

Realistic Face Image Generation from Sketch



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Abstract

Generating a face image from a sketch image given is a topic on which a lot of recent work is going on but still there has been lot of accuracy and perceptual issues with the generated image. It has a lot of applications in various fields especially criminal investigation and identification along with digital entertainment purposes. We have aimed at generating a face image which has higher accuracy perceptually. We have tried approach of using Conditional GAN's and making it an image translational task and have achieved considerable accuracy.

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Chapter 1

Introduction

Computer vision is a broad field of study that involves simulating the working of human eyes and understand the underlying processes. It makes computer to view and process objects in images and videos just like a human eye does.

Computer vision tasks include not only identifying objects in an image but identify all the objects and the underlying features like texture, shape, colour so as to completely describe an image. Neural networks and Convolutional neural networks form the backbone of computer vision systems.

This field is an exciting new field with everyday new and new inventions and progress being done. It has applications in wide number of fields including retail systems, behavioural tracking, manufacturing etc besides usual face recognition, generation, biometric and various other applications.

These project deal with a particular branch of computer vision that entails generating a human face image from a given sketch image of a human face. This falls under the category of image-to-image translation where we are trying to find some kind of mapping between two images.

This field of work has application in various fields including criminal identification, digital entertainment purposes. There has been various models and methods to generate image from a sketch with varied degree of success. We have approached deep learning models to target our problem with a aim to better perceptual quality of the generated image.

1.1 Problem Definition and Objective

Generation of a realistic face image of a human being from a given sketch drawn of a human face.

Our aim is to generate corresponding human face image with significant accuracy and which is perceptually close to ground truth face image from the sketch image.



Fig 1.1 Sketch image and its corresponding ground truth real face image

As shown in above figure are the sketch image and the real ground truth face image of the human being. Our aim is to generate an image which is as close as possible to the given ground truth image and is perceptually accurate.

1.2 Motivation

In various fields generating a face image from a sketch image can be of immense help. One such is in field of criminal identification. Many situations arise where it becomes difficult to capture photo of a criminal suspect due to insufficient CCTV cameras in a location and other time related constraints. In



Fig1.2 A police sketch of a criminal suspect

such situations we have to depend on memory of witnesses and his description. From such a description a sketch is drawn by an expert and on its basis, investigation is performed. If we can generate a realistic perceptually accurate face image of the person from the sketch it can help in criminal identification and tracking and make the overall investigation more accurate and efficient. Also, it has application where robots draw human faces and for educational and digital entertainment purposes.

1.3 Solution Approach

The problem falls in the category of image-to-image translation where recently various Deep Learning Models are being applied to varied success. We decided to apply Generative Adversarial Model (GAN) as it working is similar to our problem. GAN generates a data distribution similar to an existing data distribution from a random distribution. We have applied GAN in the conditional setting which helps in controlling the input and in our case, condition is a particular ground truth face image. Our aim is to generate a mapping between the input sketch image and the output face image and training it to reduce losses and increase accuracy.

1.4 Tools and Technologies used

The following tools and technologies were used for implementation purposes.

-NumPy

-Pandas

-OpenCV

-Pytorch

-Google Colab

-Python

Chapter 2

Literature Review

There has been a lot of work done and also going on in this problem. Earlier works include traditional non-Deep Learning based models as well as recent works based on Deep learning. We have discussed here some of the relevant methods and work done.

Existing methods can be classified into three main categories on the basis of: subspace learning, sparse representation, and Bayesian inference. Subspace learning mainly refers to linear subspace-based methods (e.g., principal component analysis, or PCA), and nonlinear subspace methods such as manifold learning-based methods (e.g., local linear embedding). Tang and Wang [1], proposed a linear face sketch synthesis method based on PCA called eigen sketch transformation. They assumed that a source input photo and the target output sketch shared the same projection coefficients obtained from the PCA procedures. The coefficients are first obtained by projecting the input photo onto the training photos. The target sketch is then synthesized from a linear combination of training sketches weighted by the obtained projection coefficients. Tang and Wang then proposed an improved method by separating the shape from the texture. The eigen sketch transformation method is applied to shape and texture to compute the target shape and texture, respectively. The synthesized shape and texture are fused to obtain the final target sketch.

Li et al. [2] proposed a hybrid subspace method for face photo synthesis by concatenating the training sketches and photos. This type of methods could hardly synthesize a realistic sketch, especially when the hair region was included. As the mapping between sketches and corresponding face photos are not linear.

