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$\forall a$  If  $a^2$  is even, then  $a$  is even.

Proof by Contradiction:

Suppose  $a^2$  is even and  $a$  is not even.

Then  $a^2$  is even and  $a$  is odd.

Since  $a$  is odd, there is an integer  $c$  which  $a = 2c + 1$

Then  $a^2 = (2c+1)^2 = 4c^2 + 4c + 1 = 2(2c^2 + 2c) + 1$ , so  $a^2$  is odd.

Thus  $a^2$  is even and  $a^2$  is odd, a contradiction.

2. Proof  $A \cap B \subseteq A$  by contradiction.

Proof

Proof by contradiction.

We know that " $A \cap B \subseteq A$ " means " $\forall x \in A \text{ and } x \in B \rightarrow x \in A$ "

We assume that " $\forall x \in A \text{ and } x \in B \text{ and } x \notin A$ "

$x \in A \text{ and } x \notin A$ , a contradiction.

$\therefore (A \cap B) \subseteq A$  \*