Earley's Algorithm (1970)

Nice combo of our parsing ideas so far:

- no restrictions on the form of the grammar:
 - A \rightarrow B C spoon D x
- incremental parsing (left to right, like humans)
- left context constrains parsing of subsequent words
 - so waste less time building impossible things
 - makes it faster than O(n³) for many grammars

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About Jay <u>Pi⊕i</u>≣



Jay Earley, Ph.D., is a transformational psychologist, group leader, psychotherapist, coach, author, teacher, and theorist.

Jay is trained in Internal Family Systems Therapy and assists with professional trainings in IFS. He leads IFS Classes for the general public which teach IFS as a practice for self-help and peer counseling. He is active in the IFS community and has presented a number of workshops at IFS annual conferences. He also teaches classes on Communication from the Heart, based on IFS, interactive groups, and the Pattern System.

He is nationally known for his innovation in the group psychotherapy field. His book, Interactive Group Therapy: Integrating Interpersonal, Action-Oriented, and Psychodynamic Approaches, Brunner/Mazel, describes his group therapy method in which people learn interpersonal relationship

group therapy method in which people learn interpersonal relationship skills by working directly on their relationships with each other. During his ten years on the east coast, Jay was Director of the Group Therapy Center of Long Island, where he trained group therapists in this method. He has written a number of articles on interactive groups and made numerous presentations at regional and national psychotherapy conferences. He continues to lead interactive therapy groups in the Bay Area.

Jay offers Life Purpose Coaching and Change Agent Coaching, on finding your life purpose and making a difference in the world. He has been writing about and leading workshops on Life Purpose since 1984. He has collected his writings on life purpose into an ebook Finding Your Life Purpose.

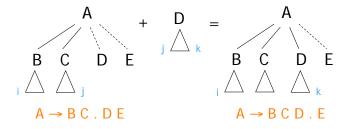
Jay also has a Ph.D. in computer science from Carnegie-Mellon University and was formerly on the U.C. Berkeley faculty, where he published 12 computer science papers, one of which was voted one of the best 25 papers of the quarter century by the Communications of the A.C.M.

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Overview of Earley's Algorithm

- Finds constituents and <u>partial</u> constituents in input
 - A \rightarrow B C . D E is partial: only the first half of the A



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Overview of Earley's Algorithm

- Proceeds <u>incrementally</u>, left-to-right
 - Before it reads word 5, it has already built all hypotheses that are consistent with first 4 words
 - Reads word 5 & attaches it to immediately preceding hypotheses. Might yield new constituents that are then attached to hypotheses immediately preceding them ...
 - E.g., attaching D to A → B C . D E gives A → B C D . E
 - Attaching E to that gives A → B C D E.
 - Now we have a complete A that we can attach to hypotheses immediately preceding the A, etc.

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Our Usual Example Grammar

```
ROOT \rightarrow S
                                NP → Papa
S
          \rightarrow NP VP
NP
          \rightarrow Det N
                                N \rightarrow caviar
NP
          \rightarrow NP PP
                                N \rightarrow spoon
VP
          \rightarrow VP PP
                                V \rightarrow ate
VP
          \rightarrow V NP
                                P \rightarrow with
PΡ
          \rightarrow P NP
                                Det \rightarrow the
                                Det \rightarrow a
```

^oPapa ¹ ate ² the ³ caviar ⁴ with ⁵ a ⁶ spoon ⁷

First Try: Recursive Descent

```
ROOT → S
                                               NP → Papa
              → NP VP
                            VP → V NP
                                                                  P \rightarrow with
                                               N → caviar
       ΝP
                            PP → PNP
              → Det N
                                               N \rightarrow spoon
                                                                  Det → the
       NP
              \rightarrow NP PP
                                                                  Det → a
• 0 ROOT → . S 0
                                   "goal stack"
    • 0 S \rightarrow . NP VP 0
        • 0 NP → . Papa 0
```

- 0 NP → Papa . 1
 0 S → NP . VP 1
 1 VP → . VP PP 1
 1 VP → . VP PP 1
 1 VP → . VP PP 1
 - 1 VP → . VP PP 1

 oops, stack overflowed
- OK, let's pretend that didn't happen.
- Let's suppose we didn't see VP → VP PP, and used VP → V NP instead.