Further improvement was done on these linear models by same authors by using concept of LLE. In this case images are divided into patches which overlap with each other. From every photo patch, X photo patches are selected from the training set according to the Euclidean distance metric. At the same time, the corresponding X sketch patches are taken as the candidates. The weights for combining the X candidates are calculated by minimizing the least square of the reconstruction residual between the test photo patch and its K nearest neighbours. The target sketch patch is generated from a linear combination of those K candidates. A degree of blurring is seen as patches are fused with an averaged overlapping area to form the final target sketch.

Another approach is of Bayesian inference-based methods. It includes embedded hidden Markov model (E-HMM)-based and Markov random fields (MRF)-based methods. Gao et al. [3] approached by doing the mapping between sketches and images by using E-HMM. A face is decomposed into five components (forehead, eye, nose, mouth, and chin) and sub components (sub components in each components). Joint training is done by assuming the sketch and the photo have the same transition probability matrix. Further improvements were incorporated by applying method in a local patch-based form which generated more details. Above methods didn't take into account the neighbouring relation between overlapping patches. Taking this into account many more methods based on MRF were also proposed

All the above discussed methods synthesize photo from the inductive learning perspective. Although they are able to do well in generating and synthesizing images well but in many cases showed high losses for particular set of test samples. Minimizing the empirical loss for training samples was the root cause behind it. But using transductive learning algorithms in place of inductive learning algorithms this problem of high losses were solved by incorporating the given test samples into the learning process. In this proposed method authors adopted a transductive face sketch-photo synthesis method. Face images in frontal pose with normal lighting and having neutral expression are main area of focus. Sketches and photos were divided into even patches with

some overlap between neighbouring patches. A probabilistic graphic model is used to map the relation between sketch and photo patch pairs. The reconstruction fidelity of the input sketch and the synthesis fidelity of the target output photo is taken into account. Additionally, it is seen that, the relation between neighbouring sketch patches acts as regularizer. The minimum error boundary is found out by applying a min cut algorithm. This method can generate both face images from sketches and vice versa as both are symmetric to each other.

Jian Zhao et al in their proposed model, treat the problem as a problem of face hallucination reconstruction. They proposed an image translation network with generated adversarial network (GAN). Accuracy is improved by adding additional attribute features of face. The generator has a feature extracting network and a down sampling up sampling network, both networks use skip-connection to reduce the number of layers without affecting network performance. The discriminator checks whether faces generated are how much accurate. This model differs from other most attribute-embedded networks in feature extraction phase. Sketch images and attributes are fused perceptually in this method.

Chapter 3

Prerequisites

3.1 Convolutional Neural Network.

A **Convolutional Neural Network (CNN)** [5] is a Deep Learning algorithm which takes in an input image, assign weights and biases to various objects in the image and is able to differentiate one from the other. The pre-processing steps in CNN is negligible compared to other classification algorithms based on machine learning(primitive). While in such primitive methods feature engineering is needed for learning the filters, in case of CNN the model itself learns the filters and other features itself through thorough training process.

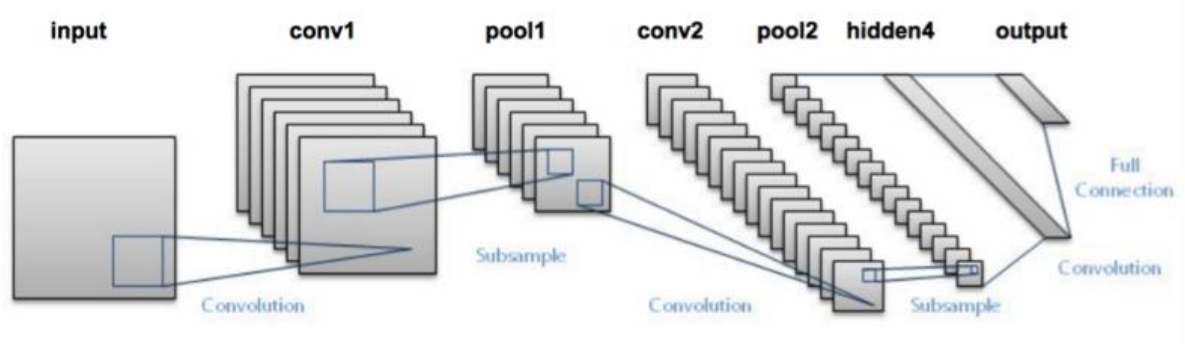


Fig3.1 Structure of a typical CNN with all the layers.

The architecture of a CNN is similar to that of the human brain. Connectivity patterns of neurons in the human brain and organization of the Visual Cortex is the inspiration behind CNN architecture. Individual neurons respond to stimuli only in a particular region of the visual field known as the receptive field and for others don't respond. Entire visual area is covered by collection of such fields. In the same manner a CNN works.

