QF301. Homework #4.

2022-11-08

I pledge on my honor that I have not given or received any unauthorized assistance on this assignment/examination. I further pledge that I have not copied any material from a book, article, the Internet or any other source except where I have expressly cited the source.

By filling out the following fields, you are signing this pledge. No assignment will get credit without being pledged.

Name: Arjun Koshal CWID: 10459064 Date: 11/05/2022

Instructions

In this assignment, you should use R markdown to answer the questions below. Simply type your R code into embedded chunks as shown above. When you have completed the assignment, knit the document into a PDF file, and upload both the .pdf and .Rmd files to Canvas.

```
CWID = 10459064 #Place here your Campus wide ID number, this will personalize #your results, but still maintain the reproducible nature of using seeds.
#If you ever need to reset the seed in this assignment, use this as your seed #Papers that use -1 as this CWID variable will earn 0's so make sure you change #this value before you submit your work.

personal = CWID %% 10000

set.seed(personal) #You can reset the seed at any time in your code,
#but please always set it to this seed.
```

Question 1 (40pt)

Question 1.1

Use the quantmod package to obtain the daily adjusted close prices 2 different stocks. You should have at least two years of data for both assets. You should inspect the dates for your data to make sure you are including everything appropriately. Create a data frame of the daily log returns both both stocks along with the lagged returns (2 lags). Also include the direction (positive or negative) for both stocks in the current time point (not lagged). You may wish to remove the date from your data frame for later analysis. Print the first 6 lines of your data frame. (You may use the same two stocks as in Homework 2 or 3.)

```
library(quantmod)
getSymbols(c("AMZN","TSLA"),from="2018-01-01",to="2021-12-31")
```

```
## [1] "AMZN" "TSLA"
```

```
rAMZN = dailyReturn(AMZN$AMZN.Adjusted,type="log")
rTSLA = dailyReturn(TSLA$TSLA.Adjusted,type="log")
rAMZN1 = as.numeric(lag(rAMZN, k=1))[-(1:2)]
rAMZN2 = as.numeric(lag(rAMZN, k=2))[-(1:2)]
rAMZN = as.numeric(rAMZN)[-(1:2)]
rAMZN.dir = (rAMZN > 0) + 0
rTSLA1 = as.numeric(lag(rTSLA,k=1))[-(1:2)]
rTSLA2 = as.numeric(lag(rTSLA,k=2))[-(1:2)]
rTSLA = as.numeric(rTSLA)[-(1:2)]
rTSLA.dir = (rTSLA > 0) + 0
df = data.frame(rAMZN,rAMZN.dir,rTSLA,rTSLA.dir,rAMZN1,rTSLA1,rAMZN2,rTSLA2)
head(df)
```

```
##
         rAMZN rAMZN.dir
                             rTSLA rTSLA.dir
                                               rAMZN1
                                                           rTSLA1
## 2 0.016033295
                    1 0.006210381
                                         1 0.004466030 -0.008324529
                                         1 0.016033295  0.006210381
                     1 0.060754725
## 3 0.014321625
## 4 0.004664811
                     1 -0.008118266
                                         0 0.014321625  0.060754725
## 5 0.001300360
                     1 0.003320920
                                         1 0.004664811 -0.008118266
## 6 0.017661409
                     1 0.009364661
                                         1 0.001300360 0.003320920
                   rTSLA2
        rAMZN2
## 1 0.00000000 0.000000000
## 2 0.012694401 -0.010285832
## 3 0.004466030 -0.008324529
## 4 0.016033295 0.006210381
## 5 0.014321625 0.060754725
## 6 0.004664811 -0.008118266
```

Question 1.2

Split your data into training and testing sets (80% training and 20% test).

Run a logistic regression for the direction of one of your stock returns as a function of the lagged returns (2 lags) for both stocks. This should be of the form $\log(p_{1,t}/(1-p_{1,t})) = \beta_0 + \beta_{1,1}r_{1,t-1} + \beta_{1,2}r_{1,t-2} + \beta_{1,2}r_{1,t-2}$ $\beta_{2,1}r_{2,t-1} + \beta_{2,2}r_{2,t-2}$. Evaluate the performance of this model with the test accuracy and confusion matrix.

