

# Lab 3

## ECE 380 W21

### Group 8

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## Declaration of Authorship

We acknowledge and promise that:

- a) We are the sole authors of this lab report and associated simulation files/code.
- b) This work represents our original work.
- c) We have not shared detailed analysis or detailed design results, computer code, or Simulink diagrams with any other student.
- d) We have not obtained or looked at lab reports from any other current or former student of ECE/SE 380, and we have not let any other student access any part of our lab work.
- e) We have completely and unambiguously acknowledged and referenced all persons and aids used to help us with our work.

Student1 Name and Signature:

**Arjun Bawa**

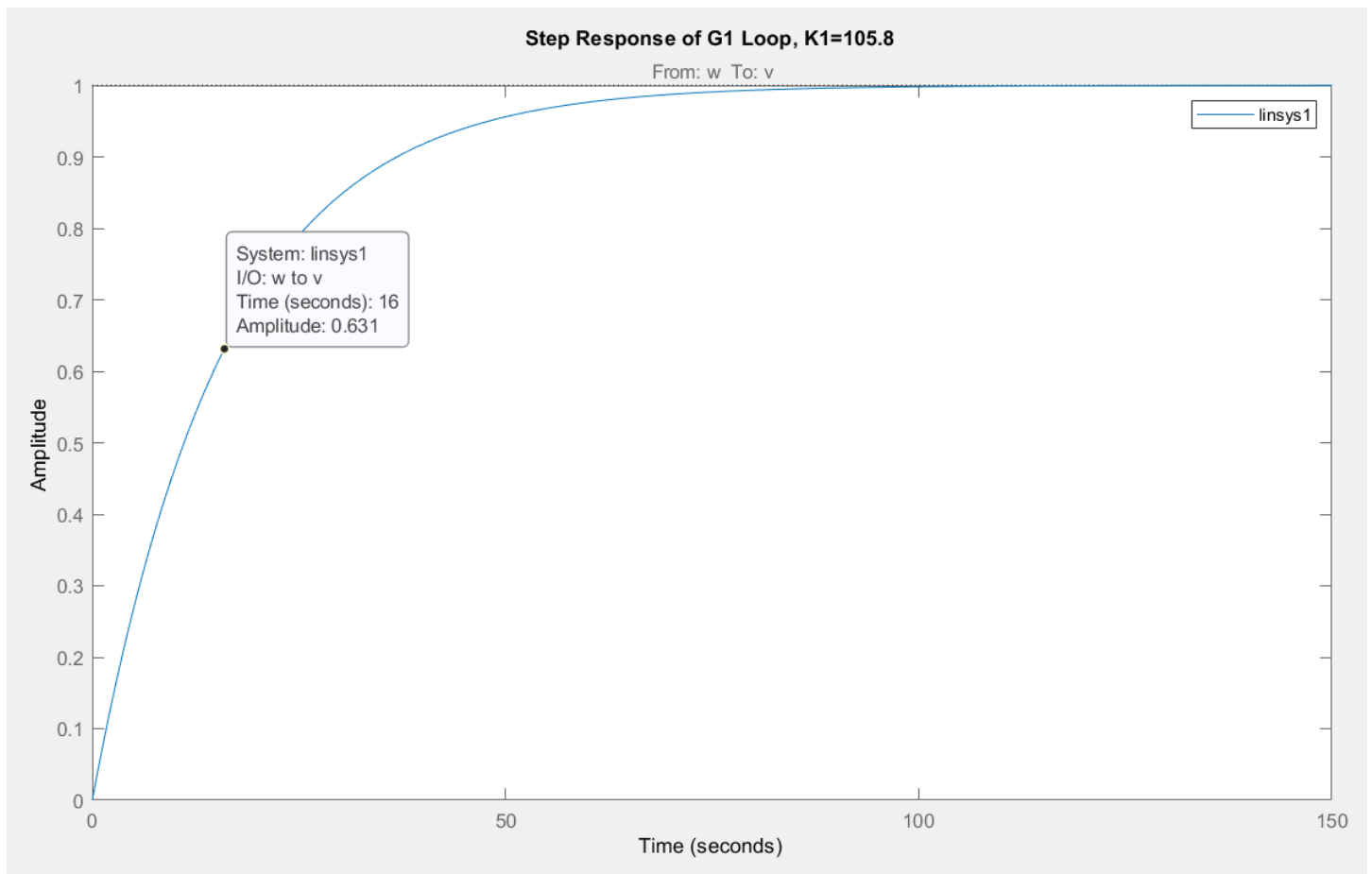
Handwritten signature of Arjun Bawa in black ink.