A CNN **captures the spatial and temporal dependencies** in an image through the application of suitable filters. It performs better on a image dataset compared to normal Deep Neural network as the complexity of the models is reduced because of reduction in overall number of parameters. It is made possible by use of weight sharing and sparse connectivity which reduces lots of parameters in the network.

The role of the CNN is to transform the images into a form which is easier to work upon, without losing relevant information about the images which are important for getting an accurate prediction.

A CNN consists of an input and an output layer, as well as multiple hidden layers. The hidden layers of a CNN consist of convolutional layers, non-linear layers i.e., activation function (e.g: ReLU,tanH), max pooling layers, fully connected layers and normalization layers.

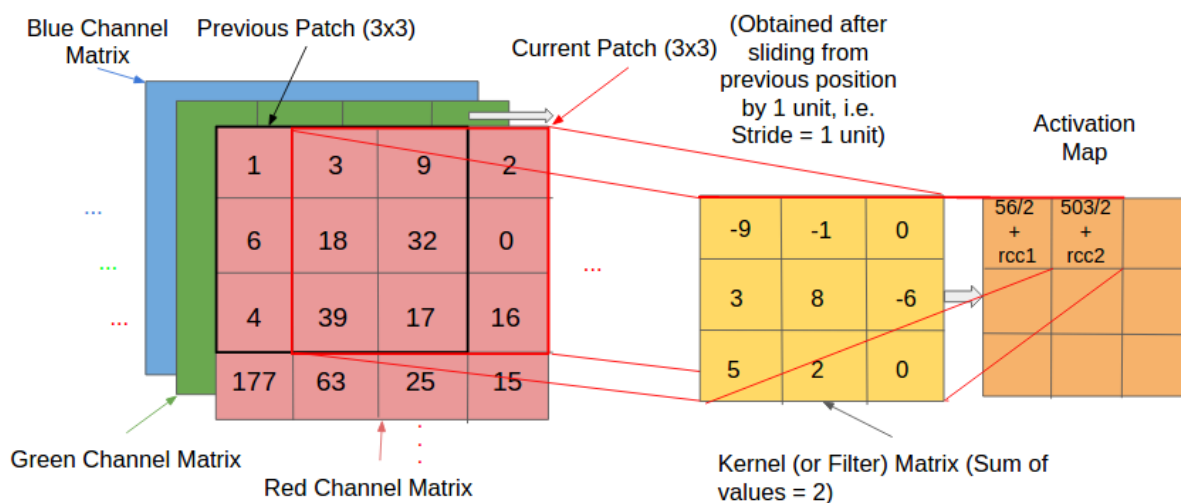


Fig. 3.2 An example of a convolution operation in CNN in convolutional layer

Convolution operation occurs with a filter slides over the input image pixel and does the convolve operation and stores the most important features of the input information. It is further pruned using a max pooling layer. Information then passes through an activation layer to add non linearity. This same process can be repeated again or not depending on the architecture. Then a fully connected layer and at end the output

layer. Training is done on whole model to reduce loss by backpropagation and its many variants like Adam optimiser.

3.2 Generative Adversarial Network (GAN)

GAN's[6][7] are deep neural networks which consists of two sub networks competing against each other in zero sum fashion to produce a data distribution. consists of two neural networks fighting with each other to generate a probability distribution. The neural networks can be DNN, CNN. The two networks are called generator and discriminator. By mimicking an input probability distribution from a given random distribution, the generator generates a distribution. Discriminator now checks how close are the two distributions by checking how close the generated distribution is close to the actual distribution. Training is done then to both generator and discriminator in zero-sum manner to reduce the error between actual distribution and generated distribution

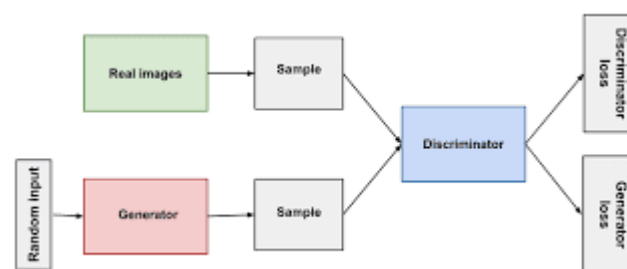


Fig 3.3. A model of simple vanilla GAN

GANs are a rapidly transforming field, giving great results in the domain of generative problems. It has been able to generate realistic examples across a range of problem domains, especially in image-to-image translation tasks such as translating photos and in generating realistic photos of objects, scenes, and people that are even tough for humans to tell whether they are real or fake.

3.3 Conditional Generative Adversarial Networks

GAN's have various number of variations and among them Conditional Generative Adversarial Network(cGAN) [8] is one.