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^oPapa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

```
ROOT → S
                             VP → V NP
                                                  NP → Papa
                             VP → VP PP
            → NP VP
                                                  N → caviar
                                                                       P \rightarrow with
    NP
            → Det N
                             PP \rightarrow PNP
                                                  N → spoon
                                                                       Det → the
    NP
            → NP PP
                                                                       Det \rightarrow a
0 \text{ ROOT} \rightarrow . S 0

    0 S → . NP VP 0

      • 0 NP \rightarrow . Papa 0

    0 NP → Papa . 1

    0 S → NP . VP 1

                               after dot = nonterminal, so recursively look for it ("predict")
      • 1 VP → . V NP 1
                               after dot = nonterminal, so recursively look for it ("predict")
           • 1 V \rightarrow . ate 1
                               after dot = terminal, so look for it in the input ("scan")
           • 1 V → ate.2
                               after dot = nothing, so parent's subgoal is completed ("attach")
      • 1 VP → V . NP 2
                               predict (next subgoal)
           • 2 NP → . ... 2
                               do some more parsing and eventually ..
           • 2 NP → .... 7
                               we complete the parent's NP subgoal, so attach
      • 1 VP → V NP . 7
                               attach again
  600.5465 NPro VP NLP - J. Eisner attach again
```

oPapa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

NP → Papa

First Try: Recursive Descent

VP → V NP

```
S
            → NP VP
                            VP → VP PP
                                                N → caviar
                                                                    P \rightarrow with
    NP
            → Det N
                           PP \rightarrow P NP
                                                N → spoon
                                                                    Det \rightarrow the
    NP
           → NP PP
                                                                    Det → a
0 \text{ ROOT} \rightarrow . S 0

    0 S → . NP VP 0

    0 NP → . Papa 0

    0 NP → Papa . 1

    0 S → NP . VP

      • (1 VP → . VP PP)
           • (VP → . V NP) we'd better backtrack here too!

    1 V → . ate 1

                                                   (why?)
                • 1 V → ate.2
           • 1 VP → V . NP 2
                • 2 NP → . ... 2
                                    do some more parsing and eventually ...
                ■ 2 NP → ... . 4
                                    ... the correct NP is from 2 to 4 this time
```

Use a Parse Table

- Earley's algorithm resembles recursive descent, but solves the left-recursion problem. No recursive function calls.
- Use a parse table as we did in CKY, so we can look up anything we've discovered so far.
 "Dynamic programming."
- Entries in column 5 look like (3, S → NP . VP)

(but we'll omit the → etc. to save space)

- Built while processing word 5
- Means that the input substring from 3 to 5 matches the initial NP portion of a S → NP VP rule
- Dot shows how much we've matched as of column 5
- Perfectly fine to have entries like (3, S → is it . true that S)

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^oPapa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

First Try: Recursive Descent

```
ROOT → S
                            VP → V NP
                                               NP → Papa
                           VP \rightarrow VP PP
            → NP VP
                                              N → caviar
                                                                  P \rightarrow with
    NP
           → Det N
                           PP \rightarrow P NP
                                               N \rightarrow spoon
                                                                  Det → the
    NP
           \rightarrow NP PP
                                                                  Det \rightarrow a
0 \text{ ROOT} \rightarrow . S 0
                              implement by function calls:
 • 0 S \rightarrow . NP VP 0
                              S() calls NP() and VP(), which recurse
      - 0 NP \rightarrow . Papa 0

    0 NP → Papa . 1

    0 S → NP . VP

      ■ (VP → . V NP 1) must backtrack to try predicting
                              a different VP rule here instead

    1 V → . ate 1

           • 1 V → ate.2
       • 1 VP → V . NP 2
           ■ 2 NP → . ... 2
                             But how about the other parse?
           • 2 NP → .... 7
        1 \text{ VP} \rightarrow \text{V NP} . 7
```

oPapa 1 ate 2 the 3 caviar 4 with 5 a 6 spoon 7

NP → Papa

First Try: Recursive Descent

VP → V NP

```
S
              → NP VP
                                 VP → VP PP
                                                                                P \rightarrow with
                                                        N → caviar
     NP
             → Det N
                                PP \rightarrow P NP
                                                        N \rightarrow spoon
                                                                                Det \rightarrow the
     NP
             → NP PP
                                                                                Det → a
0 \text{ ROOT} \rightarrow . S 0
 • 0 S \rightarrow . NP VP 0

    0 NP → . Papa 0

    0 NP → Papa . 1

 0 S \rightarrow NP.VP
       • (1 VP → . VP PP)
             VP → . VP PP
                      1 VP → . VP PP
                         1 \text{ VP} \rightarrow . \text{ VP PP } 1
                              1 \text{ VP} \rightarrow . \text{ VP PP } 1
                                 oops, stack overflowed
                                 no fix after all
                              - must transform grammar to eliminate left-recursive rules
```