Student2 Name and Signature:

**Andrew Tran**

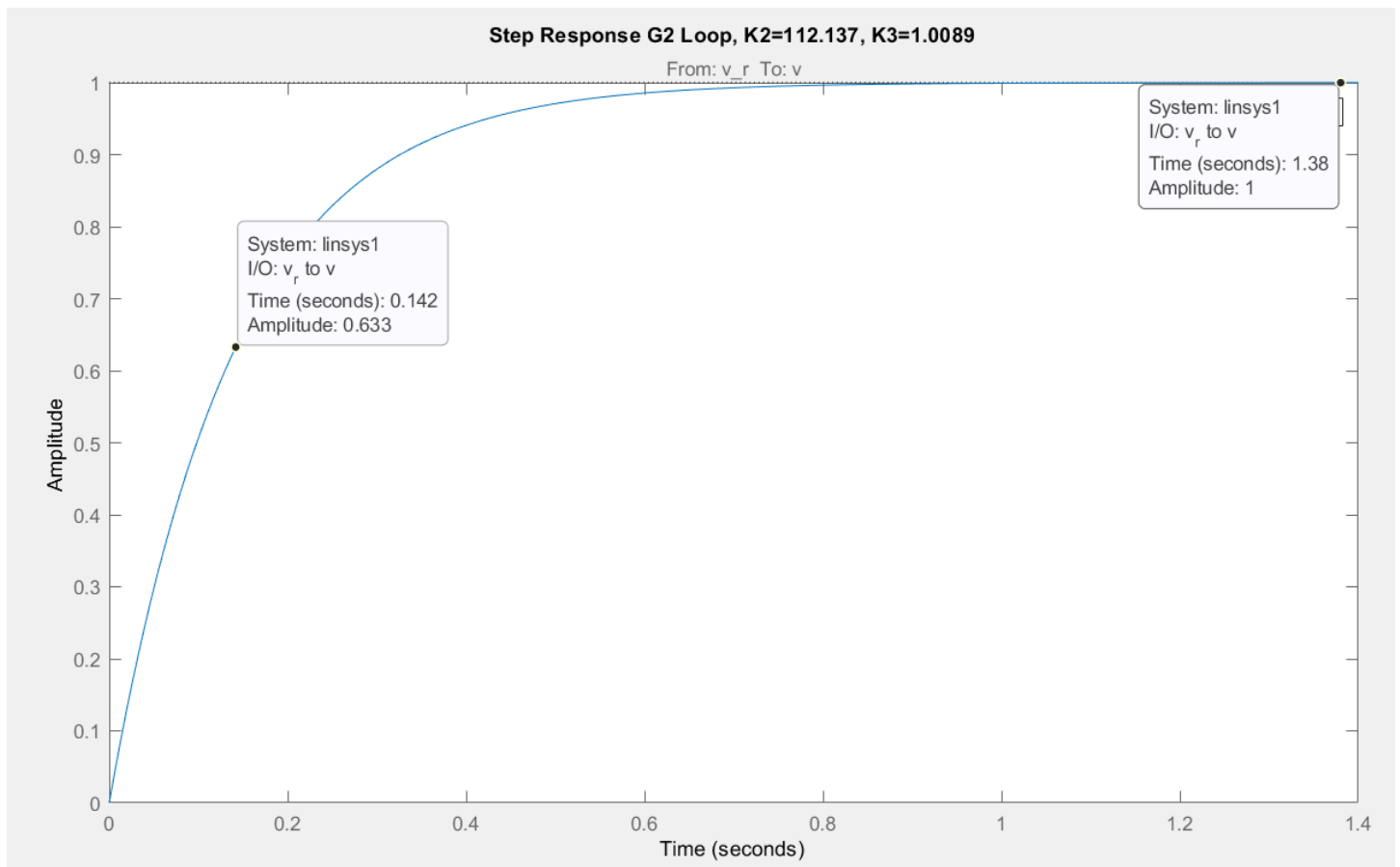
Handwritten signature of Andrew Tran in black ink.

