

Tutorial 6 (week 7)

Temporal difference learning

Given the following situation:

3				+ 1
2				- 1
1	Start			
	1	2	3	4

Task: Use the temporal difference learning algorithm to compute the utilities when using the following trial:

Trial n=1: (1,1) -> (1,2) -> (1,3) -> (1,2) -> (1,3) -> (2,3) -> (3,3) -> (4,3)

Rewards: $R(s) = -0.04$ for all states s which are not a goal state.

Learning rate: $\alpha(n) = 60/(59+n)$, where n is a counter which counts trials (here we have the first trial. Hence: $n=1$).

Discount factor: Assume that $\gamma = 1$

The temporal difference algorithm is given as follows:

```

function Passive-TD-Agent(percept) returns an action
inputs: percept, a percept indicating the current state  $s'$  and reward signal  $r'$ 
variable:  $\pi$ , a fixed policy
              $U$ , a table of utilities, initially empty
              $Ns$ , a table of frequencies for states, initially zero
              $s, a, r$ , the previous state, action, and reward, initially null
if  $s'$  is new then  $U[s'] \leftarrow r'$ 
if  $s$  is not null then
    increment  $Ns[s]$ 
     $U[s] \leftarrow U[s] + \alpha(Ns[s])(r + \gamma U[s'] - U[s])$ 
if Terminal[ $s'$ ] then  $s, a, r \leftarrow \text{null}$  else  $s, a, r \leftarrow s', \pi[s'], r'$ 
return  $a$ 
end
  
```

Homework:

- Repeat the algorithm for 2 more iterations by using trial 1.
- Continue the above exercise by using a second trial:
(1,1) -> (1,2) -> (1,3) -> (2,3) -> (3,3) -> (2,3) -> (3,3) -> (4,3)
- Continue the above exercise by using a third trial:
(1,1) -> (2,1) -> (3,1) -> (3,2) -> (4,2)