Solution:

##

##

```
train = sample(length(rAMZN), 0.8*length(rAMZN), replace=FALSE)
logistic.reg = glm(rAMZN.dir ~ rAMZN1 + rAMZN2 + rTSLA1 + rTSLA2 , data=df , subset=train , family=binom
summary(logistic.reg)
##
## Call:
## glm(formula = rAMZN.dir ~ rAMZN1 + rAMZN2 + rTSLA1 + rTSLA2,
       family = binomial, data = df, subset = train)
```

```
## Deviance Residuals:
##
       Min
                 10
                     Median
                                   30
                                           Max
## -1.4770 -1.2197
                      0.9927
                               1.1263
                                        1.4184
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
                                     1.806
## (Intercept) 0.12883
                           0.07135
                                             0.0710 .
## rAMZN1
               -2.00711
                           3.95915 -0.507
                                             0.6122
## rAMZN2
               -1.53355
                           3.93218
                                    -0.390
                                             0.6965
## rTSLA1
               -3.35167
                           1.87451
                                    -1.788
                                             0.0738 .
## rTSLA2
                2.20770
                           1.92141
                                     1.149
                                             0.2506
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 1111.7 on 803 degrees of freedom
## Residual deviance: 1105.2 on 799
                                      degrees of freedom
## AIC: 1115.2
##
## Number of Fisher Scoring iterations: 4
logistic.prob=predict(logistic.reg,df[-train,])
logistic.pred=rep(0,length(logistic.prob))
logistic.pred[logistic.prob>.5] = 1
mean(logistic.pred==df$rAMZN.dir[-train])
## [1] 0.3930348
table(predict=logistic.pred , truth=df$rAMZN.dir[-train])
##
          truth
## predict
             0
                1
##
         0
           77 121
         1
```

Question 1.3

Consider the same classification problem as in Question 1.2 but with a Naive Bayes classifier. Use the same train/test split as in Question 1.2. Evaluate the performance of this model with the test accuracy and confusion matrix.

```
library("e1071")
df.x = data.frame(rAMZN1,rTSLA1,rAMZN2,rTSLA2)

nb = naiveBayes(df.x[train,] , df$rAMZN.dir[train])
```

```
nb.prob = predict(nb , newdata=df.x[-train,] , type="raw")
head(nb.prob)
##
                0
                          1
## [1,] 0.4850410 0.5149590
## [2,] 0.4721470 0.5278530
## [3,] 0.4529759 0.5470241
## [4,] 0.5132381 0.4867619
## [5,] 0.5087249 0.4912751
## [6,] 0.3775865 0.6224135
nb.pred = (nb.prob[,1] < nb.prob[,2])+0
mean(nb.pred==df$rAMZN.dir[-train])
## [1] 0.5572139
table(predict=nb.pred , truth=df$rAMZN.dir[-train])
##
          truth
## predict 0 1
##
         0 20 31
##
         1 58 92
nb.prob.train = predict(nb , newdata=df.x[train,] , type="raw")
nb.pred.train = (nb.prob.train[,1] < nb.prob.train[,2]) + 0</pre>
mean(nb.pred.train==df$rAMZN.dir[train])
```

Question 1.4

Consider the same classification problem as in Question 1.2 but with a Random Forest classifier with 300 trees and 2 predictors in each tree. Use the same train/test split as in Question 1.2. Evaluate the performance of this model with the test accuracy and confusion matrix.

```
library(randomForest)

rAMZN.factor = as.factor(rAMZN.dir)

df.tree = data.frame(rAMZN.dir=rAMZN.factor , rAMZN1,rTSLA1,rAMZN2,rTSLA2)

rf.class = randomForest(rAMZN.dir ~ .,data=df.tree,subset=train,mtry=2,ntree=300,importance=TRUE)

rf.class
```

```
##
## Call:
##
   randomForest(formula = rAMZN.dir ~ ., data = df.tree, mtry = 2,
                                                                        ntree = 300, importance = TRUE
##
                  Type of random forest: classification
##
                        Number of trees: 300
## No. of variables tried at each split: 2
##
##
           OOB estimate of error rate: 53.73%
## Confusion matrix:
##
       0
           1 class.error
## 0 138 240
               0.6349206
## 1 192 234
               0.4507042
rf.pred = predict(rf.class,newdata=df.tree[-train,])
mean(rf.pred==df.tree$rAMZN.dir[-train])
## [1] 0.5422886
table(predict=rf.pred,truth=df.tree$rAMZN.dir[-train])
##
          truth
## predict
           0 1
         0 33 47
         1 45 76
##
rf.pred.train = predict(rf.class,newdata=df.tree[train,])
mean(rf.pred.train==df$rAMZN.dir[train])
## [1] 1
```