GANs are capable of producing examples ranging from simple handwritten digits to realistic images of human faces. However, we cannot control the output of our GAN i.e., we cannot specify any of the characteristics of the output samples the GAN would generate. For example, the GAN could synthesize handwritten digits with high degree of accuracy, but we cannot be sure which number will be generated at a time say, for example it can be number 7 or number 9 or anything at any given time.

On simple datasets like the MNIST, in which examples belong to only one of 10 classes, this concern may seem trivial. If, for instance, our goal is to produce the number 9, we can just keep generating examples until we get the number we want. On more complex data-generation tasks, however, the domain of possible answers gets too large for such a brute-force solution to be practical.

The ability to decide what kind of data will be generated opens the door to a vast array of applications.

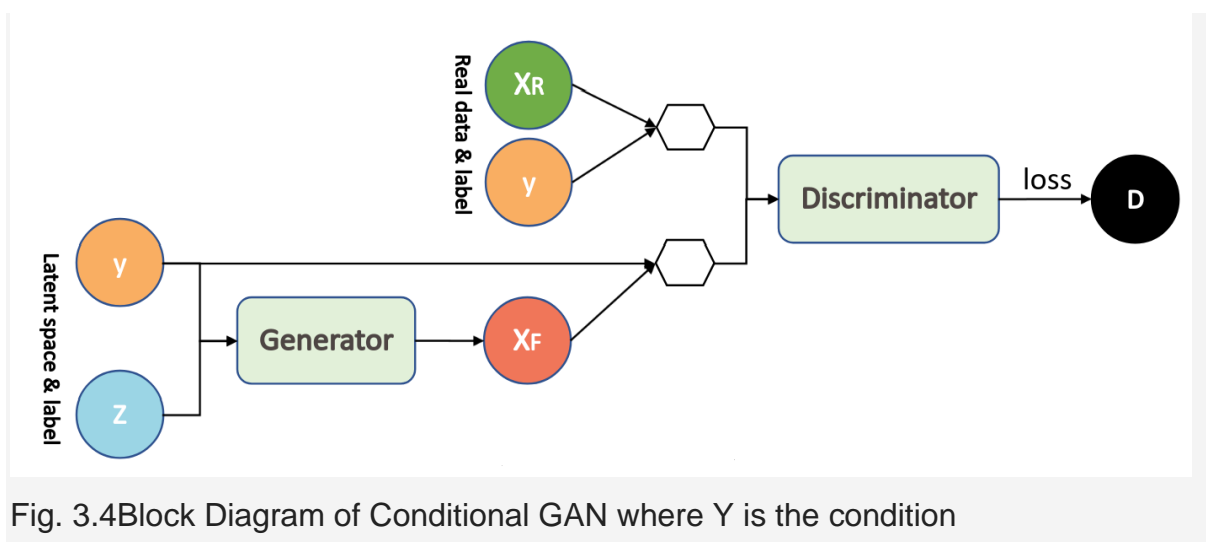


Fig. 3.4 Block Diagram of Conditional GAN where Y is the condition

Architecture of cGAN:

CGAN Generator

The Generator uses the noise vector z and the label y to synthesize a fake example $G(z, y) = x^*|y$ (read as “ x^* given that, or conditioned on, y ”). The goal of this fake example is to look (in the eyes of the Discriminator) as close as possible to a real example for the given label.

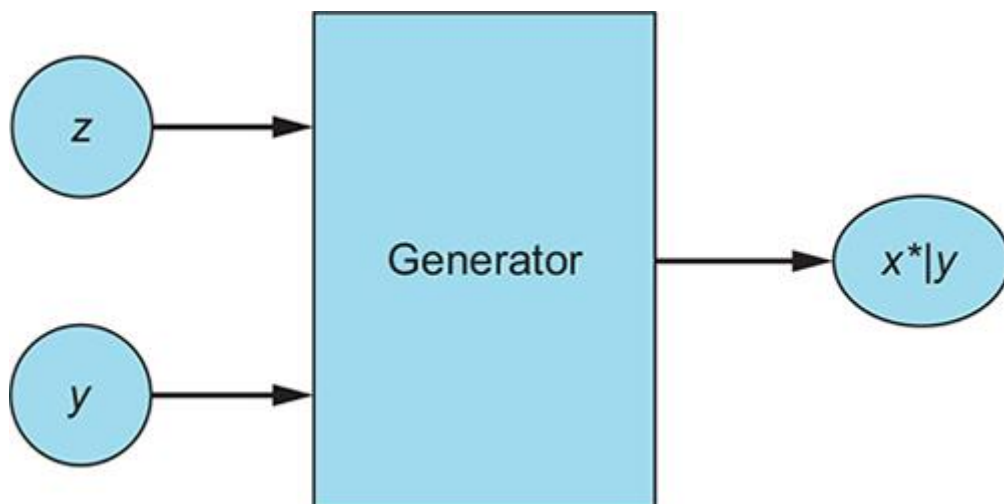


Fig 3.5 Block diagram showing working of generator of cGAN

CGAN Discriminator

The Discriminator receives real examples with labels (x, y) , and fake examples with the label used to generate them, $(x^*|y, y)$. On the real example-label pairs, the Discriminator learns how to recognize real data and how to recognize matching pairs. On the Generator-produced examples, it learns to recognize fake image-label pairs, thereby learning to tell them apart from the real ones.