### 3.1 to 3.3

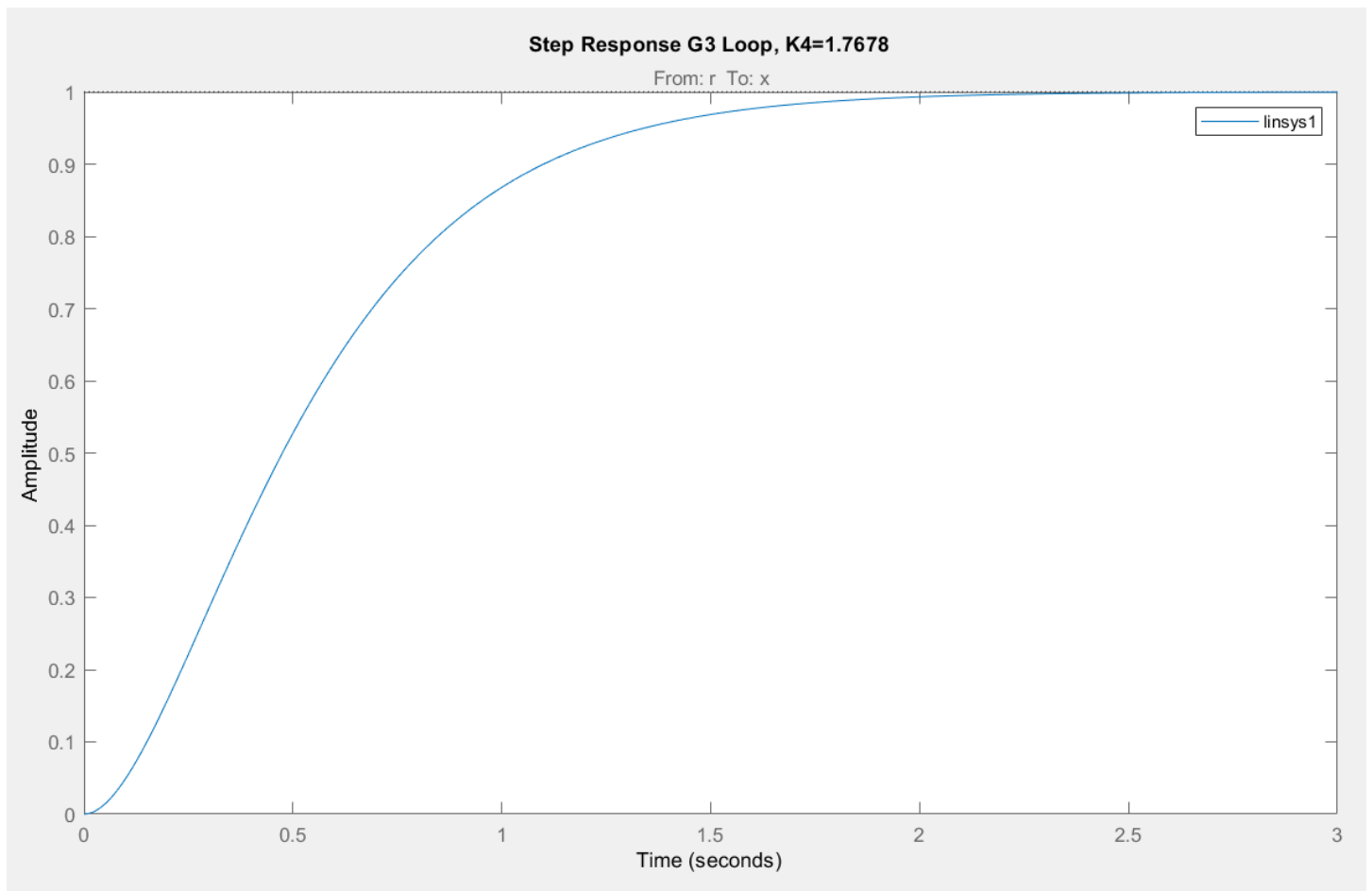


Time constant = 16s