Question 1.5

Consider the same classification problem as in Question 1.2 but with a neural network of your own design with at least 1 hidden layer and at least 3 hidden nodes. Use the same train/test split as in Question 1.2. Evaluate the performance of this model with the test accuracy and confusion matrix.

Solution:

See python code

Question 1.6

Consider the same classification problem as in Question 1.2 but with a support vector machine using a radial basis kernel. Use the same train/test split as in Question 1.2. Evaluate the performance of this model with the test accuracy and confusion matrix.

```
rAMZN.factor = as.factor(rAMZN.dir)
df.svm = data.frame(rAMZN.dir=rAMZN.factor , rAMZN1,rTSLA1,rAMZN2,rTSLA2)
tune.out = tune(svm,rAMZN.dir ~ .,data=df.svm[train,],kernel="radial",ranges=list(cost=c(0.001,.01,.1,1
summary(tune.out)
## Parameter tuning of 'svm':
  - sampling method: 10-fold cross validation
##
## - best parameters:
##
     cost gamma
   0.001
           0.5
##
## - best performance: 0.4702623
##
## - Detailed performance results:
                     error dispersion
##
      cost gamma
## 1 1e-03 0.5 0.4702623 0.02415648
## 2 1e-02
            0.5 0.4702623 0.02415648
## 3 1e-01 0.5 0.4702623 0.02415648
## 4 1e+00
             0.5 0.5025000 0.05775885
## 5 5e+00
             0.5 0.5011883 0.05632808
## 6 1e+01
             0.5 0.5161265 0.04777448
## 7 1e+02
             0.5 0.5211265 0.05684626
## 8 1e-03
              1.0 0.4702623 0.02415648
## 9 1e-02
              1.0 0.4702623 0.02415648
## 10 1e-01
             1.0 0.4702623 0.02415648
## 11 1e+00
              1.0 0.5148765 0.03626001
## 12 5e+00
             1.0 0.5137500 0.06297765
## 13 1e+01
             1.0 0.5113426 0.06108912
## 14 1e+02
             1.0 0.4990586 0.07530384
## 15 1e-03
             2.0 0.4702623 0.02415648
## 16 1e-02
              2.0 0.4702623 0.02415648
## 17 1e-01
              2.0 0.4702623 0.02415648
## 18 1e+00
              2.0 0.5073920 0.04992964
## 19 5e+00
              2.0 0.4964198 0.07575265
## 20 1e+01
             2.0 0.4716049 0.08667379
## 21 1e+02
             2.0 0.4889969 0.06696559
## 22 1e-03
             3.0 0.4702623 0.02415648
## 23 1e-02
              3.0 0.4702623 0.02415648
## 24 1e-01
              3.0 0.4702623 0.02415648
## 25 1e+00
              3.0 0.5261574 0.04763754
## 26 5e+00
              3.0 0.4976543 0.06032215
## 27 1e+01
              3.0 0.4926852 0.05527403
## 28 1e+02
             3.0 0.4926235 0.07656664
## 29 1e-03
             4.0 0.4702623 0.02415648
             4.0 0.4702623 0.02415648
## 30 1e-02
## 31 1e-01
              4.0 0.4702623 0.02415648
## 32 1e+00
              4.0 0.5162809 0.04384251
## 33 5e+00
              4.0 0.5075617 0.05016005
## 34 1e+01
              4.0 0.5038889 0.06129917
```

```
## 35 1e+02 4.0 0.4888426 0.06253778
best.svm.class = tune.out$best.model
best.svm.class$cost
## [1] 0.001
best.svm.class$gamma
## [1] 0.5
summary(best.svm.class)
##
## Call:
## best.tune(method = svm, train.x = rAMZN.dir ~ ., data = df.svm[train,
                         ], ranges = list(cost = c(0.001, 0.01, 0.1, 1, 5, 10, 100), gamma = c(0.5, 0.1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.1, 1, 0.
##
                         1, 2, 3, 4)), kernel = "radial")
##
##
## Parameters:
                    SVM-Type: C-classification
## SVM-Kernel: radial
##
                                   cost: 0.001
##
## Number of Support Vectors: 763
##
## ( 378 385 )
##
##
## Number of Classes: 2
##
## Levels:
## 0 1
best.svm.pred=predict(best.svm.class,newdata = df.svm[-train,])
mean((best.svm.pred==df.svm$rAMZN.dir[-train]))
## [1] 0.6119403
table(predict=best.svm.pred,truth=df.svm$rAMZN.dir[-train])
                                   truth
## predict 0
##
                                0
                                          0
                                                           0
```