Use a Parse Table

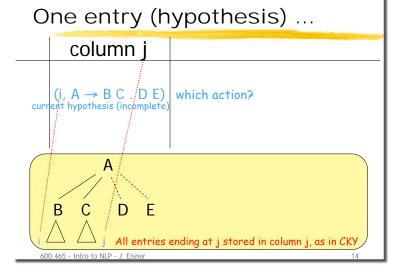
- Entries in column 5 look like (3, S → NP . VP)
- What does it mean if we have this entry?
 - Unknown right context: Doesn't mean we'll necessarily be able to find a VP starting at column 5 to complete the S.
 - Known left context: Does mean that some dotted rule back in column 3 is looking for an S that starts at 3.
 - So if we actually do find a VP starting at column 5, allowing us to complete the S, then we'll be able to attach the S to something.
 - And when that something is complete, it too will have a customer to its left ... just as in recursive descent!
 - In short, a top-down (i.e., goal-directed) parser: it chooses to start building a constituent not because of the input but because that's what the left context needs. In the spoon, won't build spoon as a verb because there's no way to use a verb there.
 - So any hypothesis in column 5 could get used in the correct parse, if words 1-5 are continued in just the right way by words 6-n.

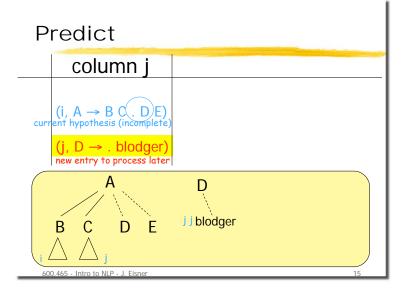
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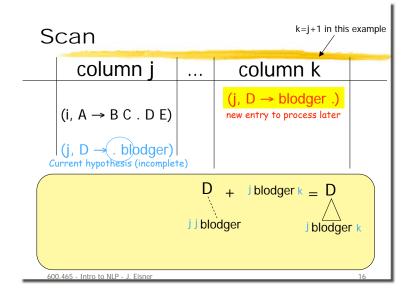
Operation of the Algorithm

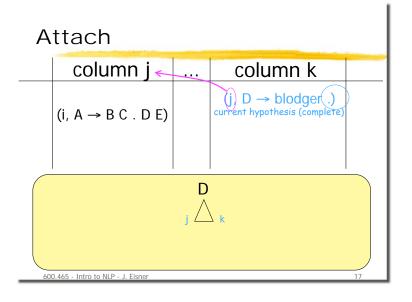
- Process all hypotheses one at a time in order.
 (Current hypothesis is shown in blue, with substring.)
- This may add new hypotheses to the end of the to-do list, or try to add old hypotheses again.
- Process a hypothesis according to what follows the dot – just as in recursive descent:
 - If a word, scan input and see if it matches
 - If a nonterminal, predict ways to match it
 (we'll predict blindly, but could reduce # of predictions by
 looking ahead k symbols in the input and only making
 predictions that are compatible with this limited right context)
 - If nothing, then we have a complete constituent, so attach it to all its customers (shown in purple).

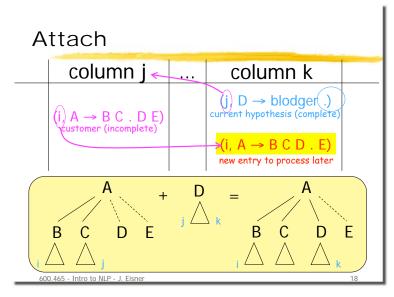
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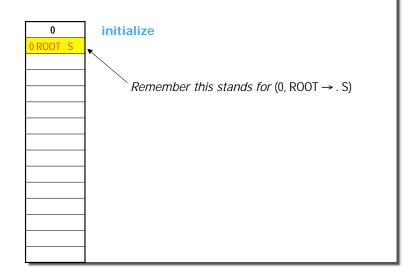