The Discriminator outputs a single probability indicating its conviction that the input is a real, matching pair. The Discriminator's goal is to learn to reject all fake examples and all examples that fail to match their label, while accepting all real example-label pairs.

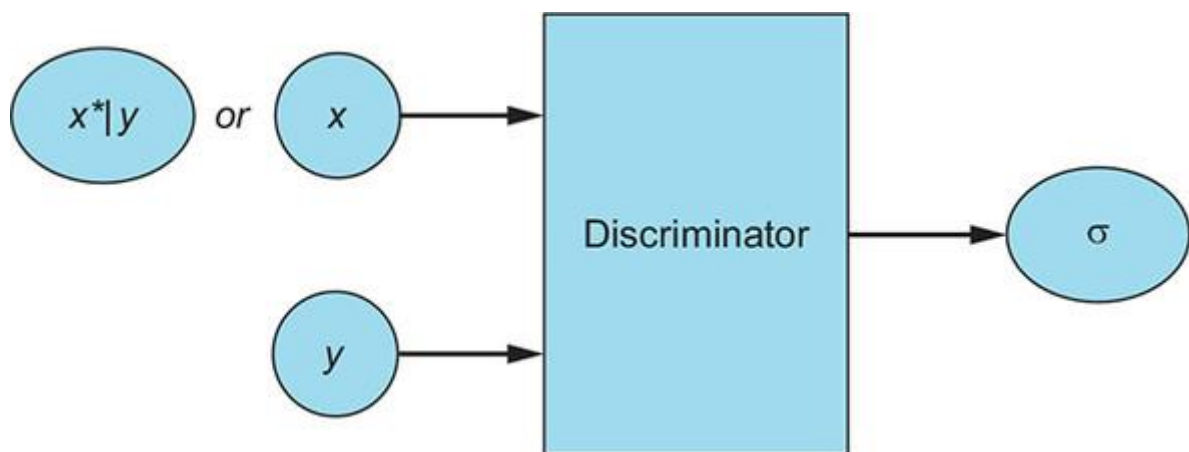


Fig3.6 Block diagram showing working of discriminator of cGAN

GAN's are trained similar to any normal deep neural network but here the generator and discriminator are separately trained which in combination trains the GAN. Optimisers like Adam are used which are based on backpropagation techniques.

Chapter 4

Project Implementation

4.1 Dataset

The dataset is sourced from face -sketch image pairs from CUHK database. CUHK stands for Chinese University of Hong Kong. CUHK Face Sketch database (CUFS) is for face sketch synthesis and face sketch recognition purposes. It consists of labelled sketch images of a human face and along with its corresponding ground truth image collected from two sources. It includes 188 faces from the Chinese University of Hong Kong (CUHK) student database and 139 faces from the AR database. All the sketches are drawn by an artist based on a photo taken in a frontal pose, under normal lighting condition with a neutral expression. The dataset is divided into training, test and validation set in the ratio 70:25:5 for our problem.

4.2 Experimental Configuration

Data Pre-processing:

- All images are resized to 256x256

- Input sketch image and ground truth Face image are combined by concatenating horizontally to form a single image. Above process is followed as a requisite for Conditional GAN. The combined image is then fed to the model.

4.3 Network Architecture

1) Using Conditional GAN to perform sketch to image translation.

The model consists of a generator to generate images and a discriminator to verify whether they are coming from fake or real source.

Here for a data, combined image of input image(sketch) and ground truth image is fed to the generator. The ground truth image acts as the conditional component.

2) Generator is using a U-net architecture[9]. It consists of an encoder-decoder network. Here the $256 \times 256 \times 3$ input image is fed which goes through layers of down sampling followed by up sampling to generate the face image. Here i th layer of encoder concatenated with $n-i$ th layer of decoder where n is total no of layers in encoder part. All ReLUs in the encoder is leaky, with slope 0.2, while ReLUs in the decoder is not leaky.