##

1 78 123

```
best.svm.pred.train = predict(best.svm.class,newdata = df.svm[train,])
mean(best.svm.pred.train==df$rAMZN.dir[train])
```

Question 2 (10pt)

Question 2.1

Of the methods considered in Question 1, which would you recommend in practice? Explain briefly (1 paragraph) why you choose this fit.

Solution:

Though Random forest appears to have performed the best for me in the test data, it has a training accuracy of 100%. This gives strong indications of overfitting and could result in poor performance on other (new) data. Instead, I would recommend the neural network even though SVM has slightly higher test accuracy. This is because the neural network provides more balanced predictions.

Random forest performed the best for me in the test data; however, it has a training accuracy of 100%. This probably means that the data was overfitting and would most likely imply poor performance on other data

Question 3 (40pt)

Question 3.1

Using the same data as in Question 1.1, partition the predicted (current) stock returns into 5 possible "market directions". Add this data to your data frame and print the first 6 lines. Briefly (2-3 sentences) justify the choices of cutoff levels for the partitioning.

Solution:

```
quantile(rAMZN,c(0.2,0.4,0.6,0.8))

## 20% 40% 60% 80%

## -0.011432761 -0.001858162 0.005126694 0.013490184

rAMZN.dir5 = rep("DDown",length(rAMZN.dir))
rAMZN.dir5[rAMZN > -0.01] = "Down"
rAMZN.dir5[rAMZN > -0.0025] = "Flat"
rAMZN.dir5[rAMZN > 0.0025] = "Up"
rAMZN.dir5[rAMZN > 0.001] = "UUp"

sum(rAMZN.dir5 == "DDown")
```

[1] 222

```
sum(rAMZN.dir5 == "Down")
## [1] 165
sum(rAMZN.dir5 == "Flat")
## [1] 144
sum(rAMZN.dir5 == "Up")
## [1] 199
sum(rAMZN.dir5 == "UUp")
## [1] 275
df = data.frame(rAMZN,rAMZN.dir,rAMZN.dir5,rTSLA,rTSLA.dir,rAMZN1,rTSLA1,rAMZN2,rTSLA2)
           rAMZN rAMZN.dir rAMZN.dir5
##
                                             rTSLA rTSLA.dir
                                                                  rAMZN1
## 1 0.004466030
                                   Up -0.008324529
                                                           0 0.012694401
                         1
                                  UUp 0.006210381
## 2 0.016033295
                         1
                                                           1 0.004466030
## 3 0.014321625
                         1
                                  UUp 0.060754725
                                                           1 0.016033295
## 4 0.004664811
                         1
                                   Up -0.008118266
                                                           0 0.014321625
## 5 0.001300360
                                 Flat 0.003320920
                                                           1 0.004664811
## 6 0.017661409
                                  UUp 0.009364661
                                                           1 0.001300360
                         1
##
           rTSLA1
                       rAMZN2
                                    rTSLA2
## 1 -0.010285832 0.000000000 0.000000000
## 2 -0.008324529 0.012694401 -0.010285832
## 3 0.006210381 0.004466030 -0.008324529
## 4 0.060754725 0.016033295 0.006210381
## 5 -0.008118266 0.014321625 0.060754725
```

Question 3.2

6 0.003320920 0.004664811 -0.008118266

Run a logistic regression for the generalized directions produced in Question 1.1 of one of your stock returns as a function of the lagged returns (2 lags) for both stocks.

