

a)

$$\frac{V(s)}{U(s)} = \frac{1}{s^2 + 6s + 5}$$

$$A + B$$

$$As = 1$$

$$A + 5B = 6$$

$$A = 6 - 5B$$

$$6 - 4B = 1$$

$$B = \frac{5}{4}$$

$$A = -\frac{1}{4}$$

1) a)

$$\cancel{y''(s) + 6y'(s) + 5y(s) = 0}$$

$$\cancel{(s^2 + 6s + 5)y(s) = 0}$$

$$\cancel{s^2 + 6s + 5 = \frac{0(s)}{y(s)}}$$

$$\cancel{\frac{1}{s^2 + 6s + 5} = \frac{1}{(s+1)(s+5)}}$$

$$\cancel{\frac{1}{(s+1)(s+5)} = \frac{1}{(s+1)(s+5)}}$$

1) b)

$$\mathcal{L}(1 \ddot{y} + 6 \dot{y} + 5 y) = 0 \quad y(0) = 1 \quad \dot{y}(0) = 0$$

~~1.~~

$$1(s^2 Y(s) - s y(0) - \dot{y}(0)) + 6(s Y(s) - y(0)) + 5 Y(s) = 0$$

$$(s^2 + 6s + 5) Y(s) - 5 - 0 - 6 = 0$$

$$Y(s) = \frac{s+6}{s^2+6s+5} = \frac{s+6}{(s+1)(s+5)} \quad A(s+1) + B(s+5)$$

$$\mathcal{L}^{-1}(Y(s)) = \mathcal{L}^{-1}\left(\frac{s+3}{(s^2+6s+5)}\right) + \mathcal{L}^{-1}\left(\frac{3}{(s+1)(s+5)}\right)$$

$$= -\frac{1}{4} \frac{1}{s+5} + \frac{5}{4} \frac{1}{s+1}$$

$$y(t) = -\frac{1}{4} e^{-5t} + \frac{5}{4} e^{-t}$$

2

$$U = m_1 \ddot{x}_1 + b_1 \dot{x}_1 + k_3 (\dot{x}_1 - x_2) + k_1 x_1$$

$$0 = m_2 \ddot{x}_2 + b_2 \dot{x}_2 + k_3 (x_2 - x_1) + k_2 x_2$$

L form

$$U(s) = m_1 s^2 x_1(s) + b_1 s x_1(s) + k_3 (x_1(s) - x_2(s)) + k_1 x_1(s)$$

$$0 = m_2 s^2 x_2(s) + b_2 s x_2(s) + k_3 (x_2(s) - x_1(s)) + k_2 x_2(s)$$

$$\frac{U(s)}{K_3} = (m_1 s^2 + b_1 s + k_3 + k_1) x_1(s) - k_3 x_2(s)$$

$$(m_2 s^2 + b_2 s + k_3 + k_2) x_2(s) - k_3 x_1(s)$$

$$\frac{(m_2 s^2 + b_2 s + k_3 + k_2) x_2(s) - k_3 x_1(s)}{K_3} = \frac{U(s)}{K_3}$$

$$\frac{(m_1 s^2 + b_1 s + k_3 + k_1)(m_2 s^2 + b_2 s + k_3 + k_2) - k_3}{K_3} = \frac{U(s)}{x_2(s)}$$

$$\frac{x_2(s)}{U(s)} = \frac{K_3}{(m_1 s^2 + b_1 s + k_3 + k_1)(m_2 s^2 + b_2 s + k_3 + k_2) - k_3}$$

$$m_1 s^2 + b_1 s + k_3 + k_1 - (m_2 s^2 + b_2 s + k_3 + k_2) = \frac{U(s)}{x_1(s)}$$

$$\frac{1}{(m_1 s^2 + b_1 s + k_3 + k_1) - (m_2 s^2 + b_2 s + k_3 + k_2)} = \frac{x_1(s)}{U(s)}$$

$$\frac{e_2}{e_1} = \frac{R_2}{R_1 + R_2}$$

$$Z_1 = R_1 + \frac{1}{C_1 s}$$

$$Z_2 = R_2 + \frac{1}{C_2 s}$$

$$\frac{e_2}{e_1} = \frac{R_2 \frac{1}{C_2 s}}{(R_1 + \frac{1}{C_1 s})(R_2 + \frac{1}{C_2 s})}$$



4)

$$G(s) = \frac{2s+4}{s^2+6s+10} = \frac{2s+4}{(s+3)^2+1} = 2 \frac{s+2}{(s+3)^2+1}$$

$$= 2 \left(\frac{s+3}{(s+3)^2+1} + \frac{1}{(s+3)^2+1} \right)$$

~~$\mathcal{L}^{-1}(G(s)) = 2e^{-3t} \cos(t) - 2e^{-3t} \sin(t)$~~ $\mathcal{L}^{-1}(G(s)) = 2e^{-3t} \cos(t) + 2e^{-3t} \sin(t)$

$$\mathcal{L}^{-1}(G(s)) = 2(e^{-3t} \cos(t) + e^{-3t} \sin(t))$$

5)

$$G(s) = \frac{s^2+s+2}{(s+1)^3} = \frac{s^2+2s+1}{(s+1)^3} + \frac{(-s+1)}{(s+1)^3}$$

$$= \frac{(s+1)^2}{(s+1)^3} + \frac{(-s+1)}{(s+1)^3}$$

$$= \frac{1}{s+1} - \frac{s-1}{(s+1)^3}$$

$$= \frac{1}{s+1} - \frac{s+1}{(s+1)^3} + \frac{2}{(s+1)^3}$$

$$= \frac{1}{s+1} - \frac{1}{(s+1)^2} + \frac{2}{(s+1)^3}$$

$$\mathcal{L}^{-1}(G(s)) = e^{-t} - t + t^2$$

