

General Physics I

Classnotes

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02/08/2016

February 08

1 Vector

$$\begin{array}{ll}\hat{i} & \text{unit vector in } x \text{ direction} \\ \hat{j} & \text{unit vector in } y \text{ direction} \\ \hat{k} & \text{unit vector in } z \text{ direction}\end{array}$$

A unit vector has length 1 unit.

$$|\hat{i}| = 1$$

$$|\hat{j}| = 1$$

$$|\hat{k}| = 1$$

$$A_x = 4$$

$$A_y = 3$$

$$\vec{A} = 4\hat{i} + 3\hat{j}$$

Example:

$$\vec{A} = 8 \text{ m} @ 30^\circ$$

Find A_x , A_y

$$\begin{aligned}A_x &= A \cos \theta_A \\&= (8 \text{ m}) \cos(30^\circ) \\&= 6.928 \text{ m} \\A_y &= A \sin \theta_A \\&= (8 \text{ m}) \sin(30^\circ) \\&= 4.00 \text{ m} \\\vec{A} &= (6.928 \text{ m})\hat{i} + (4.00 \text{ m})\hat{j}\end{aligned}$$

Example:

$$\begin{aligned}\vec{B} &= 12 \text{ m}@140^\circ \\B_x &= B \cos \theta_B \\&= (12 \text{ m}) \cos(140^\circ) \\&= -9.19 \text{ m} \\B_y &= B \sin \theta_B \\&= (12 \text{ m}) \sin(140^\circ) \\&= 7.71 \text{ m} \\\vec{B} &= (-9.19 \text{ m})\hat{i} + (7.71 \text{ m})\hat{j}\end{aligned}$$

Example:

$$\vec{C} = 4\hat{i} + 3\hat{j}$$

Find c , θ_C

$$\begin{aligned}
C &= \sqrt{C_x^2 + C_y^2} \\
&= \sqrt{4^2 + 3^2} \\
&= \sqrt{16 + 9} \\
&= \sqrt{25} \\
&= 5.0 \\
\tan \theta_C &= \frac{C_y}{C_x} = \frac{3}{4} = 0.75 \\
\theta_C &= \tan^{-1}(0.75) \\
&= 36.87^\circ \\
\vec{C} &= 5.0@36.87^\circ
\end{aligned}$$

Example:

$$\begin{aligned}
\vec{D} &= -9\hat{i} + 12\hat{j} \\
D &= \sqrt{D_x^2 + D_y^2} \\
&= \sqrt{(-9)^2 + 12^2} \\
&= \sqrt{81 + 144} \\
&= \sqrt{225} \\
&= 15 \\
\tan \theta_D &= \frac{D_y}{D_x} = \frac{12}{-9} = -\frac{4}{3} \\
\theta_D &= \tan^{-1}\left(-\frac{3}{4}\right) \\
&= -53.13^\circ + 180^\circ \\
&= 126.87^\circ \\
\vec{D} &= 15.0@126.87^\circ
\end{aligned}$$

Rule: when x -component is negative:

$$\theta = \theta + 180^\circ \quad (1)$$

$$\begin{aligned}\vec{R} &= \vec{A} + \vec{B} \\ \vec{R}_x &= \vec{A}_x + \vec{B}_x \\ \vec{R}_y &= \vec{A}_y + \vec{B}_y\end{aligned}\tag{2}$$

Example:

$$\begin{aligned}\vec{A} &= 10 \text{ @ } 37^\circ \\ \vec{B} &= 12 \text{ @ } -60^\circ\end{aligned}$$

Find magnitude and direction of $\vec{R} = \vec{A} + \vec{B}$

$$\begin{aligned}A_x &= A \cos \theta_A \\ &= 10 \cos(37^\circ) \\ &= 7.98 \\ A_y &= A \sin \theta_A \\ &= 10 \sin(37^\circ) \\ &= 6.02\end{aligned}$$

$$\begin{aligned}B_x &= B \cos \theta_B \\ &= 12 \cos(-60^\circ) \\ &= 6.00 \\ B_y &= B \sin \theta_B \\ &= 12 \sin(-60^\circ) \\ &= -10.39\end{aligned}$$

$$\begin{aligned}
\vec{R}_x &= \vec{A}_x + \vec{B}_x \\
&= 7.98 + 6.00 \\
&= 13.98 \\
\vec{R}_y &= \vec{A}_y + \vec{B}_y \\
&= 6.02 + (-10.39) \\
&= -4.37
\end{aligned}$$

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$$\begin{aligned}
\vec{R} &= 13.98\hat{i} - 4.37\hat{j} \\
R &= \sqrt{(13.98)^2 + (-4.37)^2} \\
&= 14.6 \\
\tan \theta_R &= \frac{R_y}{R_x} = \frac{-4.37}{13.98} = -0.313 \\
\theta_R &= \tan^{-1}(-0.313) = -17.4^\circ \\
\vec{R} &= 14.6 @ -17.4^\circ
\end{aligned}$$

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