate the number of coins for each node.

Overall Process:

 The code ensures that the cost is calculated according to the specified conditions, and the time complexity is determined by the recursive traversal of the tree.

Returning the Result:

• The coins vector containing the number of coins for each node is returned as the final result.