

1. Determine whether each of these functions is a bijection. **If it is a bijection, prove it; if not a bijection, give a counterexample.**

1.1  $f : \mathbb{R} \rightarrow \mathbb{R}$ :  $f(x) = 7x - 2$

1.2  $f : \mathbb{R} \rightarrow \mathbb{Z}$ :  $f(x) = \lfloor x \rfloor$  (that is,  $f(x) = \text{floor}(x)$ )

1.3 f:  $\mathbb{R} \rightarrow \mathbb{R}$ :  $f(x) = x^2$

1.4 f:  $\{1,2,3\} \rightarrow \{2\}$ :  $\{(1,2), (2,2), (3,2)\}$

1.5 f:  $\{1,2,3\} \rightarrow \{1,2, 3\}$ :  $\{(1,2), (1,3), (2,1), (2,2)\}$

2. Show that  $2^x + 17$  is  $O(3^x)$ .

3. Let  $k$  be a positive integer. Show that  $1^k + 2^k + \dots + n^k$  is  $O(n^{k+1})$ .

4. Compute formula for

$$2 + \sum_{i=1}^n \left( 3 + \sum_{j=i}^n 6 \right)$$