

# 1. ECHIVALENȚA GRAMATICILOR REGULATE ȘI A AUTOMATELOR FINITE

1. *Din gramatica dată să se genereze trei forme propoziționale (cuvinte).*
2. *Să se construiască arborele de derivare pentru fiecare din cuvintele generate.*
3. *Să se construiască automatul finit echivalent.*
4. *Printr-un calcul de configurații să se demonstreze că formele propoziționale generate de gramatică sunt acceptate și de automatul finit construit.*
5. *Să se scrie expresia regulată a cuvintelor generate de gramatica dată.*

1.  $G = (\{S, C, D\}, \{0, 1\}, P, S)$ , unde  $P$ :

1)  $S \rightarrow 1C \mid 0D$ ; 2)  $C \rightarrow 0D \mid 0S \mid 1$ ; 3)  $D \rightarrow 1C \mid 1S \mid 0$ .

2.  $G = (\{S, A, B, C\}, \{a, b, c\}, P, S)$ , unde  $P$ :

1)  $S \rightarrow aA \mid bB \mid aC$ ; 2)  $A \rightarrow bA \mid bB \mid c$ ; 3)  $B \rightarrow aA \mid cC \mid b$ ; 4)  $C \rightarrow bB \mid bC \mid a$ .

3.  $G = (\{K, L, M, N\}, \{a, b, +, -, \perp\}, P, K)$ , unde  $P$ :

1)  $K \rightarrow aL \mid bM$ ; 2)  $L \rightarrow -N \mid -M$ ; 3)  $M \rightarrow +N$ ; 4)  $N \rightarrow aL \mid bM \mid \perp$ .

4.  $G = (\{X, Y, Z, W, V\}, \{0, 1, \sim, \#, \&\}, P, X)$ , unde  $P$ :

1)  $X \rightarrow 0Y \mid 1Z \mid 1$ ; 2)  $Y \rightarrow 0Z \mid \sim W \mid \#$ ; 3)  $Z \rightarrow 1Y \mid 1W \mid 0V$ ;  
4)  $W \rightarrow 0W \mid 1W \mid \#$ ; 5)  $V \rightarrow \&Z$ .

6.  $G = (\{K, L, M, N, Q, P, R, S\}, \{0, 1, *, \$, /\}, V, K)$ , unde  $V$ :

1)  $K \rightarrow 1L \mid 0N$ ; 2)  $L \rightarrow 0M \mid 0P \mid /Q$ ; 3)  $N \rightarrow 1R \mid 1M \mid *S$ ;  
4)  $Q \rightarrow 1P$ ; 5)  $P \rightarrow *L \mid \$$ ; 6)  $M \rightarrow \$$ ; 7)  $S \rightarrow 0R$ ; 8)  $R \rightarrow /N \mid \$$ .

7.  $G = (\{E, A, B, C, D\}, \{0, 1, a, b, c\}, P, E)$ , unde  $P$ :

1)  $E \rightarrow 0A \mid c$ ; 2)  $A \rightarrow aB \mid aD$ ; 3)  $B \rightarrow bB \mid 1C \mid c$ ; 4)  $D \rightarrow aD \mid 0C \mid$

c.

8.  $G = (\{S, A, B, C, D\}, \{a, b, c, d, \perp\}, P, S)$ , unde  $P$ :

1)  $S \rightarrow aA \mid bB$ ; 2)  $A \rightarrow cC \mid \perp$ ; 3)  $C \rightarrow cC \mid cA$ ; 4)  $B \rightarrow dD \mid \perp$ ;  
5)  $D \rightarrow dD \mid dB$ .

9.  $G = (\{K, L, M, N, P\}, \{0, 1, \&, \%, a, b\}, C, K)$ , unde  $C$ :

1)  $K \rightarrow 1M \mid 1$ ; 2)  $M \rightarrow 0L \mid \&N \mid \&P$ ; 3)  $L \rightarrow 1L \mid 0L \mid \%P$ ;  
4)  $N \rightarrow aN \mid bN \mid \%P$ ; 5)  $P \rightarrow 1P \mid aP \mid 0$ .