Use the same train/test split as in Question 1.2. Evaluate the performance of this model with the test accuracy and confusion matrix.

```
library(nnet)
logistic.reg = multinom(rAMZN.dir5 ~ rAMZN1 + rAMZN2 + rTSLA1 + rTSLA2 , data=df , subset = train)
```

```
## # weights: 30 (20 variable)
## initial value 1293.988082
## iter 10 value 1261.231766
## iter 20 value 1258.261915
## iter 30 value 1258.250688
## final value 1258.249923
## converged
summary(logistic.reg)
## Call:
## multinom(formula = rAMZN.dir5 ~ rAMZN1 + rAMZN2 + rTSLA1 + rTSLA2,
       data = df, subset = train)
##
##
## Coefficients:
                                 rAMZN2
##
        (Intercept)
                      rAMZN1
                                             rTSLA1
## Down -0.3112787 -7.862107 -3.508649 -0.07679674 6.380442
## Flat -0.5094570 13.287297 6.909072 -2.84335786 3.960596
        -0.1910080 -2.961411 3.187844 -4.41931938 3.818332
## Up
## UUp
         0.2145021 -4.463688 -5.040209 -3.87628542 5.196774
##
## Std. Errors:
##
        (Intercept)
                     rAMZN1
                              rAMZN2
                                       rTSLA1
                                                 rTSLA2
## Down
        0.1161869 6.479734 6.330763 2.995812 3.079238
         0.1247934 6.689720 6.724008 3.107279 3.218670
## Flat
## Up
         0.1119557 6.277908 6.197927 2.905824 3.013450
         0.1012300\ 5.694587\ 5.579218\ 2.651664\ 2.720293
## UUp
## Residual Deviance: 2516.5
## AIC: 2556.5
logistic.pred = predict(logistic.reg , newdata = df[-train,])
mean(logistic.pred==df$rAMZN.dir5[-train]) # Test accuracy
## [1] 0.2288557
table(predict=logistic.pred , truth=df$rAMZN.dir5[-train]) # Confusion matrix of results
##
         truth
## predict DDown Down Flat Up UUp
    DDown
              7
                   6
##
    Down
                        0 0 0
              0
                   1
##
    Flat
              2
                   0
                        0 1
                   0
##
              1
                        0 2
    Uр
                        25 38 36
    UUр
              29
                   24
logistic.pred.train = predict(logistic.reg , newdata = df[train,])
mean(logistic.pred.train==df$rAMZN.dir5[train])
```

Question 3.3

Consider the same classification problem as in Question 3.2 but with a Naive Bayes classifier. Use the same train/test split as in Question 1.2. Evaluate the performance of this model with the test accuracy and confusion matrix.

```
nb = naiveBayes(df.x[train,] , df$rAMZN.dir5[train])
nb.prob = predict(nb , newdata=df.x[-train,] , type="raw")
head(nb.prob)
##
            DDown
                        Down
                                    Flat
## [1,] 0.1177756 0.23132331 0.229665813 0.28107840 0.1401569
## [2,] 0.1152037 0.23946225 0.200107133 0.30368052 0.1415464
## [3,] 0.1057241 0.28532086 0.160683634 0.29892600 0.1493454
## [4,] 0.1526273 0.17775038 0.309719993 0.19426867 0.1656336
## [5,] 0.1387090 0.22856018 0.233356451 0.25406625 0.1453081
## [6,] 0.4144476 0.01659864 0.002051151 0.01012925 0.5567734
max.prob = pmax(nb.prob[,1],nb.prob[,2],nb.prob[,3],nb.prob[,4],nb.prob[,5])
nb.pred = rep("DDown",length(max.prob))
nb.pred[nb.prob[,1] == max.prob] = "DDown"
nb.pred[nb.prob[,2] == max.prob] = "Down"
nb.pred[nb.prob[,3] == max.prob] = "Flat"
nb.pred[nb.prob[,4] == max.prob] = "Up"
nb.pred[nb.prob[,5] == max.prob] = "UUp"
mean(nb.pred==df$rAMZN.dir5[-train]) #Test accuracy
## [1] 0.2338308
table(pred=nb.pred , true=df$rAMZN.dir5[-train]) #Test confusion matrix
##
          true
## pred
           DDown Down Flat Up UUp
##
    DDown
               4
                    2
                         1 5
                                5
##
    Down
                    1
                         4 3
##
                         2 1 10
    Flat
               4
                    5
                   14
                        15 27
##
    Uр
              13
##
              14
                    9
                         7 14
     qUU
nb.prob.train = predict(nb , newdata=df.x[train,] , type="raw")
max.prob.train = pmax(nb.prob.train[,1],nb.prob.train[,2],nb.prob.train[,3],nb.prob.train[,4],nb.prob.tr
nb.pred.train = rep("DDown",length(max.prob.train))
nb.pred.train[nb.prob.train[,1] == max.prob.train] = "DDown"
```

```
nb.pred.train[nb.prob.train[,2] == max.prob.train] = "Down"
nb.pred.train[nb.prob.train[,3] == max.prob.train] = "Flat"
nb.pred.train[nb.prob.train[,4] == max.prob.train] = "Up"
nb.pred.train[nb.prob.train[,5] == max.prob.train] = "UUp"
mean(nb.pred.train==df$rAMZN.dir5[train])
```

