

# Elementary Number Theory: Fermat's Theorem

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## 1 Fermat's Little Theorem and Pseudoprimes

- **Fermat's little theorem:** Let  $p$  be prime and suppose that  $p$  does not divide  $a$ . Then  $a^{p-1} \equiv 1 \pmod{p}$ . *Proof:*
- **Corollary:** If  $p$  is prime, then  $a^p \equiv a \pmod{p}$  for any integer  $a$ . *Proof:*
- A composite integer  $n$  is called a pseudoprime whenever  $n \mid 2^n - 2$ .
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## 2 Wilson's Theorem

- **Wilson's Theorem:** If  $p$  is prime, then  $(p-1)! \equiv -1 \pmod{p}$ . *Proof:*