10.  $G = (\{I, J, K, M, N\}, \{0, 1, \sim, !\}, P, I)$ , unde  $P$ :

1)  $I \rightarrow 0J \mid 1K \mid 0M$ ; 2)  $J \rightarrow \sim K \mid 0M$ ; 3)  $K \rightarrow \sim M \mid 0J \mid 0N$ ; 4)  $M \rightarrow 1K \mid$   
!  
5)  $N \rightarrow 0I \mid 1I \mid !$ .

11.  $G = (\{S, A, B, C, D, E\}, \{a, b, c, d, e, \$, \perp\}, P, S)$ , unde  $P$ :

1)  $S \rightarrow aA \mid bB \mid cC$ ; 2)  $A \rightarrow dD$ ; 3)  $B \rightarrow \#D \mid \$E$ ; 4)  $D \rightarrow dD \mid dB \mid$   
 $\perp$ ;  
5)  $C \rightarrow cE$ ; 6)  $E \rightarrow eE \mid eB \mid \perp$ .

12.  $G = (\{X, Y, Z, V\}, \{(, ), y, z, v\}, P, X)$ , unde  $P$ :

1)  $X \rightarrow (Y \mid y$ ; 2)  $Y \rightarrow yY \mid zY \mid zZ$ ; 3)  $Z \rightarrow zZ \mid vZ \mid vV$ ; 4)  
 $V \rightarrow vV \mid )$ .

13.  $G = (\{A, B, C\}, \{a, b\}, P, A)$ , unde  $P$ :

1)  $A \rightarrow bC \mid aC$ ; 2)  $C \rightarrow bB \mid 0A \mid 1$ ; 3)  $B \rightarrow aC \mid bA \mid a$ .

14.  $G = (\{S, A, B, C\}, \{1, 2, 3\}, P, S)$ , unde  $P$ :

1)  $S \rightarrow 2A \mid 1B \mid 1C$ ; 2)  $A \rightarrow 3A \mid 1B \mid 3$ ; 3)  $B \rightarrow 3A \mid 2C \mid 3$ ;  
4)  $C \rightarrow 2B \mid 3C \mid 1$ .

15.  $G = (\{A, L, G, N\}, \{a, b, +, -, \} P, A)$ , unde  $P$ :

1)  $A \rightarrow aL \mid bN$ ; 2)  $L \rightarrow -N \mid -G$ ; 3)  $G \rightarrow +N$ ; 4)  $N \rightarrow aL \mid bG \mid b$ .