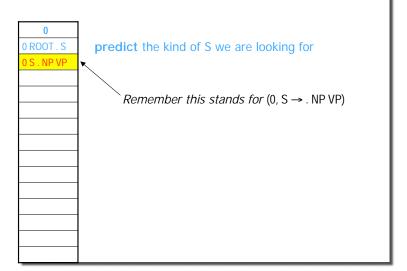


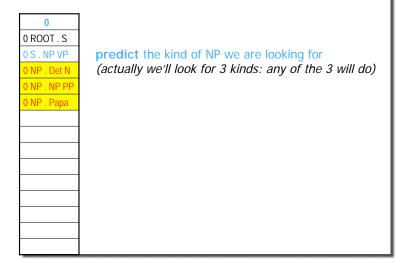
^oPapa ¹ ate ² the ³ caviar ⁴ with ⁵ a ⁶ spoon ⁷

Our Usual Example Grammar

```
ROOT \rightarrow S
                                        NP → Papa
          S
                   \rightarrow NP VP
          NP
                   → Det N
                                        N \rightarrow caviar
                                        N \rightarrow spoon
                   \rightarrow NP PP
          NP
          VP
                   \rightarrow VP PP
                                        V \rightarrow ate
                   \rightarrow V NP
                                        P \rightarrow with
          VP
          PP
                    \rightarrow P NP
                                        Det \rightarrow the
                                        Det \rightarrow a
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```







0	
0 ROOT . S	
0 S . NP VP	
0 NP . Det N	predict the kind of Det we are looking for (2 kinds)
0 NP . NP PP	
0 NP . Papa	
0 Det . the	
0 Det . a	

0 S . NP VP	
0 NP . Det N	
0 NP . NP PP	<pre>predict the kind of NP we're looking for</pre>
0 NP . Papa	but we were already looking for these so
0 Det . the	don't add duplicate goals! Note that this happened
0 Det . a	when we were processing a left-recursive rule.

0 ROOT . S

0 Pa	pa 1
0 ROOT . S	0 NP Papa.
0 S . NP VP	
0 NP . Det N	
0 NP . NP PP	
0 NP . Papa	scan: t
0 Det . the	
0 Det . a	

0 Pa	pa 1
0 ROOT . S	0 NP Papa .
0 S . NP VP	
0 NP . Det N	
0 NP . NP PP	
0 NP . Papa	
0 Det . the	scan: f
0 Det . a	

0 Pa	pa 1
0 ROOT . S	0 NP Papa .
0 S . NP VP	
0 NP . Det N	
0 NP . NP PP	
0 NP . Papa	
0 Det . the	
0 Det . a	scan: f

predict

0 Pa	pa 1	
0 ROOT . S	0 NP Papa.	attach the newly created NP
0 S . NP VP	0 S NP . VP	(which starts at 0) to its customers
0 NP . Det N	0 NP NP . PP	(incomplete constituents that end at 0
0 NP . NP PP		and have NP after the dot)
0 NP . Papa		
0 Det . the		
0 Det . a		

0 Papa 1				
0 ROOT . S	0 NP Papa .			
0 S . NP VP	0 S NP . VP			
0 NP . Det N	0 NP NP . PP			
0 NP . NP PP	1 VP . V NP			
0 NP . Papa	1 VP . VP PP			
0 Det . the				
0 Det . a				

0 Papa 1
0 ROOT.S 0 NP Papa.
0 S.NP VP 0 S NP. VP
0 NP. Det N 0 NP NP.PP
0 NP. NP PP 1 VP. V NP
0 NP. Papa 1 VP. VP PP
0 Det. the 1 PP. P NP
0 Det. a

predict

		İ
0 Pa	pa 1	
0 ROOT . S	0 NP Papa.	
0 S . NP VP	0 S NP . VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	predict
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	

0 Pa	ıpa 1
0 ROOT . S	0 NP Papa .
0 S . NP VP	0 S NP . VP
0 NP . Det N	0 NP NP . PP
0 NP . NP PP	1 VP . V NP
0 NP . Papa	1 VP . VP PP
0 Det . the	1 PP . P NP
0 Det . a	1 V . ate

0 Papa 1				
0 ROOT . S	0 NP Papa .			
0 S . NP VP	0 S NP . VP			
0 NP . Det N	0 NP NP . PP			
0 NP . NP PP	1 VP . V NP			
0 NP . Papa	1 VP . VP PP			
0 Det . the	1 PP . P NP			
0 Det . a	1 V . ate			
	1 P . with			

predict

0 Pa	pa 1 ate	e 2
0 ROOT . S	0 NP Papa .	1 V ate .
0 S . NP VP	0 S NP . VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	scan: su
	1 P . with	

0 Pa	pa 1 ate	2	
0 ROOT . S	0 NP Papa .	1 V ate.	
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP		
0 NP . Papa	1 VP . VP PP		
0 Det . the	1 PP . P NP		
0 Det . a	1 V . ate		
	1 P . with	scan: fail	ure

0 Papa 1 ate 2					
0 ROOT . S	0 NP Papa .	1 V ate.			
0 S . NP VP	0 S NP . VP	1 VP V . NP			
0 NP . Det N	0 NP NP . PP				
0 NP . NP PP	1 VP . V NP				
0 NP . Papa	1 VP . VP PP				
0 Det . the	1 PP . P NP				
0 Det . a	1 V . ate				
	1 P . with				

attach

0 Pa	pa 1 ate	2
0 ROOT . S	0 NP Papa.	1 V ate .
0 S . NP VP	0 S NP . VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	
	1 P . with	

predict

0 Pa	pa 1 ate	2
0 ROOT . S	0 NP Papa.	1 V ate .
0 S . NP VP	0 S NP . VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the
0 Det . a	1 V . ate	2 Det . a
	1 P . with	

predict (these next few steps
should look familiar)

0 Pa	pa 1 ate	e 2
0 ROOT . S	0 NP Papa .	1 V ate .
0 S . NP VP	0 S NP . VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the
0 Det . a	1 V . ate	2 Det . a
	1 P . with	

predict

0 Pa	pa 1 ate	2
0 ROOT . S	0 NP Papa.	1 V ate .
0 S . NP VP	0 S NP . VP	1 VP V . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the
0 Det . a	1 V . ate	2 Det . a
	1 P . with	

scan (this time we fail since Papa is not the next word)

