

408D Course Guide

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1 Derivatives

$$\frac{d}{dx} \sin(x) = \cos(x)$$

$$\frac{d}{dx} \cos(x) = -\sin(x)$$

$$\frac{d}{dx} \tan(x) = \sec^2(x)$$

$$\frac{d}{dx} \sec(x) = \sec(x) \tan(x)$$

$$\frac{d}{dx} \cot(x) = -\csc^2(x)$$

$$\frac{d}{dx} \csc(x) = -\csc(x) \cot(x)$$

2 Integration

$$\int \sin(x) dx = -\cos(x) + C$$

$$\int \tan(x) dx = -\ln|\cos(x)| + C$$

$$\int \sec(x) dx = \ln|\sec(x) + \tan(x)| + C$$

$$\int \cos(x) dx = \sin(x) + C$$

$$\int \cot(x) dx = \ln|\sin(x)| + C$$

$$\int \csc(x) dx = -\ln|\csc(x) + \cot(x)| + C$$

Integrate by Parts $\int u dv = \int v du$

3 Product of sines and cosines

$$\int \sin^n(x) \cos^m(x)$$

Case 1 : $m = 1$ $\frac{\sin^{n+1}(x)}{n+1} + C$

Case 2 : $m = \text{odd}$

Use $\cos^2(x) = 1 - \sin^2(x)$ to convert all but one power of cosine to sine.

Case 3 : $n = 1$ $-\frac{\cos^{m+1}(x)}{m+1} + C$

Case 4 : $n = \text{odd}$

Use $\cos^2(x) = 1 - \sin^2(x)$ to convert all but one power of sine to cosine.

Case 5: Both are even, Use Double Angle Formulas

$$\sin^n(x) \cos^m(x) = \left(\frac{1}{2}(1 - \cos(2x))\right)^{\frac{n}{2}} \left(\frac{1}{2}(1 + \cos(2x))\right)^{\frac{m}{2}}$$

4 Product of secants and tangents

$$\int \sec^n(x) \tan^m(x)$$

Case 1 : $n = 2$ $u = \tan(x), \int u^m du$

Case 2: $n = \text{even}$ Convert all but two secants to tangents

Case 3 : $m = 1$ $u = \sec(x), \int u^{n-1} du$

Case 4: $m = \text{odd}$ Convert all but one power of tangent into secants

Be sure to factor out any coefficient inside trig function, e.g. $\cos(3x)$ becomes $\frac{1}{3} \int (u - \text{sub})$

5 Trigonometric Formulas

Double Angle Formulas:

$$\sin(2x) = 2\sin(x)\cos(x)$$

$$\cos(2x) = \cos^2(x) - \sin^2(x)$$

$$\cos(2x) = 1 - 2\sin^2(x)$$

$$\cos(2x) = 2\cos^2(x) - 1$$

Products of Trig Functions with Different Angles

$$\sin(A)\sin(B) = \frac{\cos(A - B) - \cos(A + B)}{2}$$

$$\cos(A)\cos(B) = \frac{\cos(A - B) + \cos(A + B)}{2}$$

$$\sin(A)\cos(B) = \frac{\sin(A + B) + \sin(A - B)}{2}$$

6 Trig Substitution