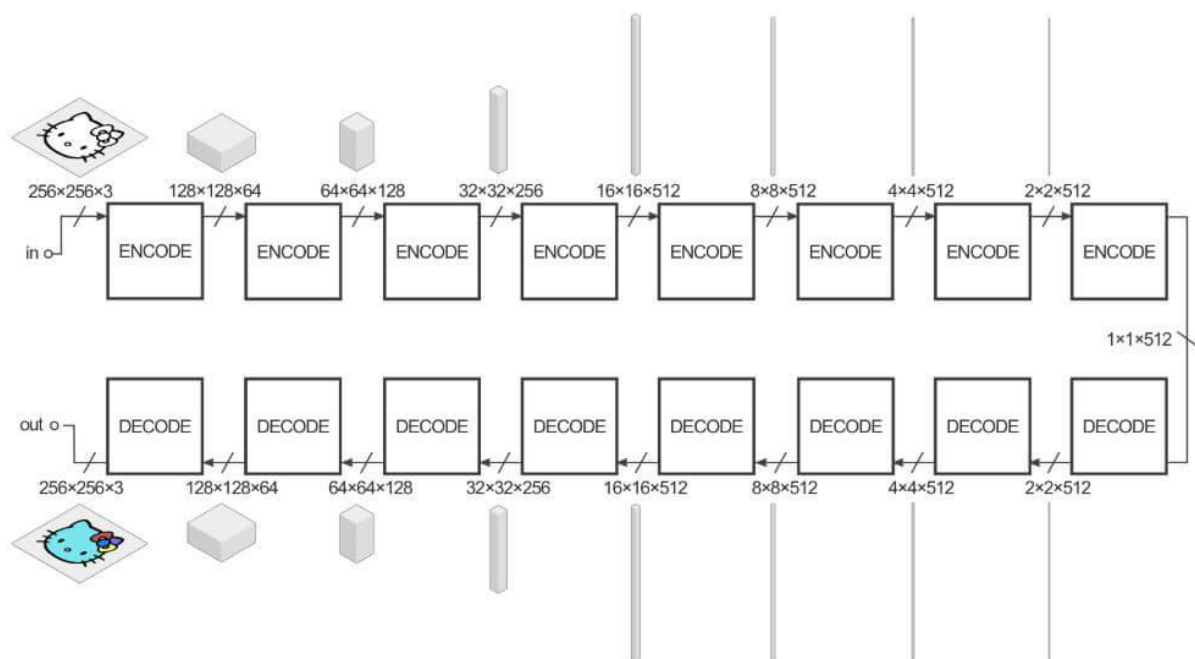


Fig4.1. Generator Architecture- consisting of encoder decode network

3) The generated image, input image pair are then compared with discriminator to check how close the generated image is to the target image.

Discriminator in these case uses the method of PatchGAN where instead of looking at the whole image at once, it checks the structure in patches of $N \times N$. The discriminator classifies each $N \times N$ patch in an image is real or fake and this operation is done on the whole image and the average all responses generate the final output of Discriminator. A convolution operation is applied after the last layer to map to a 1-dimensional output, followed by a Sigmoid function. All ReLUs used are leaky, with slope 0.2

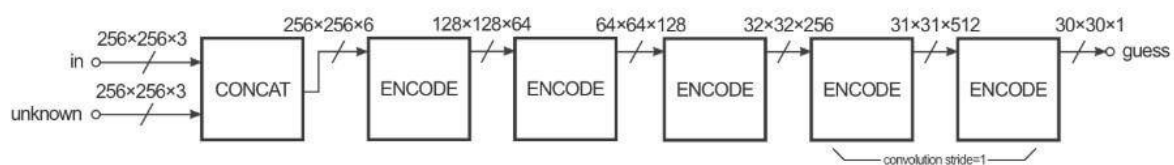


Fig4.2 Discriminator Architecture

3) Loss functions:

Normal adversarial losses along with L1 norm loss[13] is done on the images generated by generator to check how much it differs from target image.

L1 norm loss calculates the loss pixel wise in the two images and sums up the loss.

4) Training:

For training mini batch SGD is used alongside Adam Solver[14].

The model is run for 200 epochs using a pre-trained model on Google Colab environment using their GPU.

Chapter 5

Results

5.1 Accuracy

The face images generated are fairly accurate and can be easily identified from a perceptual viewpoint. Here given below is an example of the input sketch, generated image and the ground truth face image



Fig5.1 Input Sketch, Generated Face image and Ground truth image

5.2 Experiments

Two standard image similarity metrics were used to check the accuracy of our result. The first test is Fréchet Inception Distance (FID) between the ground truth image and the generated images. The second one is another such similarity measurement metric

Feature Similarity Index (FSIM). The experiment was performed gradually over the dataset taking on random 10% of the dataset and gradually increasing the dataset.