0 Pa	pa 1 ate	e 2 the	3	
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .	
0 S . NP VP	0 S NP . VP	1 VP V . NP		
0 NP . Det N	0 NP NP . PP	2 NP . Det N		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the	scan: su	ccess
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

0 Papa 1 ate 2 the 3						
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .			
0 S . NP VP	0 S NP . VP	1 VP V . NP				
0 NP . Det N	0 NP NP . PP	2 NP . Det N				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa				
0 Det . the	1 PP . P NP	2 Det . the				
0 Det . a	1 V . ate	2 Det . a				
	1 P . with					

0 Pa	pa 1 ate	e 2 the	3
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N
0 NP . Det N	0 NP NP . PP	2 NP . Det N	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the	
0 Det . a	1 V . ate	2 Det . a	
	1 P . with		

0 Pa	pa 1 ate	e 2 the	3
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon
0 NP . Papa	1 VP . VP PP	2 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the	
0 Det . a	1 V . ate	2 Det . a	
	1 P . with		

0 Papa 1 ate 2 the 3 caviar 4					
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N		
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon		
0 NP . Papa	1 VP . VP PP	2 NP . Papa			
0 Det . the	1 PP . P NP	2 Det . the			
0 Det . a	1 V . ate	2 Det . a			
	1 P . with				

0 Pa	pa 1 ate	2 the	e 3 ca	viar 4
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .	3 N caviar .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		
0 Det . a	1 V . ate	2 Det . a		
	1 P . with			

0 Pa	pa 1 ate	2 the	e 3 ca	viar 4	
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .	3 N caviar .	attach
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon		
0 NP . Papa	1 VP . VP PP	2 NP . Papa			
0 Det . the	1 PP . P NP	2 Det . the			
0 Det . a	1 V . ate	2 Det . a			
	1 P . with				

0 Papa 1 ate 2 the 3 caviar 4							
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .	3 N caviar .			
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.			
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.			
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP			
0 NP . Papa	1 VP . VP PP	2 NP . Papa					
0 Det . the	1 PP . P NP	2 Det . the					
0 Det . a	1 V . ate	2 Det . a					
	1 P . with						

attach (again!)

0 Pa	pa 1 ate	e 2 the	e 3 ca	viar 4	
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .	3 N caviar .	
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	attach
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	(again!)
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	
0 Det . a	1 V . ate	2 Det . a			
	1 P . with				

0 Papa 1 ate 2 the 3 caviar 4								
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N.				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP				
	1 P . with							

caviar

3 N caviar .

2 NP Det N

1 VP V NP .

2 NP NP . PP

0 S NP VP.

1 VP VP . PP

4 PP . P NP

 $0\ ROOT\ S$.

2 Det the .

2 NP Det . N

3 N . caviar

3 N . spoon

0 Pa	0 Papa 1 ate 2 the 3 caviar 4							
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP				
	1 P . with			0 ROOT S.				

attach (again!) 0

0 ROOT . S

0 S . NP VP

0 NP . Det N

0 NP . NP PP

0 NP . Papa

0 Det . the

0 Det . a

Papa

0 NP Papa.

0 S NP . VP

0 NP NP . PP

1 VP . V NP

1 VP . VP PP

1 PP . P NP

1 V . ate

1 P . with

1 V ate.

1 VP V . NP

2 NP . Det N

2 NP . NP PP

2 NP . Papa

 $2\mbox{ Det}$. the

2 Det . a

0 Pa	0 Papa 1 ate 2 the 3 caviar 4						
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .			
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .			
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.			
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP			
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.			
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP			
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP			
	1 P . with			0 ROOT S.			
				4 P . with			

0 Papa 1 ate 2 the 3 caviar 4							
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .	3 N caviar .			
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .			
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .			
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP			
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.			
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP			
