RegressionModelAssessment

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Regression Models Course Project

Synopsis

The Project work for Motor Trend, a magazine about the automobile industry. Looking at a data set of a collection of cars, they are interested in exploring the relationship between a set of variables and miles per gallon (MPG). They are particularly interested in the following two questions:

"Is an automatic or manual transmission better for MPG" "Quantifying how different is the MPG between automatic and manual transmissions?"

Data Loading

Load the data

data(mtcars)

Exploratory analysis

```
summary(mtcars)
##
                          cyl
                                          disp
                                                            hp
         mpg
                    Min.
                                     Min.
                                                      Min.
##
   Min.
           :10.40
                            :4.000
                                             : 71.1
                                                              : 52.0
    1st Qu.:15.43
                    1st Qu.:4.000
                                     1st Qu.:120.8
                                                      1st Qu.: 96.5
    Median :19.20
                    Median :6.000
                                     Median :196.3
                                                      Median :123.0
##
##
   Mean
           :20.09
                    Mean
                            :6.188
                                     Mean
                                             :230.7
                                                      Mean
                                                             :146.7
    3rd Qu.:22.80
                                     3rd Qu.:326.0
##
                    3rd Qu.:8.000
                                                      3rd Qu.:180.0
##
    Max.
           :33.90
                    Max.
                            :8.000
                                     Max.
                                             :472.0
                                                      Max.
                                                              :335.0
##
         drat
                           wt
                                                            ٧S
                                          qsec
##
    Min.
           :2.760
                    Min.
                            :1.513
                                     Min.
                                             :14.50
                                                      Min.
                                                              :0.0000
    1st Qu.:3.080
                    1st Qu.:2.581
                                     1st Qu.:16.89
                                                      1st Qu.:0.0000
##
    Median :3.695
                    Median :3.325
                                     Median :17.71
                                                      Median :0.0000
##
    Mean
           :3.597
                    Mean
                            :3.217
                                     Mean
                                             :17.85
                                                      Mean
                                                              :0.4375
    3rd Qu.:3.920
                    3rd Qu.:3.610
                                     3rd Qu.:18.90
                                                      3rd Qu.:1.0000
##
                            :5.424
##
    Max.
           :4.930
                    Max.
                                     Max.
                                             :22.90
                                                      Max.
                                                             :1.0000
##
                                            carb
          am
                           gear
                     Min.
##
           :0.0000
                                      Min.
   Min.
                             :3.000
                                              :1.000
##
    1st Qu.:0.0000
                      1st Qu.:3.000
                                      1st Qu.:2.000
##
    Median :0.0000
                     Median :4.000
                                      Median :2.000
   Mean :0.4062
                     Mean :3.688
                                      Mean :2.812
```