5.2.1 Database Description Experiments are performed on the test results generated. We conducted experiments publicly available dataset: the CUHK Face Sketch database provided by Chinese University of Hong Kong.

- The CUFS dataset consists of 327 sketches of face drawn by an artist and corresponding face photo from following two datasets:

- the CUHK student dataset [54] (188 persons),
- the AR dataset [55] (139 persons),

Female photos: 29

Male Photos:53

Dataset partition. Dataset is partitioned into training, testing and validation sets in the ratio 75:20:5. Experiments are performed on the test set consisting of 82 images.

Pre-processing. Using existing methods, all face images (photos and sketches) are geometrically aligned based on three points: two eye centers and the mouth center. The images are then cropped to the size of 256X 256 pixels. The input sketch image and the ground truth image are concatenated and then fed into the model.

Of the test dataset randomly 10% is chosen and the experiment is performed. Then same process performed on 20% and repeated until experiment is performed on the whole dataset.

FID: Fréchet Inception distance (FID) used to evaluate the realism and similarity between the generated face photos and ground truth image. FID measures the Earth-Mover Distance (EMD) between the distribution of generated samples and that

of the ground-truth samples, in the feature space. The 2048-dimensional feature of the Inception-v3 network pre-trained on ImageNet is used for the experiment. Lower FID values means closer distances between the generated face image and the ground truth images.

Experimental Results

FID

Percentage of Dataset	FID Score obtained
10	129.8941362722024
20	96.96407251277694
30	101.5418828753562
40	102.19270259222989
50	106.29098120348479
60	103.25030773186066
70	103.39977730588271
80	98.59174647477053
90	94.77772414677688
100	93.38565774468366

Fig5.1. FID scores obtained on various sized data of result.

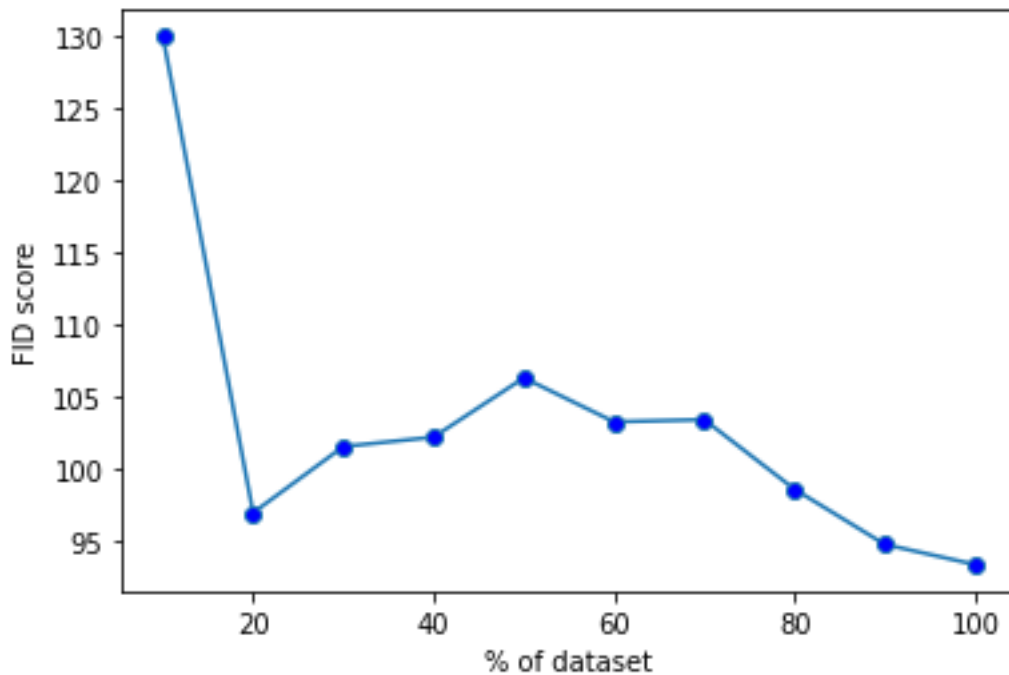


Figure 5.2 graphical representation of the experiment with x-axis representing the %of the dataset and y-axis representing the score achieved.

FSIM

Feature Similarity Index Metric is another prevalent metric to asses similarity between a synthesized image and the corresponding ground-truth image. Here the phase congruency (PC) and the image gradient magnitude (GM) is employed as features, and the feature similarity between a test image and its corresponding reference image is employed as the quality index. FSIM is good benchmark for evaluating quality of natural images and is frequently used, still it is of low consistency from perceptual similarity between two images .