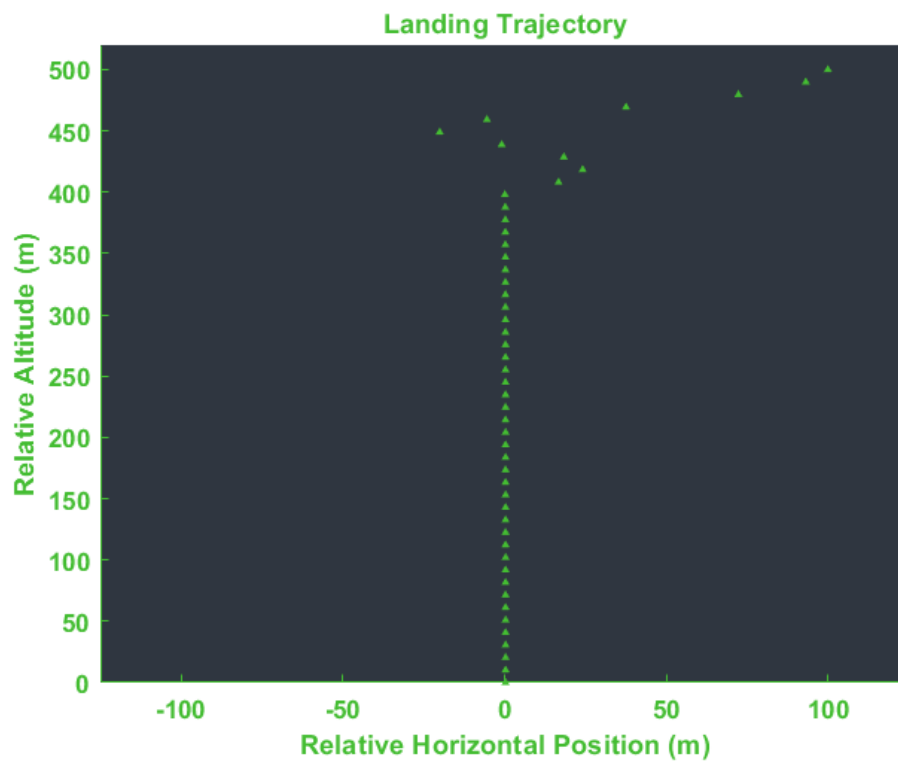
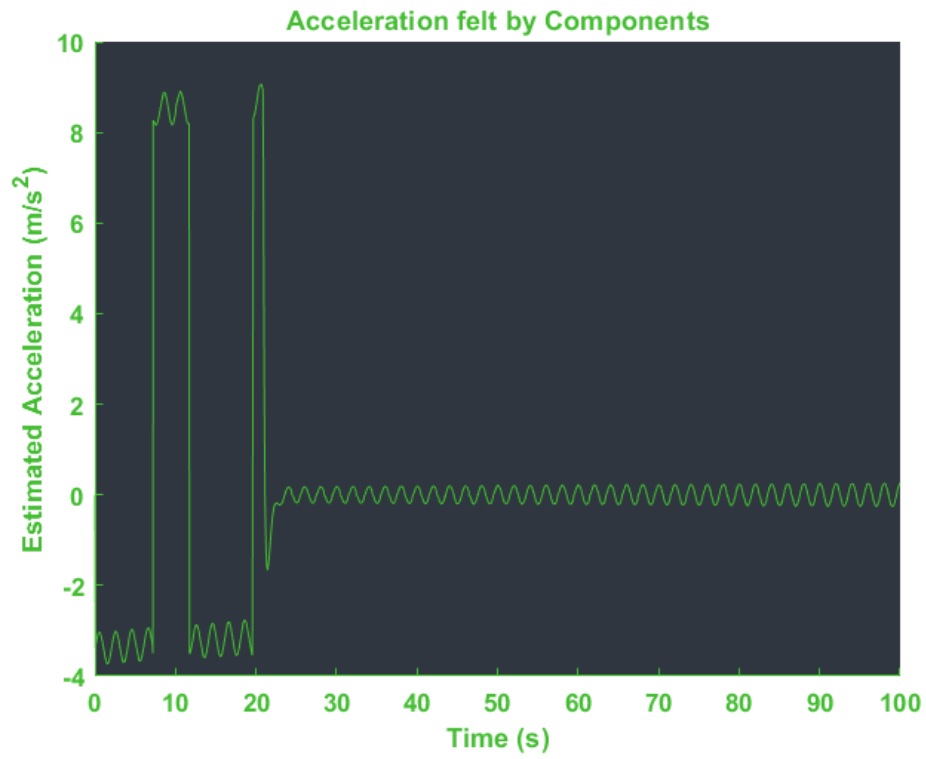
### 3.4