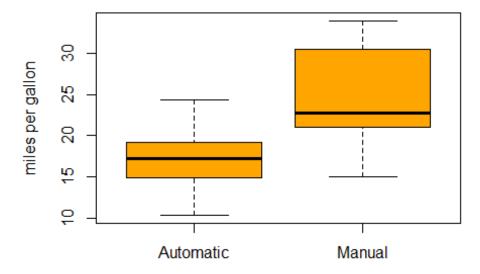
```
3rd Qu.:1.0000
                      3rd Qu.:4.000
                                      3rd Qu.:4.000
##
    Max.
           :1.0000
                      Max.
                             :5.000
                                      Max.
                                              :8.000
mtcars$cyl <- factor(mtcars$cyl)</pre>
mtcars$vs <- factor(mtcars$vs)</pre>
mtcars$gear <- factor(mtcars$gear)</pre>
mtcars$carb <- factor(mtcars$carb)</pre>
mtcars$am <- factor(mtcars$am,labels=c('Automatic','Manual'))</pre>
summary(mtcars)
##
                                 disp
                                                                   drat
                     cyl
                                                   hp
         mpg
                                                    : 52.0
##
    Min.
           :10.40
                     4:11
                            Min.
                                   : 71.1
                                             Min.
                                                             Min.
                                                                     :2.760
##
    1st Qu.:15.43
                    6: 7
                            1st Qu.:120.8
                                             1st Qu.: 96.5
                                                             1st Qu.:3.080
##
    Median :19.20
                    8:14
                            Median :196.3
                                             Median :123.0
                                                             Median :3.695
##
    Mean
           :20.09
                            Mean
                                   :230.7
                                             Mean
                                                    :146.7
                                                             Mean
                                                                     :3.597
    3rd Qu.:22.80
                                                             3rd Qu.:3.920
                            3rd Qu.:326.0
                                             3rd Qu.:180.0
##
##
    Max.
           :33.90
                                   :472.0
                                                    :335.0
                                                             Max.
                                                                     :4.930
                            Max.
                                             Max.
##
          wt
                          qsec
                                     ٧S
                                                     am
                                                            gear
                                                                    carb
##
    Min.
           :1.513
                            :14.50
                                     0:18
                                             Automatic:19
                                                            3:15
                                                                    1: 7
                    Min.
## 1st Qu.:2.581
                    1st Qu.:16.89
                                     1:14
                                             Manual
                                                     :13
                                                            4:12
                                                                    2:10
## Median :3.325
                    Median :17.71
                                                             5: 5
                                                                    3: 3
## Mean
           :3.217
                                                                    4:10
                    Mean
                            :17.85
##
    3rd Qu.:3.610
                     3rd Qu.:18.90
                                                                    6: 1
    Max. :5.424
                    Max. :22.90
                                                                    8: 1
```