Experimental Results

Percentage of Dataset	FSIM score
10	0.513098781
20	0.470293226
30	0.501717344
40	0.48682433
50	0.48682433
60	0.486779394
70	0.5027147
80	0.516639213
90	0.486637213
100	0.532996056

Figure 5.3 FSIM scores obtained on various sized data of result

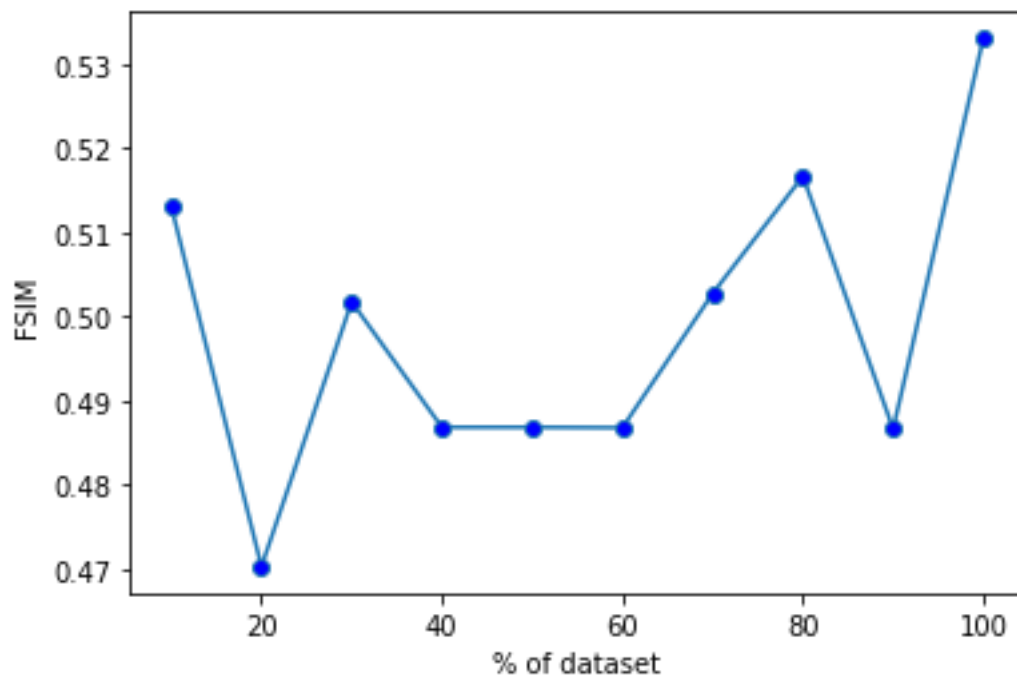


Figure 5.4 represents the graphical representation of the experimental results.

x-axis is the %of dataset and y-axis represents the FSIM score achieved.

5.3 Analysis and Discussions

As we can see from the figures of FID there is a steady decrease in FID score with increase in size of dataset and there are some variations which is due to the randomness of the data chosen. Lowest score 93 is achieved which is quite good. If larger dataset is available then we think even better score can be achieved.

In the other experiment of FSIM the graphical data shows a lot of variations and its it tough to draw any conclusions. As dataset is chosen randomly that also impacts the experiment. But we can see that for 80% of dataset and when complete dataset is used a higher score of 0.535 and 0.555 is achieved. Considerable amount of similarity has been achieved from this experiment. As this metric is for evaluating the quality degradation of photos due to blurring, noise, or compression, and is not much suitable for evaluating perceptual similarity between two images and so higher value of FSIM will lead to lesser perceptual accuracy between the images.

This shows that our methods have significantly improved the realism of the synthesized sketches

Comparisons

Our method is compared with previous existing methods on the above two parameters of FID and FSIM tests with similar experimental settings as ours.

Criterion	Dataset	Traditional Methods	Deep Methods	Our Method
FID	CUFS	106.9	99.7	93
FSIM	CUFS	69.6	69.3	53.5

Fig5.5 Comparison values of experiments with other methods

We can see that our method performs better in FID test compared to older traditional methods and other Deep Learning based methods. In case of the other test FSIM our methods performs considerably but not as good as other methods.

Chapter 6

Conclusion

6.1 Conclusion

The model has performed quite well in generating realistic face images which are quite accurate even in loose comparison between ground truth images and fake generated images.

The model could work better with if dataset with more labelled images are found.

Certain deformities were found in eyes which we feel can be rectified with addition of component-based checking.

6.2 Future Scope

There is a lot of scope of future work and adding other features. One primary addition is adding feature of age detection in the generated images. For example, for a missing person whose sketch is available, his face can have certain changes in features with age. Specially for a child his/her face can have considerable changes with passage of time. So, our model should accordingly generate the face image taking the age or time elapsed in cognisance.

Chapter 7

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