Question 3.4

Consider the same classification problem as in Question 3.2 but with a Random Forest classifier with 300 trees and 2 predictors in each tree. Use the same train/test split as in Question 1.2. Evaluate the performance of this model with the test accuracy and confusion matrix.

Solution:

predict DDown Down Flat Up UUp

```
rAMZN.factor = as.factor(rAMZN.dir5)
df.tree = data.frame(rAMZN.dir5=rAMZN.factor, rAMZN1,rTSLA1,rAMZN2,rTSLA2)
rf.class = randomForest(rAMZN.dir5 ~ .,data=df.tree,subset=train,mtry=2,ntree=300,importance=TRUE)
rf.class
##
## Call:
##
   randomForest(formula = rAMZN.dir5 ~ ., data = df.tree, mtry = 2,
                                                                          ntree = 300, importance = TRU
##
                  Type of random forest: classification
                        Number of trees: 300
##
## No. of variables tried at each split: 2
##
##
           OOB estimate of error rate: 76.74%
## Confusion matrix:
         DDown Down Flat Up UUp class.error
##
## DDown
            54
                18
                      17 26 68
                                  0.7049180
## Down
            25
                 22
                      8 29
                             50
                                  0.8358209
## Flat
            22
                 13
                      14 28
                             38
                                  0.8782609
            35
## Up
                 22
                      17 19
                             56
                                  0.8724832
## UUp
                 25
                      25 34 78
                                  0.6502242
rf.pred = predict(rf.class,newdata=df.tree[-train,])
mean(rf.pred==df.tree$rAMZN.dir5[-train])
## [1] 0.2686567
table(predict=rf.pred,truth=df.tree$rAMZN.dir5[-train])
##
          truth
```

```
##
     DDown
               13
                    11
                          7 13
                                  6
##
     Down
               2
                     1
                          3 11
                                  8
                          3 4
##
     Flat
               3
                     2
                                  5
                6
                                  5
##
     Uр
                     5
                          5 9
##
     UUp
               15
                    12
                         11 13
                                 28
rf.pred.train = predict(rf.class,newdata=df.tree[train,])
mean(rf.pred.train==df$rAMZN.dir5[train])
```

[1] 1

Question 3.5

Consider the same classification problem as in Question 3.2 but with a neural network of your own design with at least 1 hidden layer and at least 3 hidden nodes. Use the same train/test split as in Question 1.2. Evaluate the performance of this model with the test accuracy and confusion matrix.

Solution:

See python code

Question 3.6

Consider the same classification problem as in Question 3.2 but with a support vector machine using a radial basis kernel. Use the same train/test split as in Question 1.2. Evaluate the performance of this model with the test accuracy and confusion matrix.