Regression model

```
full.model <- lm(mpg \sim ., data = mtcars)
best.model <- step(full.model, direction = "backward")</pre>
## Start: AIC=76.4
## mpg \sim cyl + disp + hp + drat + wt + qsec + vs + am + gear + carb
##
##
          Df Sum of Sq
                          RSS
                                 AIC
## - carb 5
               13.5989 134.00 69.828
                3.9729 124.38 73.442
## - gear
          2
           1
                1.1420 121.55 74.705
## - am
## - qsec 1
               1.2413 121.64 74.732
## - drat 1
                1.8208 122.22 74.884
## - cyl
           2
               10.9314 131.33 75.184
## - vs
                3.6299 124.03 75.354
           1
## <none>
                       120.40 76.403
## - disp 1
                9.9672 130.37 76.948
               25.5541 145.96 80.562
## - wt
           1
## - hp
           1
               25.6715 146.07 80.588
##
## Step: AIC=69.83
## mpg \sim cyl + disp + hp + drat + wt + qsec + vs + am + gear
##
##
          Df Sum of Sq
                          RSS
                                 AIC
## - gear 2 5.0215 139.02 67.005
```

```
## - disp 1 0.9934 135.00 68.064
## - drat 1
             1.1854 135.19 68.110
## - VS
         1
              3.6763 137.68 68.694
## - cyl
          2
             12.5642 146.57 68.696
## - qsec 1 5.2634 139.26 69.061
## <none>
                      134.00 69.828
              11.9255 145.93 70.556
## - am
          1
## - wt
              19.7963 153.80 72.237
          1
              22.7935 156.79 72.855
## - hp
          1
##
## Step: AIC=67
## mpg \sim cyl + disp + hp + drat + wt + qsec + vs + am
##
##
         Df Sum of Sq
                         RSS
                                AIC
               0.9672 139.99 65.227
## - drat 1
## - cyl
          2
              10.4247 149.45 65.319
## - disp 1
              1.5483 140.57 65.359
## - vs
          1
              2.1829 141.21 65.503
## - qsec 1
             3.6324 142.66 65.830
## <none>
                      139.02 67.005
## - am
          1
              16.5665 155.59 68.608
## - hp
          1
              18.1768 157.20 68.937
## - wt
          1
              31.1896 170.21 71.482
##
## Step: AIC=65.23
## mpg \sim cyl + disp + hp + wt + qsec + vs + am
##
##
         Df Sum of Sq
                         RSS
                                AIC
## - disp 1
               1.2474 141.24 63.511
## - vs
         1
               2.3403 142.33 63.757
## - cyl
          2
              12.3267 152.32 63.927
## - qsec 1 3.1000 143.09 63.928
## <none>
                      139.99 65.227
## - hp
        1
              17.7382 157.73 67.044
## - am
        1 19.4660 159.46 67.393
## - wt
          1
              30.7151 170.71 69.574
##
## Step: AIC=63.51
## mpg \sim cyl + hp + wt + qsec + vs + am
##
         Df Sum of Sq
##
                         RSS
                                AIC
               2.442 143.68 62.059
## - qsec 1
## - VS
          1
                2.744 143.98 62.126
## - cyl
          2
               18.580 159.82 63.466
## <none>
                      141.24 63.511
## - hp
         1
              18.184 159.42 65.386
## - am
               18.885 160.12 65.527
          1
## - wt
          1
               39.645 180.88 69.428
##
## Step: AIC=62.06
## mpg \sim cyl + hp + wt + vs + am
```

```
##
          Df Sum of Sq
##
                          RSS
                                 AIC
## - VS
           1
                7.346 151.03 61.655
## <none>
                       143.68 62.059
           2
## - cyl
                25.284 168.96 63.246
## - am
           1
                16.443 160.12 63.527
## - hp
           1
                36.344 180.02 67.275
## - wt
                41.088 184.77 68.108
           1
##
## Step: AIC=61.65
## mpg \sim cyl + hp + wt + am
##
##
          Df Sum of Sq
                          RSS
                                 AIC
## <none>
                       151.03 61.655
                 9.752 160.78 61.657
## - am
           1
           2
                29.265 180.29 63.323
## - cyl
                31.943 182.97 65.794
## - hp
           1
## - wt
           1
                46.173 197.20 68.191
summary(best.model)
##
## Call:
## lm(formula = mpg \sim cyl + hp + wt + am, data = mtcars)
##
## Residuals:
##
       Min
                10 Median
                                3Q
                                       Max
## -3.9387 -1.2560 -0.4013 1.1253 5.0513
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                         2.60489 12.940 7.73e-13 ***
## (Intercept) 33.70832
               -3.03134
                           1.40728 -2.154 0.04068 *
## cyl6
## cyl8
               -2.16368
                           2.28425
                                    -0.947 0.35225
## hp
                           0.01369
                                    -2.345 0.02693 *
               -0.03211
## wt
               -2.49683
                           0.88559
                                   -2.819 0.00908 **
## amManual
                1.80921
                           1.39630
                                     1.296 0.20646
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.41 on 26 degrees of freedom
## Multiple R-squared: 0.8659, Adjusted R-squared: 0.8401
## F-statistic: 33.57 on 5 and 26 DF, p-value: 1.506e-10
t.test(mpg ~ am, data = mtcars)
##
    Welch Two Sample t-test
##
##
## data: mpg by am
## t = -3.7671, df = 18.332, p-value = 0.001374
## alternative hypothesis: true difference in means is not equal to 0
```

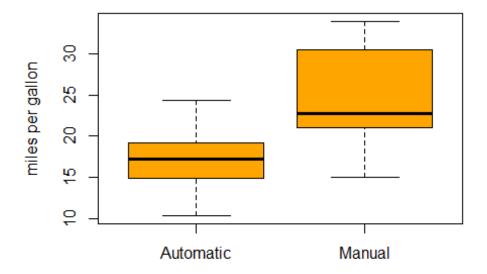


The boxplots show a difference in mpg depending on the type of transmission. The t-test output confirms that this difference is statistically significant (p-value < 0.05)

Appendix

Plots

```
boxplot(mpg ~ am, data = mtcars, col = "orange", ylab = "miles per gallon")
```



par(mfrow=c(2, 2)) plot(best.model)