16.  $G=(\{X, Y, Z, W, V\}, \{0, 1, a, b, c\}, P, X)$ , unde  $P$ :
- 1)  $X \rightarrow 0Y \mid 1Z \mid a$ ; 2)  $Y \rightarrow 0Z \mid cW \mid b$ ; 3)  $Z \rightarrow 1Y \mid 1W \mid 0V$ ;
  - 4)  $W \rightarrow 0W \mid 1W \mid a$ ; 5)  $V \rightarrow bZ$ .
17.  $G=(\{K, L, M, N, Q, P, R, S\}, \{0, 1, 2\}, V, K)$ , unde  $V$ :
- 1)  $K \rightarrow 1L \mid 0N$ ; 2)  $L \rightarrow 0M \mid 0P \mid 1Q$ ; 3)  $N \rightarrow 1R \mid 1M \mid 2S$ ;
  - 4)  $Q \rightarrow 1P$ ; 5)  $P \rightarrow 2L \mid 2$ ; 6)  $M \rightarrow 1$ ; 7)  $S \rightarrow 0R$ ; 8)  $R \rightarrow 2N \mid 0$ .
18.  $G=(\{E, A, B, C, D\}, \{0, 1, 2, a, b, c\}, P, E)$ , unde  $P$ :
- 1)  $E \rightarrow 0A \mid 2$ ; 2)  $A \rightarrow aB \mid aD$ ; 3)  $B \rightarrow bB \mid 1C \mid c$ ; 4)  $D \rightarrow aD \mid 0C \mid$
- 2.
19.  $G=(\{F, A, B, C, D\}, \{0, 1, 2, 3, 4\}, P, F)$ , unde  $P$ :
- 1)  $F \rightarrow 0A \mid 2$ ; 2)  $A \rightarrow 4B \mid 3D$ ; 3)  $B \rightarrow 1B \mid 0C \mid 0$ ; 4)  $D \rightarrow 4D \mid 3C \mid$
- 2.
20.  $G=(\{S, A, B, C, D\}, \{a, b, c, d, e\}, P, S)$ , unde  $P$ :
- 1)  $S \rightarrow cA \mid bB$ ; 2)  $A \rightarrow cC \mid e$ ; 3)  $C \rightarrow cC \mid cA$ ; 4)  $B \rightarrow dD \mid e$ ;
  - 5)  $D \rightarrow dD \mid aB$ .
21.  $G=(\{K, L, M, N, P\}, \{0, 1, a, b\}, C, K)$ , unde  $C$ :
- 1)  $K \rightarrow 1M \mid 0$ ; 2)  $M \rightarrow 0L \mid 1N \mid aP$ ; 3)  $L \rightarrow 1L \mid 0L \mid bP$ ;
  - 4)  $N \rightarrow aN \mid bN \mid 0P$ ; 5)  $P \rightarrow 1P \mid aP \mid 0$ .
22.  $G=(\{F, J, K, M, N\}, \{0, 1, e, t\}, P, F)$ , unde  $P$ :
- 1)  $F \rightarrow 0J \mid 1K \mid 0M$ ; 2)  $J \rightarrow tK \mid 0M$ ; 3)  $K \rightarrow eM \mid 0J \mid 0N$ ; 4)  $M \rightarrow 1K \mid$
- $t$ ;
- 5)  $N \rightarrow 0I \mid 1F \mid e$ .
23.  $G=(\{S, A, B, C, D, E\}, \{a, b, c, d, e\}, P, M)$ , unde  $P$ :
- 1)  $M \rightarrow aA \mid bB \mid cC$ ; 2)  $A \rightarrow dD$ ; 3)  $B \rightarrow aD \mid bE$ ; 4)  $D \rightarrow dD \mid dB \mid e$ ;
  - 5)  $C \rightarrow cE$ ; 6)  $E \rightarrow eE \mid eB \mid b$ .
24.  $G=(\{X, Y, Z, V\}, \{a, b, y, z, v\}, P, X)$ , unde  $P$ :

- 1)  $X \rightarrow aY \mid b$ ; 2)  $Y \rightarrow yY \mid zY \mid zZ$ ; 3)  $Z \rightarrow zZ \mid vZ \mid vV$ ;  
4)  $V \rightarrow bV \mid y$ .

25.  $G = (\{S, A, B, C, D\}, \{a, b, c, d, e\}, P, S)$ , unde  $P$ :

- 1)  $S \rightarrow cA \mid bB$ ; 2)  $A \rightarrow cC \mid e$ ; 3)  $C \rightarrow cC \mid cA$ ; 4)  $B \rightarrow dD \mid d$ ;  
5)  $D \rightarrow dB \mid aA$ .

26.  $G = (\{M, A, B, D, E\}, \{a, b, c, d, e\}, P, M)$ , unde  $P$ :

- 1)  $M \rightarrow aA \mid bB$ ; 2)  $A \rightarrow dD$ ; 3)  $B \rightarrow aD \mid bE$ ; 4)  $D \rightarrow dD \mid e$ ;  
5)  $E \rightarrow eE \mid eB \mid b$ .