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP			
	1 P . with			0 ROOT S.			
				4 P . with			

0 Pa	0 Papa 1 ate 2 the 3 caviar 4 with 5						
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .	3 N caviar .	4 P with .		
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .			
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.			
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP			
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.			
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP			
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP			
	1 P . with			0 ROOT S .			
				4 P . with			

0 Pa	pa 1 ate	2 the	e 3 ca	viar 4 wi	th 5
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	
	1 P . with			0 ROOT S.	
				4 P . with	

0 Pa	0 Papa 1 ate 2 the 3 caviar 4 with 5						
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .		
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP		
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	5 NP . Det N		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa		
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP			
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP			
	1 P . with			0 ROOT S.			
				4 P . with			

0 Papa 1 ate 2 the 3 caviar 4 with 5						
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .	
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	5 NP . Det N	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a	
	1 P . with			0 ROOT S.		
				4 P . with		

0 Papa 1 ate 2 the 3 caviar 4 with 5						
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .	
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a	
	1 P . with			0 ROOT S .		
				4 P . with		

0 Pa	pa 1 ate	e 2 the	e 3 ca	viar 4 wi	th 5
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1 P . with			0 ROOT S .	
				4 P . with	

0 Pa	pa 1 ate	2 the	e 3 ca	viar 4 wi	th 5
0 ROOT . S	0 NP Papa.	1 V ate .	2 Det the .	3 N caviar .	4 P with .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	5 NP . Det N
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	5 Det . the
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	5 Det . a
	1 P . with			0 ROOT S.	
				4 P . with	

ate	e 2 the	e 3 ca	viar 4 wi	th 5	a 6
Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .
O. VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	
NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	
V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	
VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa	
P NP	2 Det . the		1 VP VP . PP	5 Det . the	
ite	2 Det . a		4 PP . P NP	5 Det . a	
<i>i</i> th			0 ROOT S .		
			4 P . with		

ate	e 2 the	e 3 ca	viar 4 wi	th 5	a 6
Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a.
P. VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N
NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	
V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	
VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa	
P NP	2 Det . the		1 VP VP . PP	5 Det . the	
te	2 Det . a		4 PP . P NP	5 Det . a	
vith			0 ROOT S .		
			4 P . with		

ate	e 2 the	e 3 ca	viar 4 wi	th 5	a 6
Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .
P . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N
VP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar
V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon
VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa	
P NP	2 Det . the		1 VP VP . PP	5 Det . the	
ite	2 Det . a		4 PP . P NP	5 Det . a	
/ith			0 ROOT S .		
			4 P . with		

ate	e 2 the	e 3 ca	viar 4 wit	th 5	a 6
Papa .	1 V ate.	2 Det the .	3 N caviar .	4 P with .	5 Det a .
P. VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N
NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar
V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon
VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa	
P NP	2 Det . the		1 VP VP . PP	5 Det . the	
te	2 Det . a		4 PP . P NP	5 Det . a	
vith			0 ROOT S .		
			4 P . with		

ate	2 the	e 3 ca	viar 4 wi	th 5	a 6 sp	oon 7
Papa .	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon.
2 . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N	
NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	5 NP . Det N	6 N . caviar	
V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	
VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa		
P NP	2 Det . the		1 VP VP . PP	5 Det . the		
