## Homework 9:

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- 1. For  $X(t) = W^3(t) 3tW(t)$ , find dX(t)
- 2. Simplify  $\int_0^t W^3(u)dW(u)$
- 3. For dY(t) = 3Y(t)dt + 2dW(t), determine  $d(e^{-3t}Y(t))$ .
- 4. If X(t) = 3tW(t) and  $Y(t) = 2 + \int_0^t 6u^2 dW(u)$ , then determine dX(t)dY(t).
- 5. If  $Z(t) = \int_0^t 3uW(u)dW(u) + \int_0^t 6W(u)du$  and  $X(t) = e^{Z^2(t)}$ , find dX(t).
- 6. Let  $Y(t) = 6 + \int_0^t W(u)dW(u) + \int_0^t e^{3u}du$ , find  $\mathbb{E}[Y(t)]$ .
- 7. Simplify  $\int_0^p t^2 W(t) dW(t)$