



CONVERGENT SEQUENCE

Mathematics-III (Differential Calculus)

Code: BSC-301

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CONTENT

INTRODUCTION

- • What is a sequence ?
- • What is a convergent sequence ?
- **PROPERTIES OF CONVERGENT SEQUENCE**
- • A few basic theorems
- **APPLICATIONS**
- ***REFERENCE***

SEQUENCE

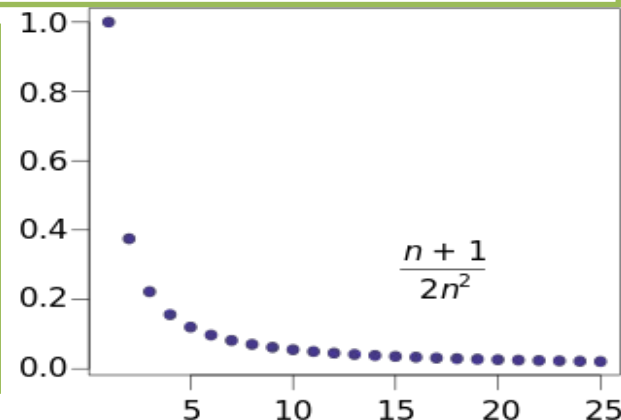
- ✗ A collection S of real numbers is said to be a *sequence of numbers* if corresponding to every positive integer n , there exists a unique element a_n of S .
- ✗ *Example:* $\{5, 7, 9, 11\}$ is *finite* sequence.
 $\{1, \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \dots\}$ is *harmonic* sequence.

CONVERGENT SEQUENCE

➔ A sequence $\{a_n\}$ is said to be convergent if $\lim_{n \rightarrow \infty} a_n = L$ is finite.

Example: In $\{1, 1/3, 1/3^2, \dots, 1/3^n, \dots\}$, the sequence $\{a_n\}$ where $a_n = 1/3^n$, is convergent since $\lim_{n \rightarrow \infty} a_n = L$, $L=0$ is finite.

➔ A convergent sequence determines its limit uniquely. Every convergent sequence is bounded. A monotonic increasing or decreasing sequence which is bounded above or below respectively is said to be convergent.



APPLICATIONS

Convergence is a concept used throughout calculus in the context of limits, sequences, and series.

A convergent sequence is one in which the sequence approaches a finite, specific value.

convergence is used to show that an algorithm is correct or behaves like it should, e.g. in machine learning and probabilistic algorithms.

REFERENCES



The information in this presentation has been taken from the book
ENGINEERING MATHEMATICS Volume IIIA by B.K. Pal , K. Das.

[analysis - Applications of Convergence of a series in Algorithms - Mathematics Stack Exchange](#)