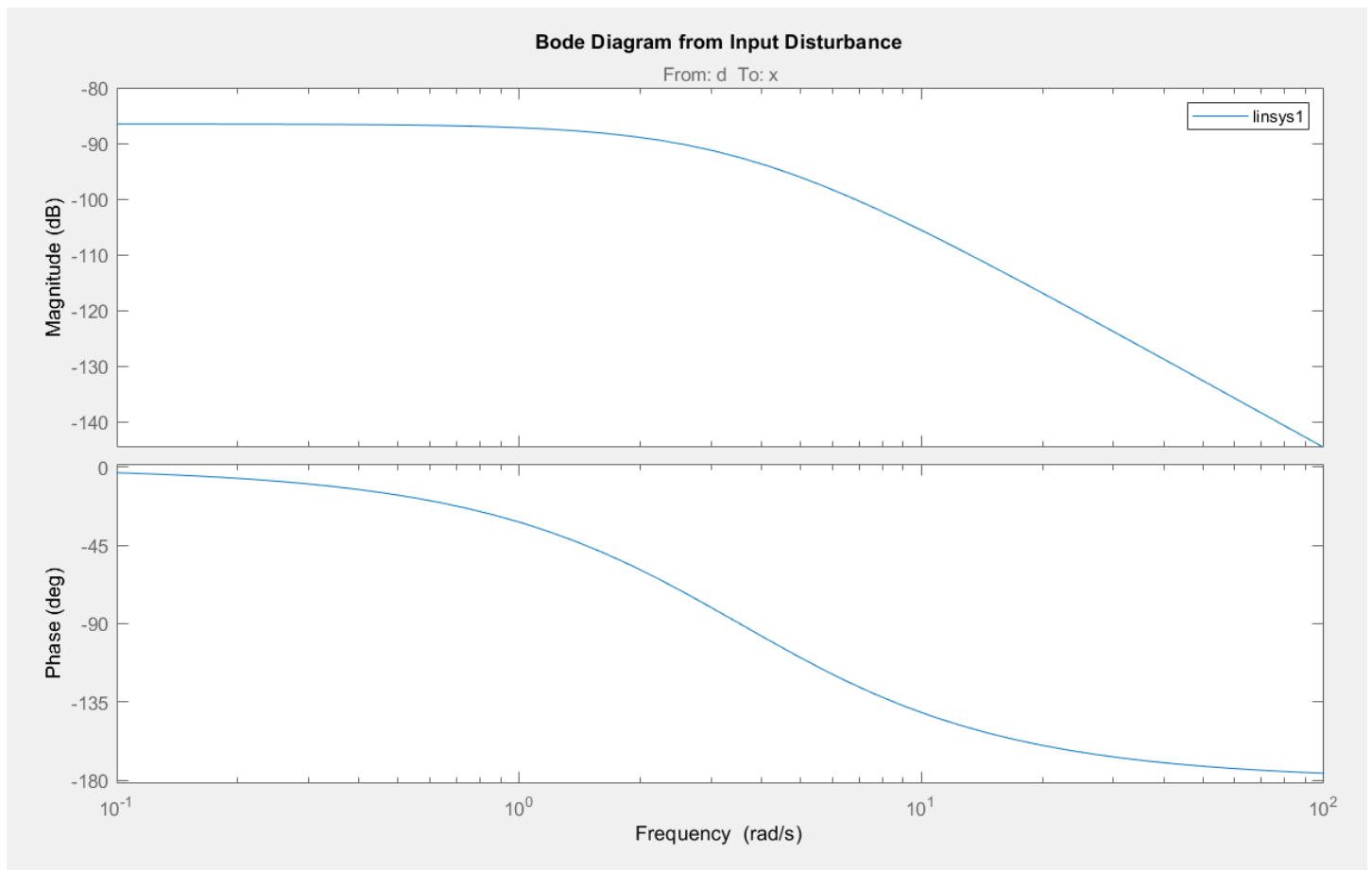
### 3.5



3.6



## 3.7





1) Derive transfer func. from  $r(t)$  to  $x(t)$

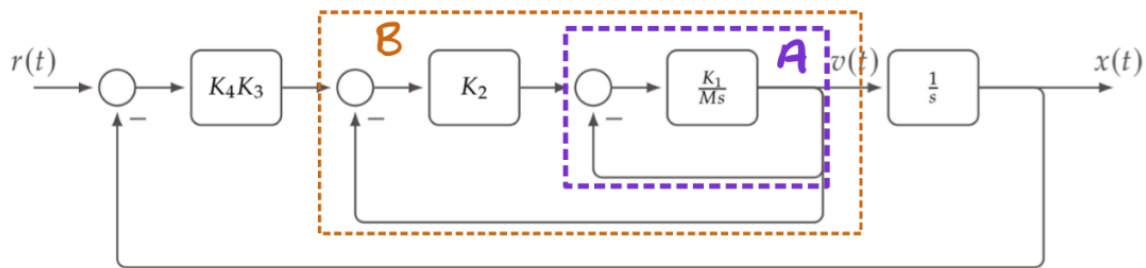


Figure 3.1: Entire closed-loop architecture for Lab 3.

$$A = \frac{k_1}{k_1 + Ms}$$

$$B = \frac{k_2 A}{1 + k_2 A} = \frac{k_1 k_2}{k_1 + Ms + k_2 k_1}$$

$$\Rightarrow \frac{X(s)}{R(s)} = \frac{\frac{1}{s} k_4 k_3 B}{1 + \frac{1}{s} k_4 k_3 B}$$

$$= \frac{\frac{1}{s} k_4 k_3 \frac{k_1 k_2}{k_1 + Ms + k_2 k_1}}{1 + \frac{1}{s} k_4 k_3 \frac{k_1 k_2}{k_1 + Ms + k_2 k_1}}$$

$$= \frac{k_1 k_2 k_3 k_4}{(k_1 + k_1 k_2 + Ms)s + k_1 k_2 k_3 k_4}$$

$$= \frac{k_1 k_2 k_3 k_4}{Ms^2 + (k_1 + k_1 k_2)s + k_1 k_2 k_3 k_4}$$

$$= \frac{1}{M} \cdot \frac{k_1 k_2 k_3 k_4}{s^2 + \left(\frac{k_1 + k_1 k_2}{M}\right)s + \frac{k_1 k_2 k_3 k_4}{M}}$$

