

$$\begin{aligned}
f(x) &= 0 \\
0 &= 2 \cdot ((\ln x)^2 - 1) \\
1 &= (\ln x)^2 \\
\pm 1 &= \ln x \\
e^{\pm 1} &= e^{\ln x} \\
x_1 &= e^1 = e \\
x_2 &= e^{-1}
\end{aligned}$$

$$\begin{aligned}
f'(x) &= \frac{4}{x} \cdot \ln x \\
f'(x) &= 0 \\
\ln x = 1 &\rightarrow x = e \\
f'(0,5) &\approx 8 \cdot -0,69 < 0 \\
f'(4) &\approx 1 \cdot \ln(4) > 0 \\
f(1) &= 2 \cdot (0^2 - 1) = -2 \Rightarrow T(1| -2)
\end{aligned}$$

$$\begin{aligned}
\text{b) } f'(x) &= 4x^{-1} \cdot \ln x = -4x^{-2} \cdot \ln x + \frac{4}{x} \cdot \frac{1}{x} = -\frac{4}{x^2} \ln x + \frac{4}{x^2} = \frac{4}{x^2} \cdot (-\ln x + 1) \\
0 &= f''(x) \\
0 &= \frac{4}{x^2} \cdot (-\ln x + 1) \\
0 &= -\ln x + 1 \\
1 &= \ln x \rightarrow x = e \\
f''(1) &= 4 \cdot 1 > 0 \quad f''(4) = \frac{1}{4} \cdot (-\ln(4) + 1) < 0 \\
f(e) &= 2 \cdot ((\ln e)^2 - 1) = 2 \cdot (1^2 - 1) = 0 \rightarrow W(e|0) \\
f'(e) &= \frac{4}{e} \\
0 &= \frac{4}{e} \cdot e + t \quad | -4 \\
t = -4 &\Rightarrow t(x) = \frac{4}{e} \cdot x - 4
\end{aligned}$$