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$\forall a$ If a^2 is even, then a is even.

Proof by Contradiction:

Suppose a^2 is even and a is not even.

Then a^2 is even and a is odd

Since a is odd, there is an integer c which $a = 2c + 1$

Then $a^2 = (2c + 1)^2 = 4c^2 + 4c + 1 = \underline{2(2c^2 + 2c) + 1}$, so a^2 is odd.

Thus a^2 is even and a^2 is odd, a contradiction.

2. Proof $A \cap B \subseteq A$ by contradiction.

Proof by contradiction.

We know that " $A \cap B \subseteq A$ " means " $\forall x, x \in A \text{ and } x \in B \rightarrow x \in A$ "

We assume that " $\forall x$ $x \in A$ and $x \in B$ and $x \notin A$
 $x \in A$ and $x \notin A$, a contradiction.

$\therefore (A \cap B) \subseteq A$ \checkmark