

SSN COLLEGE OF ENGINEERING, KALAVAKKAM
Department of Computer Science and Engineering
UCS1503 - Theory of Computation
Tutorial
Due Date 08.10.2022

1. Consider the grammar $G = (\{S, A\}, \{a, b\}, P, S)$, where P consists of
 $S \rightarrow aAS \mid b$
 $A \rightarrow SbA \mid ba$
Write the derivation and draw its equivalent parse tree for $w = abbbab$
2. If G is a grammar $S \rightarrow SbS \mid a$ prove that G is ambiguous.
3. Consider the grammar $S \rightarrow aS \mid aSbS \mid \epsilon$. This grammar is ambiguous. Show that the string aab has two
(a) Parse trees (b) Leftmost derivations (c) Rightmost derivations
4. For the grammar
 $S \rightarrow A1B$
 $A \rightarrow 0A \mid \epsilon$
 $B \rightarrow 0B \mid 1B \mid \epsilon$
Give left most and right most derivation for the string 00101 .
5. Construct CFG to generate $\{a^n b^n \mid n \in \mathbb{Z}^+\}$
6. Consider the alphabet $\Sigma = \{a, b, (,), +, *, ., \epsilon\}$. Construct a context free grammar that generates all strings in Σ^* that are regular expressions over the alphabet $\{a, b\}$.
7. Convert the given CFG to CNF
 $S \rightarrow a \mid aA \mid B$
 $A \rightarrow aBB \mid \epsilon$
 $B \rightarrow Aa \mid b$
8. Convert the given CFG to GNF
 $S \rightarrow XB \mid AA$
 $A \rightarrow a \mid BA \mid AB$
 $B \rightarrow b$
 $X \rightarrow a$
9. Construct PDA
(a) $L = \{a^n b^m c^n \mid m, n \geq 1\}$ Acceptance by emptying the stack
(b) $L = \{wcw^R \mid w \in (a/b)^*, c \in a/b/\epsilon\}$ Acceptance by reaching the final state
(c) $L = \{a^n b^m c^m d^n \mid m, n \geq 1\}$ Acceptance by emptying the stack and reaching the final state