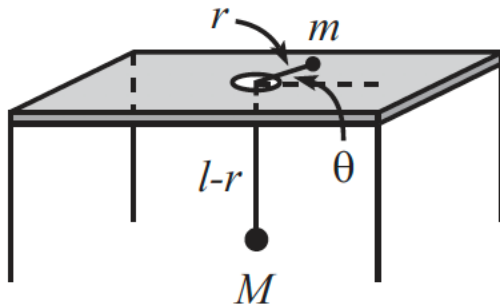


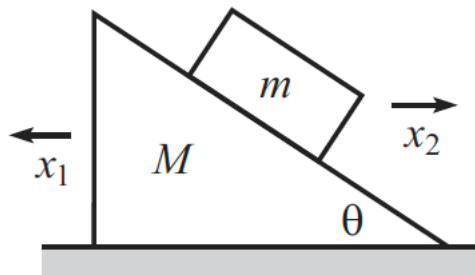
Problem I



A mass m is free to slide on a frictionless table and is connected by a string, which passes through a hole in the table, to a mass M which hangs below M . Assume that M moves in a vertical line only, and assume that the string always remains taut.

- 1) Find the equations of motion for the variables r and θ shown in the figure, meaning θ is used instead of x , in producing Euler Lagrange equation $\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{x}} \right) = \frac{\partial L}{\partial x}$ or r is used instead of x .
- 2) Discuss the behavior of the θ (or rotation of m) using the E-L equation of θ .
- 3) Discuss the behavior of the string, using the E-L equation of r .
- 4) Under what condition, the m has circular motion ($\dot{r}, \ddot{r} = 0$)?

Problem II



A block of mass m is held motionless on a frictionless plane of mass M and angle of inclination θ . The plane rests on a frictionless horizontal surface. The block is released. What is the horizontal acceleration of the plane? Use Lagrangian, and E-L, not newton approach.