2) Write T.F. in standard 2<sup>nd</sup> order form. Find DC Gain  $\hat{K}$ ,  $\omega_n$  and  $\zeta$

$$\frac{X(s)}{R(s)} = \frac{\frac{1}{M} K_1 K_2 K_3 K_4}{s^2 + \left(\frac{K_1 + K_1 K_2}{M}\right)s + \frac{K_1 K_2 K_3 K_4}{M}}$$

$$\text{let } H(s) = \frac{X(s)}{R(s)} \Rightarrow \hat{K} = |H(0)| = 1$$

$$\omega_n^2 = \frac{K_1 K_2 K_3 K_4}{M} \Rightarrow \omega_n = \sqrt{\frac{K_1 K_2 K_3 K_4}{M}}$$

$$\begin{aligned} \zeta &= \frac{K_1 + K_1 K_2}{2M\omega_n} = \frac{\sqrt{M}(K_1 + K_1 K_2)}{2M\sqrt{K_1 K_2 K_3 K_4}} \\ &= \frac{K_1 + K_1 K_2}{2\sqrt{MK_1 K_2 K_3 K_4}} \end{aligned}$$

3) Identify the two gains that affect  $T_{2\%}$

$$\begin{aligned} T_{2\%} &\approx \frac{4}{\zeta \omega_n} = \frac{4}{\frac{K_1 + K_1 K_2}{2\sqrt{MK_1 K_2 K_3 K_4}} \cdot \sqrt{\frac{K_1 K_2 K_3 K_4}{M}}} \\ &= \frac{4 \cdot 2 \cdot \sqrt{M} \sqrt{MK_4 K_3 K_2 K_1}}{(K_1 + K_1 K_2) \sqrt{K_4 K_3 K_2 K_1}} = \frac{8M}{K_1 + K_1 K_2} \end{aligned}$$

$\Rightarrow K_1$  and  $K_2$  affect  $T_{2\%}$

4) Determine a gain that can be changed to reduce %OS w/out affecting  $T_2$ .

$$\ln(O.S.) = \frac{-\zeta\pi}{\sqrt{1-\zeta^2}} \Rightarrow \ln\left(\frac{1}{O.S.}\right) = \frac{\zeta\pi}{\sqrt{1-\zeta^2}}$$

$$\Rightarrow \ln\left(\frac{1}{O.S.}\right) = \frac{\frac{(k_1+k_1k_2)\pi}{2\sqrt{Mk_1k_2k_3k_4}}}{\sqrt{1 - \frac{(k_1+k_1k_2)^2}{4Mk_1k_2k_3k_4}}}$$

$$= \frac{(k_1+k_1k_2)\pi}{(4Mk_1k_2k_3k_4 - (k_1+k_1k_2)^2)^{1/2}}$$

$$\Rightarrow O.S. = \exp\left[\frac{-(k_1+k_1k_2)\pi}{(4Mk_1k_2k_3k_4 - (k_1+k_1k_2)^2)^{1/2}}\right]$$

$$a := k_1+k_1k_2 \quad b := 4Mk_1k_2$$

$$\Rightarrow O.S. = \exp\left(\frac{-a\pi}{\sqrt{bk_3k_4 - a^2}}\right)$$

$\propto$  := proportional,  $\propto^{-1}$  := inversely proportional

$$\Rightarrow O.S. \propto^{-1} \frac{a\pi}{\sqrt{bk_3k_4 - a^2}} \propto^{-1} bk_3k_4 - a^2$$

$$\Rightarrow k_3k_4 \gg \frac{(k_1+k_1k_2)^2}{4Mk_1k_2} : O.S. \rightarrow 1$$

Increasing the product of  $k_3$  and  $k_4$  increases

O.S.  $\Rightarrow$  decreasing  $k_3k_4$  decreases O.S.