27.  $G = (\{X, Y, Z, V\}, \{a, b, y, z, v\}, P, X)$ , unde  $P$ :

- 1)  $X \rightarrow aY \mid b$ ; 2)  $Y \rightarrow yY \mid zY \mid zZ$ ; 3)  $Z \rightarrow zZ \mid vZ \mid vV$ ; 4)  $V \rightarrow bV \mid y$ .

28.  $G = (\{S, C, D\}, \{0, 1\}, P, S)$ , unde  $P$ :

- 1)  $S \rightarrow 1C \mid 0D$ ; 2)  $C \rightarrow 0D \mid 0S \mid 1$ ; 3)  $D \rightarrow 0$ .

29.  $G = (\{S, A, B, C\}, \{a, b, c\}, P, S)$ , unde  $P$ :

- 1)  $S \rightarrow aA \mid bB \mid aC$ ; 2)  $A \rightarrow bA \mid c$ ; 3)  $B \rightarrow b$ ; 4)  $C \rightarrow bC \mid a$ .

30.  $G = (\{K, L, M, N\}, \{a, b, +, -, \perp\}, P, K)$ , unde  $P$ :

- 1)  $K \rightarrow aL \mid bM$ ; 2)  $L \rightarrow -N$ ; 3)  $M \rightarrow +N$ ; 4)  $N \rightarrow bM \mid \perp$ .

31.  $G = (\{X, Y, Z, W\}, \{0, 1, \sim, \#, \&\}, P, X)$ , unde  $P$ :

- 1)  $X \rightarrow 0Y \mid 1Z \mid 1$ ; 2)  $Y \rightarrow \sim W$ ; 3)  $Z \rightarrow 1Y \mid 1W$ ; 4)  $W \rightarrow 0W \mid 1W \mid$

$\#$ .

32.  $G = (\{K, L, M, N, R\}, \{0, 1, *, \$, /\}, P, K)$ , unde  $P$ :

- 1)  $K \rightarrow 1L \mid 0N$ ; 2)  $L \rightarrow 0M$ ; 3)  $N \rightarrow 1R \mid 1M$ ; 4)  $M \rightarrow \$$ ; 5)  $R \rightarrow /R$

$\mid 0$ .

33.  $G = (\{E, A, B, C, D\}, \{0, 1, a, b, c\}, P, E)$ , unde  $P$ :

- 1)  $E \rightarrow 0A \mid c$ ; 2)  $A \rightarrow aB \mid aD \mid fE$ ; 3)  $B \rightarrow bB \mid 1C$ ; 4)  $D \rightarrow aD \mid 0C$ ;  
5)  $C \rightarrow c$ .

34.  $G=(\{E, A, B, D\}, \{0, 1, a, b, c\}, P, E)$ , unde  $P$ :

1)  $E \rightarrow 0A \mid a$  2)  $A \rightarrow aB \mid aD \mid fD$ ; 3)  $B \rightarrow 1D \mid c$ ; 4)  $D \rightarrow aD \mid 0$ .

35.  $G=(\{S, A, B, C, D\}, \{a, b, c, d, \perp\}, P, S)$ , unde  $P$ :

1)  $S \rightarrow aA \mid bB$ ; 2)  $A \rightarrow dC \mid \perp$ ; 3)  $C \rightarrow cC \mid bA$ ; 4)  $B \rightarrow aD \mid \perp$ ;

5)  $D \rightarrow cD \mid dB$ .

36.  $G=(\{K, L, M, N, P\}, \{0, 1, \&, a, b\}, P, K)$ , unde  $P$ :

1)  $K \rightarrow 1M$ ; 2)  $M \rightarrow 0L \mid \&N \mid \&P$ ; 3)  $L \rightarrow 1L \mid 0L \mid 1$ ; 4)  $N \rightarrow aN \mid bN \mid$

$a$ ;

5)  $P \rightarrow 0$ .