

1. Determine whether each of these functions is a bijection. **If it is a bijection, prove it; if not a bijection, give a counterexample.**

1.1 $f : \mathbb{R} \rightarrow \mathbb{R}: f(x) = 7x - 2$

1.2 $f: \mathbb{R} \rightarrow \mathbb{Z}: f(x) = \lfloor x \rfloor$ (that is, $f(x) = \text{floor}(x)$)

1.3 $f: \mathbb{R} \rightarrow \mathbb{R}: f(x) = x^2$

1.4 $f: \{1,2,3\} \rightarrow \{2\}: \{(1,2), (2,2), (3,2)\}$

1.5 $f: \{1,2,3\} \rightarrow \{1,2,3\}: \{(1,2), (1,3), (2,1), (2,2)\}$

2. Show that $2^x + 17$ is $O(3^x)$.

3. Let k be a positive integer. Show that $1^k + 2^k + \dots + n^k$ is $O(n^{k+1})$.

4. Compute formula for

$$2 + \sum_{i=1}^n \left(3 + \sum_{j=i}^n 6 \right)$$