ite	2 Det . a		4 PP . P NP	5 Det . a		
<i>i</i> th			0 ROOT S.			
			4 P . with			

ate	2 the	e 3 ca	viar 4 wi	th 5	a 6 sp	oon 7
Рара .	1 V ate .	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon .
P. VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N	5 NP Det N.
NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar	
V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	
VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa		
P NP	2 Det . the		1 VP VP . PP	5 Det . the		
te	2 Det . a		4 PP . P NP	5 Det . a		
vith			0 ROOT S .			
			4 P . with			

ate	2 the	e 3 ca	viar 4 wi	th 5	a 6 sp	oon 7
^o apa .	1 V ate.	2 Det the .	3 N caviar .	4 P with .	5 Det a .	6 N spoon .
⁹ . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	4 PP P . NP	5 NP Det . N	5 NP Det N.
VP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .	5 NP . Det N	6 N . caviar	4 PP P NP.
V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP . NP PP	6 N . spoon	5 NP NP . PP
VP PP	2 NP . Papa		0 S NP VP.	5 NP . Papa		
P NP	2 Det . the		1 VP VP . PP	5 Det . the		
ite	2 Det . a		4 PP . P NP	5 Det . a		
vith			0 ROOT S.			
			4 P . with			
•						

0 Pa	pa 1 ate	2 the	3 ca\	viar 4 with	ı a	spoon 7
0 ROOT . S	0 NP Papa .	1 V ate.	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP.
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		
	1 P . with			0 ROOT S .		
				4 P . with		

0 Pa	0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7								
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	6 N spoon .				
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	5 NP Det N .				
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	4 PP P NP .				
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP NP . PP				
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	2 NP NP PP .				
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	1 VP VP PP.				
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	7 PP . P NP				
	1 P . with			0 ROOT S .					
				4 P . with					

0 Pa	pa 1 ate	2 the	3 cav	viar 4 with	a	spoon 7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP .		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP.
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP.
				4 P . with		2 NP NP . PP

0 Pa	pa 1 ate	2 the	3 ca	viar 4 with	ı a	spoon 7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP.
				4 P . with		2 NP NP . PP
						0SNPVP.
						1 VP VP . PP

0 Pa	0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	6 N spoon .		
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	5 NP Det N .		
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	4 PP P NP .		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP NP . PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	2 NP NP PP .		
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	1 VP VP PP.		
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	7 PP . P NP		
	1 P . with			0 ROOT S.	1 VP V NP.		
				4 P . with	2 NP NP . PP		
					0 S NP VP.		
					1 VP VP . PP		
					7 P . with		

O Papa 1 ate 2 the 3 caviar 4 with a spoon 7							
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP	
	1 P . with			0 ROOT S.		1 VP V NP.	
				4 P . with		2 NP NP . PP	
						0 S NP VP.	
						1 VP VP . PP	
						7 P . with	

0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7								
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	ļ	6 N spoon .		
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .		
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP .		
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP		
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .		
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.		
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP		
	1 P . with			0 ROOT S.		1 VP V NP.		
				4 P . with		2 NP NP . PP		
						0SNPVP.		
						1 VP VP . PP		
						7 P . with		

0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7							
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP .	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP	
	1 P . with			0 ROOT S.		1 VP V NP.	
				4 P . with		2 NP NP . PP	
						0SNPVP.	
						1 VP VP . PP	
						7 P . with	
						0 ROOT S .	

0 Pa	O Papa 1 ate 2 the 3 caviar 4 with a spoon 7								
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .			
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .			