Solution:

0.001

0.5

cost gamma

- best performance: 0.722608

- Detailed performance results:

error dispersion

##

##

##

##

```
rAMZN.factor = as.factor(rAMZN.dir5)
df.svm = data.frame(rAMZN.dir5=rAMZN.factor , rAMZN1,rTSLA1,rAMZN2,rTSLA2)

tune.out = tune(svm,rAMZN.dir5 ~ ., data=df.svm[train,],kernel="radial",ranges=list(cost=c(0.001,.01,.1 summary(tune.out))

##
## Parameter tuning of 'svm':
##
## - sampling method: 10-fold cross validation
##
## - best parameters:
## cost gamma
```

```
## 1 1e-03
             0.5 0.7226080 0.03353627
## 2 1e-02
             0.5 0.7226080 0.03353627
## 3 1e-01
             0.5 0.7226080 0.03353627
             0.5 0.7561728 0.03426026
## 4 1e+00
## 5
     5e+00
             0.5 0.7910340 0.05092449
## 6
    1e+01
             0.5 0.7922531 0.04663705
## 7
     1e+02
             0.5 0.8059259 0.03311776
     1e-03
             1.0 0.7226080 0.03353627
## 8
## 9 1e-02
             1.0 0.7226080 0.03353627
## 10 1e-01
             1.0 0.7226080 0.03353627
## 11 1e+00
             1.0 0.7910340 0.03477826
## 12 5e+00
             1.0 0.7910340 0.04159761
## 13 1e+01
             1.0 0.7947222 0.03850403
## 14 1e+02
             1.0 0.7959877 0.03731279
## 15 1e-03
             2.0 0.7226080 0.03353627
## 16 1e-02
             2.0 0.7226080 0.03353627
## 17 1e-01
             2.0 0.7226080 0.03353627
## 18 1e+00
             2.0 0.7811111 0.03548557
## 19 5e+00
             2.0 0.7784877 0.03537900
## 20 1e+01
             2.0 0.7810494 0.02094459
## 21 1e+02
             2.0 0.7734722 0.05085940
## 22 1e-03
             3.0 0.7226080 0.03353627
## 23 1e-02
             3.0 0.7226080 0.03353627
## 24 1e-01
             3.0 0.7226080 0.03353627
## 25 1e+00
             3.0 0.7799074 0.03666464
## 26 5e+00
             3.0 0.7710802 0.04407294
## 27 1e+01
             3.0 0.7611111 0.03595852
## 28 1e+02
             3.0 0.7723457 0.04564035
## 29 1e-03
             4.0 0.7226080 0.03353627
## 30 1e-02
             4.0 0.7226080 0.03353627
## 31 1e-01
             4.0 0.7226080 0.03353627
## 32 1e+00
             4.0 0.7699383 0.04246447
## 33 5e+00
             4.0 0.7648920 0.04087990
## 34 1e+01
             4.0 0.7586574 0.04933454
## 35 1e+02
             4.0 0.7723457 0.05239580
best.svm.class = tune.out$best.model
best.svm.class$cost
## [1] 0.001
best.svm.class$gamma
## [1] 0.5
summary(best.svm.class)
##
## Call:
## best.tune(method = svm, train.x = rAMZN.dir5 ~ ., data = df.svm[train,
      1, 2, 3, 4)), kernel = "radial")
##
```

```
##
##
## Parameters:
##
      SVM-Type: C-classification
##
   SVM-Kernel: radial
          cost: 0.001
##
##
                               800
## Number of Support Vectors:
##
   ( 183 134 219 149 115 )
##
##
##
## Number of Classes:
##
## Levels:
  DDown Down Flat Up UUp
best.svm.pred=predict(best.svm.class,newdata = df.svm[-train,])
mean((best.svm.pred==df.svm$rAMZN.dir5[-train]))
## [1] 0.2587065
table(predict=best.svm.pred,truth=df.svm$rAMZN.dir5[-train])
##
          truth
## predict DDown Down Flat Up UUp
     DDown
##
               0
                    0
                         0 0
     Down
               0
                         0 0
##
                                0
##
    Flat
               0
                    0
                         0 0
                                0
##
               0
                    0
                         0 0
                                0
     Uр
##
     UUp
              39
                   31
                        29 50
                               52
best.svm.pred.train = predict(best.svm.class,newdata = df.svm[train,])
mean(best.svm.pred.train==df$rAMZN.dir5[train])
## [1] 0.2773632
```

Question 4 (10pt)

Question 4.1

Of the methods considered in Question 3, which would you recommend in practice? Explain briefly (1 paragraph) why you choose this fit.

Solution:

Neural network appears to be the best since the accuracy is the best.