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP .			
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP			
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .			
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.			
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP			
	1 P . with			0 ROOT S.		1 VP V NP.			
				4 P . with		2 NP NP . PP			
						0 S NP VP.			
						1 VP VP . PP			
						7 P . with			
						0 ROOT S.			

0 Pa	pa 1 ate	2 the	3 ca	viar 4 with	a spoon 7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP NP . PF
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	2 NP NP PP
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	1 VP VP PP
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	7 PP . P NP
	1 P . with			0 ROOT S .	1 VP V NP.
				4 P . with	2 NP NP . PF
					0 S NP VP.
					1 VP VP . PF
					7 P . with
					0 ROOT S .

0 D-		0 41	2	dan 4dil	7
0 Pa	pa 1 ate	2 the	3 ca\	iar 4 with	a spoon 7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	7 PP . P NP
	1 P . with			0 ROOT S .	1 VP V NP.
				4 P . with	2 NP NP . PP
					0 S NP VP.
					1 VP VP . PP
					7 P . with
					0 ROOT S .

0 Pa	pa 1 ate	2 the	3 cav	viar 4 with	ı a	spoon 7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP
	1 P . with			0 ROOT S.		1 VP V NP.
				4 P . with		2 NP NP . PP
						0 S NP VP.
						1 VP VP . PP
						7 P . with
						0 ROOT S.

Left Recursion Kills Pure Top-Down Parsing ...

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makes new hypotheses ad infinitum before we've seen the PPs at all

hypotheses try to predict in advance how many PP's will arrive in input

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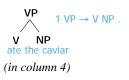
... but Earley's Alg is Okay!

$$VP$$
 $VP \rightarrow VP PP$
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0.5

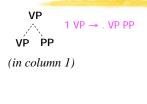
... but Earley's Alg is Okay!

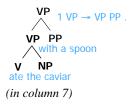
$$VP$$
 $VP \rightarrow VP PP$
 $VP PP$
 $(in \ column \ 1)$



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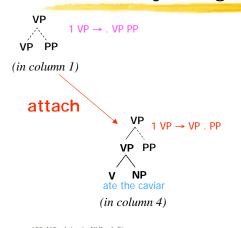
... but Earley's Alg is Okay!



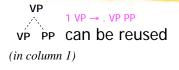


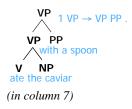
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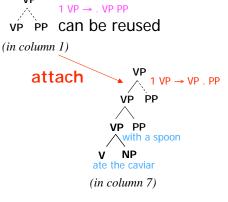
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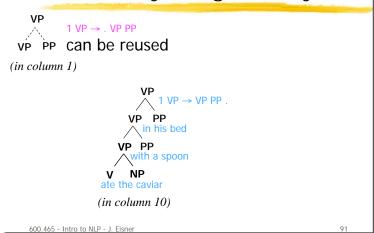
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... but Earley's Alg is Okay!

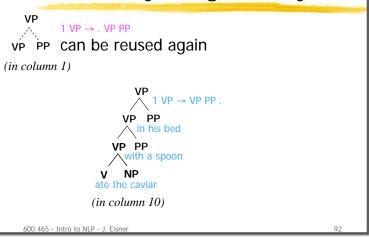


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... but Earley's Alg is Okay!



... but Earley's Alg is Okay!



... but Earley's Alg is Okay!



0 Pa	pa 1 ate	2 the	3 ca\	iar 4 with	a spoon 7
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .	6 N spoon .
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .	5 NP Det N.
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.	4 PP P NP .
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP	5 NP NP . PP
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.	2 NP NP PP .
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP	1 VP VP PP.
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP	7 PP . P NP
	1 P . with			0 ROOT S.	1 VP V NP.
				4 P . with	2 NP NP . PP
comple	ted a VP i	n col 4			0 S NP VP.
col 1 le	ts us use	it in a VP	PP struct	ure	1 VP VP . PP
					7 P. with
					0 ROOT S.

0 Pa	0 Papa 1 ate 2 the 3 caviar 4 with a spoon 7						
0 ROOT . S	0 NP Papa .	1 V ate .	2 Det the .	3 N caviar .		6 N spoon .	
0 S . NP VP	0 S NP . VP	1 VP V . NP	2 NP Det . N	2 NP Det N .		5 NP Det N .	
0 NP . Det N	0 NP NP . PP	2 NP . Det N	3 N . caviar	1 VP V NP.		4 PP P NP .	
0 NP . NP PP	1 VP . V NP	2 NP . NP PP	3 N . spoon	2 NP NP . PP		5 NP NP . PP	
0 NP . Papa	1 VP . VP PP	2 NP . Papa		0 S NP VP.		2 NP NP PP .	
0 Det . the	1 PP . P NP	2 Det . the		1 VP VP . PP		1 VP VP PP.	
0 Det . a	1 V . ate	2 Det . a		4 PP . P NP		7 PP . P NP	
	1 P . with			0 ROOT S .		1 VP V NP.	
				4 P . with		2 NP NP . PP	
comple	ted that V	P = VP P	P in col 7	·		0 S NP VP.	
col 1 w	col 1 would let us use <i>it</i> in a VP PP structure						
can reuse col 1 as often as we need						7 P . with	
						0 ROOT S.	

What's the Complexity?

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